《芯片设计自动化与智能优化》
Technology Mapping

The slides are based on Prof. Weikang Qian's lecture notes at SJTU and Prof. Rob Rutenbar's lecture notes at UIUC

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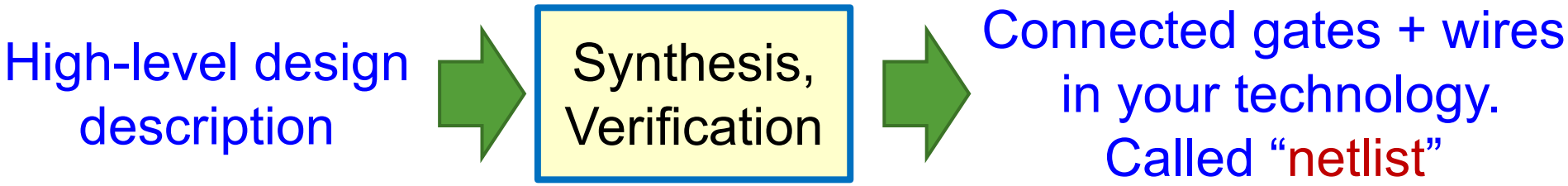
From Logic… To Layout…

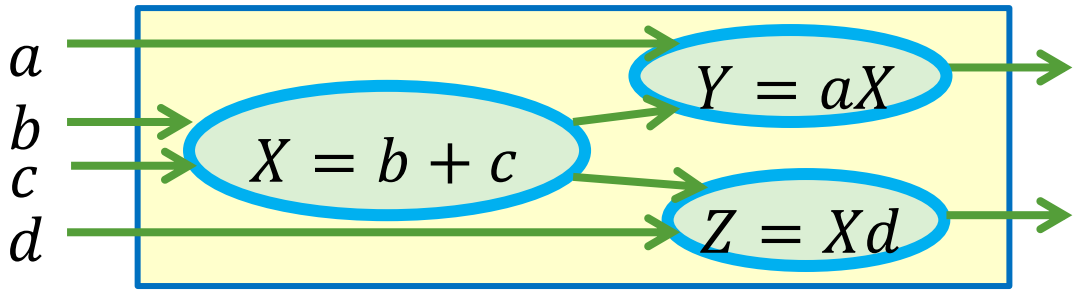
- What you know…
  - Computational Boolean algebra, representation, some verification, some synthesis.
  - This is what happens in the "**front end**" of the ASIC design process.



- One key **connecting** step:
  - How to **transform** result of multi-level synthesis into real gates for layout task.
  - Called: **Technology Mapping**, or **Tech Mapping**.

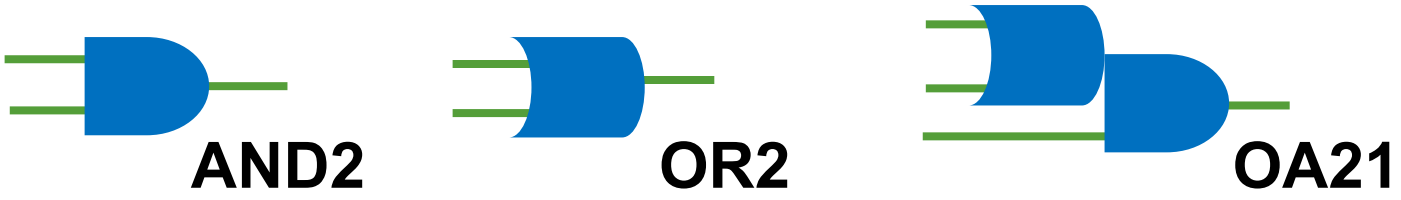
Tech Mapping: The Problem

- Multi-level model is still a little **abstract**.
  - Structure of the Boolean logic network is fixed.
  - ESPRESSO-style 2-level simplification done on each node of network.
  - … but that still does **not** give us the actual **gate-level netlist**.

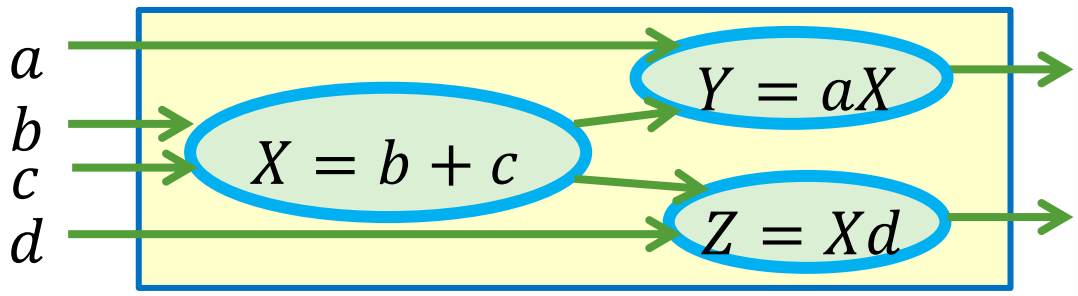


Tech Mapping: Problem

- Suppose we have these gates in our "**library**".
  - This is called "**the technology**" we are allowed to use to build this optimized netlist.



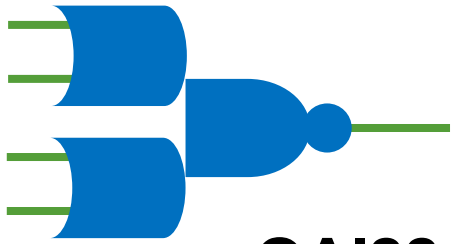
  - Note: OA21 is an OR-AND, a so-called **complex gate** in our library.



How do we build the 2 functions specified in this Boolean Logic Network using **only** these gates from our library?

Aside: Complex Gates

OR-AND-Inverter



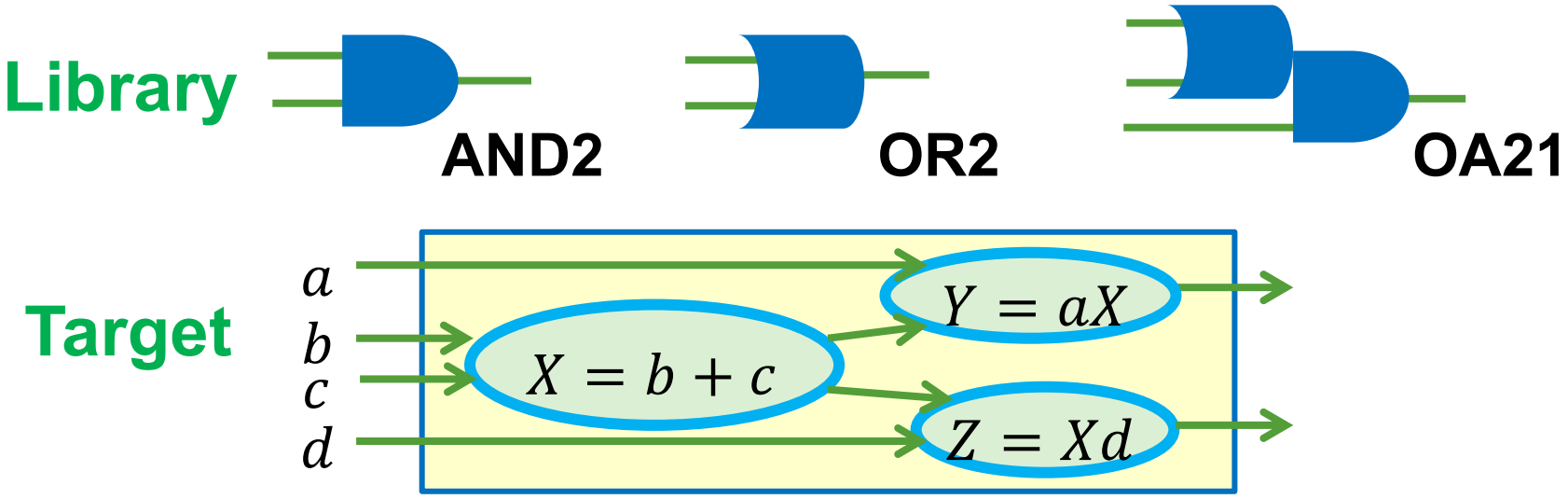
OAI22

AND-OR-Inverter

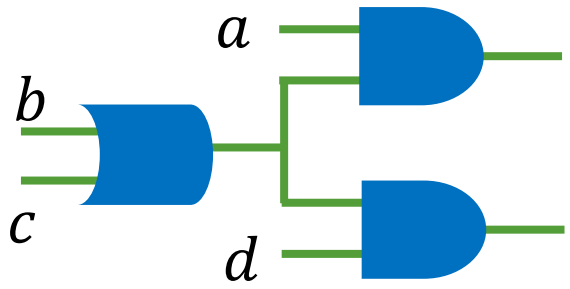
AOI221

- In CMOS, OAI and AOI gate structures are **efficient** at transistor level.

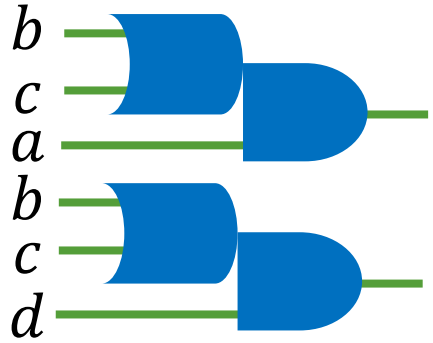
Tech Mapping: Simple Example



Obvious Mapping

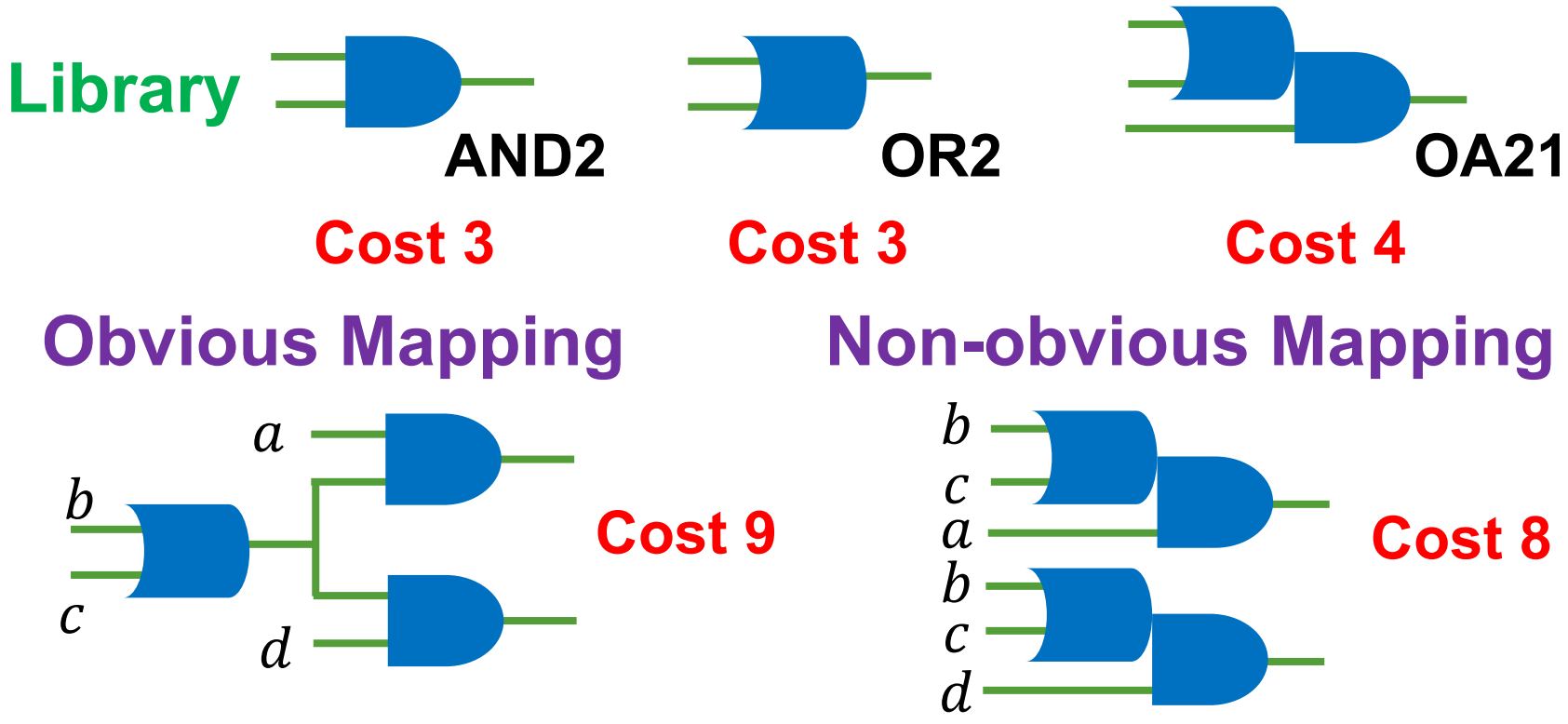


Non-obvious Mapping



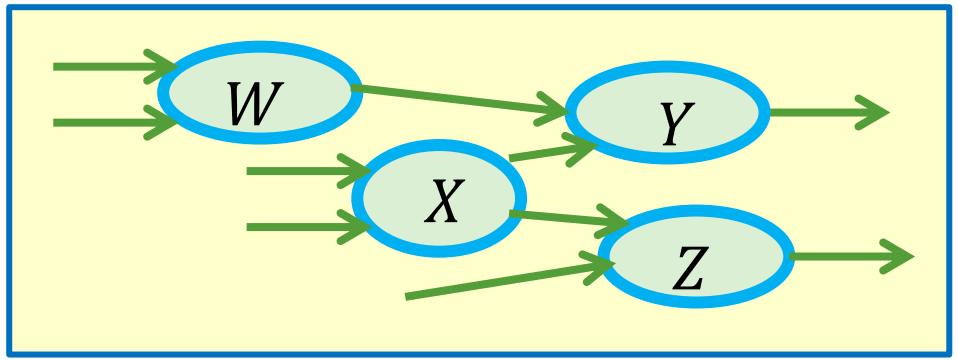
Tech Mapping

- Why choose a **non-obvious** mapping?
  - Answer 1: **Cost**. Suppose each gate in library has a cost associated with it, e.g., the **silicon area** of the standard cell gate.



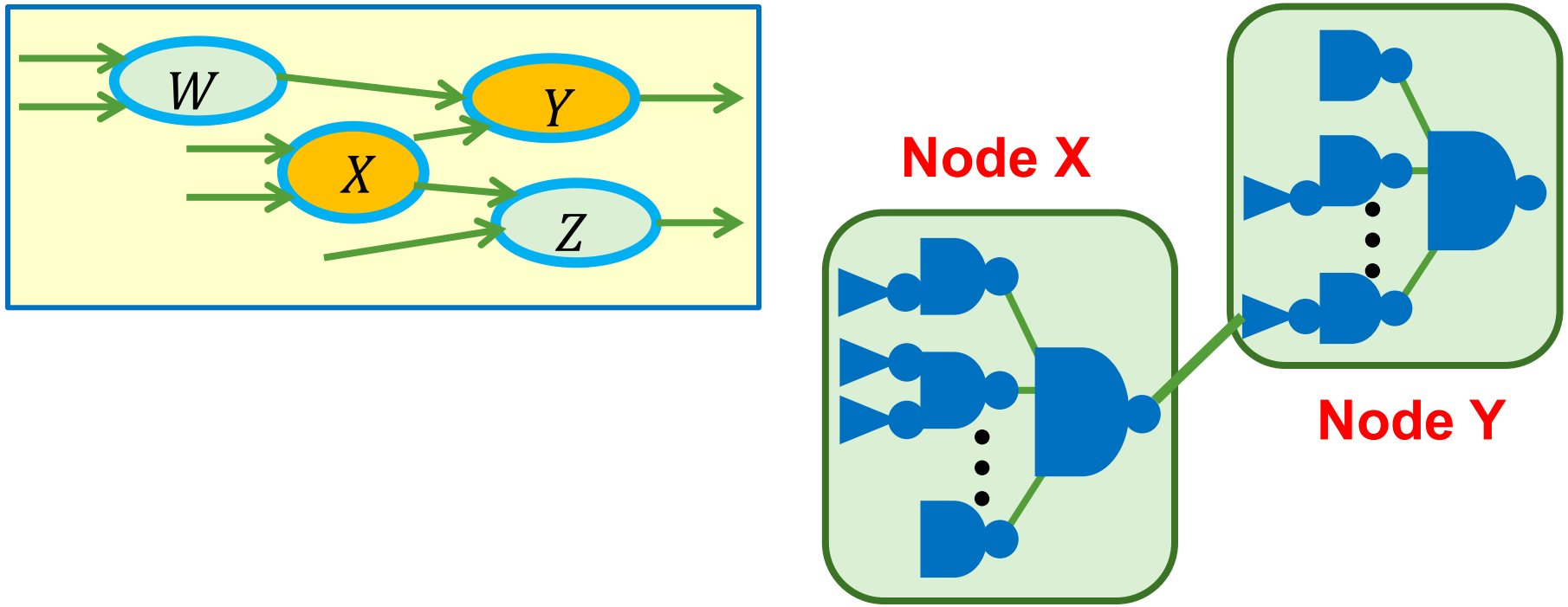
What “Multilevel Synthesis” Does?

- Helpful “mental” model to use: Multi-level synthesis does this...
  - **Structures** the multiple-node Boolean logic network “**well**”.
  - **Minimizes** SOP contents of each vertex in the network “**well**”, ie, # of literals.
  - **But** it does **not create real logic gates**.
  - This result is called: “**uncommitted**” logic, or “**technology independent**” logic.

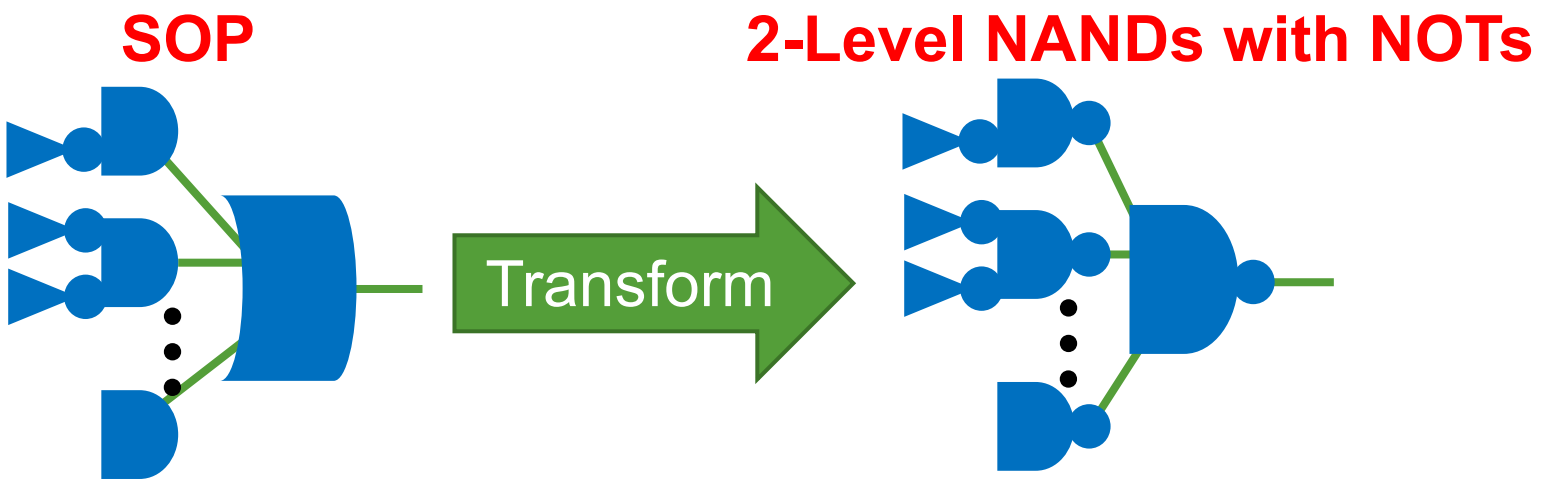


What “Technology Mapping” Does?

- First, we transform **uncommitted logic** into simple, **real** gates.
  - We transform **every** SOP form in **each** node into **NAND** & **NOT** gates. Nothing else!



Aside: We Can Map SOP into NANDs & NOTs

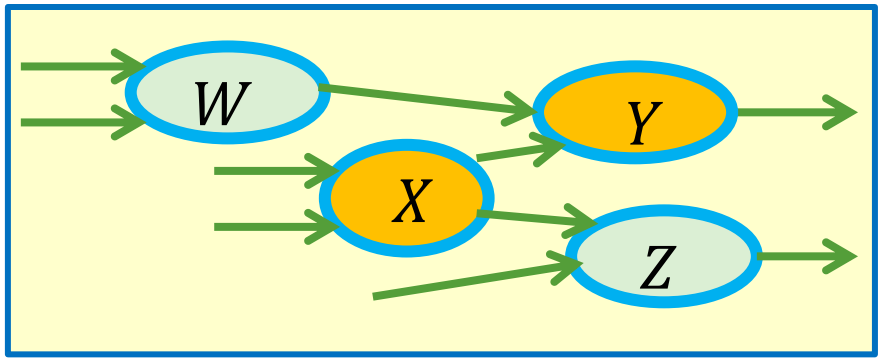


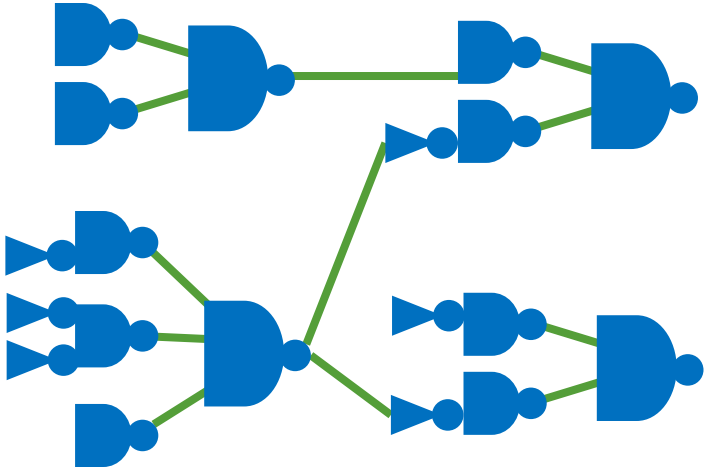
Because

By De Morgan's Law

What “Technology Mapping” Does?

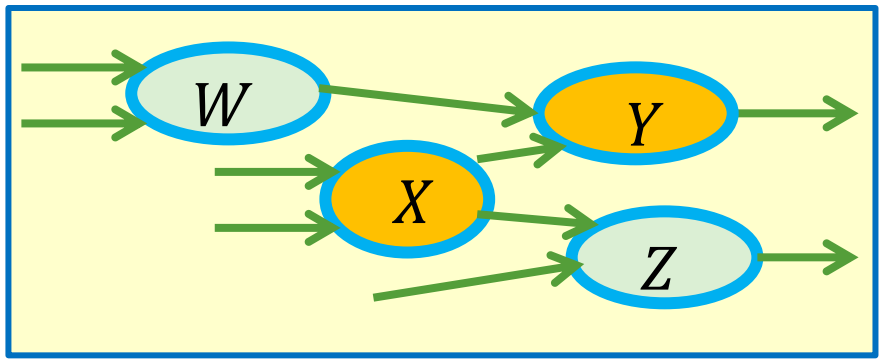
- By transforming every SOP form in each node into NAND & NOT gates …
  - … Boolean logic network **disappears**. W, X, Y, Z boundaries go away.
  - We have one BIG “**flat**” network of **NANDs** and **NOTs**. This is what we are going to map.

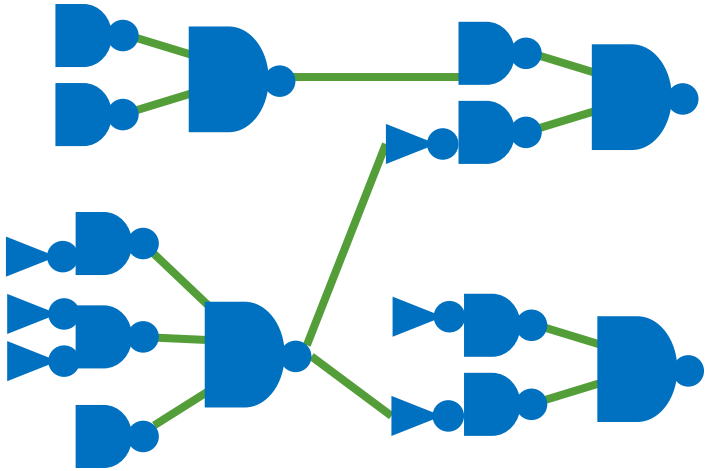




Technology Mapping

- Multi-level synthesis produces this big network of simple gates.
- How to transform – **map** – this onto standard cells in our library?





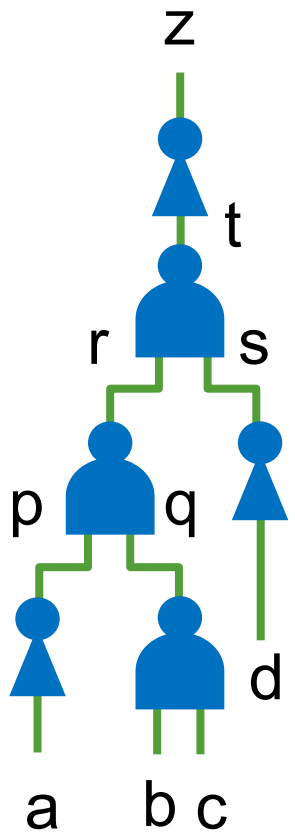
Technology Mapping as Tree Covering

- One famous, simple model of problem:
  - Your logic network to be mapped is **a tree of simple gates**.
    - We assume uncommitted form is **2-input NAND** ("**NAND2**") and **NOT** gates, only.
  - Your library of available "real" gate types is also represented in this form.
    - Each gate is represented as a **tree** of **NAND2** and **NOT** gates, with associated **cost**.

- Method is surprisingly **simple** and **optimal**.
  - Reference: Kurt Keutzer, "DAGON: Technology Binding and Local Optimization by DAG Matching," Proc. ACM/IEEE Design Automation Conference (DAC), 1987.

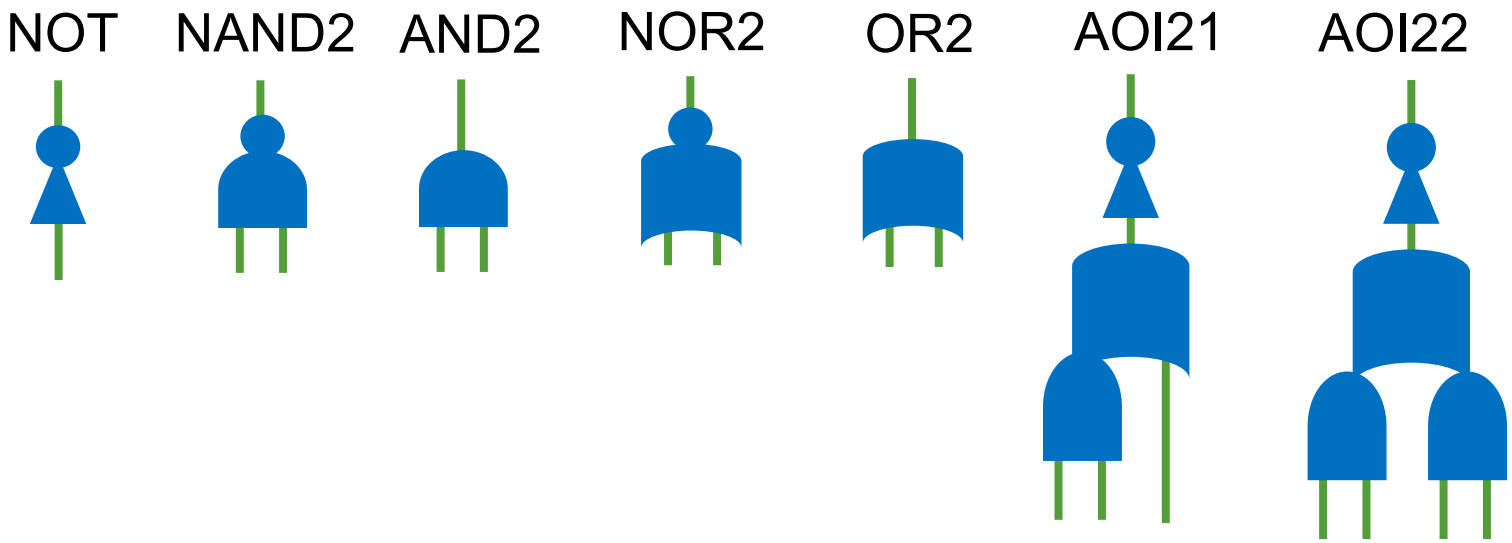
Tree Covering Example: Start with…

- Here is your uncommitted logic to be **tech mapped**.
  - This is what results from our multi-level synthesis optimization…
  - … after replacing all SOP forms in the network nodes with **NAND2/NOT**.
  - Called the **subject tree**.
  - (Restrict to **NAND2** to keep this simple. Also label not only inputs but all internal wires too.)



Tree Covering: Your Technology Library

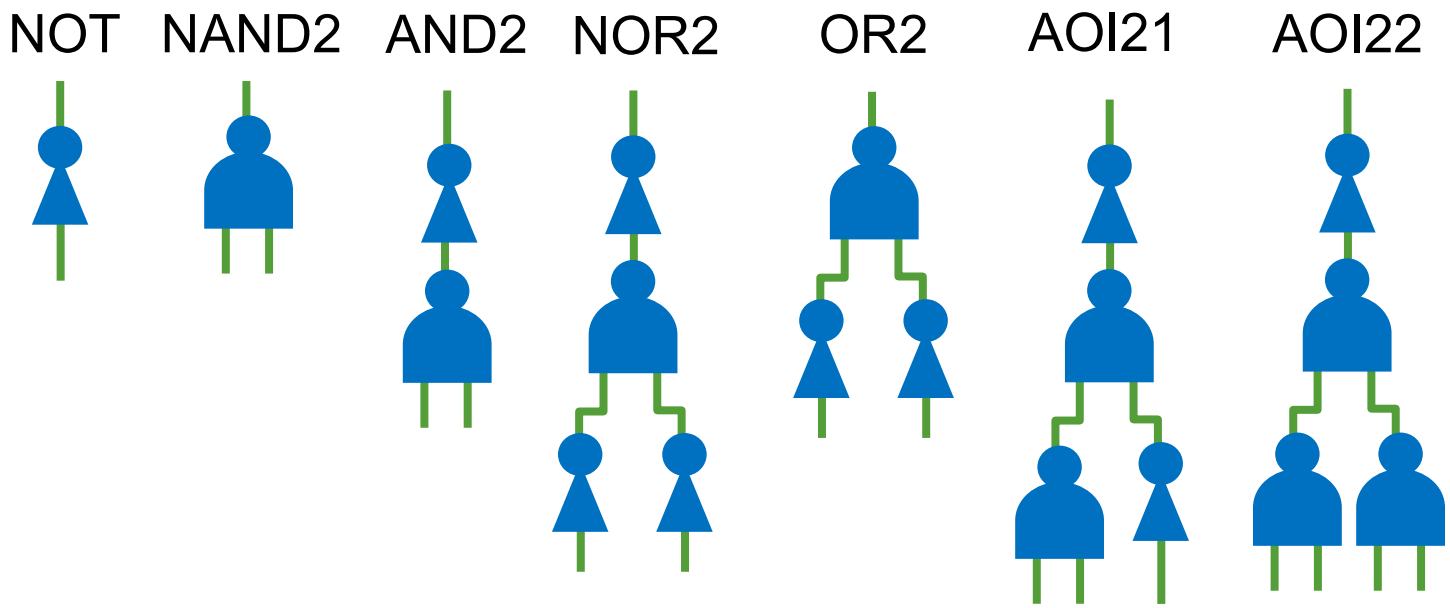
- And, here is a very simple **technology library**.



- First problem: this is **not** in the required **NAND2/NOT-only** form. **Must transform**.

Tree Covering: Representing Library

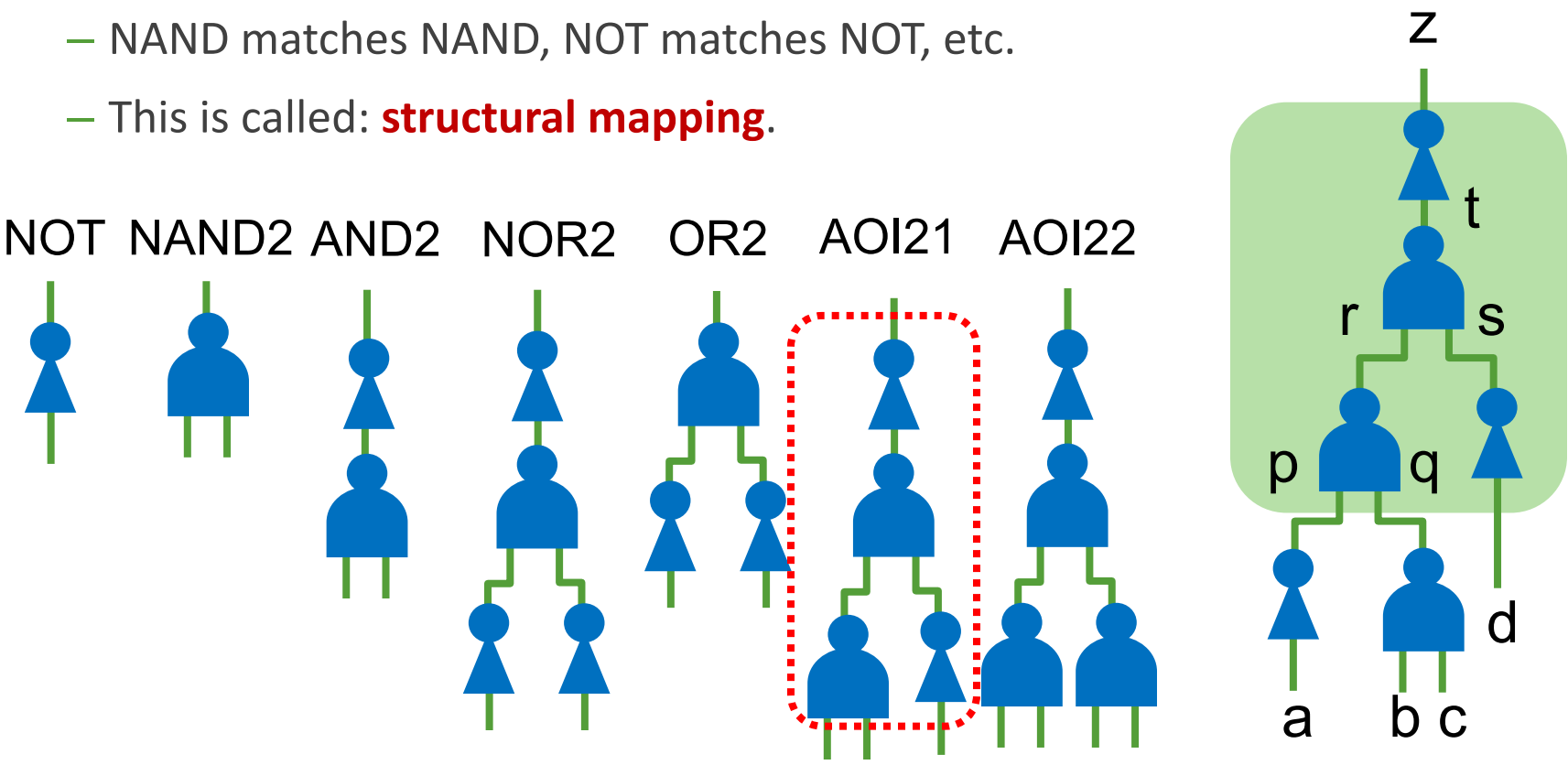
- Transforming to NAND2/NOT form is **easy**.
  - Just apply **De Morgan's law**.



- Each library element in this form is called a **pattern tree**.

Essential Idea in “Tree Covering”

- **Avoid** any **Boolean algebra**!
- Just do “**pattern matching**”.
  - Find where, in subject graph, the library pattern “matches”.
  - NAND matches NAND, NOT matches NOT, etc.
  - This is called: **structural mapping**.

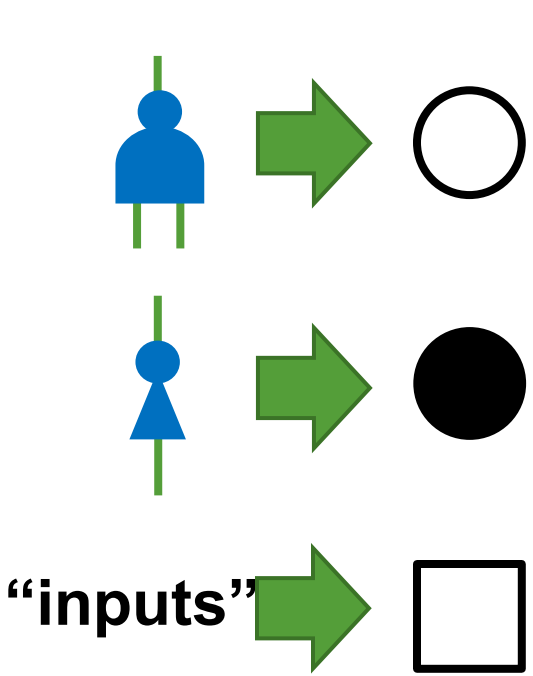


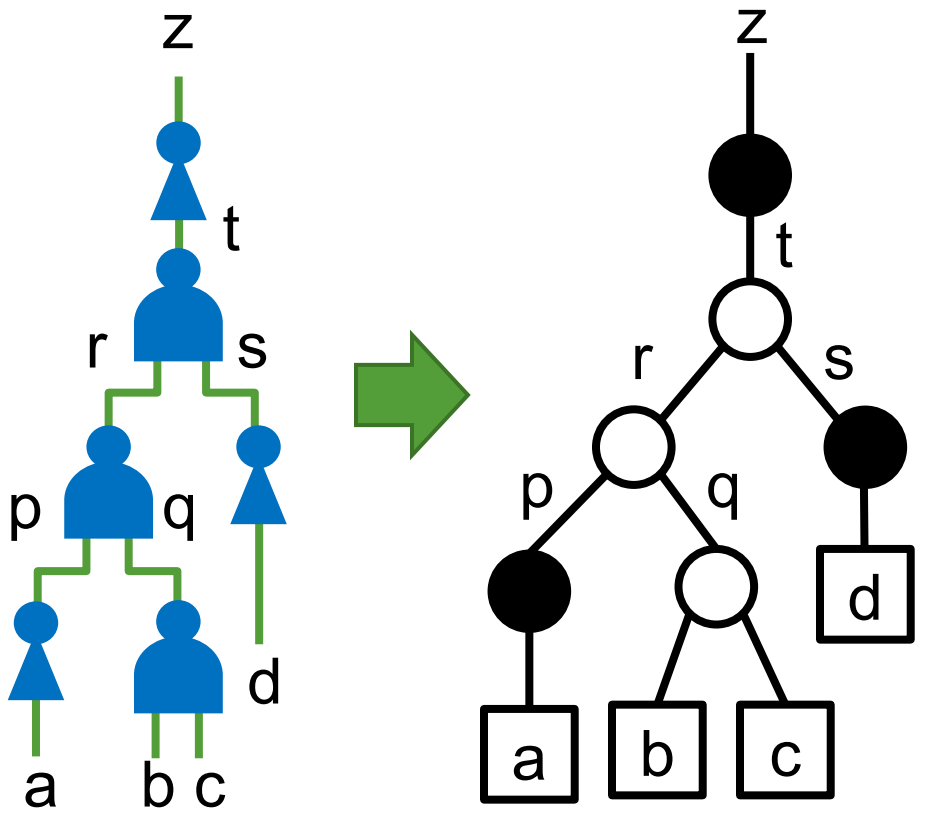
The General “Tree Covering”

- This is called a **structural tech mapper**.
- Why?
  - Because there is no Boolean algebra here!
  - We just match the gates, wires in a simple **pattern-match** way.
- Result
  - Surprisingly simple covering algorithm for **cost-optimal** cover.
- … But first, lets simplify the way we draw these, to emphasize “structural” match.

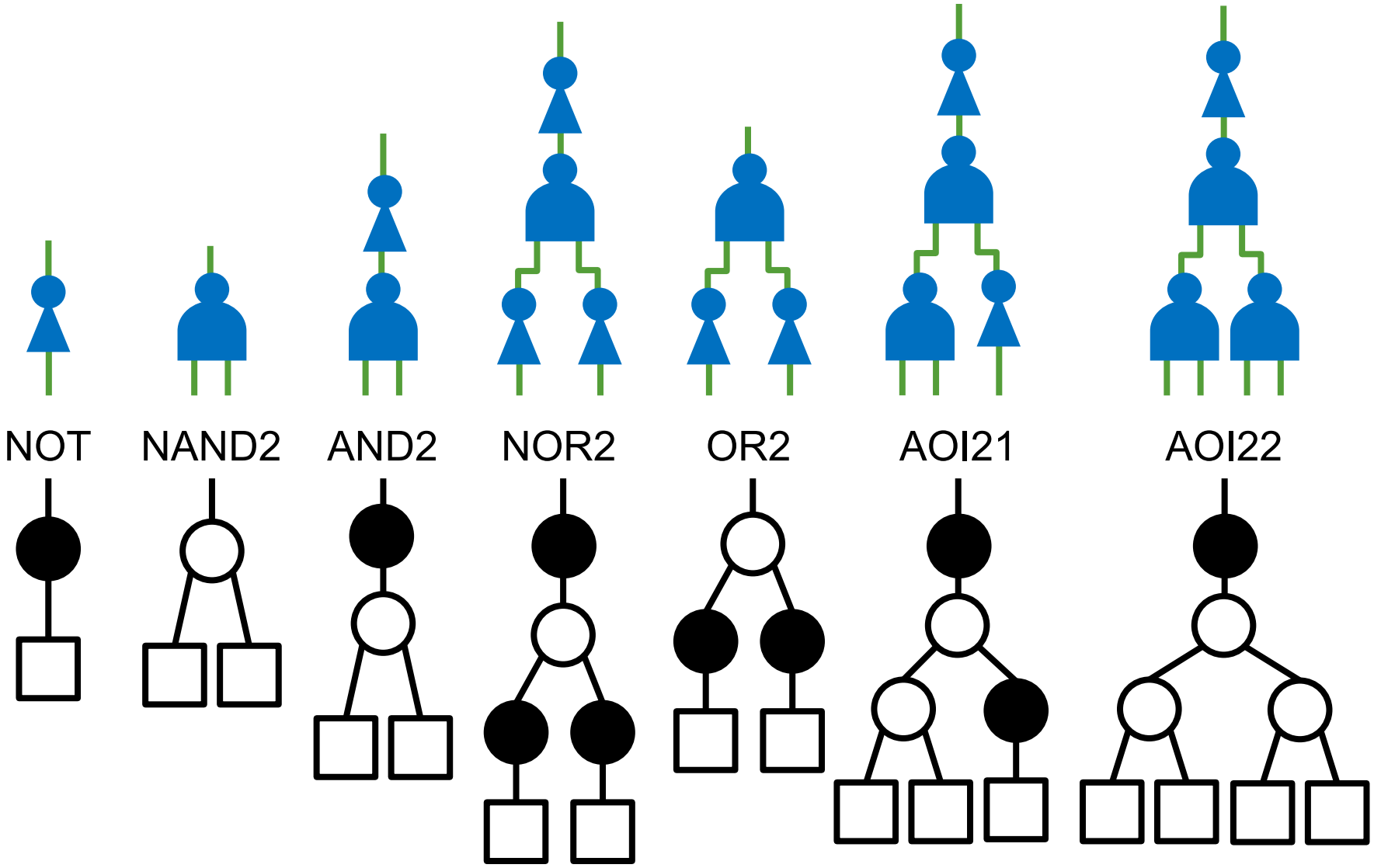
Representing Trees for Covering

- Only **three** kinds of structures that we need **match** in any tree.

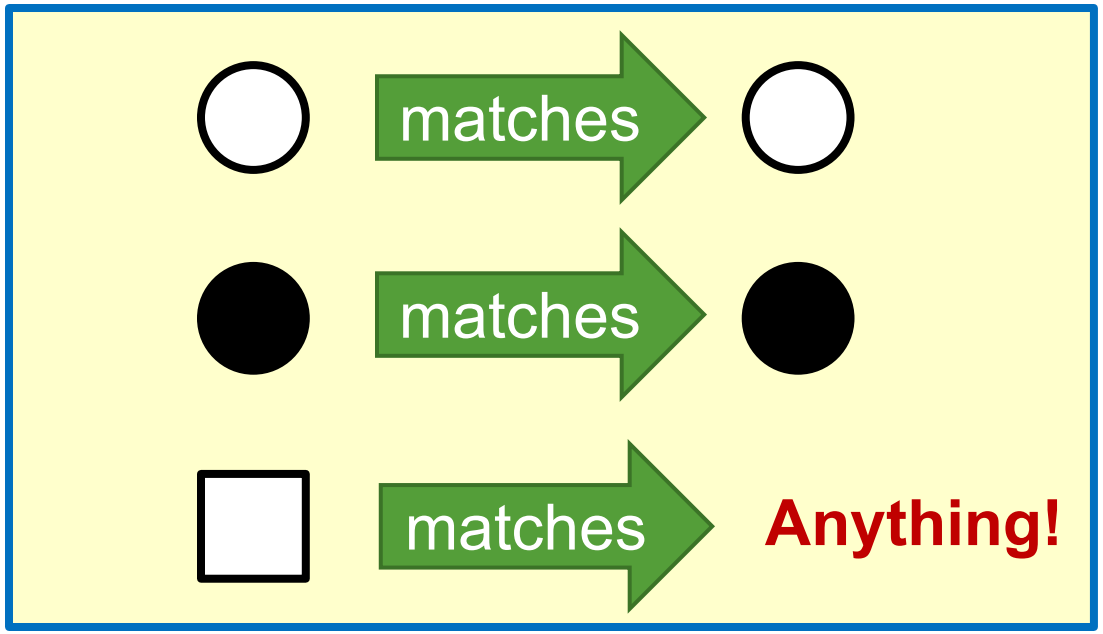


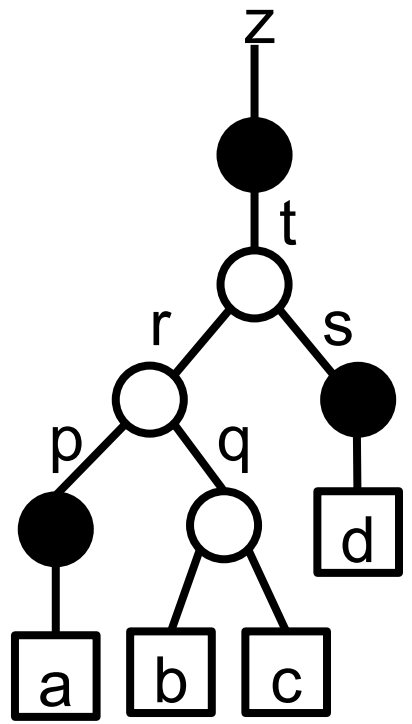


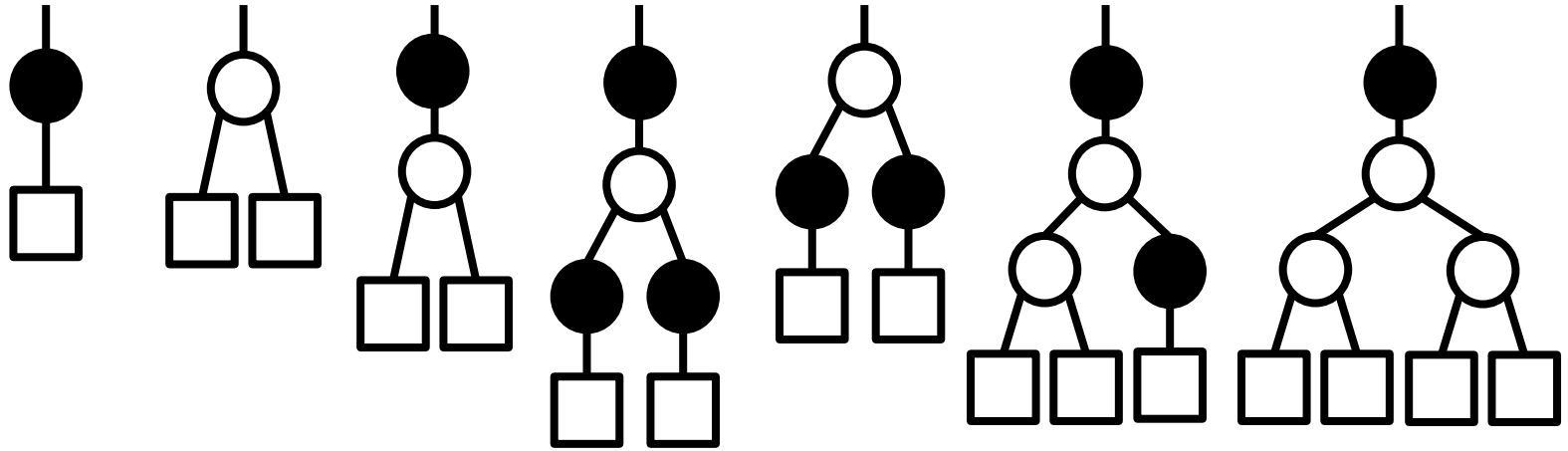
Represent Library in this Same Style



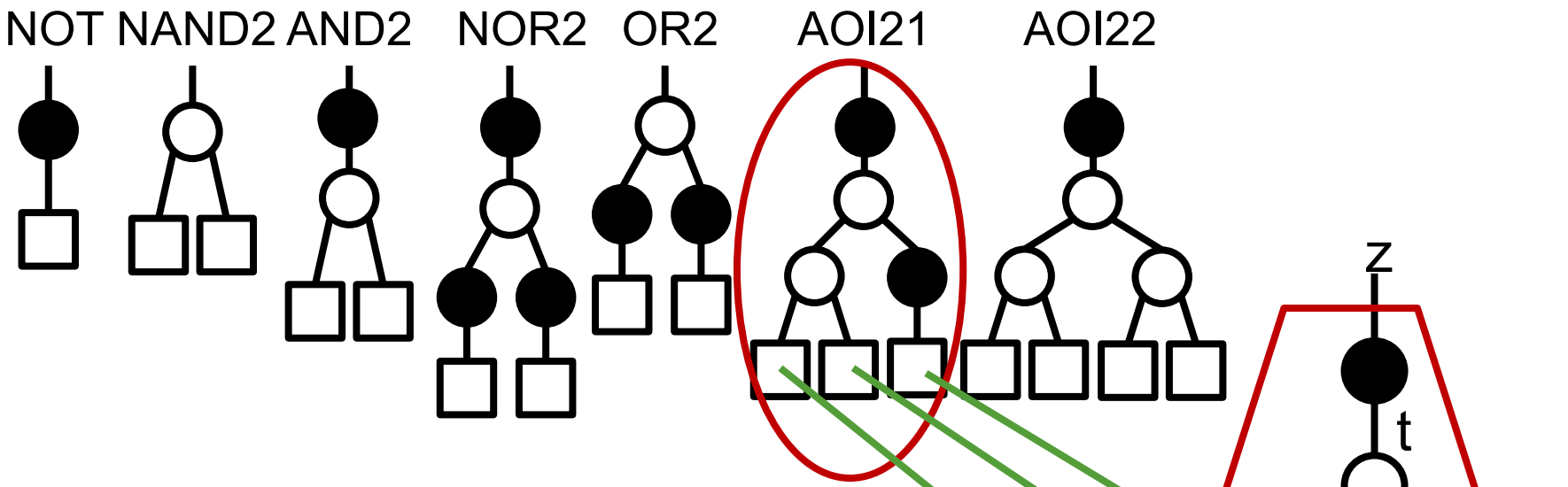
Structural Mapping Rules

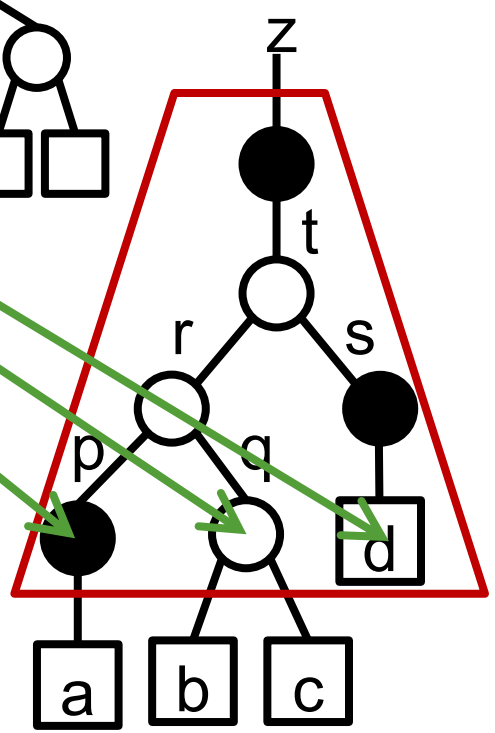






How a “Target Gate” Matches Subject Tree

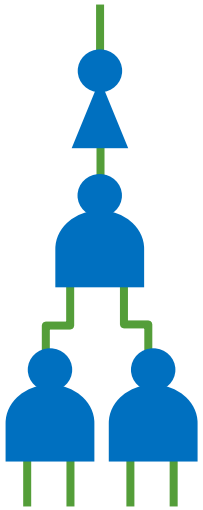




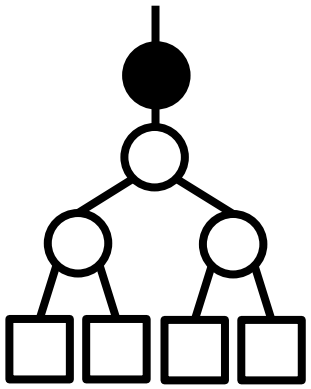
- AOI21 matches at Z.
  - Because all internal nodes **match exactly**.
  - And the inputs match “**anything**”.

Be Careful: Symmetries Matter!

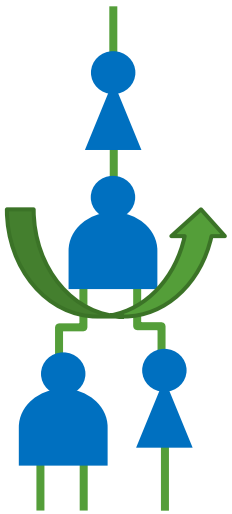
AOI22

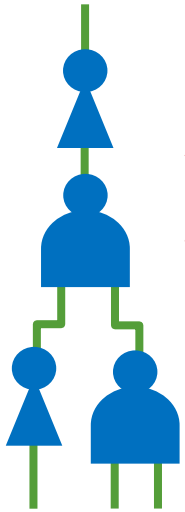


Symmetric tree,
1 way to match

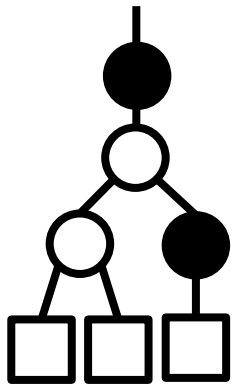


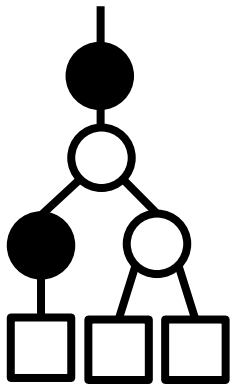
AOI21





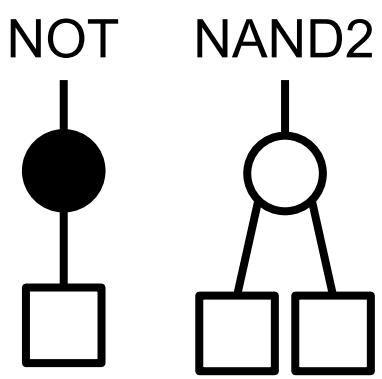
Not symmetric
2 ways to match



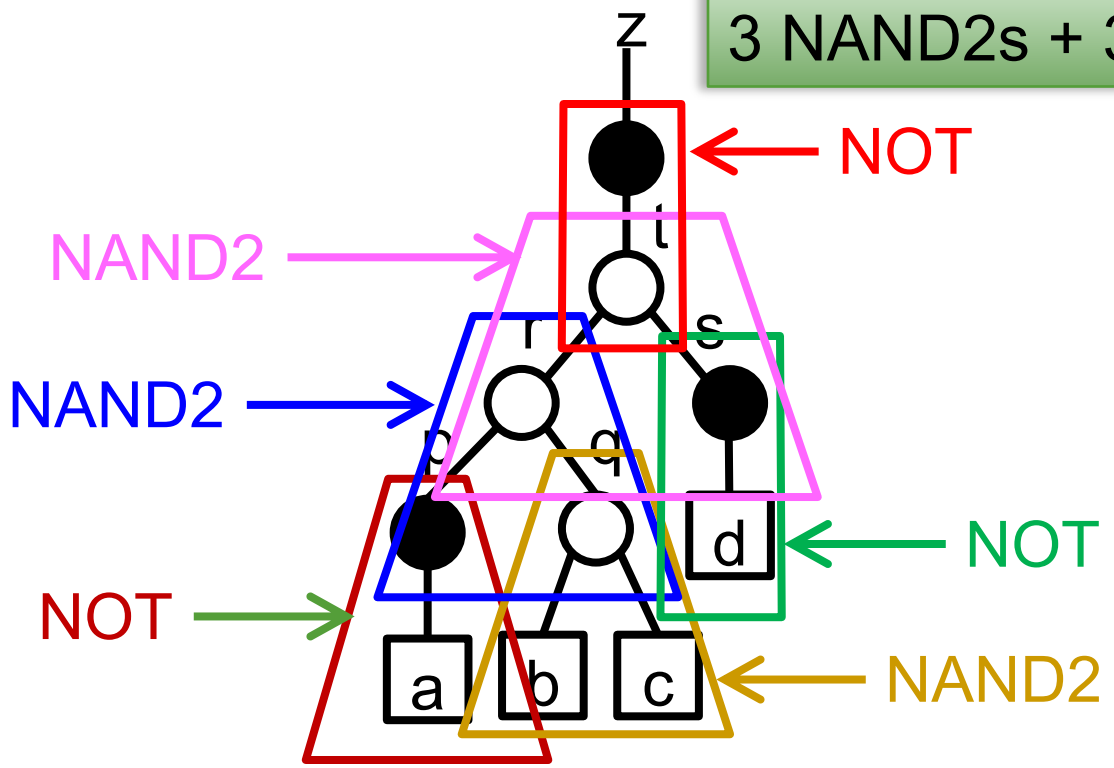


Rules for a Complete Tree Cover

- Every node in subject tree is **covered** by some library tree.
- **Output** of every library gate **overlaps input** of next library pattern.

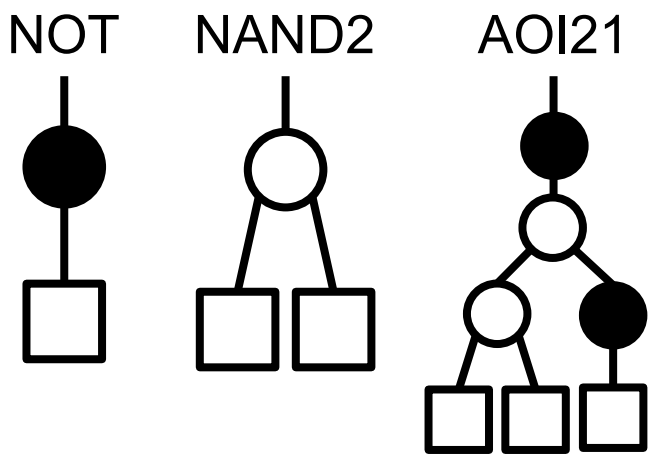


One correct tree cover:
3 NAND2s + 3 NOTs

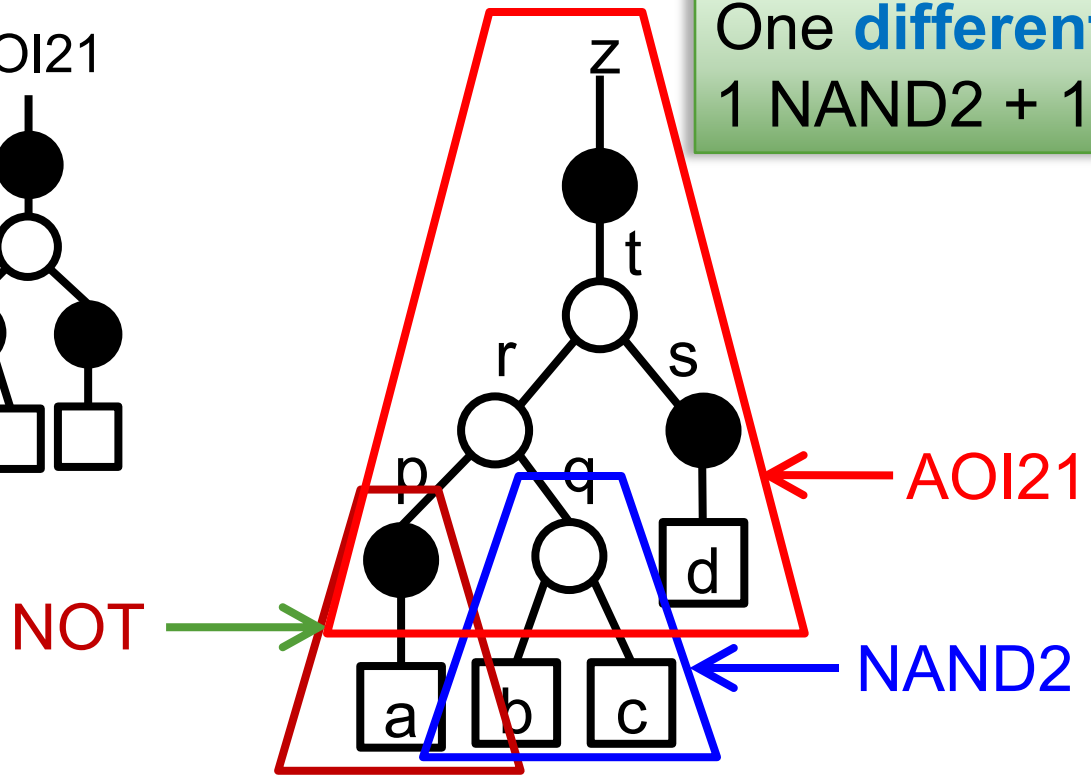


Rules for a Complete Tree Cover

- **Note**: usually there are **many different** legal covers.
- Which one do we choose? The one **with minimum cost**.



One **different** tree cover:
1 NAND2 + 1 NOT + 1 AOI21



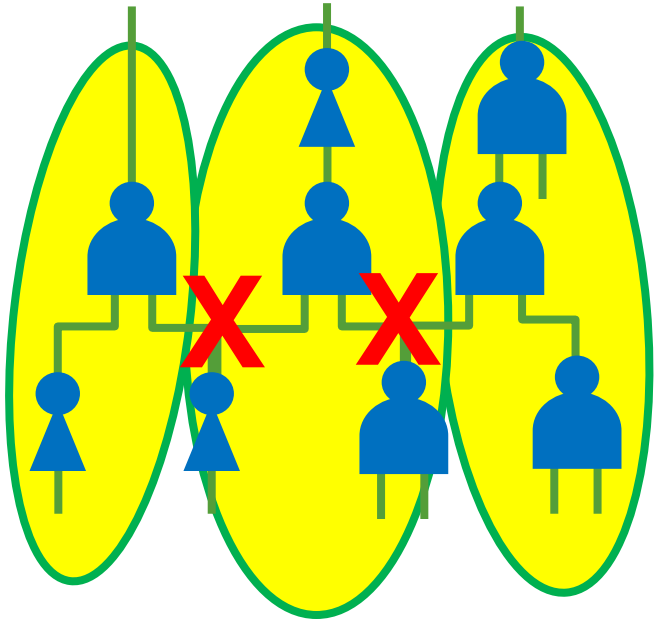
Tech Mapping via Tree Covering

- What do we need for a **complete** algorithm?

- **Treeifying** the input netlist
- **Tree matching**
  - For each node in the subject tree, find pattern trees in library that **match**.
- **Minimum-cost covering**
  - Assume you know what can match at each node of subject tree
  - … so, which ones do you pick for a **minimum cost** cover?

Treeifying the Netlist

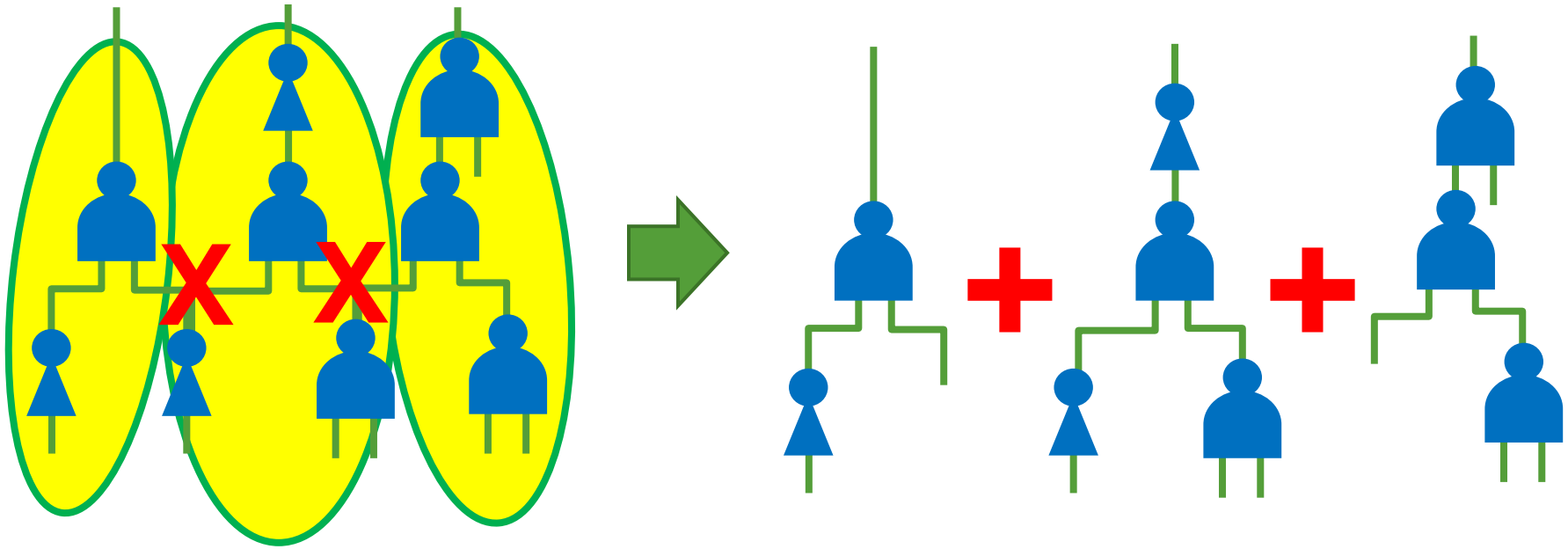
- These algorithms **only** work on trees, not on general graphs.
  - **Note**: general gate netlists are **Directed Acyclic Graphs (DAGs)**.
- **Treeifying**: every place you see a gate with fanout > 1, you **need to split**.



Must **split** this DAG into **3 separate trees**, map each separately.

This entails some clear loss of optimality, since **cannot** map across trees.

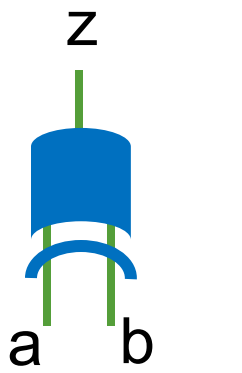
Treeifying Netlist: Result



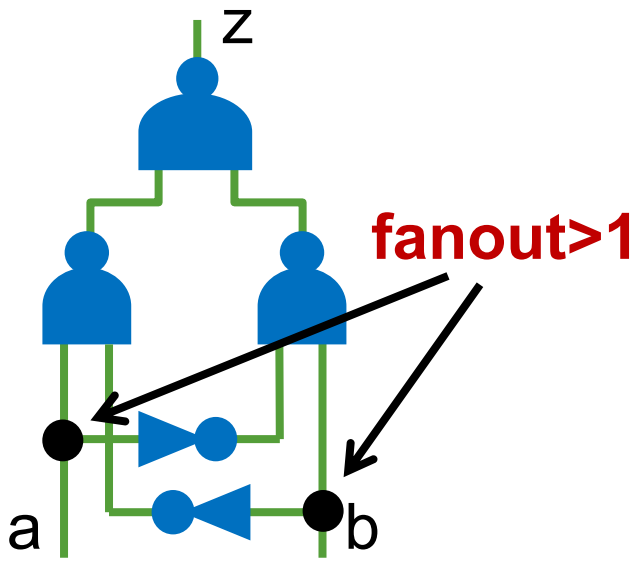
- We’re going to map these **3 trees** separately.
- Loses some optimality.
  - There are ways around these, but we won’t discuss these.

Aside: How Restrictive is "Tree" Assumption?

- Subject graph and each pattern graph **must be trees**.
  - Subject tree must be treeified.
- What about **pattern trees**?
  - Are there common, useful gates that **cannot** be trees?
  - Yes! For example, XOR gate.
  - There are tricks to deal with this, but for us, these are forbidden!



$$z = a\bar{b} + \bar{a}b$$



So, no XOR gates for mapping!

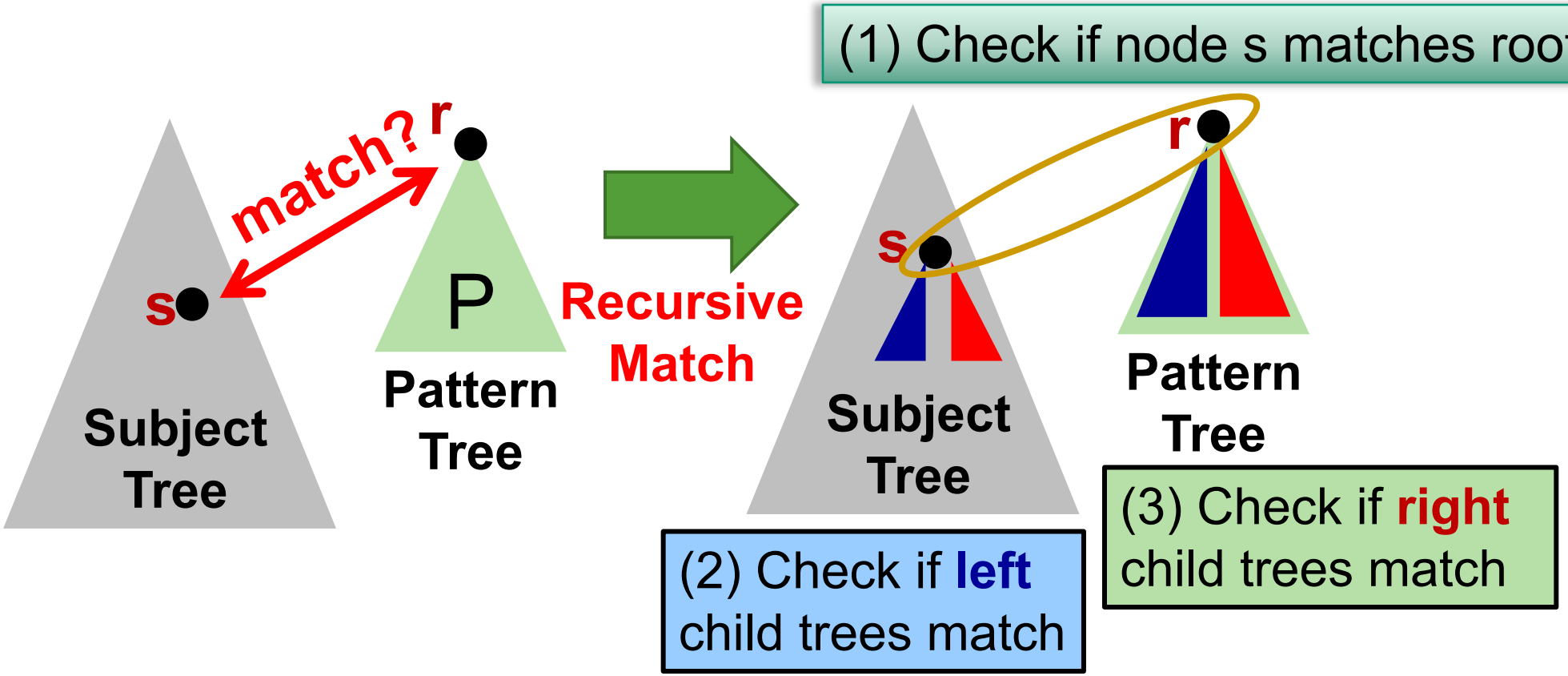
Tree Matching

- **Goal**: Determine, for every node in subject tree, what library gate can **match** (structurally).

- Straightforward approach: **Recursive matching**
  - Simple idea is to just try **every library gate** at **every node of subject tree**.
  - Library gates are small patterns – this is not too much work.
  - **Recursive** means: match **root** of subject with **root** of pattern, and then **recursively match children** of subject to **children** of pattern.

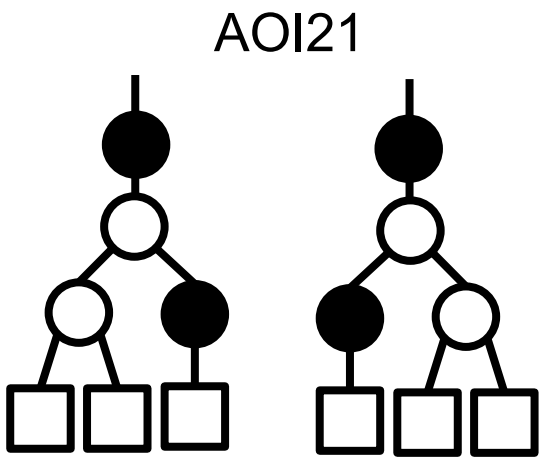
Recursive Tree Matching

- Does library pattern tree P match node s in our subject tree?
  - First, check if node s matches root r of pattern P.
  - If so, **recursively** match **left child trees** of s and r, and then **right child trees** of s and r.



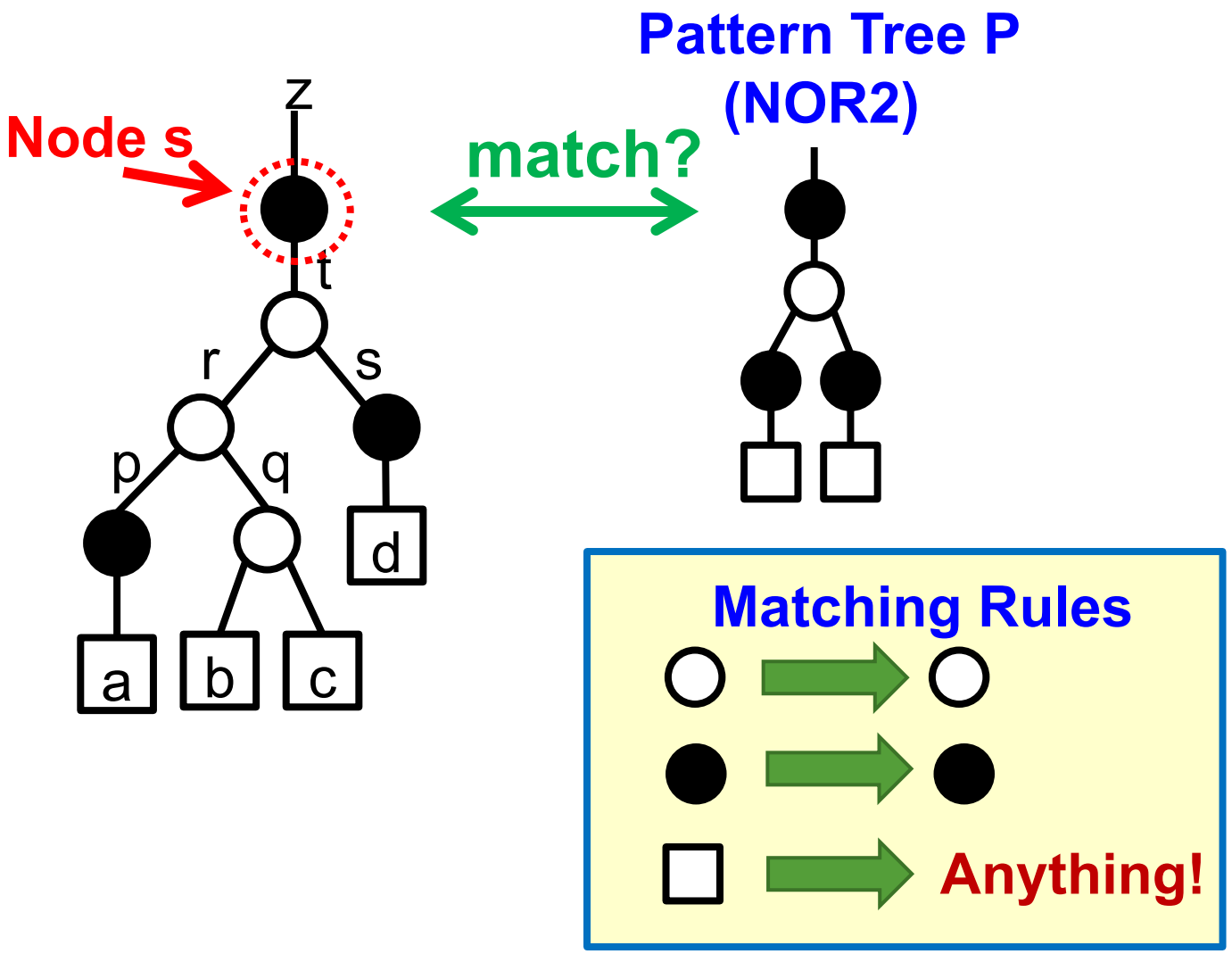
Tree Matching: One Subtlety

- Be careful matching asymmetric library patterns.
  - One example was AOI21. Need to check all possible matches by "**rotating**" the pattern tree.

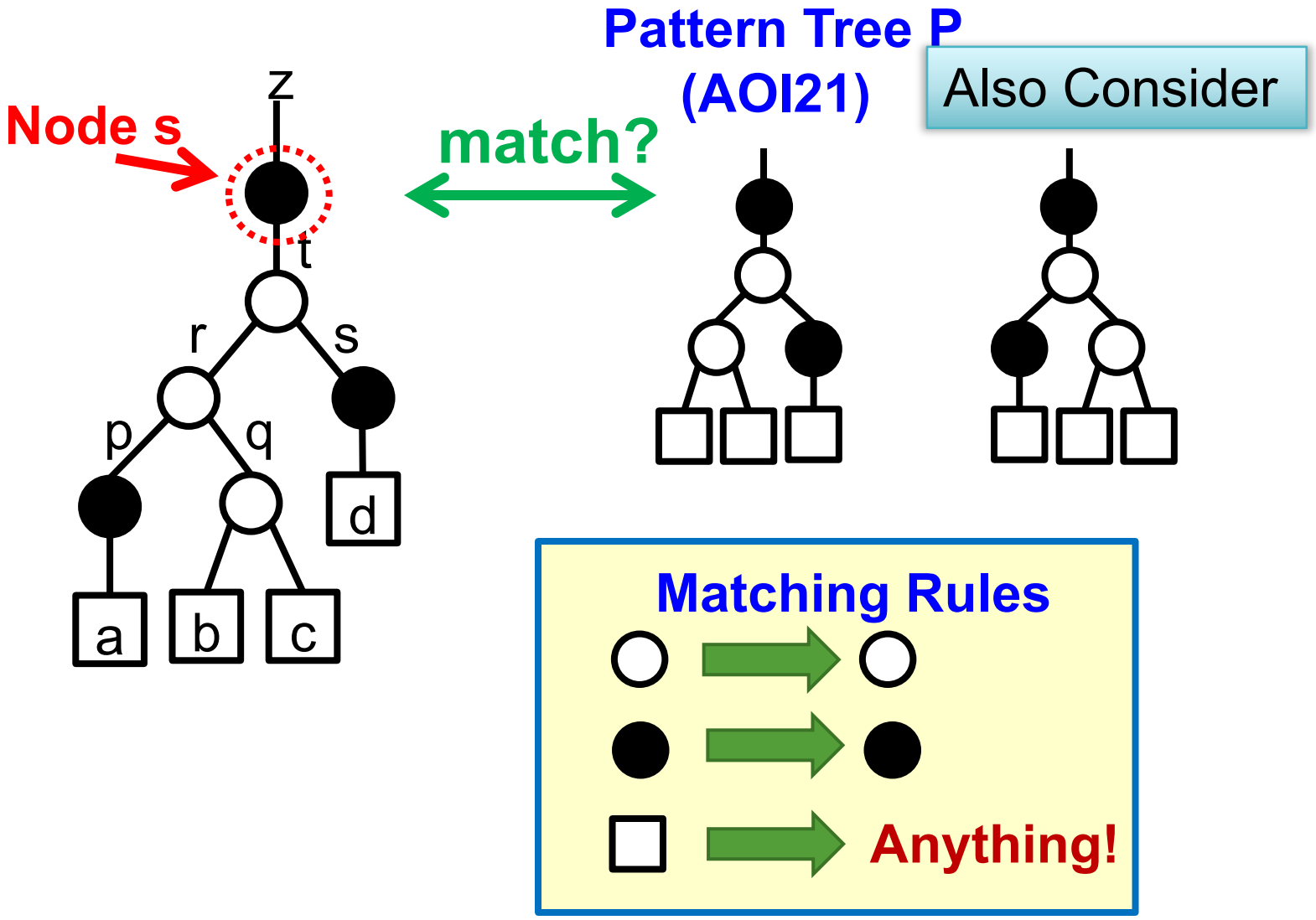


Both orientations are possible!

Tree Matching Example



Tree Matching Example

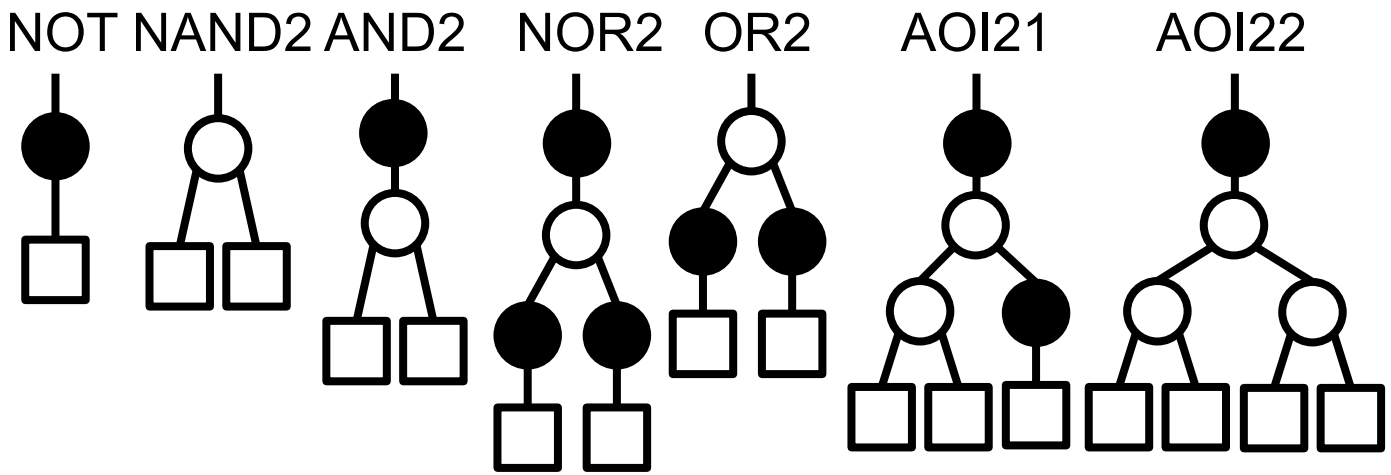


Result After Matching

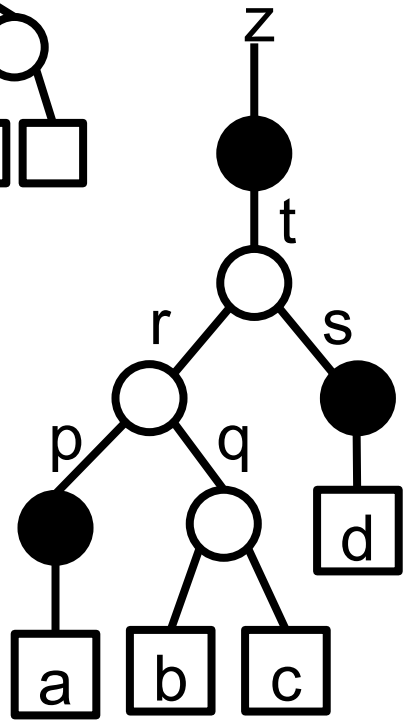
- For each internal node of subject tree, we will get which library pattern trees **match** that node.

- We **annotate** each internal node in the tree with this matching information.

Tree Matching Result Example



- **List of matching gates**
  - Node z: {NOT, AND2, AOI21}
  - Node t: {NAND2}
  - Node r: {NAND2}
  - Node s: {NOT}
  - Node p: {NOT}
  - Node q: {NAND2}



Tech Mapping via Tree Covering

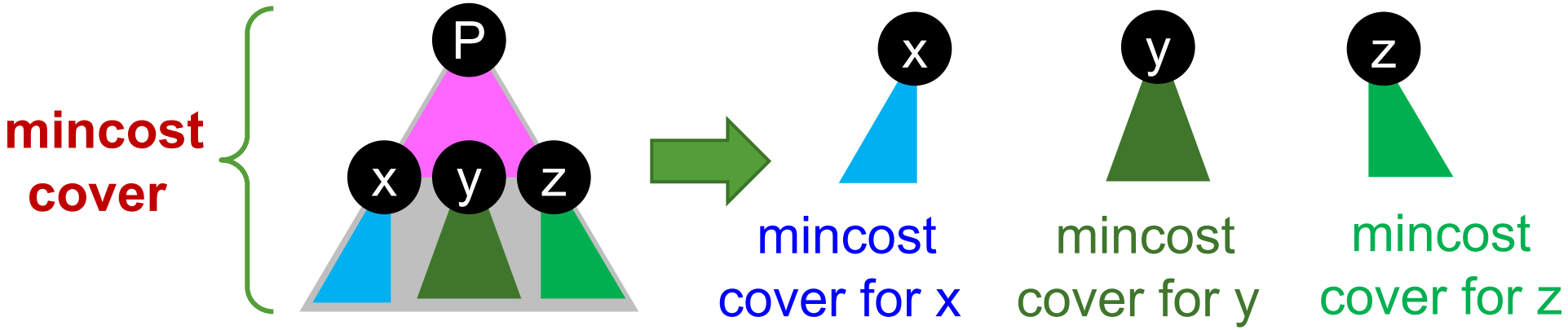
- **Subroutines**:
  - **Treeifying** the input netlist
    - Loses some optimality, but make things simple.
  - **Tree matching**
    - For each node in the subject tree, find pattern trees in library that **match**.
  - **Minimum-cost covering**
    - Assume you know what can match at each node of subject tree. Then, which ones do you pick for a **minimum cost** cover?

Minimum Cost Covering of Subject Tree

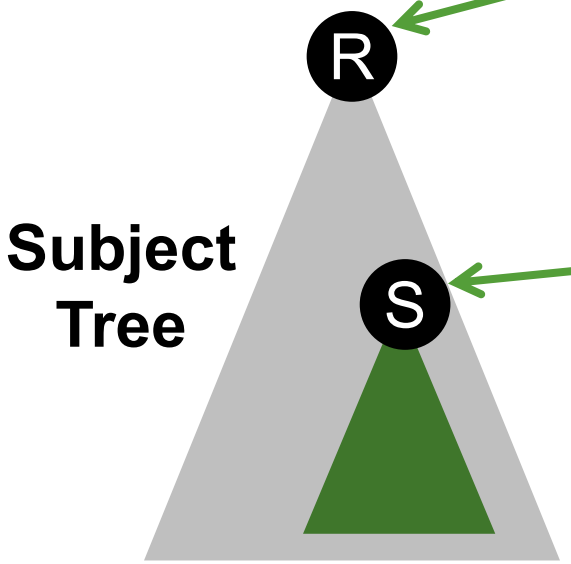
- What cover do we choose?
  - We assign a **cost** to each library pattern.
  - We choose a **minimum cost** (“**mincost**”) cover of the subject tree.

Minimum Cost Covering of Subject Tree

- One big idea makes this **easy** to do:
  - If pattern P is a **mincost** match at some node s of subject tree, then, **each leaf** of pattern tree must also be the root of some **mincost** matching pattern.
    - Why? By contraposition…
  - Leads to a nice recursive algorithm for **mincost** on **any node** in subject tree.
    - This is actually a **dynamic programming** algorithm.



Some Terminology



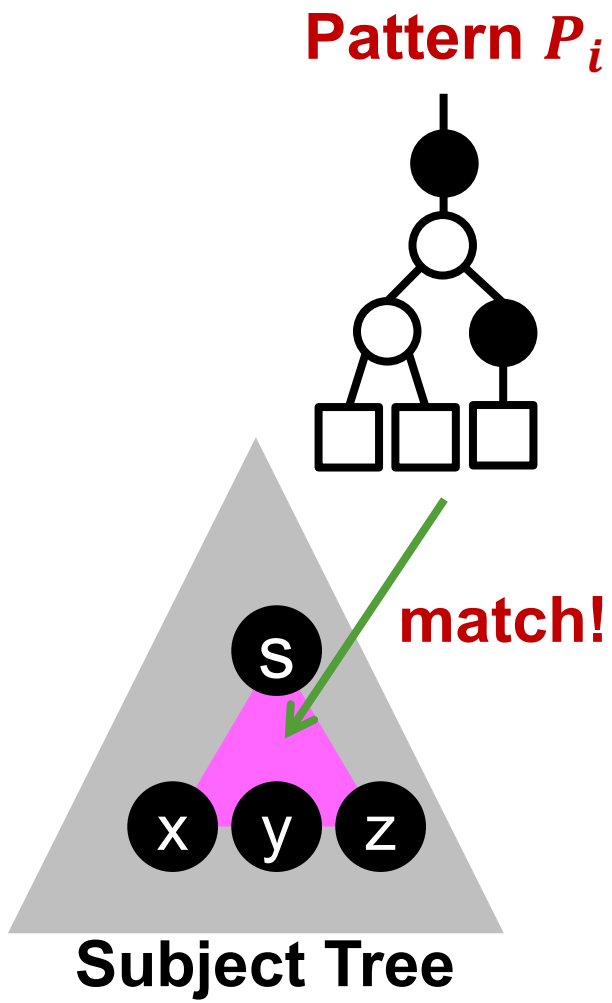
Root R of subject tree. Best cover (mapping) of this tree has cost = **mincost(R)**

Internal node s of subject tree. Best cover (mapping) of this tree has cost = **mincost(s)**

Note: we treeified the netlist. Thus, every **internal node** (like node s) is the **root** of another, **smaller tree**. This is crucial for our mapping algorithm.

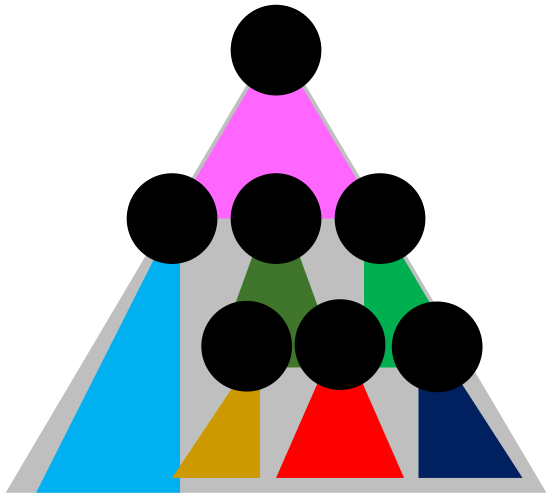
Some Terminology (cont.)

- **Suppose**:
  - Library pattern P_i matches at internal node s of the subject tree.
  - Library pattern P_i has m **input nodes**.
- Each of these m "**input nodes**" in library pattern tree P_i will be matched to some nodes in subject tree.
- We call these nodes in the subject tree **leaf nodes** for this matching library pattern tree.
  - E.g., x, y, z are leaf nodes.



Calculating Cost of Mapping

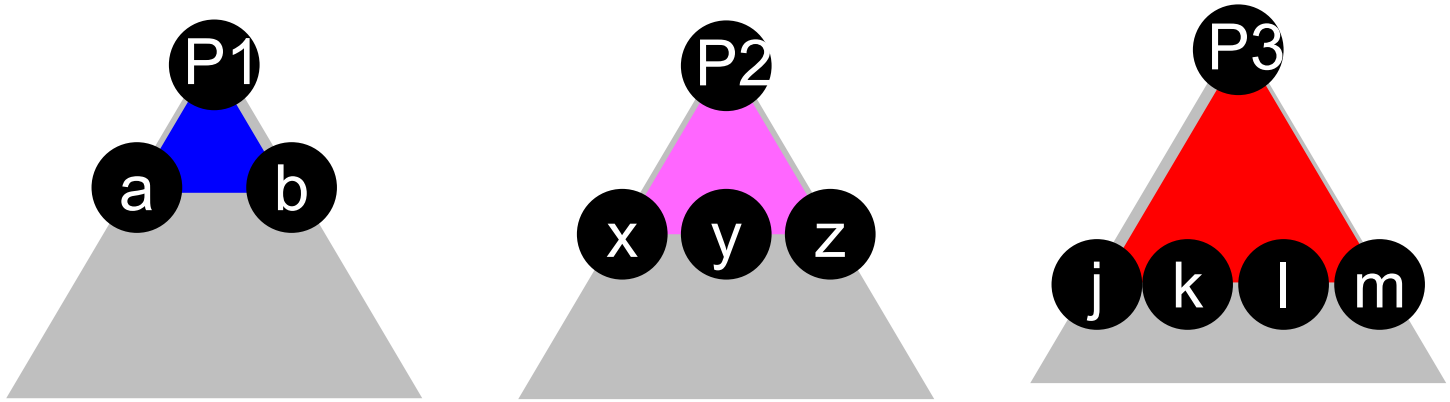
- Every gate pattern in target library has a **cost**.
  - Gate pattern P_i has $\text{cost}(P_i)$.
- To calculate cost of mapping the **entire** subject tree:
  - We add up **cost** for each node where a pattern matches, for all patterns covering subject.



The cost is the sum of the costs of 7 pattern trees.

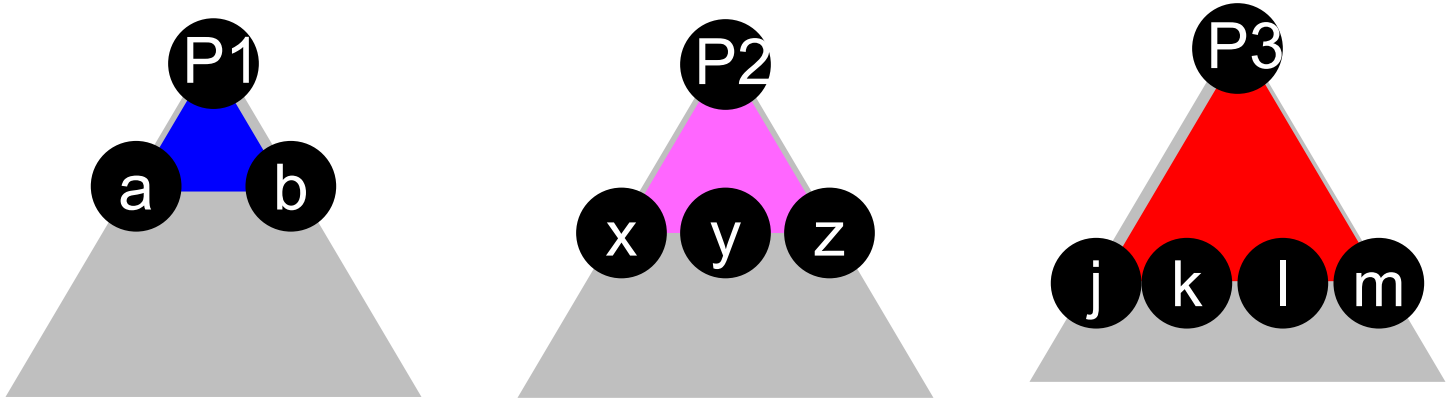
Mincost Tree Covering: The Idea

- Assume 3 **different** library patterns match at root R of subject tree:
  - Pattern $P1$ has 2 leaf nodes: a, b
  - Pattern $P2$ has 3 leaf nodes: x, y, z
  - Pattern $P3$ has 4 leaf nodes: j, k, l, m.



Which of these gates produces the **smallest** value of mincost(R)?

Mincost Tree Cover: The Idea



- Minimum cost of mapping the entire subject tree is

  mincost(R**)**

  =min{ **minimal** cost with **P1** matching root R,

  minimal cost with **P2** matching root R,

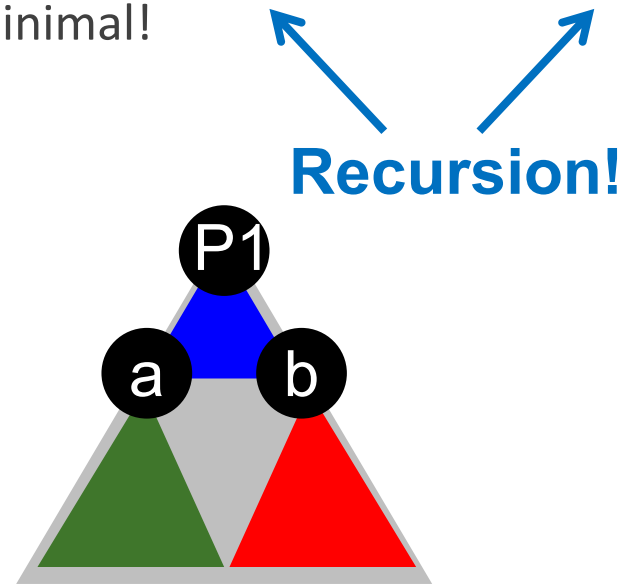
  minimal cost with **P3** matching root R**}**

What are these?

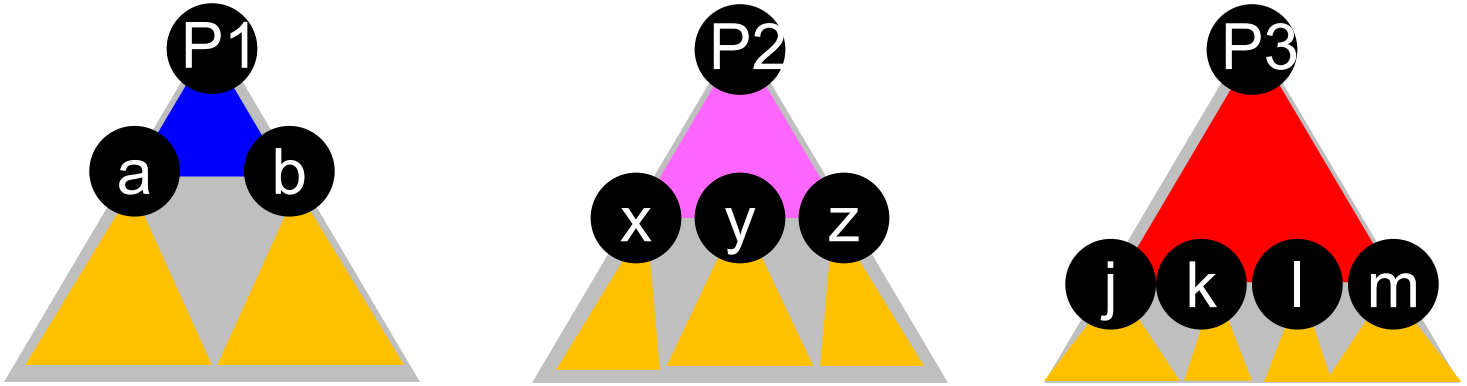
Mincost Tree Cover: Recursive Formula

- In calculating **mincost**(R), we need to answer:
  - What is **minimal** cost with **P1** matching root R?

- **Answer**: = **cost**(P1) + **mincost**(a) + **mincost**(b)
  - Otherwise, **not** minimal!



Mincost Tree Cover: Recursive Formula



- **mincost(**R**)**
  = min{ minimal cost with **P1** matching root R,
  minimal cost with **P2** matching root R,
  minimal cost with **P3** matching root R **}**

  = min{ cost(P1**) + mincost(**a**) + mincost(**b**),**
  cost(P2**) + mincost(**x**) + mincost(**y**) + mincost(**z**),**
  cost(P3**) + mincost(**j**) + mincost(**k**)**
  + mincost(l**) + mincost(**m**) }**

Mincost Cover: Algorithm

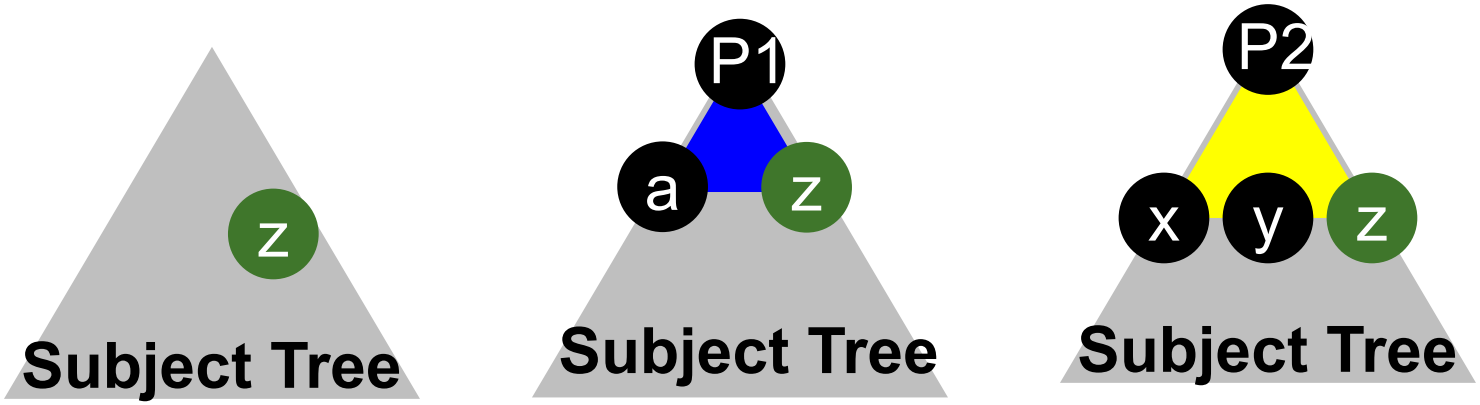
```
mincost( treenode) {
    cost = ∞
    foreach( pattern P matching at subject treenode) {
        let L = {nodes in subject tree corresponding to leaf nodes in P
            when P is placed with its root at treenode }
        newcost = cost(P)
        foreach( node n in L } {
            newcost = newcost +  mincost( n );
        }
        if ( newcost < cost ) then  {
            cost = newcost;
            treenode.BestLibPattern = P;
        }
    }
}
```

Min Cost Tree Cover

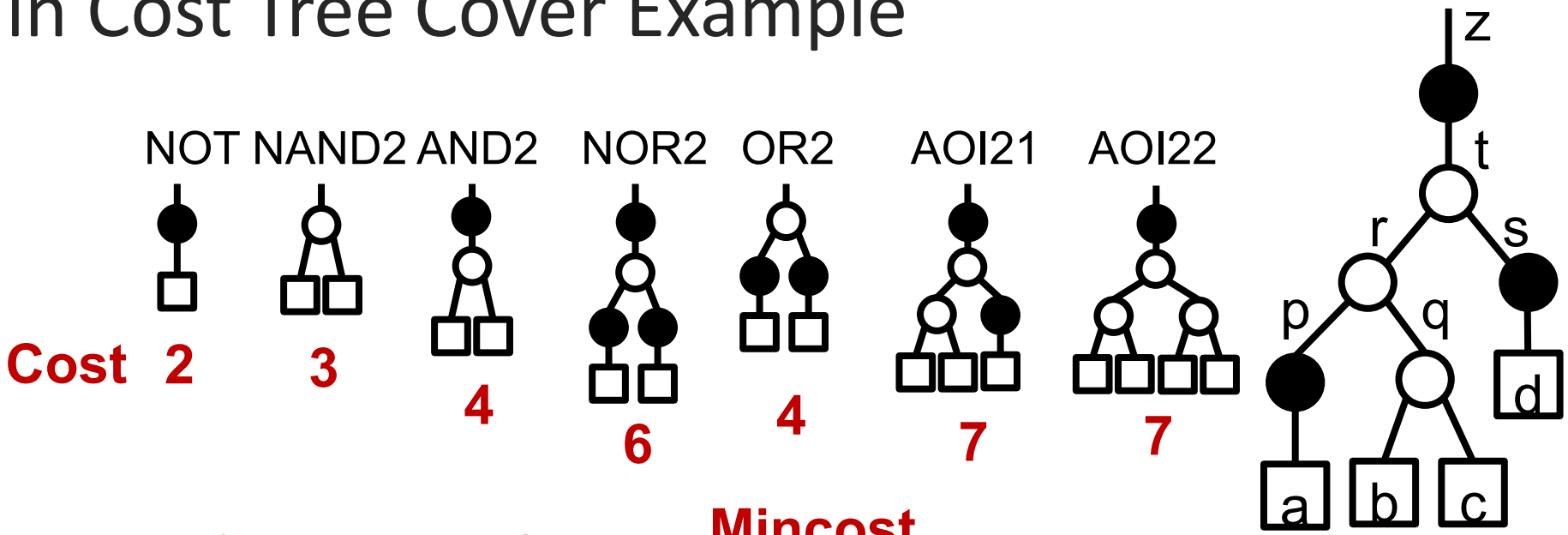
- One **redundant** computation we must note:
  - This algorithm will **revisit** same tree node many times during recursions...
  - ...and it will **recompute** the mincost cover for that node each time.
- Can we do better...?
  - Yes, just keep a table with **mincost** value for each node.
  - Start with value ∞ and when node's cost gets computed, this value gets **updated**.
  - Each time computing **mincost(node), check first** to see if **node** has been visited before computing it--saves computation!

Illustration

- Node “z” in this subject tree
  - will get its **mincost(z)** cover computed when we put **P1** at root of subject tree...
  - ...and again when we put **P2** at the root.
  - **Better solution**: just compute it **once**, first time, **save** it, and **look it up** later!

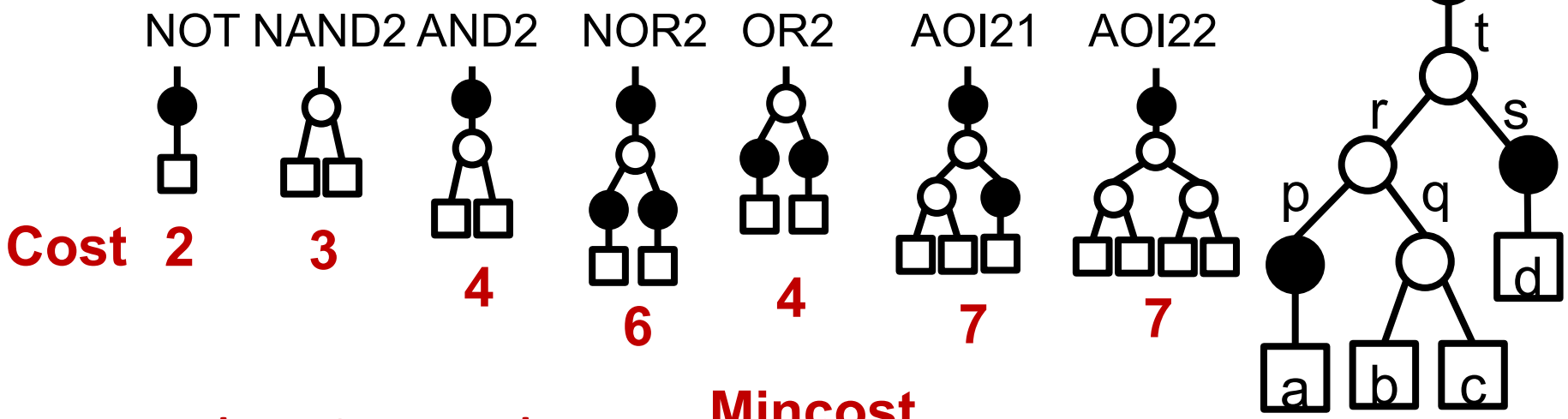


Min Cost Tree Cover Example



Node	Can Match	Mincost
z	NOT	2+mincost(t)
	AND2	4+mincost(r)+mincost(s)
	AOI21	7+mincost(p)+mincost(q)
		min
t	NAND2	3+mincost(r)+mincost(s)
r	NAND2	3+mincost(p)+mincost(q)
p	NOT	2 ⇒ mincost(p)=2
q	NAND2	3 ⇒ mincost(q)=3
s	NOT	2 ⇒ mincost(s)=2

Min Cost Tree Cover Example



Node	Can Match	Mincost
z	NOT	2+mincost(t)
	AND2	4+mincost(r)+mincost(s)
	AOI21	7+mincost(p)+mincost(q)
t	NAND2	3+mincost(r)+mincost(s)
r	NAND2	3+mincost(p)+mincost(q)
p	NOT	2
q	NAND2	3
s	NOT	2

min ⇒ mincost=12

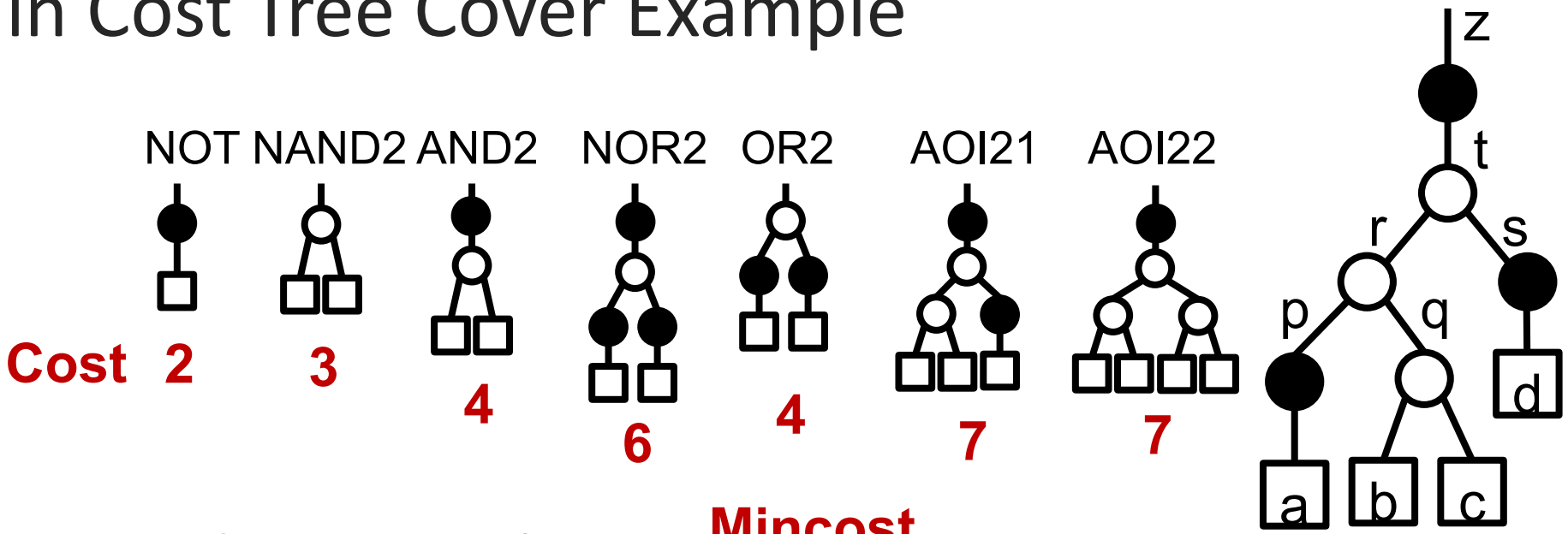
⇒ mincost(r)=8

⇒ mincost(p)=2

⇒ mincost(q)=3

⇒ mincost(s)=2

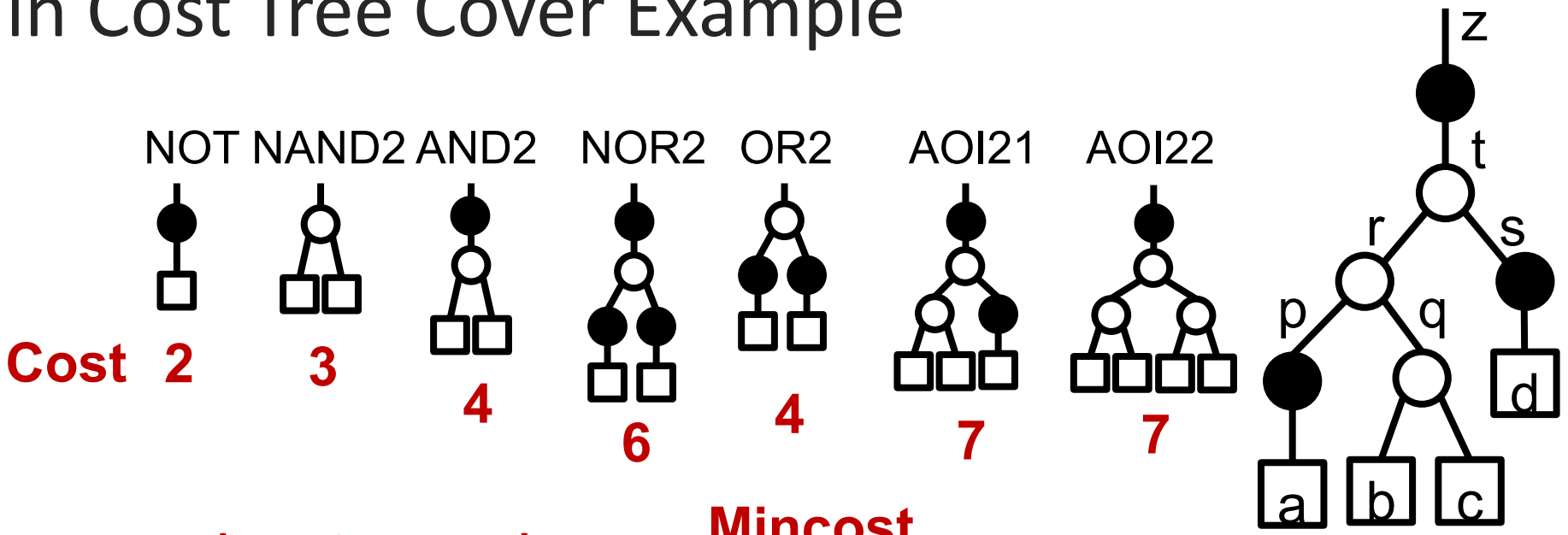
Min Cost Tree Cover Example



Node	Can Match	Mincost
z	NOT	2+mincost(t)
	AND2	4+mincost(r)+mincost(s)
	AOI21	7+mincost(p)+mincost(q)
t	NAND2	3+mincost(r)+mincost(s)
r	NAND2	3+mincost(p)+mincost(q)
p	NOT	2 ⇒ mincost(p)=2
q	NAND2	3 ⇒ mincost(q)=3
s	NOT	2 ⇒ mincost(s)=2

min
⇒ mincost=14
⇒ mincost=12
⇒ mincost(t)=13
⇒ mincost(r)=8

Min Cost Tree Cover Example



Node	Can Match	Mincost
z	NOT	2+mincost(t)
	AND2	4+mincost(r)+mincost(s)
	AOI21	7+mincost(p)+mincost(q)
t	NAND2	3+mincost(r)+mincost(s)
r	NAND2	3+mincost(p)+mincost(q)
p	NOT	2 ⇒ mincost(p)=2
q	NAND2	3 ⇒ mincost(q)=3
s	NOT	2 ⇒ mincost(s)=2

⇒ mincost=15

min

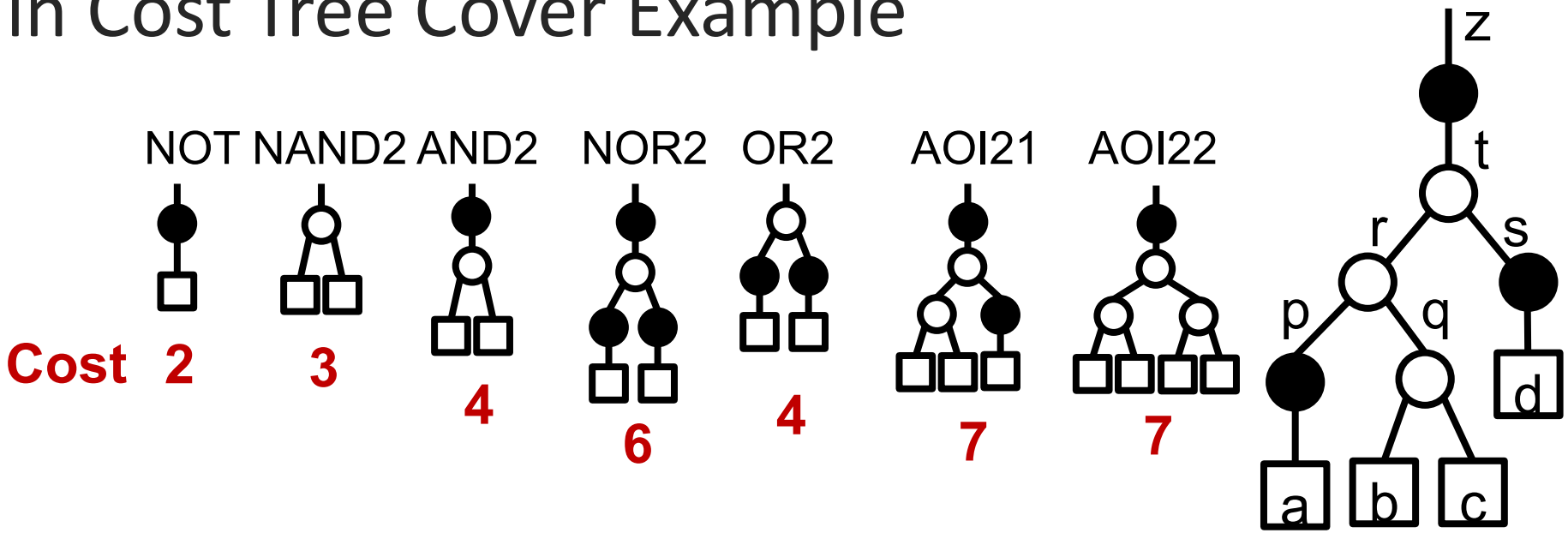
⇒ mincost=14

⇒ mincost=12

⇒ mincost(t)=13

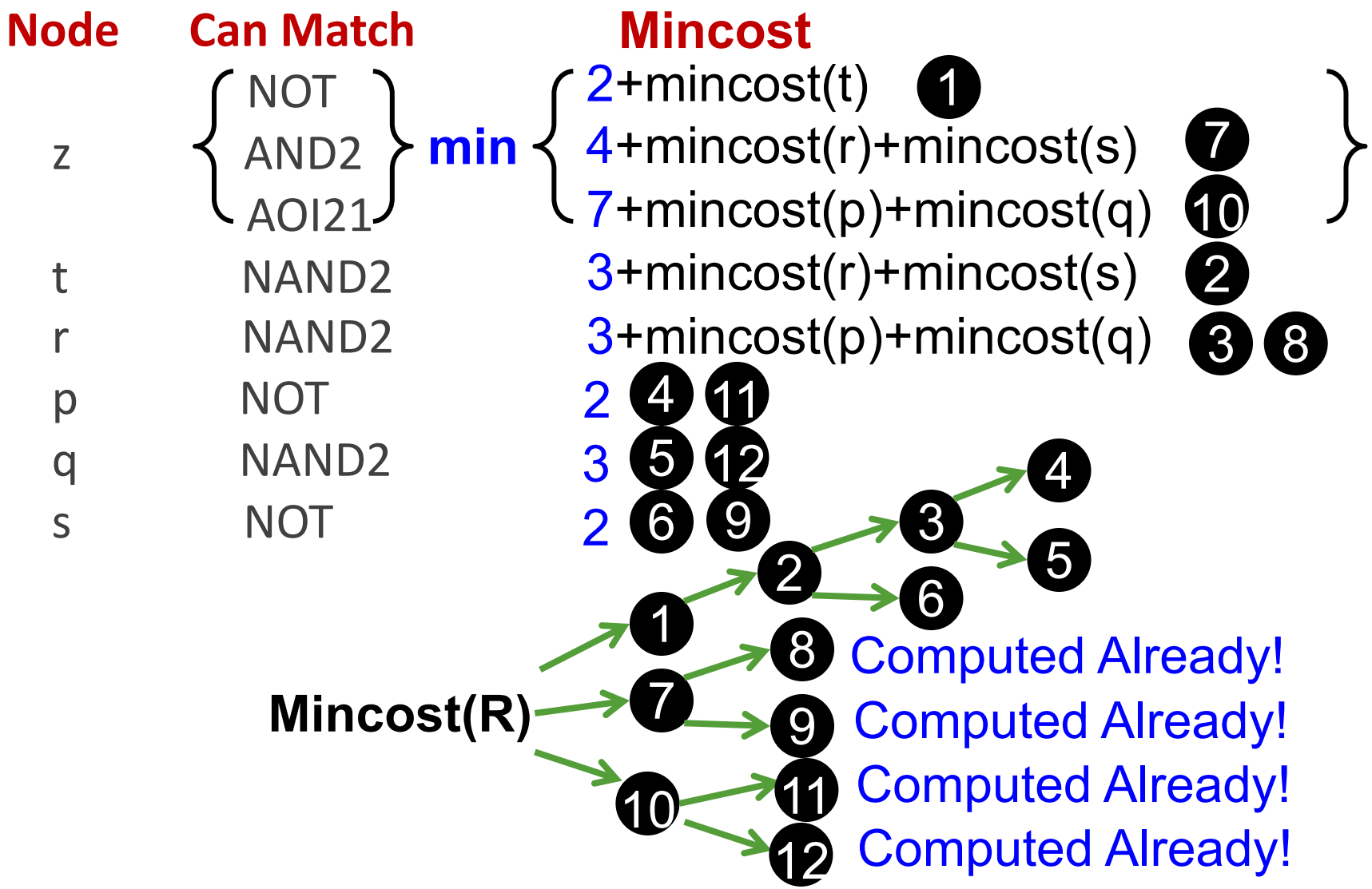
⇒ mincost(r)=8

Min Cost Tree Cover Example



Node	Can Match	Mincost	
z	NOT	15	min
	AND2	14	
	AOI21	12	Best!
t	NAND2	13	
r	NAND2	8	
p	NOT	2	
q	NAND2	3	
s	NOT	2	

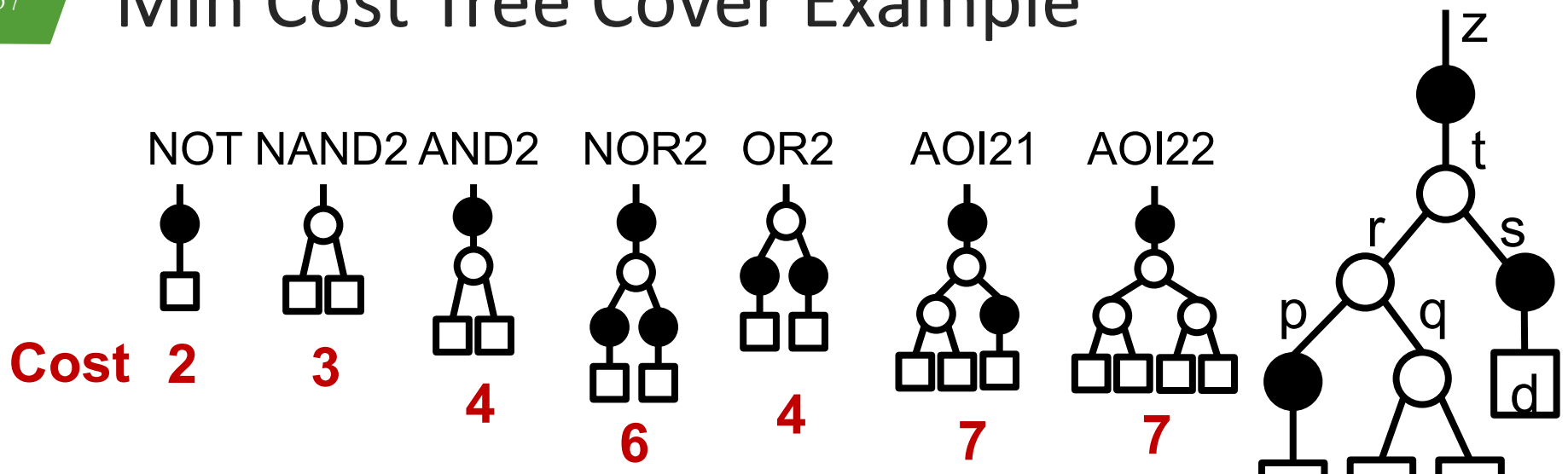
Actual Execution Sequence



Min Cost Cover: How To Get Final Cover?

- Look at **best cost** at subject root. Find pattern P at the root that gives the cost.
- Find **leaf nodes** in the subject tree for pattern P.
  - Look at the **best cost** at each of these leaf nodes.
  - Find the pattern P_i that is associated with each of these best costs.
  - Look again at leaf nodes in the subject tree that are associated with each of these patterns P_i.
    - Repeat…

Min Cost Tree Cover Example



Node	Can Match	Mincost	
z	NOT	2+mincost(t) =15	min
	AND2	4+mincost(r)+mincost(s) = 14	
	AOI21	7+mincost(p)+mincost(q) = 12	Best!
t	NAND2	3+mincost(r)+mincost(s) = 13	
r	NAND2	3+mincost(p)+mincost(q) = 8	
p	NOT	2	
q	NAND2	3	
s	NOT	2	

Min Cost Tree Cover

- Turns out to be several nice **extensions** possible
  - Can modify algorithm a little to minimize **delay** instead of cost.
  - Many interesting and useful variations, starting from this algorithm skeleton.

Technology Mapping: Summary

- Synthesis gives you "**uncommitted**" or "technology independent" design, e.g., NAND2 and NOT.
- Technology mapping turns this into **real gates** from library.
  - Can determine difference between good and bad implementations.
- Tree covering
  - One nice, simple, elegant approach to the problem.
  - 3 parts: treeify input, match all library patterns, find min cost cover.
- There are other ways to do this. Some work with real Boolean algebra in mapping.
- Has other applications, like for Lookup-Table (LUT) FPGA.
  - With different algorithm.