Abstract

This project has revolved around creating a proof checker in python. This proof checker checks proofs that are written in the Hilbert Style as seen in the book *Understanding* by Klenk. It does a reasonably good job, but could also be expanded upon a great deal. Also, because this was only for a two credit class for one semester there were certain things that I was not able to do simply due to the fact that my time was limited. I will be going over what I did during this semester, some of the research that I did.

1 QED Manifesto

The QED Manifesto is a paper that was written in *insert year* and provides an argument for the standardization of mathematical proofs. This standardization would make checking the validity of proofs much easier as it could be done with a computer program. The standardization of mathematical proofs would also have some pedagogical benefits as well.

2 Proof Checkers and Proof Assists

I have looked at various proof checkers over the course of this semester, but very few of them seem to be focused on Mathematicians and what they would like to see. I am hoping that my proof checker will require minimum programming knowledge.

3 Using the Proof Checker

The proof checker has a simple GUI interface with load, save, and confirm validity buttons. If we click confirm validity without typing anything into the text box we see at the bottom of the screen the word Valid. This is because a proof where not statements are made is valid. If we type in the letter a and nothing else and press confirm validity we get $Is\ Not\ Valid$. This is because we have not yet said anything about what a is. We do not know that it is a premise. If we type in the following line

1. a Pr

and press confirm validity we get is valid. In this we are making one premise and nothing else.

```
1. A

/A Pr 2. A

/( A*B) Pr 3. (A

/ A)*(A

/B) Dist 2 4. A

/ A Simp 3
```

4 Applications in Teaching

Here we will write out a proof of \boldsymbol{x}

 \square

C. Restrictions on the Use of C.P. and I.P.

Biconditional Exchange (B.E.)

 $(p \equiv q) :: ((p \supset q) \cdot (q \supset p))$

Distribution (Dist.)

 $(p \cdot (q \vee r)) :: ((p \cdot q) \vee (p \cdot r))$

 $(p \lor (q \cdot r)) :: ((p \lor q) \cdot (p \lor r))$

Conditional Exchange (C.E.)

 $(p \supset q) :: (\sim p \lor q)$

Exportation (Exp.)

 $((p \cdot q) \supset r) :: (p \supset (q \supset r))$

- 1. Every assumption made in a proof must eventually be discharged.
- 2. Once an assumption has been discharged, neither it nor any step that falls within its scope may be used in the proof again.
- 3. Assumptions inside the scope of other assumptions must be discharged in the reverse order in which they were made; that is, not two schope markers may cross.

D. General Instructions for Using C.P. and I.P.

- 1. For both C.P. and I.P., an assumption may be introduced at any point in the proof, provided we label it as an assumption.
- 2. In using C.P., we assume the antecedent of the conditional to be proved and then derive the consequent. In using I.P., we assume the opposite of what we want to prove and then derive a contradiction. All the steps from the assumption to the consequent (for C.P.) or the contradiction (for I.P.) are said to be within the scope of the assumption.

Quantifier Negation (Q.N.) Equivalences

1.
$$\sim (\exists x)\phi x \equiv (x) \sim \delta x$$

2.
$$\sim (x)\phi x \equiv (\exists x) \sim \phi x$$

3.
$$\sim (\exists x) \sim \phi x \equiv (x)\phi x$$

4.
$$\sim (x) \sim \phi x \equiv (\exists x) \phi x$$

STATEMENT OF THE QUANTIFIER RULES, WITH ALL NECESSARY RESTRICTIONS

A. Preliminary Definitions

- 1. ϕx is a propositional function on x, simple or complex. If complex it is assumed that it is enclosed in parentheses, so that the scope of any prefixed quantifier extends to the end of the formula.
- 2. ϕa is a formula just like ϕx , except that every occurrence of x in ϕx has been replaced by an a.

- 3. An instance of a general formula is the result of deleting the initial quantifier and replacing each variable bound by that quantifier uniformly with some name.
- 4. An a-flagged subproof is a subproof that begins with the words "flag a" and ends with some instance containing a.
- B. The Four Quantifier Rules Universal Instantiation (U.I.)

Existential Instantiation (E.I.)

$$\frac{(x)\phi x}{/ \therefore \phi a}$$

$$\frac{(\exists x)\phi x}{/ \therefore \phi a}$$
 provided we flag a

Existential Generalization (E.G.)

Universal Generalization (U.G.)

$$\frac{\phi a}{/ \therefore (\exists x) \phi x}$$

- C. Flagging Restrictions
- 1. A letter being flagged must be new to the proof; that is, it may not appear, either in a formula or as a letter being flagged, previous to the step in which it gets flagged.
- 2. A flagged letter may not appear either in the premises or in the conclusion of a proof.
- 3. A flagged letter may not appear outside the subproof in which it gets flagged.

```
#!/usr/bin/python
import re
from pyparsing import Literal, Word, ZeroOrMore, Forward, nums, oneOf, Group, srange
class Prop():
    def ___init___(self):
        pass
        self.flagset = set()
#The following two methods define wffs and check them in the proof.
    def syntax(self):
        op = oneOf( ' \setminus / -> * ::')
        lpar = Literal('('))
        rpar = Literal(')')
        statement = Word(srange('[A-Z]'), srange('[a-z]'))
        expr = Forward()
        atom = statement | lpar + expr + rpar
        expr << atom + ZeroOrMore( op + expr )</pre>
        expr.setResultsName("expr")
        return expr
    def confirm_wff(self, form1):
        expr = self.syntax()
        form1 = self.strip_form(form1)
        try:
            result = ''.join(list(expr.parseString(form1)))
        except:
            result = None
        return result == form1
#Rules of inference.
    def mp(self, form1, form2, form3):
        Checks for the correct use of Modus Ponens.
        Both A->B, A, B and A, A->B, B are valid.
        return (self.__mp_one_way(form1, form2, form3) or
                self.__mp_one_way(form2, form1, form3))
```

```
def __mp_one_way(self, form1, form2, form3): #Modus Ponens
    The first formula is split up and compared to the
    other two formulas.
    11 11 11
    a = self.split_form(form1)
    try:
        return (a[2] == 'imp' and
                self.strip_form(form2) == a[0] and
                self.strip_form(form3) == a[1])
    except:
        return False
def mt(self, form1, form2, form3):
    return (self.__mt_one_way(form1, form2, form3) or
            self.__mt_one_way(form2, form1, form3))
def __mt_one_way(self, form1, form2, form3): # Modus Tollens
    The first formula is split and compared to the other
    two.
    11 11 11
    a = self.split_form(form1)
    strip2 = self.strip_form(form2)
    strip3 = self.strip_form(form3)
    try:
        return (a[2] == 'imp' and
                strip2[0] == '~' and
                strip3[0] == '~' and
                a[0] == self.strip_form(strip3[1:]) and
```

```
a[1] == self.strip_form(strip2[1:])
                )
    except:
        return False
def hs(self, form1, form2, form3):
    return (self.__hs_one_way(form1, form2, form3) or
            self.__hs_one_way(form2, form1, form3))
def __hs_one_way(self, form1, form2, form3): #Hypothetical Syllogism
    All three formulas are split and compared to one another.
    a = self.split_form(form1)
    b = self.split_form(form2)
    c = self.split_form(form3)
    try:
        return (a[2] == 'imp' and
                b[2] == 'imp' and
                c[2] == 'imp' and
                a[0] == c[0] and
                a[1] == b[0] and
                b[1] == c[1]
    except:
        return False
def simp(self, form1, form2): #Simplification
    The first formula is split and compared to the
    second.
    11 11 11
    a = self.split_form(form1)
    strip2 = self.strip_form(form2)
```

```
try:
        return (a[2] == 'and' and
                (a[0] == strip2 or
                 a[1] == strip2)
                )
    except:
        return False
def conj(self, form1, form2, form3): #Conjunction
    Conjunction uses the simplification method to
    validate that form1 is a simplification of form3
    and form2 is a simplification of form3.
    return self.simp(form3, form1) and self.simp(form3, form2)
def dil(self, form1, form2, form3, form4):
    return (self.__dil_one_way(form1, form2, form3, form4) or
            self.__dil_one_way(form1, form3, form2, form4) or
            self.__dil_one_way(form2, form1, form3, form4) or
            self.__dil_one_way(form2, form3, form1, form4) or
            self.__dil_one_way(form3, form1, form2, form4) or
            self.__dil_one_way(form3, form2, form1, form4))
def __dil_one_way(self, form1, form2, form3, form4): #Dilemma
    tup1 = self.split_form(form1)
    tup2 = self.split_form(form2)
    tup3 = self.split_form(form3)
    tup4 = self.split_form(form4)
    return ((tup1[2], tup2[2], tup3[2], tup4[2]) == ('imp','imp','or','or')
            and \{tup3[0], tup3[1]\} == \{tup1[0], tup2[0]\}
            and \{tup4[0], tup4[1]\} == \{tup1[1], tup2[1]\})
def ds(self, form1, form2, form3):
    return (self.__ds_one_way(form1, form2, form3) or
            self.__ds_one_way(form2, form1, form3))
```

```
def __ds_one_way(self, form1, form2, form3): #Disjunctive Syllogism
       try:
            a = self.split_form(form1)
           b = self.split_form(form2)
            c = self.strip_form(form3)
            return ((a[2] == 'or' and
                    b[1] == 'neg') and
                    ((a[0] == b[0] and
                    a[1] == c)
                     or
                    (a[1] == b[0]  and
                    a[0] == c)
                     ))
        except:
            return False
   def add(self, form1, form2): #Addition
        a = self.split_form(form2)
        strip1 = self.strip_form(form1)
       try:
            return (a[2] == 'or' and
                    (a[0] == strip1 or a[1] == strip1))
        except:
            return False
#Replacement Rules
   def dn(self, form1, form2): #Double Negation
        return ((form1[:2] == '~~' and
                self.strip_form(form1[2:]) == self.strip_form(form2))
                (form2[:2] == '~~' and
```

```
self.strip_form(form2[2:]) == self.strip_form(form1))
            )
def dup(self, form1, form2):
    return (self.__dup1(form1, form2) or
            self.__dup1(form2, form1))
def __dup1(self, form1, form2): #Duplication
    a = self.split_form(form2)
    return (self.conj(form1, form1, form2) or(
            self.add(form1, form2) and
            a[0] == a[1]))
def comm(self, form1, form2): #Commutation
    a = (self.find_main_op(form1)[0], self.find_main_op(form1)[1],
         self.find_main_op(form2)[1])
    return ((a[1],a[2]) in [('or','or'),('and','and')] and
             form1[a[0]+1:] + form1[a[0]] + form1[:a[0]] == form2)
def assoc(self, form1, form2): #Association
    First we will decide which way the association rule is applied.
    Then we will apply it and finally we will decide if
    it is valid.
    11 11 11
    a = self.split_form(form1)
    try:
        if a[2] == 'or':
            return self.assocor(form1, form2)
            return self.assocand(form1, form2)
    except:
        return False
```

```
def assocor(self, form1, form2):
    try:
        a = self.split_form(form1)
        b = self.split_form(form2)
        c = self.split_form(a[0])
        d = self.split_form(b[1])
        if (a[1] == d[1] and
            b[0] == c[0] and
            c[1] == d[0] and
            (a[2],b[2],c[2],d[2]) ==
            ('or','or','or','or')):
            return True
    except:
        pass
    try:
        a = self.split_form(form1)
        b = self.split_form(form2)
        c = self.split_form(a[1])
        d = self.split_form(b[0])
        if (a[0] == d[0] and
            b[1] == c[1] and
            c[0] == d[1] and
            (a[2],b[2],c[2],d[2]) ==
            ('or','or','or','or')):
            return True
    except:
        pass
    return False
```

```
def assocand(self, form1, form2):
    try:
        a = self.split_form(form1)
        b = self.split_form(form2)
        c = self.split_form(a[0])
        d = self.split_form(b[1])
        if (a[1] == d[1] and
            b[0] == c[0] and
            c[1] == d[0] and
            (a[2],b[2],c[2],d[2]) ==
            ('and','and','and','and')):
            return True
    except:
        pass
    try:
        a = self.split_form(form1)
        b = self.split_form(form2)
        c = self.split_form(a[1])
        d = self.split_form(b[0])
        if (a[0] == d[0] and
            b[1] == c[1] and
            c[0] == d[1] and
            (a[2],b[2],c[2],d[2]) ==
            ('and','and','and','and')):
            return True
    except:
        pass
    return False
```

```
def contra(self, form1, form2):
    return (self.__contral(form1, form2) or
            self.__contral(form2, form1))
def __contral(self, form1, form2): #Contraposition
    a = self.split_form(form1)
   b = self.split_form(form2)
   try:
        return (self.strip_form(b[0][1:]) == a[1] and
                self.strip_form(b[1][1:]) == a[0] and
                a[2] == 'imp' and
                b[2] == 'imp')
    except:
        return False
def dem(self, form1, form2):
    return (self.__dem1(form1, form2) or
            self.__dem1(form2, form1))
def __dem1(self, form1, form2): #DeMorgan's
    try:
        split_form1 = self.split_form(form1)
        split_form2 = self.split_form(form2)
        if split_form1[1] != 'neg':
            return False
        split_form1 = self.split_form(split_form1[0])
        if split_form1[2] == 'and':
            return self.__demand(split_form1, split_form2)
        else:
            return self.__demor(split_form1, split_form2)
    except:
        return False
```

```
def __demor(self, split_form1, split_form2):
    a = split_form1
    b = split_form2
    try:
        return ('~' + a[0] == b[0] and
                 '^{-}' + a[1] == b[1] and b[2] == 'and')
    except:
        return False
def __demand(self, split_form1, split_form2):
    a = split_form1
    b = split_form2
    try:
        return ('~' + a[0] == b[0] and
                 '^{-}' + a[1] == b[1] and b[2] == 'or')
    except:
        return False
def be(self, form1, form2):
    try:
        return (self.__bel(forml, form2) or
            self.__be1(form2, form1))
    except:
        return False
def __bel(self, form1, form2):
    a = self.split_form(form1)
    b = self.split_form(form2)
    c = self.split_form(b[0])
    d = self.split_form(b[1])
    return (a[2] == 'equiv' and
            b[2] == 'and' and
```

```
c[2] == 'imp' and
            d[2] == 'imp' and
            a[0] == c[0] and
            a[0] == d[1] and
            a[1] == c[1] and
            a[1] == d[0]
            )
def ce(self, form1, form2):
    try:
        return (self.__ce1(form1, form2) or
            self.__ce1(form2, form1))
    except:
        return False
def __ce1(self, form1, form2):
    a = self.split_form(form1)
    b = self.split_form(form2)
    return (a[2] == 'imp' and
            b[2] == 'or' and
            '~' + a[0] == b[0] and
            a[1] == b[1]
def dist(self, form1, form2):
    try:
        return (self.__dist1(form1, form2) or
                self.__dist1(form2, form1))
    except:
        return False
def __dist1(self, form1, form2):
    try:
        a = self.split_form(form1)
```

```
b = self.split_form(form2)
        c = self.split_form(a[1])
        d = self.split_form(b[0])
        e = self.split_form(b[1])
        if a[2] == 'and':
            return self.__distand(a,b,c,d,e)
            return self.__distor(a, b, c, d, e)
    except:
        return False
def __distand(self,a,b,c,d,e):
   try:
        return (a[2] == 'and' and
                b[2] == 'or' and
                c[2] == 'or' and
                d[2] == 'and' and
                e[2] == 'and' and
                a[0] == d[0] and
                c[0] == d[1] and
                c[1] == e[1] and
                d[0] == e[0]
    except:
        return False
def __distor(self,a,b,c,d,e):
    try:
        return (a[2] == 'or' and
                b[2] == 'and' and
                c[2] == 'and' and
                d[2] == 'or' and
                e[2] == 'or' and
                a[0] == d[0] and
```

```
c[0] == d[1] and
                    c[1] == e[1] and
                    d[0] == e[0]
        except:
            return False
    def exp(self, form1, form2): #Exportation
        try:
            return (self.__exp1(form1, form2) or
                    self.__exp1(form2, form1))
        except:
            return False
    def __exp1(self, form1, form2):
        try:
            a = self.split_form(form1)
            b = self.split_form(form2)
            c = self.split_form(a[0])
            d = self.split_form(b[1])
            return (a[2] == 'imp' and
                    b[2] == 'imp' and
                    c[2] == 'and' and
                    d[2] == 'imp' and
                    a[1] == d[1] and
                    b[0] == c[0] and
                    c[1] == d[0]
        except:
            return False
#Conditional proof methods and structural checks.
    def cp(self, form1, form2, form3):
        a = self.split_form(form3)
        form1 = self.strip_form(form1)
        form2 = self.strip_form(form2)
```

```
return (form1 == a[0] and
            form2 == a[1] and
            a[2] == 'imp')
def ip(self, form1, form2, form3):
    form1 = self.strip_form(form1)
    form3 = self.strip_form(form3)
    return (self.__is_contradiction(form2) and
             (form1 == '~' + form3 or
                  form3 == '~' + form1 or
                  form1 == '~(' + form3 + ')' or
                  form3 == '^{(\prime)} + form1 + ')')
def __is_contradiction(self, form1):
    a = self.split_form(form1)
    try:
        return (a[2] == 'and' and
                 (a[0] == '^{\sim}' + a[1] \text{ or }
                  a[1] == '^{\sim}' + a[0] \text{ or }
                  a[0] == '^{(')} + a[1] + ')' or
                  a[1] == '^{(')} + a[0] + ')')
    except:
        return False
def confirm_structure(self, ip, refs):
    for tuple1 in refs:
        if not len(tuple1) == 1:
            lst1 = []
            for tuple2 in ip:
                 # if the line number is outside the scope of
                 # an assumption we must be cautious
                 if tuple1[0] > tuple2[1]:
                     lst1.append(tuple2)
            for ref in tuple1[1:]:
                 if self.__is_between(ref,lst1):
                     return False
```

return True def __is_between(self, ref, lst1): if lst1: for range1 in lst1: if (ref <= range1[1] and</pre> ref >= range1[0]): return True return False def ip_do_not_cross(self,lst1): lst2 = []for element in lst1: if (element[1] == 'assp' or element[1] == 'fs'): lst2.append(element[0]) if element[1] in ('ip','cp', 'ug'): x = lst2.pop()if not element[2] == x: return False return not bool(lst2) #Predicate Logic Methods def ui(self, form1, form2): try: $dict1 = {}$ form1 = self.strip_form(form1) form2 = self.strip_form(form2) var = form1[1]form1 = form1[4:-1]for i in range(len(form1)): if form1[i] == var: if not dict1.has_key(var):

else:

dict1[var] = form2[i]

```
return re.sub(var,dict1[var],form1) == form2
    except:
        return False
def eg(self, form1, form2):
    try:
        dict1 = {}
        form1 = self.strip_form(form1)
        form2 = self.strip_form(form2)
        var = form2[8]
        form2 = form2[11:-1]
        for i in range(len(form2)):
            if form2[i] == var:
                if not dict1.has_key(var):
                    dict1[var] = form1[i]
                else:
                    return re.sub(var, dict1[var], form2) == form1
    except:
        return False
def ei(self, form1, form2):
    try:
        dict1 = \{\}
        form1 = self.strip_form(form1)
        form2 = self.strip_form(form2)
        var = form1[8]
        form1 = form1[11:-1]
        for i in range(len(form1)):
            if form1[i] == var:
                if not dict1.has_key(var):
                    dict1[var] = form2[i]
                    break
        if dict1[var] not in self.flagset and re.sub(var,dict1[var],form1) == form
            self.flagset.add(dict1[var])
            return True
```

```
except:
        return False
def ug(self, flag, form1, form2): #Universal Generalization
    This method compares the flagged variable, the first
    formula in the Universal Generalization subproof and
    the conclusion to the subproof. The flagged variable
    is discarded if the proof is valid.
    try: #Anything that goes wrong here means that something is incorrect.
        form1 = self.strip_form(form1) #Get rid of access space
        form2 = self.strip_form(form2)
        var = form2[1]
        form2 = form2[4:-1]
        bool1 = bool(re.sub(var,flag,form2) == form1)
        if bool1:
            self.flagset.discard(flag) #Once the ug subproof is complete flagged v
            return True
        else:
            return False
    except:
        return False
def fs(self, flag):
    try:
        bool1 = bool(flag not in self.flagset)
        if bool1:
            self.flagset.add(flag)
            return True
        else:
            return False
    except:
        return False
```

```
#ON Rules
   def qn1(self, form1, form2):
        return (self.__qnloneway(form1, form2) or
                self.__qn1oneway(form2, form1))
   def __qn1oneway(self, form1, form2):
       try:
            form1 = self.strip_form(form1)
            form2 = self.strip_form(form2)
            var = form1[2]
            return (form1[0:4] == '~('+var+')' and
                    form2[0:10] == "(\\exists" + var + ")" and
                    self.split_form('~' + form1[4:]) == self.split_form(form2[10:]))
        except:
            return False
   def qn2(self, form1, form2):
       try:
            return (self.__qn2oneway(form1, form2) or
                    self.__qn2oneway(form2, form1))
        except:
            return False
   def __qn2oneway(self, form1, form2):
       try:
            form1 = self.strip_form(form1)
            form2 = self.strip_form(form2)
            var = form2[1]
            return (form1[0:11] == '~(\\exists'+var+')' and
```

```
self.split_form('~('+form1[11:]+')') == self.split_form(form2[3:])
                form2[0:3] == '('+var+')')
    except:
        return False
def qn3(self, form1, form2):
    return (self.__qn3oneway(form1, form2) or
            self.__qn3oneway(form2, form1))
def __qn3oneway(self, form1, form2):
   try:
        form1 = self.strip_form(form1)
        form2 = self.strip_form(form2)
        var = form1[2]
        return (form1[0:4] == '~('+var+')' and
                form2[0:10] == '(\\exists'+var+')' and
                self.split_form(form1[4:]) == self.split_form('~('+form2[10:]+')')
    except:
        return False
def qn4(self, form1, form2):
    return (self.__qn4oneway(form1, form2) or
            self.__qn4oneway(form2, form1))
def __qn4oneway(self, form1, form2):
   try:
        form1 = self.strip_form(form1)
        form2 = self.strip_form(form2)
       var = form2[1]
        return (form1[0:11] == '~(\\exists'+var+')' and
```

```
self.split_form(form1[11:]) == self.split_form('~('+form2[3:]+')')
                    form2[0:3] == '('+var+')')
        except:
            return False
#CQN Rules
#Utilities used by above methods.
   def strip_form(self, form):
        form = re.sub(' ','', form)
        depth = 0
        for i, char in enumerate(form):
            if char == '(':
                depth += 1
            if char == ')':
                depth -= 1
            if depth == 0 and i == len(form) -1 and len(form) > 1:
                return self.strip_form(form[1:-1])
            elif depth == 0:
                break
        return form
   def find_main_op(self, form):
        Takes a stripped formula as an argument. Not used
        directly. Used as a helper function to split_form.
        subdepth = 0
       try:
            for i, char in enumerate(form):
                if char == '(':
                    subdepth += 1
                if char == ')':
                    subdepth -= 1
                if char == '*' and subdepth == 0:
                    return (i, 'and')
                if char == '\\' and subdepth == 0:
```

if form[i+1] == '/':

```
return (i, 'or')
            if char == ':' and subdepth == 0:
                if form[i+1] == ':':
                    return (i, 'equiv')
            if char == '-' and subdepth == 0:
                if form[i+1] == '>':
                    return (i, 'imp')
        if form[0] == '~':
            return (0, 'neg')
    except:
       pass
def split_form(self, form):
    Splits a formula up into a tuple where the first element is the
    first part of the formula before the main operator, the second
    element is the second part of the formula after the main operator,
    and the third is the name of the main operator.
    form = self.strip_form(form)
    a = self.find_main_op(form)
    #checks for None
    if not a:
        return None
    if a[1] == 'neg':
        return (self.strip_form(form[1:]), 'neg')
    if a[1] in ['or','imp','equiv']:
        tuple1 = (self.strip_form(form[:a[0]]), self.strip_form(form[a[0]+2:]),
                   a[1])
    else:
        tuple1 = (self.strip_form(form[:a[0]]), self.strip_form(form[a[0]+1:]),
                   a[1])
```

return tuple1

```
#The following methods control the entire checking process.
   def confirm_validity(self, file1):
        lst1,ip,refs = self.proof_to_list(file1)
        lst2 = []
        for element in lst1:
            lst2.append(self.test(element))
        return (all(lst2) and
                self.confirm_structure(ip, refs)
                and
                self.ip_do_not_cross(lst1))
   def confirm_validity_string(self, file1):
        str1 = ("There is a problem with the " +
                "following lines: ")
        lst1,ip,refs = self.proof_to_list(file1)
        lst2 = []
        for element in lst1:
            lst2.append(self.test(element))
        if all(lst2):
            return "Proof is valid."
        else:
            for i,elem in enumerate(lst2):
                if elem == False:
                    str1 += str(i+1) + ", "
            return str1[:-2]
   def test(self, lst1):
        lst1[1]
        lst2 = []
        if lst1[0] == 'return False':
            return False
```

```
if not (lst1[1] == 'pr' or lst1[1] == 'assp'
            or lst1[1] == 'fs'):
        str1 = "self." + lst1[1] + "(*lst2)"
        for x in lst1[2:]:
            lst2.append(x)
        lst2.append(lst1[0])
        try:
            return eval(str1)
        except:
            return False
    return True
def proof_to_list(self, file1):
    lst1 = []
    lst3 = []
    for line in file1:
        line = line.rstrip()
        line = re.sub(r"\t+","\t",line)
        line = re.sub(r"\.\t+","\t-",line)
        lst2 = line.split("\t")
        if len(1st2) == 3:
            lst2 = lst2[1:]
            lst2 = self.convert1(lst2)
            lst1.append(lst2)
        elif re.sub(r"\s+","", lst2[0]):
            lst1.append(['return False','return False'])
    ip = self.__ip(lst1)
    refs = self.__refs(lst1)
    for element in lst1:
        lst2 = self.convert2(element, lst1)
        lst2[1] = lst2[1].lower()
        1st3.append(1st2)
    return (lst3,ip,refs)
```

```
def __refs(self,lst1):
    lst2 = []
    for i, element in enumerate(lst1):
        if (not isinstance(element[-1],int)
            element[-3].lower() in ('cp','ip','ug')):
            lst2.append((i+1,))
        elif not isinstance(element[-2], int):
            lst2.append((i+1,element[-1]))
        else:
            lst2.append((i+1,element[-2],element[-1]))
    return 1st2
def __ip(self,lst1):
    lst2 = []
    for element in lst1:
        try:
            if element[1].lower() in ('cp','ip','ug'):
                lst2.append((element[-2],element[-1]))
        except:
            pass
    return 1st2
def flatten(self, x):
    result = []
    for el in x:
        if hasattr(el, "__iter__") and not isinstance(el, basestring):
            result.extend(self.flatten(el))
        else:
            result.append(el)
    return result
def convert1(self, lst1):
    lst1[1] = lst1[1].split(' ')
```

```
try:
            lst1[1][1] = lst1[1][1].split(',')
        except:
            pass
        lst1 = self.flatten(lst1)
        if len(lst1) > 2:
            for i, x in enumerate(lst1[2:]):
                lst1[i + 2] = int(x)
        return 1st1
    def convert2(self, lst1, lst2):
        if not len(lst1) == 2: #Not a premise or assumption.
            for i, x in enumerate(lst1[2:]):
                lst1[i+2] = lst2[x - 1][0]
        return 1st1
    def prompt_for_file(self):
        filename = raw_input("Please enter the name of the file to be checked: ")
        return open(filename, 'r')
if __name__ == '__main__':
    a = Prop()
    print a.confirm_validity_string(file1)
#
    a.mt("Za->(Ha*Wa)","~(Ha*Wa)","~Za")
    file1 = a.prompt_for_file()
    print a.confirm_validity(file1)
    print a.split_form("(F::G) -> (A -> F )")
    file1 = open("proofs/proof14.txt",'r')
    print a.confirm_validity(file1)
```

```
#!/usr/bin/python
import unittest
from prop import Prop
class TestProp(unittest.TestCase):
    def setUp(self):
        self.prop = Prop()
        self.expr = self.prop.syntax()
#Tests for the Rules of Inference
    def test_mp(self):
        self.assertTrue(self.prop.mp("(A\\/B)->^cC","A\\/B","^cC"))
        self.assertTrue(self.prop.mp("A\\/B","(A\\/B)->~C","~C"))
        self.assertTrue(self.prop.mp("(A\\\B) \rightarrow C", "A\\\B", "C"))
        self.assertFalse(self.prop.mp("(A \setminus B)->C","A \setminus B","~C"))
        self.assertFalse(self.prop.mp("A", "A\\/B", "~C"))
    def test mt(self):
        self.assertTrue(self.prop.mt("Za->(Ha*Wa)","~(Ha*Wa)","~Za"))
        self.assertFalse(self.prop.mt("Za->(Ha*Wa)","Ha*Wa","~Za"))
        self.assertFalse(self.prop.mt("Za", "Ha*Wa", "~Za"))
    def test_hs(self):
        self.assertTrue(self.prop.hs("(A\\/B) -> (C*D)","(C*D) -> (^E*F)","(A\\/B) -> (^E*F)")
        self.assertTrue(self.prop.hs("(A\\/B) -> (D)","(D) -> (E*F)","(A\\/B) -> (E*F)"))
        self.assertTrue(self.prop.hs("(A \setminus B)->D", "(D)->(~E*F)", "(A \setminus B)->(~E*F)"))
        self.assertFalse(self.prop.hs("(A\\/B)*(D)","(D)->(~E*F)","(A\\/B)->(~E*F)"))
        self.assertFalse(self.prop.hs("(A)","(D)\rightarrow(~E*F)","(A\\/B)\rightarrow(~E*F)"))
    def test_simp(self):
        self.assertFalse(self.prop.simp("(A \setminus B) -> C", "C"))
        self.assertFalse(self.prop.simp("(A \setminus B) *~C", "C"))
        self.assertTrue(self.prop.simp("(A \setminus B) *~C", "~C"))
    def test_conj(self):
        self.assertTrue\,(self.prop.conj\,("A\\\\B","~(C->D)","\,(A\\\\\) *~(C->D)")\,)
        self.assertFalse(self.prop.conj("A", "B", "A*B*C"))
```

```
self.assertTrue(self.prop.dil("((A\\/B)->C)->(D\\/F)","(F::G)->(A->F)",
                                     "((A\\/B)->C)\\/(F::G)","(D\\/F)\\/(A->F)"))
       self.assertTrue(self.prop.dil("(F::G) -> (A->F)", "((A\\/B) -> C) -> (D\\/F)",
                                     "((A\\/B)->C)\\/(F::G)","(D\\/F)\\/(A->F)"))
   def test_ds(self):
       self.assertTrue(self.prop.ds("(^A\\/(B->C))\\/^D","^(^A\\/(B->C))","^D"))
       self.assertTrue(self.prop.ds("(~A\\/(B->C))\\/~D","~(~D)","(~A\\/(B->C))"))
       self.assertFalse(self.prop.ds("(^A\\/(B->C))\\/^D","(^D)","(^A\\/(B->C))"))
       self.assertFalse(self.prop.ds("A","(^{\circ}D)","(^{\circ}A\\/(B->C))"))
       self.assertTrue(self.prop.ds("^(B\\\))), "^(A*D)", "^(A*D)", "^(B\\\))
       self.assertTrue(self.prop.ds("~(B\\/C)\\/~(A\\/D)", "~~(A\\/D)", "~~(B\\/C)"))
   def test_add(self):
       self.assertTrue(self.prop.add("(A->B)","(A->B) \setminus /C"))
       self.assertFalse(self.prop.add("(B)","(A)"))
#Tests for the Replacement Rules
   def test dn(self):
       self.assertTrue(self.prop.dn("A","~~A"))
       self.assertTrue(self.prop.dn("~~A", "A"))
       self.assertTrue(self.prop.dn("^{-}(A->(B*C))","A->(B*C)"))
   def test_dup(self):
       self.assertTrue(self.prop.dup("A", "A*A"))
       self.assertTrue(self.prop.dup("A", "A\\/A"))
       self.assertTrue(self.prop.dup("A*A", "A"))
       self.assertTrue(self.prop.dup("A\\/A", "A"))
   def test_comm(self):
       self.assertTrue(self.prop.comm("E*F", "F*E"))
       self.assertTrue(self.prop.comm("E*(F->G)","(F->G)*E"))
   def test_assoc(self):
       self.assertTrue(self.prop.assoc("(A*B)*C", "A*(B*C)"))
       self.assertTrue(self.prop.assoc("A*(B*C)","(A*B)*C"))
       self.assertTrue(self.prop.assoc("(A*B)*(C->D)","A*(B*(C->D))"))
```

def test_dil(self):

```
self.assertTrue(self.prop.assoc("(A*B)*(C*D)","A*(B*(<math>C*D))"))
    self.assertTrue(self.prop.assoc("(A\\/B)\\/C","A\\/(B\\/C)"))
    self.assertFalse(self.prop.assoc("",""))
def test assocand(self):
    self.assertTrue(self.prop.assocand("(A*B)*C","A*(B*C)"))
    self.assertTrue(self.prop.assocand("A*(B*C)","(A*B)*C"))
    self.assertTrue(self.prop.assocand("(A*B)*(C->D)","A*(B*(C->D))"))
def test_assocor(self):
    self.assertTrue(self.prop.assoc("(A\\/B)\\/C","A\\/(B\\/C)"))
    self.assertFalse(self.prop.assoc("(A\\/B)*C","A\\/(B\\/C)"))
def test_contra(self):
    self.assertTrue(self.prop.contra("A->B", "~B->~A"))
    self.assertTrue(self.prop.contra("~B->~A", "A->B"))
    self.assertFalse(self.prop.contra("",""))
def test_dem(self):
    self.assertTrue(self.prop.dem("^(A*B)", "^A \setminus /^B"))
    self.assertTrue(self.prop.dem("~(A\\/B)","~A*~B"))
    self.assertTrue(self.prop.dem("~A\\/~B","~(A*B)"))
    self.assertTrue(self.prop.dem("~A*~B","~(A\\/B)"))
    self.assertFalse(self.prop.dem("",""))
def test be(self):
    self.assertTrue(self.prop.be("A::B","((A->B)*(B->A))"))
    self.assertTrue(self.prop.be("((A->B)*(B->A))","A::B"))
    self.assertFalse(self.prop.be("",""))
def test_ce(self):
    self.assertTrue(self.prop.ce("A->B","~A\\/B"))
    self.assertTrue(self.prop.ce("~A\\/B", "A->B"))
    self.assertFalse(self.prop.ce("",""))
def test_dist(self):
    self.assertTrue(self.prop.dist("A*(B\\/C)","(A*B)\\/(A*C)"))
    self.assertTrue(self.prop.dist("Ax*(By\\/Cz)","(Ax*By)\\/(Ax*Cz)"))
    self.assertTrue(self.prop.dist("(A*B)\\/(A*C)","A*(B\\/C)"))
    self.assertTrue(self.prop.dist("A\\/(B*C)","(A\\/B)*(A\\/C)"))
```

```
self.assertFalse(self.prop.dist("",""))
    def test_exp(self):
        self.assertTrue(self.prop.exp("(A*B)->C","A->(B->C)"))
        self.assertTrue(self.prop.exp("A\rightarrow (B\rightarrow C)","(A\star B)\rightarrow C"))
        self.assertFalse(self.prop.exp("",""))
#Predicate Logic Methods
    def test_ui(self):
        self.assertTrue(self.prop.ui("(x)(Cx->Mx)", "Ca->Ma"))
        self.assertTrue(self.prop.ui("(x)(Mx->Vx)","Ma->Va"))
        self.assertTrue(self.prop.ui("( x )( Mx -> Vx )","Ma->Va"))
        self.assertFalse(self.prop.ui("",""))
    def test_eq(self):
        self.assertTrue(self.prop.eg("Oa*Ea*Na","(\exists x)(Ox*Ex*Nx)"))
    def test_ei(self):
        self.assertTrue(self.prop.ei("(\exists x)(Ox*Ex*Nx)","Oa*Ea*Na"))
        self.assertFalse(self.prop.ei("(\exists x)(Ox*Ex*Nx)","Oa*Ea*Na"))
    def test_ug(self):
        self.assertTrue(self.prop.ug("a", "Ca->Ma", "(x) (Cx->Mx)"))
    def test_fs(self):
        self.assertTrue(self.prop.fs("a"))
        self.assertTrue(self.prop.fs("b"))
#Tests for conditional and indirect proofs.
    def test_cp(self):
        self.assertTrue(self.prop.cp("A", "F->~E", "A->(F->~E)"))
        self.assertTrue(self.prop.cp("Ax", "Fy->~Ez", "Ax->(Fy->~Ez)"))
    def test_ip(self):
        self.assertTrue(self.prop.ip("E", "I*~I", "~E"))
        self.assertTrue(self.prop.ip("E","~I*~~I","~E"))
        self.assertTrue(self.prop.ip("E", "(I) *~I", "~E"))
```

```
self.assertTrue(self.prop.ip("E", "(A->B)*^(A->B)", "^E"))
               self.assertTrue(self.prop.ip("E", "^{\sim}(A->B) *^{\sim}(A->B)", "^{\sim}E"))
               self.assertTrue(self.prop.ip("Ex"," (Ax-By)* (Ax-By)"," (Ax-By)",
               self.assertFalse(self.prop.ip("E", "~~ (A->B) \star~~ (A->B) ", "~E"))
#Tests for QN
       def test qn(self):
               self.assertTrue(self.prop.qn1("^(x)(Ax)","(\ensuremath{^{"}}(x)(Ax)"))
               self.assertTrue(self.prop.qn1("(\exists x)(^Ax)", "^(x)(Ax)"))
               self.assertTrue(self.prop.qn1("(\exists x)~(Ax)","~(x)(Ax)"))
               self.assertTrue(self.prop.qn2("~(\exists x)(Ax)","(x)(~Ax)"))
               \texttt{self.assertTrue} (\texttt{self.prop.qn3} \, (\texttt{"}^{\sim} \, (\texttt{x}) \, \texttt{"} \, (\texttt{Ax}) \, \texttt{"}, \texttt{"} \, (\texttt{\ } (\texttt{xists} \, \, \texttt{x}) \, (\texttt{\ } (\texttt{Ax}) \, \texttt{"})))
               self.assertTrue(self.prop.qn4("~(\exists x)~(Ax)","(x)(Ax)"))
#Tests for utilities
       def test_split_form(self):
               self.assertEqual(self.prop.split_form("(F::G) -> (A->F)"), ("F::G", "A->F", "imp")
               self.assertEqual(self.prop.split_form("(F::G)->(A ->F)"), ("F::G","A->F","imp"
               self.assertEqual(self.prop.split_form("(F::G) -> (A -> F )"), ("F::G","A->F","
               self.assertEqual(self.prop.split_form("(A*B) -> C"), ("(A*B)","C","imp"))
               self.assertEqual\,(self.prop.split\_form\,("~(A\\/B) \ \ \ \ ("~(A\\/B)","C","or")
               self.assertEqual(self.prop.split_form("^{(B)}/C)\/^{(A*D)}"), ("^{(B)}/C)","^{(A*D)}
               self.assertEqual(self.prop.split_form("~(A*B)"), ("A*B",'neg'))
               self.assertTrue(self.prop.split_form("A") == None)
       def test_find_main_op(self):
               self.assertEqual(self.prop.find_main_op("~(A*B)->C"), (6,'imp'))
               self.assertEqual(self.prop.find_main_op("(A \setminus B)->~C"),(6,'imp'))
               self.assertEqual(self.prop.find_main_op("((A*B)\\/(A*B))->(B\\/C"),(14,'imp'))
               self.assertEqual(self.prop.find_main_op("(A \setminus B)*C"),(6,'and'))
               self.assertEqual(self.prop.find_main_op("(A\\/B)\\/~C"),(6,'or'))
               self.assertEqual(self.prop.find_main_op("(A\\/B)::~C"),(6,'equiv'))
               self.assertEqual(self.prop.find_main_op("~(A\\/D)"),(0,'neg'))
               self.assertEqual(self.prop.find_main_op("~~(A\\/D)"),(0,'neg'))
               self.assertTrue(self.prop.find_main_op("A") == None)
               self.assertTrue(self.prop.find_main_op("") == None)
       def test_strip_form(self):
```

```
self.assertEqual(self.prop.strip_form("( A \backslash \backslash B ) -> ~C"),"(A\backslash \backslash B)->~C")
    self.assertEqual(self.prop.strip_form(" ( ( A \backslash \backslash B ) -> ~C ) "),"(A\backslash \backslash B) -> ~C"
    self.assertEqual(self.prop.strip\_form(" ( ( A \\\ B )) "),"A\\\\ B")
    self.assertEqual(self.prop.strip_form("(F::G) \rightarrow (A \rightarrow F)"), "(F::G) \rightarrow (A->F)")
    self.assertEqual(self.prop.strip_form("(x)(Cx ->Mx)"),"(x)(Cx->Mx)")
def test_confirm_structure(self):
    self.assertTrue(self.prop.confirm_structure([(7,16),(6,17),(5,18),(4,19)],
                                                    [(1,),(2,),(3,),(4,),(5,),(6,),(7,
                                                     (9,4), (10,8,9), (11,10), (12,2,11),
                                                     (13,7,12), (14,13), (15,3,6), (16,14)
                                                     (17,),(18,),(19,),(20,)]))
def test_confirm_validity(self):
    self.assertTrue(self.prop.confirm_validity(open("./proofs/proof.txt",'r')))
    self.assertTrue(self.prop.confirm_validity(open("./proofs/proof2.txt",'r')))
    self.assertTrue(self.prop.confirm_validity(open("./proofs/proof3.txt",'r')))
    self.assertFalse(self.prop.confirm_validity(open("./proofs/proof4.txt",'r')))
    self.assertFalse(self.prop.confirm_validity(open("./proofs/proof5.txt",'r')))
    self.assertFalse(self.prop.confirm_validity(open("./proofs/proof6.txt",'r')))
    self.assertTrue(self.prop.confirm_validity(open("./proofs/proof7.txt",'r')))
    self.assertTrue(self.prop.confirm_validity(open("./proofs/proof8.txt",'r')))
    self.assertTrue(self.prop.confirm_validity(open("./proofs/proof9.txt",'r')))
def test_confirm_validity_string(self):
    self.assertEqual(self.prop.confirm_validity_string(open("./proofs/proof6.txt",
                      "There is a problem with the following lines: 5, 6")
     print self.prop.confirm_validity(open("./proofs/proof16.txt",'r'))
def test_confirm_wff(self):
    self.assertTrue(self.prop.confirm_wff("A\\/B"))
    self.assertTrue(self.prop.confirm_wff("(A\\/B)"))
    self.assertTrue(self.prop.confirm_wff("(A\\/B) -> C"))
    self.assertFalse(self.prop.confirm_wff("A\\/B)"))
```

```
if __name__ == '__main__':
    unittest.main()
```