



electric potential due to point charge

The electric potential V due to a point charge q at a distance r from the charge in a vacuum (or air) is given by:

$$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r}$$

where:

- V is the electric potential,
- q is the point charge,
- r is the distance from the charge,
- ϵ_0 is the permittivity of free space ($\epsilon_0 = 8.854 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$).

Explanation:

- The electric potential at a distance r from a point charge q represents the amount of work done in bringing a unit positive charge from infinity to that point, without acceleration.
- The direction does not matter since potential is a scalar quantity—not a vector.

Key Points:

- Potential decreases as distance r increases.
- It is positive for a positive charge and negative for a negative charge.
- The formula assumes the reference point (zero potential) is at infinity.

Let me know if you want a derivation, example calculation, or application related to this formula!

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whats permittivity

Permittivity is a physical property that describes how much resistance is encountered when forming an electric field in a particular medium.

- **Definition:** Permittivity (ϵ) quantifies how easily a material allows electric field lines to pass through it.
- **Unit:** Its SI unit is **farad per meter** (F/m).
- **Symbol:** It is denoted as ϵ .

Types:

- **Permittivity of Free Space (ϵ_0):**

The permittivity of vacuum or free space is a constant:

$$\epsilon_0 = 8.854 \times 10^{-12} \text{ F/m}$$

- **Relative Permittivity (ϵ_r):**

For materials other than vacuum, ϵ_r is the ratio of the material's permittivity to ϵ_0 :

$$\epsilon_r = \frac{\epsilon}{\epsilon_0}$$

It is also called the **dielectric constant**.

Role in Electrostatics:

- Permittivity determines how much electric force exists between charges in a medium.
- Higher permittivity means the material reduces the strength of electrostatic forces between charges.

Summary:

- **Permittivity** tells us how a medium affects electric fields.
- Vacuum has the lowest possible permittivity (ϵ_0), materials like glass or water have higher permittivity.

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why are we doing electric potential due to point charge

We study **electric potential due to a point charge** because it helps us:

- **Quantify Energy:** Electric potential allows us to calculate the electric potential energy of a charge placed in the field of another charge.
- **Simplify Calculations:** Potential is a scalar quantity, making it easier to work with than electric field (which is a vector).
- **Predict Electric Effects:** Knowing the potential at any point helps us determine how charges will behave—whether they'll move and how much energy is needed or released.
- **Foundation for Other Concepts:** The concept provides a base for understanding potentials due to multiple charges, continuous charge distributions, and more complex systems like capacitors.
- **Useful in Circuits and Devices:** Electric potential is directly related to voltage, which is a key idea in electronics and electrical engineering.

In summary:

We calculate electric potential due to a point charge to understand and predict energy changes, charge movement, and electric phenomena in physics and engineering. It is a fundamental building block for all electrostatic topics.

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what's the porpous of it

The **purpose** of finding the electric potential due to a point charge is to:

- **Measure Potential Energy:** It tells us how much potential energy a unit charge would have at any point because of another charge.
- **Predict Charge Movement:** It helps determine how and where a test charge will move in the presence of the point charge (from higher to lower potential).
- **Simplify Calculations:** Since potential is a scalar, it's much easier to use for complex problems than the electric field, which is a vector.
- **Foundation for Complex Systems:** It's the building block for finding the total potential in more complicated cases (like multiple charges, distributions, and inside devices).
- **Understand Voltage:** In circuits and real-world applications, electric potential difference (voltage) is key to how energy is transferred.

In simple words:

The main purpose is to help us calculate, understand, and use the effects of electric charges on other charges and systems, including energy and voltage.

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tell me what's charge and electro there relation

Charge is a fundamental property of particles (like electrons and protons) that causes them to experience a force when placed in an electric or magnetic field.

- **Symbol:** q
- **Unit:** Coulomb (C)
- **Types:** Positive (protons), Negative (electrons)

Electro comes from the word "electric" or "electricity", and it relates to things associated with electric charge, electric fields, electric forces, and electric energy.

Relation between Charge and Electro (Electric):

- Electric phenomena (like electric field, potential, force) all arise because of the existence of charge.
- **Electric field** is created by charges; it is the region around a charge where its influence (force) can be felt by other charges.
- The **force** between two charges is described by Coulomb's Law:

$$F = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 q_2}{r^2}$$

- **Electrostatics** is the study of forces, fields, potential, and energy due to stationary (not moving) charges.

Summary:

- Charge is the source; **electro** refers to all phenomena caused by it (fields, force, potential, energy).
- Without charge, there would be no electric fields or electric effects—everything “electro” is because of charge!

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so when i say calculate the charge what does that actualy mean

When you are asked to “calculate the charge,” it usually means one of these things:

1. Calculating Total Charge (Q) from Current and Time

If you know the electric current (I , in amperes) flowing for a certain amount of time (t , in seconds), you can calculate the total charge (Q , in coulombs) that has flowed using:

$$Q = I \times t$$

This is the most common case for electrical circuits, and the result (Q) tells you the total amount of electric charge that passed through a point or a component in a given time.^{[6] [7]}

2. Calculating Charge from Number of Particles

Sometimes, you calculate charge by knowing the number of charged particles (like electrons or protons):

$$Q = n \times e$$

where n is the number of particles and e is the elementary charge (for electron/proton, $e = 1.602 \times 10^{-19}$ C).

3. Practical Meaning

To “calculate the charge” really means you are finding out how much electric charge (in coulombs) is present or has been transferred, usually based on information about current, time, or number of particles—in physics or in an actual electrical circuit.^{[7] [6]}

In summary:

It means figuring out the exact amount of electric charge (in coulombs), based on other known quantities. This helps to understand or measure how much electricity has moved or is stored.

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whats this $dW = F dx \cos 0$

The equation $dW = F dx \cos 0$ represents the infinitesimal work done when a force F moves an object through a small displacement dx in the exact same direction as the force.

- dW : Small (infinitesimal) amount of work.
- F : Magnitude of the force applied.
- dx : Small displacement in the direction of the force.
- $\cos 0$: Cosine of the angle between force and displacement (0° means both point in the same direction), so $\cos 0 = 1$.

When is it used?

- If the force and displacement are in the same direction, $\cos 0 = 1$, so $dW = F dx$.
- This relation appears in mechanics and electrostatics, especially in derivations for work done against the electric field.

Real meaning:

- You use this equation to calculate how much energy is transferred as work in moving something a little bit, by a force, in the direction of that force. [\[18\]](#) [\[19\]](#) [\[20\]](#)
- If the motion isn't exactly parallel, you would use $\cos \theta$ where θ is the angle between direction of force and displacement.

Summary:

This formula gives the work done when a force moves something over a distance, but only the part of the force in the direction of motion counts. If the direction is perfectly aligned, $\cos 0 = 1$. If the direction isn't aligned, you adjust with the cosine factor.

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whats the formula of electric fiel

The formula for the electric field depends on what situation you are looking at:

1. General Formula (From Force)

$$E = \frac{F}{q}$$

- E is the electric field (in newtons per coulomb, N/C)
- F is the force experienced by a test charge (in newtons, N)
- q is the magnitude of the test charge (in coulombs, C)
[\[28\]](#) [\[29\]](#) [\[30\]](#)

2. Formula for a Point Charge

$$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q}{r^2}$$

- Q is the source charge (in coulombs, C)
- r is the distance from the charge (in meters, m)
- ϵ_0 is the permittivity of free space (8.854×10^{-12} F/m)
[\[31\]](#) [\[32\]](#)

Key Points

- The direction of the electric field is away from positive charges and towards negative charges.
- For multiple charges, the net electric field is the vector sum of fields from each charge.

Summary:

You can use $E = F/q$ in any context, while for fields produced by point charges, $E = (1/4\pi\epsilon_0) \times (Q/r^2)$ is commonly used. Both formulas are central to electrostatics and are used to analyze forces and electric effects in physics problems.[\[29\]](#) [\[32\]](#) [\[28\]](#)

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electric field symbol

The standard symbol for electric field is \mathbf{E} (a bold, uppercase 'E'). It is used because the electric field is a vector quantity, which means it has both magnitude and direction. When written in equations, you might see E (italic for magnitude only) or \mathbf{E} (bold/with an arrow for the full vector).[\[40\]](#) [\[41\]](#) [\[42\]](#) [\[43\]](#)

Key Points

- Symbol: \mathbf{E} (vector) or E (for just the magnitude)
- Unit: newton per coulomb (N/C) or volt per meter (V/m)
- The electric field points away from positive charges and toward negative charges.

This symbol is universally used in physics for both calculations and conceptual explanations.

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what's electro static force

Electrostatic force is the force of attraction or repulsion between two electrically charged particles when their charges are at rest.

- This force is a result of the interaction between electric charges.
- **Like charges** (both positive or both negative) repel each other.

- **Opposite charges** (one positive and one negative) attract each other.

The formula for the magnitude of this force (Coulomb's Law) is:

$$F = \frac{1}{4\pi\epsilon_0} \cdot \frac{|q_1 q_2|}{r^2}$$

Where:

- F : Electrostatic force (in newtons, N)
- q_1 and q_2 : Amounts of the two charges (in coulombs, C)
- r : Distance between the charges (in meters, m)
- ϵ_0 : Permittivity of free space ($8.854 \times 10^{-12} \text{ F/m}$)

Summary:

- Electrostatic force is a fundamental force in nature that acts between charged objects.
- It is responsible for many physical phenomena, like the forces between electrons and protons in atoms, and it can be attractive or repulsive depending on the nature of the charges involved. [52] [53] [54] [55]

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so what's this kqq/r^2

The formula $k \frac{q_1 q_2}{r^2}$ is **Coulomb's Law**. It calculates the magnitude of the electrostatic force between two point charges:

- $F = k \frac{q_1 q_2}{r^2}$
 - F : Electrostatic force (in newtons, N)
 - q_1, q_2 : The quantities of each charge (in coulombs, C)
 - r : Distance between the charges (in meters, m)
 - k : Coulomb's constant ($k = 9 \times 10^9 \text{ N m}^2/\text{C}^2$, in vacuum/air). [63] [64] [65]

Meaning

- The force is **directly proportional** to the product of the two charges.
- The force is **inversely proportional** to the square of the distance between them.
- This force is **repulsive** if the charges are the same (both positive or both negative) and **attractive** if the charges are opposite (one positive, one negative). [66] [64]

Summary:

Coulomb's Law (kqq/r^2) tells us how strong the push or pull is between two charges, based on their sizes and how far apart they are. It is fundamental in electrostatics for calculating forces between particles.

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how to do integration

Integration is a mathematical process used to find the area under a curve or to reverse the process of differentiation. In physics, it often helps you calculate quantities like distance from velocity, work done by a variable force, or the total charge from a continuous distribution.

Basic Steps for Doing Integration:

1. Know the Integral Symbol:

The integral sign is \int , and it stands for "sum up many small pieces".

2. Common Formulas:

- Power Rule:

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C \quad \text{where } n \neq -1$$

- Integral of a Constant:

$$\int k dx = kx + C$$

- Sine and Cosine:

$$\int \sin x dx = -\cos x + C$$

$$\int \cos x dx = \sin x + C$$

- Exponential:

$$\int e^x dx = e^x + C$$

3. Add the Constant of Integration:

Always add $+C$ if you are doing indefinite integration (without limits).

4. Definite Integration:

If you have limits (say from a to b), calculate the anti-derivative and then substitute the limits:

$$\int_a^b f(x) dx = F(b) - F(a)$$

where $F(x)$ is the antiderivative of $f(x)$.[\[74\]](#) [\[75\]](#)

Example Calculation:

$$\int x^2 dx = \frac{x^{2+1}}{2+1} + C = \frac{x^3}{3} + C$$

Key Tips:

- Use tables of basic integrals for reference.
- Practice, as the steps depend on the function you are integrating.
- Integration is often used in physics to "sum up" continuously changing quantities over a range.

Integration is an essential tool in both mathematics and physics for calculating totals, areas, and reversing derivatives, making it crucial in many real-life problems.[\[76\]](#) [\[75\]](#) [\[74\]](#)

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how to do $1/x^2$

To integrate $\frac{1}{x^2}$, rewrite it using exponents:

$$\int \frac{1}{x^2} dx = \int x^{-2} dx$$

Then apply the power rule for integration:

\$\$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C \quad (\text{where } n \neq -1)$$

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For $n = -2$:

$$\int x^{-2} dx = \frac{x^{-2+1}}{-2+1} + C = \frac{x^{-1}}{-1} + C = -\frac{1}{x} + C$$

Final Answer:

$$\int \frac{1}{x^2} dx = -\frac{1}{x} + C$$

This result is used frequently in physics and calculus whenever you integrate functions of the form $\frac{1}{x^2}$.[\[84\]](#) [\[85\]](#)

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in the axial point derivation the v-q he took r-a why

In the axial point derivation for the electric potential (V) due to a dipole, the terms $r - a$ and $r + a$ represent the distances from the point where you're measuring the potential (point P on the axis) to each of the two charges of the dipole.

Why $r - a$ and $r + a$ Are Used

- A dipole has two charges: $+q$ at one end and $-q$ at the other, separated by distance $2a$.
- The center of the dipole is usually the reference (origin).
- To find the potential at point P along the axis at distance r from the center:
 - The distance from P to $+q$ (on the right) is $r - a$.
 - The distance from P to $-q$ (on the left) is $r + a$.

Formula Setup

- Potential due to each charge:
 - From $+q$: $V_+ = \frac{1}{4\pi\epsilon_0} \frac{q}{r-a}$
 - From $-q$: $V_- = -\frac{1}{4\pi\epsilon_0} \frac{q}{r+a}$
- The total potential at P is the sum:

$$V = \frac{1}{4\pi\epsilon_0} \left(\frac{q}{r-a} - \frac{q}{r+a} \right)$$

Reason

These $r - a$ and $r + a$ terms simply come from the geometry of the dipole configuration—they reflect the exact distances from each charge to the observation point so that you can sum their correct contributions to the total electric potential. [87] [88] [89]

This distance difference is essential for the mathematical derivation and for understanding how the potential varies with position along the axis of a dipole.

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so if i do r-a i am going to get the distance from -q to p

No, if you calculate $r - a$, you are getting the distance from the **positive charge (+q)** to point P (when P is on the axial line, and $+q$ is positioned at $x = +a$ and $-q$ at $x = -a$).

- $r + a$ gives the distance from the **negative charge (-q)** (at $x = -a$) to point P.
- $r - a$ gives the distance from the **positive charge (+q)** (at $x = +a$) to point P.

How it works:

- Assume the dipole is centered at the origin.
- $+q$ is placed at $x = +a$, $-q$ is placed at $x = -a$.
- Point P is at $x = r$.
- Distance P from $+q = r - a$.
- Distance P from $-q = r + a$.

So, $r-a$ is the distance from $+q$ to P (not $-q$ to P), and $r+a$ is the distance from $-q$ to P.
[105] [106] [107]

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so axial line go from the origin of the dipole to point p

Yes, on the axial line of a dipole, the line goes from the origin (the center point) of the dipole through both charges and then extends to the observation point P you're interested in. The axial line is also called the "end-on line" and is defined as the straight line passing through both the positive and negative charges of the dipole and extended on either side. [109] [110] [111]

Summary:

- The axial line goes through $-q$, the center, $+q$, and the observation point P (all are aligned).
- Any point P you consider along this line forms the basis for the "axial point" derivation for electric field or potential.

This setup helps simplify calculations, lets you reference distances like $r - a$ and $r + a$, and provides maximum electric field and potential strength along that direction.

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whats dipole momoent

A **dipole moment** is a physical quantity that measures the separation of positive and negative charges within a system, like in an electric dipole, which consists of two equal and opposite charges separated by a distance.

Definition and Formula

- The dipole moment (p) is given by:

$$p = q \cdot d$$

where:

- q = magnitude of one charge
- d = distance between the charges
- It is a **vector quantity**, meaning it has both magnitude and direction.

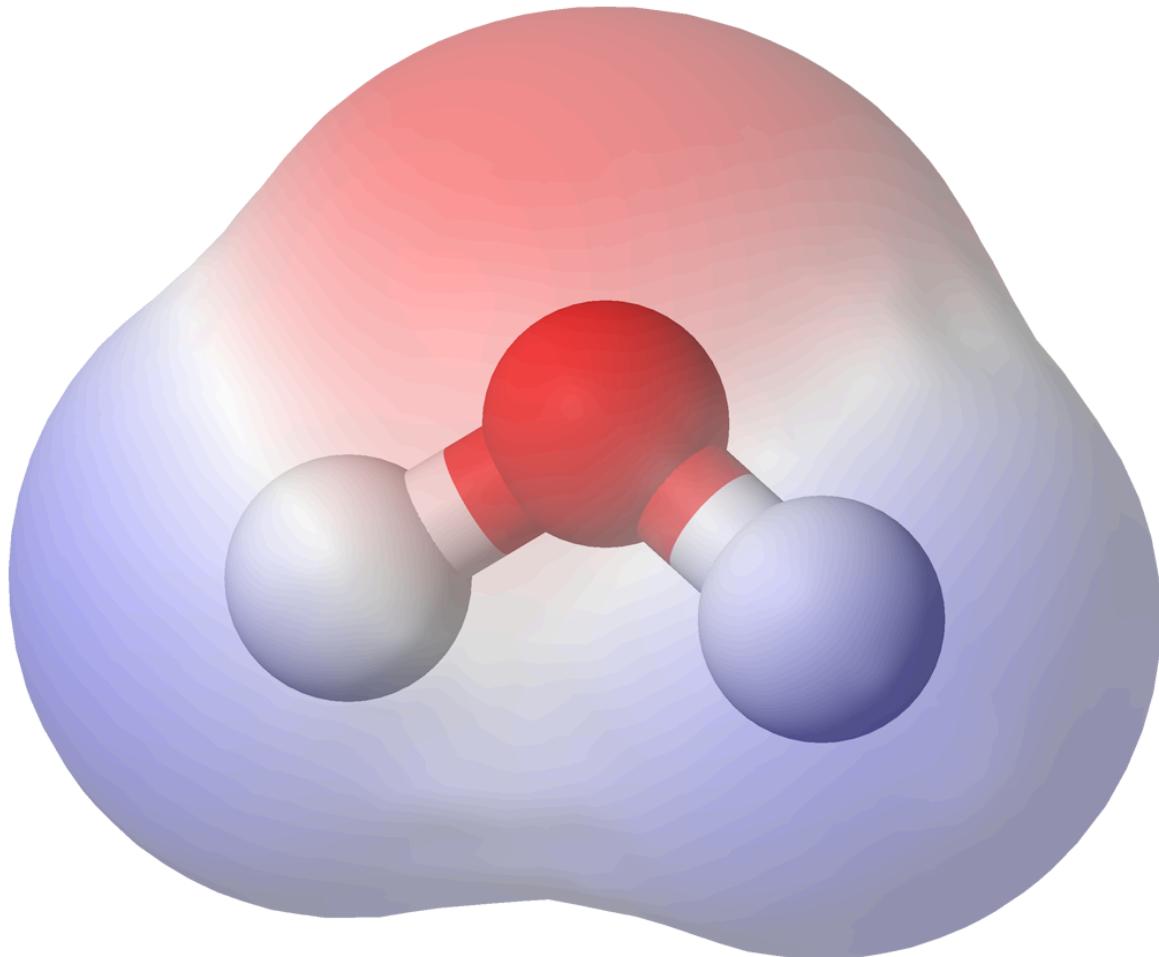
- By convention (in physics), its direction is from the negative charge to the positive charge.
- **Unit:** Coulomb-meter ($C \cdot m$) in the SI system. In chemistry, the unit Debye (D) is also used, where $1 D = 3.33564 \times 10^{-30} C \cdot m$.

Physical Meaning

- A dipole moment tells how strongly a pair of charges creates an electric field around them.
- It's important in physics (for electric dipoles) and chemistry (for molecular polarity, such as in water molecules).^[119] ^[120] ^[121] ^[122]
- The bigger the charges and the farther apart they're separated, the larger the dipole moment.

Example

- For charges $+q$ and $-q$ separated by distance d , dipole moment points from $-q$ to $+q$.
- Water (H_2O) molecules have a net dipole moment because the electrons are distributed unevenly, making the molecule polar.^[119] ^[120]



3D model of a water molecule's chemical polarity, indicating negative charge concentration near oxygen and positive charge near hydrogen atoms.

Summary:

A dipole moment measures the "strength" of an electric dipole and describes how far and how strongly charges are separated—crucial for understanding electric fields and molecular polarity.

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i don't understand

A **dipole moment** is just a way to measure how two opposite charges (like $+q$ and $-q$) are separated from each other.

Imagine This

- Take a positive charge and a negative charge.
- Place them a little distance apart—a dipole is formed.

Dipole Moment Formula

Dipole moment = charge \times distance between charges

$$p = q \cdot d$$

- If charges are bigger, or they are farther apart, the dipole moment is larger.

What Does It Mean?

- It tells us "how strong" this pair of charges acts together.
- It points from the negative to the positive charge.

Where It's Used

- In physics, it explains the electric effect of a pair of charges.
- In chemistry, it helps us know which molecules are "polar"—that is, have a slightly charged end.

In simple words:

If you stick a positive charge and a negative charge apart, their dipole moment tells you how much effect they have together—like a tiny magnet with two ends.

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measure in what way

The **dipole moment** measures two things about a pair of charges:

1. **How much charge there is:** Bigger charges create a stronger effect.
2. **How far apart the charges are:** Charges farther apart have a larger dipole effect.

What "Measurement" Means for Dipole Moment

- The **magnitude** shows the combined "pull" the two charges have because they're separated.
 - If you double the charge or double the distance, the dipole moment doubles.
- The **direction** points from the negative charge to the positive charge.
- The **unit** is coulomb-meter ($C \cdot m$), which means "coulombs separated by meters."

Real Meaning

- In physics: It tells us how strong the electric field will be around the dipole.
- In chemistry: It tells how "polar" a molecule is—if a molecule has a big dipole moment, it means one end is more positive and the other is more negative.

So, measuring the dipole moment tells you how "separated" and "strong" the effect of two opposite charges is, and points in the direction from negative to positive.

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so it says how far and how strong there forces are

Yes, exactly! The **dipole moment** tells you:

- **How far apart** the opposite charges are (distance between them).
- **How strong** their electric effect is together (proportional to the amount of charge).

A big dipole moment means:

- The charges are either large,
- Or they are far apart,
- Or both.

This combination determines how powerfully the pair of charges can create an electric field and influence other charges or molecules nearby. The dipole moment summarizes both distance and charge strength in one quantity.

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in the electric potential at an equatorial point of a dipole why we used underoot r2+a2

The reason we use $\sqrt{r^2 + a^2}$ in the electric potential derivation at an equatorial point of a dipole is because it is the distance from **each charge (+q and -q) to the point P** on the equatorial line.

Geometric Explanation

- An electric dipole has two charges: +q and -q, separated by distance 2a, centered at the origin.
- The equatorial point P is at a distance r from the center of the dipole, but at right angles to the dipole axis (the perpendicular bisector).
- The distance from either charge to point P is found by applying the **Pythagoras theorem** to the triangle formed by:
 - The line from the center to P (length r),
 - The line from the center to each charge (length a),
- The separation between charge and P is:

$$\text{Distance from charge to P} = \sqrt{r^2 + a^2}$$

Why it's Important

- When calculating potential at point P, you need the separation between each charge and P.
- Both +q and -q are at the same distance $\sqrt{r^2 + a^2}$ from P, due to symmetry.

Formula Usage

- Thus, potential from each charge at P:

$$V = \frac{1}{4\pi\epsilon_0} \left[\frac{+q}{\sqrt{r^2 + a^2}} + \frac{-q}{\sqrt{r^2 + a^2}} \right]$$

— and this distance comes directly from geometry, ensuring the correct calculation. [133] [134]

Summary:

$\sqrt{r^2 + a^2}$ is used because it is the perpendicular distance from the dipole charges to the equatorial point, found by Pythagoras, and is essential for correctly adding the potentials from both charges.

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whts the meaning of like we are trying to find the potential differenac of that equatorlal point so what we gona get fromthat

When you calculate the **electric potential at the equatorial point of a dipole**, you are actually finding the "electrical level" at that special point on the perpendicular bisector (the equator) of the dipole.

What You're Really Getting

- **Mathematically:**

The net electric potential at the equatorial point of a dipole turns out to be zero because the potential due to the $+q$ and $-q$ charges are equal in magnitude but opposite in sign, so they cancel each other out. [144] [145] [146]

- **Physically/Conceptually:**

This means that if you place a small positive test charge at the equatorial point, it does **not gain or lose electric potential energy** from the dipole's electric field at that exact position—the "push" from both charges is perfectly balanced.

What You Can Use This For

- **Understanding symmetry:** The equatorial point is a position of perfect balance between the two charges.
- **Predicting behavior:** Since the potential is zero, a test charge placed there won't move "uphill" or "downhill" in potential due to the dipole alone.
- **Solving problems:** This fact is used to simplify calculations in problems involving dipoles, and it's a key part of understanding how electric fields and potentials behave in symmetric setups.

Summary:

Finding the potential at the equatorial point tells you that—because of the symmetry and opposite signs—the electric "push" at that point is canceled out, and the potential is exactly zero due to the dipole at that spot. [145] [146] [144]

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at electric potential at any general point due to a dipole for shot dipole why did we use $2a \cos\theta$ for $r_2 - r_1$

The reason $2a \cos\theta$ appears for $r_2 - r_1$ when calculating electric potential at a general point due to a **short dipole** is because of the geometry and symmetry of the dipole and how far the point P is from the dipole.

Step-by-Step Explanation

- A dipole has charges $+q$ and $-q$ separated by a distance $2a$.
- You want the potential at point P, which is at a distance r from the center of the dipole and at an angle θ to the axis.
- The distance from P to $+q$ (r_2) and to $-q$ (r_1) depends on both r , a , and θ .
- For a **short dipole** (where $a \ll r$), you can approximate the difference in distances using trigonometry:

$$r_2 - r_1 \approx 2a \cos \theta$$

Here, this comes from the projection of $2a$ (separation between the charges) along the line joining the center to point P, using the cosine of the angle between dipole axis and the line OP.

Why is this done?

- It simplifies the formula for the potential at point P, as the exact distances are hard to use.
- When the dipole is small relative to the distance to P, the difference in distances ($r_2 - r_1$) is mainly the "shadow" or projection of the dipole length in the direction you're measuring ($\cos \theta$).
- This trick makes the formula manageable and connects the result directly to the dipole moment and the angle.

In short:

We use $2a \cos \theta$ because, for a short dipole, it is the approximate difference in distance from P to each charge, projected onto the direction of interest—making the math much simpler and letting us express the potential in terms of dipole moment ($p = 2aq$) and the angle θ .^[154] ^[155] ^[156] ^[157] ^[158]

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so in this derivation for axial why we use 0 deg

In the derivation for the axial point of a dipole, 0° (zero degrees) is used because the observation point lies **along the axis** of the dipole, in line with both charges and the dipole's center.

Why Is 0° Used?

- On the **axial line**, the vector from each charge to the observation point P is perfectly aligned with the dipole axis.
- The angle (θ) between the dipole's axis and the line connecting to the point P is exactly 0° .
- The cosine of 0° is 1:

$$\cos 0^\circ = 1$$

- In equations for electric potential or electric field, terms like $\cos\theta$ appear because physics uses the projection of vectors. On the axis, this projection is maximized.

Physical Meaning

- Using 0° means the "effect" of the dipole is strongest along its axis.
- It simplifies math in formulas involving the dipole, since you substitute $\cos 0^\circ = 1$, making calculations straightforward for the axial case.

Summary:

We use 0° because on the axial line, the dipole and the observation point are perfectly lined up, making the angle between them zero and maximizing the dipole's electric effect in that direction.

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why electric field of a are uniform at a equipoen.....

When you ask why the electric field of a charged plate (or inside something like a parallel plate capacitor) is **uniform** at an equipotential surface, it's because of two main reasons:

1. Uniform Field Means Same Strength and Direction

- In a parallel plate capacitor or between large charged plates, the electric field lines are **straight, parallel, and equally spaced**, indicating that the field has the same magnitude and direction everywhere between the plates.
- Every point at a given distance from the plate experiences the same push (force per unit charge) from the electric field, so the field is called "uniform".^[166] ^[167]

2. Equipotential Surfaces and Work

- An **equipotential surface** is a surface where the electric potential (voltage) is the same everywhere.
- Since the electric field is always **perpendicular** to equipotential surfaces, and these surfaces are parallel planes in a uniform field, moving along the surface requires **no work** (no voltage change).
- This only works when the electric field doesn't change its size or direction—meaning the field must be uniform for the equipotential to be truly "flat" and equally spaced.^[168] ^[166]

Summary

The electric field is uniform at an equipotential surface (like between two parallel plates) because it is created by charges in such a way that every part of the surface feels the same electric "force," and moving on the surface doesn't involve going "up" or "down" in electric potential—the field acts equally everywhere there.^[167] ^[166]

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Derivation of the Parallel Plate Capacitor Formula

Let's work through the derivation step-by-step, focusing on understanding each part rather than just memorizing formulas. Feel free to ask questions at any step!

Step 1: Concept - What is a Parallel Plate Capacitor?

A parallel plate capacitor consists of two conducting plates separated by a small distance (d), with area A . One plate has charge $+Q$ and the other $-Q$.

Step 2: Electric Field Between the Plates

The plates create a **uniform** electric field between them:

$$E = \frac{\sigma}{\epsilon_0}$$

Where:

- $\sigma = \frac{Q}{A}$ is the surface charge density.
- ϵ_0 is the permittivity of free space.

So,

$$E = \frac{Q}{A\epsilon_0}$$

Step 3: Potential Difference Between Plates

Potential difference (voltage) between plates is found by:

$$V = E \cdot d$$

So plug in E :

$$V = \frac{Q}{A\epsilon_0} \cdot d$$

Step 4: Capacitance Formula

Capacitance C is defined as:

$$C = \frac{Q}{V}$$

Plug in V :

$$C = \frac{Q}{Qd/(A\epsilon_0)} = \frac{A\epsilon_0}{d}$$

So, **final formula** for parallel plate capacitor:

$$C = \frac{\epsilon_0 A}{d}$$

Review Quiz!

- Can you explain why the field is uniform between the plates?
- What would happen if you increase the area A ? What about decreasing d ?

Quick Summary

- Capacitance increases with bigger area and smaller separation.
- The uniform field makes calculations simple.
- Formula: $C = \frac{\epsilon_0 A}{d}$

Would you like a deeper explanation for any step, or want to try the next concept yourself? If you tell me your course or grade level, I can make future steps even more tailored!

**

What's surface charge density

Surface charge density is a measure of how much electric charge is spread over a surface.

Definition and Formula

- It is defined as the **amount of total electric charge per unit area** on a surface.^[178] ^[179]
- The symbol for surface charge density is σ (Greek sigma).
- The formula is:

$$\sigma = \frac{q}{A}$$

where:

- σ = surface charge density (in C/m²)
- q = total charge on the surface (in coulombs)
- A = area of the surface (in square meters).^[180] ^[181]

Explanation

- Surface charge density tells you **how concentrated the charge is** on a surface.
- It is used for conductors like the plates of a capacitor, where charge distributes itself across the surface.
- If charge is spread over a large area, the surface charge density is smaller; if concentrated on a smaller area, it is larger.

Example

If a plate has 5 coulombs of charge and covers an area of 10 m^2 :

$$\sigma = \frac{5}{10} = 0.5 \text{ C/m}^2$$

Summary:

Surface charge density (σ) quantifies how much electric charge is distributed over a given surface area—it's essential for describing electric fields on such surfaces.[\[181\]](#) [\[178\]](#) [\[180\]](#)

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Capacitance of an Isolated Spherical Capacitor

Let's break down what the **capacitance of an isolated sphere** means and how it is derived.

What is an Isolated Spherical Capacitor?

- Imagine a single, conducting sphere of radius R carrying charge Q , far away from other conductors.
- It is "isolated" because there's no nearby second sphere or shell to share charge with.
- The potential of the sphere is measured with respect to infinity (where potential is zero).

Step-by-Step Derivation

1. Electric Potential of a Charged Sphere:

- The electric potential V at the surface of a sphere of radius R carrying charge Q , with the reference point at infinity, is:

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{R}$$

2. Definition of Capacitance:

- Capacitance C is defined as:

$$C = \frac{Q}{V}$$

3. Substitute the Expression for V :

- Plug in for V :

$$C = \frac{Q}{\frac{1}{4\pi\epsilon_0} \frac{Q}{R}}$$

4. Simplify:

- Q cancels:

$$C = 4\pi\epsilon_0 R$$

The Final Formula

$$C = 4\pi\epsilon_0 R$$

- **Capacitance of an isolated spherical conductor depends only on its radius.**
- ϵ_0 is the permittivity of free space ($8.85 \times 10^{-12} \text{ F/m}$).
- Larger spheres can "hold" more charge for the same potential.

Quick Check

- **If you double the radius, capacitance doubles.**
- The formula shows why small charged spheres have low capacitance (they need high potential to hold tiny charge).

Practice Question

If a sphere has radius 0.1-m , what is its capacitance?

If you'd like to see worked examples, how this compares with two-sphere capacitors, or want to relate it to practical questions (e.g., why thunderstorms charge clouds), let me know your course or grade level for a tailored explanation!

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1. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
2. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
3. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
4. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
5. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
6. <https://www.geeksforgeeks.org/physics/electric-charge-formula/>
7. <https://studymind.co.uk/notes/charge-flow-calculations/>
8. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
9. <https://www2.tntech.edu/leap/murdock/books/v4chap1.pdf>
10. <https://study.com/skill/learn/how-to-calculate-total-charge-in-coulombs-of-an-arrangement-of-protons-and-electrons-explanation.html>
11. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
12. <https://byjus.com/physics/electric-charge/>
13. <https://www.mathsisfun.com/physics/electric-charge-calcs.html>
14. <https://www.youtube.com/watch?v=VD009jiZreo>
15. <https://www.youtube.com/watch?v=94ERqNRr6Ro>

16. https://en.wikipedia.org/wiki/Electric_charge
17. <https://www.vedantu.com/question-answer/find-the-number-of-electrons-in-1-coulomb-charge-class-1-1-physics-cbse-5fc71ff42b01962f7a3a7510>
18. [https://phys.libretexts.org/Bookshelves/University_Physics/University_Physics_\(OpenStax\)/Book:_University_Physics_I-/Mechanics_Sound_Oscillations_and_Waves\(OpenStax\)/07:_Work_and_Kinetic_Energy/7.02:_Work](https://phys.libretexts.org/Bookshelves/University_Physics/University_Physics_(OpenStax)/Book:_University_Physics_I-/Mechanics_Sound_Oscillations_and_Waves(OpenStax)/07:_Work_and_Kinetic_Energy/7.02:_Work)
19. https://www.reddit.com/r/PhysicsStudents/comments/r6e3y1/for_work_in_classical_physics_why_is_dw_fdx_and/
20. https://courses.lumenlearning.com/suny_physics/chapter/7-1-work-the-scientific-definition/
21. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
22. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
23. <https://www.khanacademy.org/science/physics/work-and-energy/work-and-energy-tutorial/v/power>
24. https://courses.lumenlearning.com/suny_osuniversityphysics/chapter/7-1-work/
25. <https://www.animations.physics.unsw.edu.au/jw/work.htm>
26. <http://labman.phys.utk.edu/phys135core/modules/m6/work.html>
27. <https://www.youtube.com/watch?v=HBdIH5bVWh0>
28. <https://byjus.com/electric-field-formula/>
29. <https://www.keysight.com/used/us/en/knowledge/formulas/electric-field-formula>
30. https://courses.lumenlearning.com/suny_physics/chapter/18-4-electric-field-concept-of-a-field-revisit_ed/
31. <https://study.com/learn/lesson/electric-field-formula-magnitude.html>
32. <https://www.vedantu.com/physics/electric-field-due-to-point-charge>
33. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
34. <https://allen.in/jee/physics/electric-field>
35. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
36. <https://openstax.org/books/physics/pages/18-3-electric-field>
37. https://en.wikipedia.org/wiki/Electric_field
38. <https://testbook.com/physics/dimensions-of-electric-field>
39. <https://www.youtube.com/watch?v=V9RLc9EX1so>
40. https://en.wikipedia.org/wiki/Electric_field
41. <https://physics.info/symbols/>
42. <https://physics.info/electric-potential/>
43. <https://www.vedantu.com/question-answer/find-the-symbols-that-have-standard-meanings-a-class-12-physics-cbse-5f97371cf231cf558a3735a9>
44. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
45. <https://openstax.org/books/physics/pages/18-3-electric-field>
46. <https://www2.tntech.edu/leap/murdock/books/v4chap2.pdf>
47. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
48. <https://digilent.com/reference/learn/fundamentals/circuits/electrical-fields/start>
49. <https://byjus.com/jee/electric-field/>

50. <https://www.keysight.com/used/us/en/knowledge/formulas/electric-field-formula>
51. <https://www.physicsclassroom.com/class/estatics/Lesson-4/Electric-Field-Intensity>
52. <https://www.doubtnut.com/qna/645684764>
53. <https://www.sciencefacts.net/electrostatic-force.html>
54. <https://www.vedantu.com/physics/electrostatic-force>
55. <https://fiveable.me/key-terms/principles-physics-i/electrostatic-force>
56. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
57. https://www.shaalaa.com/question-bank-solutions/explain-in-your-own-words-and-give-one-example-electrostatic-force_130178
58. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
59. <https://en.wikipedia.org/wiki/Electrostatics>
60. <https://byjus.com/physics/electrostatics/>
61. <https://testbook.com/physics/what-is-electrostatic-force>
62. https://en.wikipedia.org/wiki/Coulomb's_law
63. https://en.wikipedia.org/wiki/Coulomb's_law
64. <https://www.vedantu.com/jee-main/physics-coulombs-law>
65. <https://electricalengineering123.com/coulombs-law-definition-equation-formula/>
66. <https://www.physicsclassroom.com/class/estatics/lesson-3/coulomb-s-law>
67. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
68. https://chem.libretexts.org/Courses/Saint_Marys_College_Notre_Dame_IN/CHEM_342:_Bio-inorganic_Chemistry/Readings/Week_1:_Analysis_of_Periodic_Trends/1.1:_Concepts_and_principles_that_explain_periodic_trends/1.1.1:_Coulomb's_Law
69. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
70. <https://byjus.com/jee/coulombs-law/>
71. <https://www.youtube.com/watch?v=kCp5yYjo9zE>
72. <https://www2.tntech.edu/leap/murdock/books/v4chap1.pdf>
73. <https://www.siyavula.com/read/za/physical-sciences/grade-11/electrostatics/09-electrostatics-02>
74. <https://byjus.com/neet/definite-integration-and-its-applications-class-11-physics/>
75. <https://articles.outlier.org/a-beginners-guide-to-integrals>
76. <https://people.math.sc.edu/josephcf/Teaching/142/Files/Lecture%20Notes/Chapter8/8.pdf>
77. [https://math.libretexts.org/Bookshelves/Calculus/Calculus_\(OpenStax\)/06:_Applications_of_Integration/6.05:_Physical_Applications_of_Integration](https://math.libretexts.org/Bookshelves/Calculus/Calculus_(OpenStax)/06:_Applications_of_Integration/6.05:_Physical_Applications_of_Integration)
78. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
79. https://www.youtube.com/watch?v=_5q01yZJ2-w
80. <https://www.youtube.com/watch?v=APRGt-zJCck>
81. https://www.youtube.com/watch?v=w2hSKNRv_64
82. <https://www.youtube.com/watch?v=zOxaUIRkFG0>
83. <https://www.teachoo.com/5643/728/Integration-Formulas---Trig--Definite-Integrals-Properties-and-more/category/Miscellaneous/>
84. <https://people.math.sc.edu/josephcf/Teaching/142/Files/Lecture%20Notes/Chapter8/8.pdf>

85. <https://www.teachoo.com/5643/728/Integration-Formulas---Trig--Definite-Integrals-Properties-and-more/category/Miscellaneous/>
86. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
87. <https://www.vedantu.com/question-answer/drive-an-expression-for-the-electric-field-due-class-12-physics-cbse-5f501eb9bb9e930be1942b16>
88. <https://www.doubtnut.com/qna/56434636>
89. <https://www.doubtnut.com/qna/642520985>
90. <https://www.scribd.com/document/617447315/ELECTRIC-FIELD-AT-A-POINT-ON-AXIAL-LINE-55f08b72-abb0-40f8-b836-e1d7d5e4a08a>
91. https://www.shaalaa.com/question-bank-solutions/derive-an-expression-for-the-electric-potential-at-any-point-along-the-axial-line-of-an-electric-dipole_100811
92. <https://www.youtube.com/watch?v=4CJNh43cbo>
93. <https://allen.in/dn/qna/642520985>
94. <https://www.vedantu.com/question-answer/derive-an-expression-for-magnetic-field-at-a-class-12-physics-cbse-5fc9f667d048b6036e136591>
95. https://www.youtube.com/watch?v=C_18PffU2_s
96. <https://assets.vmou.ac.in MPH04.pdf>
97. <https://www.vedantu.com/question-answer/derive-an-expression-for-the-electric-potential-class-12-physics-cbse-5f5bf49f68d6b37d16e3b6e4>
98. <https://www.youtube.com/watch?v=AXgVDLYVwy0>
99. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
100. <https://byjus.com/physics/electric-field-intensity-at-any-point-due-to-an-ideal-dipole/>
101. <https://www.doubtnut.com/qna/606265805>
102. <https://www.youtube.com/watch?v=rI8vqxY7ds>
103. <https://www.youtube.com/watch?v=2T43-z2jyw0>
104. <https://askfilo.com/user-question-answers-smart-solutions/find-the-expression-for-the-electric-potential-at-a-point-on-3135313830393738>
105. <https://www.doubtnut.com/qna/56434636>
106. <https://www.doubtnut.com/qna/642520985>
107. <https://www.vedantu.com/question-answer/drive-an-expression-for-the-electric-field-due-class-12-physics-cbse-5f501eb9bb9e930be1942b16>
108. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
109. <https://www.doubtnut.com/qna/647397646>
110. <https://www.doubtnut.com/qna/647282897>
111. <https://askfilo.com/user-question-answers-smart-solutions/why-do-we-find-the-axial-line-in-a-dipole-3336363739303734>
112. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
113. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
114. <https://byjus.com/physics/electric-field-intensity-at-any-point-due-to-an-ideal-dipole/>
115. <https://forum.prutor.ai/index.php?threads%2Fexplain-electric-dipole-axial-and-equatorial-line.17536%2F>

116. <https://www.vedantu.com/question-answer/drive-an-expression-for-the-electric-field-due-class-12-physics-cbse-5f501eb9bb9e930be1942b16>
117. <https://www.youtube.com/watch?v=fMfsbrJZzR4>
118. <https://allen.in/dn/qna/646644657>
119. <https://byjus.com/chemistry/dipole-moment/>
120. https://en.wikipedia.org/wiki/Electric_dipole_moment
121. <https://www.geeksforgeeks.org/physics/dipole-moment/>
122. <https://www.vedantu.com/physics/electric-dipole-moment>
123. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
124. <https://www.doubtnut.com/qna/417326576>
125. <https://byjus.com/physics/electric-dipole/>
126. https://www.shaalaa.com/question-bank-solutions/define-electric-dipole-moment-write-its-si-unit_49484
127. https://phys.libretexts.org/Courses/University_of_California_Davis/UCD:_Physics_9C__Electricity_and_Magnetism/1:_Electrostatic_Fields/1.4:_Dipoles
128. <https://en.wikipedia.org/wiki/Dipole>
129. https://www.youtube.com/watch?v=p_l_8hl-Gok
130. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
131. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
132. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
133. <https://www.doubtnut.com/qna/606266378>
134. <https://www.vedantu.com/physics/electric-potential-dipole>
135. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
136. <https://www.geeksforgeeks.org/physics/potential-due-to-an-electric-dipole/>
137. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
138. <https://www.doubtnut.com/qna/646835481>
139. <https://testbook.com/question-answer/the-electric-potential-at-the-equatorial-point-of--5fafaf223057e55bf19273d14>
140. <https://askfilo.com/user-question-answers-smart-solutions/derive-the-formula-for-electric-potential-due-to-an-electric-3236353436383832>
141. <https://askfilo.com/user-question-answers-smart-solutions/q-30-electric-potential-at-an-equatorial-point-of-a-small-31353533373737>
142. <https://allen.in/dn/qna/647933408>
143. <https://www.youtube.com/watch?v=uLGV0uR436Q>
144. <https://www.doubtnut.com/qna/606266378>
145. <https://testbook.com/question-answer/the-electric-potential-at-the-equatorial-point-of--5fafaf223057e55bf19273d14>
146. <https://www.vedantu.com/physics/electric-potential-dipole>
147. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
148. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>

149. <https://byjus.com/physics/electric-potential-dipole/>
150. <https://allen.in/dn/qna/56434764>
151. <https://www.aakash.ac.in/important-concepts/physics/electric-field-at-a-point-due-to-dipole>
152. <https://www.doubtnut.com/qna/56434636>
153. <https://www.geeksforgeeks.org/physics/potential-due-to-an-electric-dipole/>
154. <https://www.youtube.com/watch?v=L8QF3Tp3c9U>
155. https://www.youtube.com/watch?v=utY112E_Nlc
156. <https://www.geeksforgeeks.org/physics/potential-due-to-an-electric-dipole/>
157. https://www.shaalaa.com/question-bank-solutions/derive-an-expression-for-electrostatic-potential-due-to-an-electric-dipole_224288
158. <https://www.doubtnut.com/qna/11964098>
159. <https://www.scribd.com/document/863144202/L-1-Electric-potential>
160. <https://www.youtube.com/watch?v=64g8MKCfqrk>
161. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
162. <https://www2.tntech.edu/leap/murdock/books/v4chap4.pdf>
163. <https://www.doubtnut.com/qna/646835481>
164. <https://www.vedantu.com/question-answer/derive-an-expression-for-electric-potential-at-class-12-physics-cbse-5f36246b46b55f26db163abd>
165. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
166. <https://askfilo.com/user-question-answers-smart-solutions/q-19-i-derive-the-expression-for-an-electric-field-at-a-3139303933363930>
167. <https://www.slideshare.net/slideshow/electric-field-due-to-dipole/174909689>
168. <https://allen.in/dn/qna/643190577>
169. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
170. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
171. <https://www.doubtnut.com/qna/422318043>
172. <https://www.aakash.ac.in/important-concepts/physics/electric-field-at-a-point-due-to-dipole>
173. <https://www.youtube.com/watch?v=YLZPjJI7L4I>
174. <https://www.doubtnut.com/qna/56435651>
175. <https://testbook.com/question-answer/the-angle-between-the-electric-field-due-to-dipole--60784cd845d59ceb35893065>
176. <https://byjus.com/physics/torque-on-dipole/>
177. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
178. https://en.wikipedia.org/wiki/Charge_density
179. <https://www.vedantu.com/physics/surface-charge-density-formula>
180. <https://www.geeksforgeeks.org/physics/surface-charge-density-formula/>
181. <https://testbook.com/physics-formulas/surface-charge-density-formula>
182. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
183. https://en.wikipedia.org/wiki/Surface_charge

184. <https://www.youtube.com/watch?v=9Hf-v8-WTtY>
185. <https://www.vedantu.com/formula/surface-charge-density-formula>
186. <https://www.doubtnut.com/qna/647282855>
187. <https://byjus.com/surface-charge-density-formula/>
188. <https://www.doubtnut.com/qna/12296638>
189. <https://www.youtube.com/watch?v=9Hf-v8-WTtY&t=5765s>