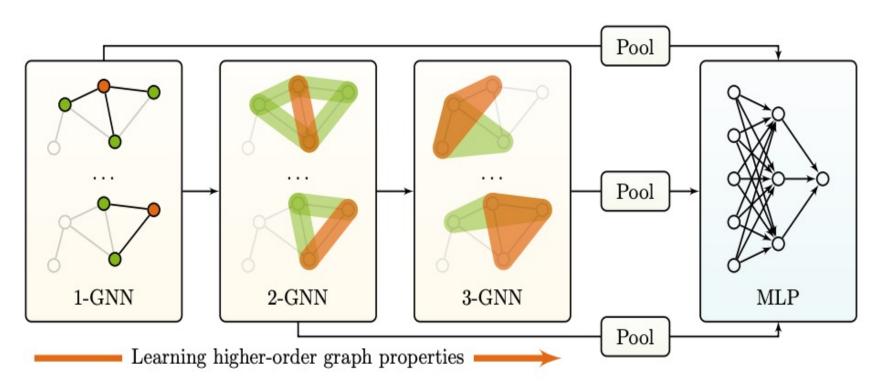
Comparative Study of GCN and HGConv: Structure, Features, and Noise

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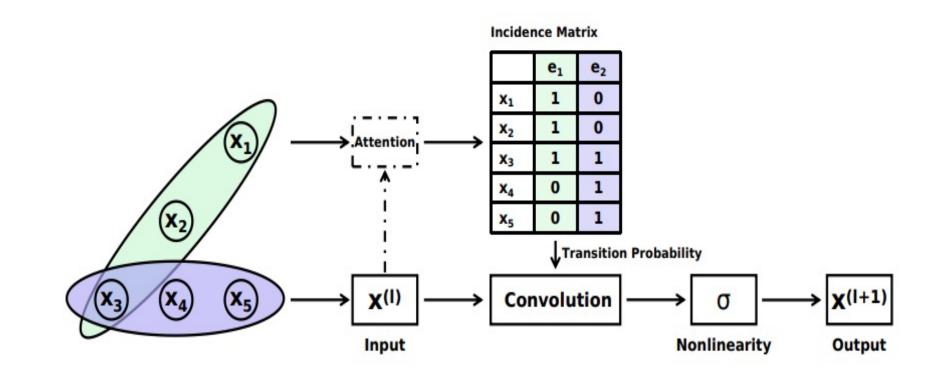
Backgrounds

- Graph Convolutional Network (GCN)
 aggregates information from neighboring nodes
 via pairwise edges
- Known for its simplicity and interpretability,
 GCN performs well on homophilic graphs with clear structural patterns



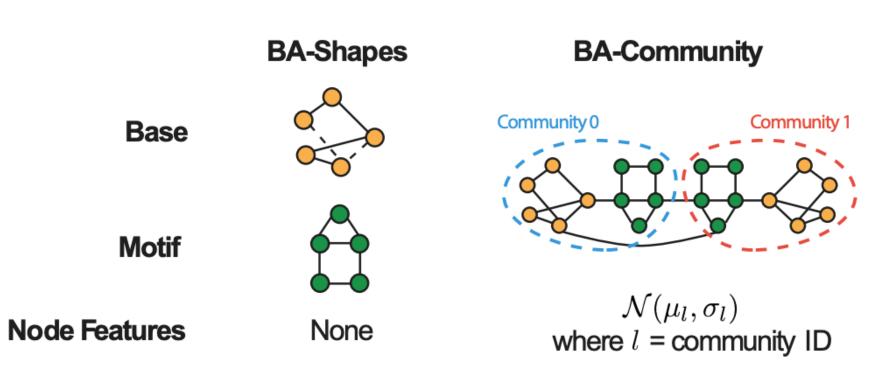
Morris, C., Ritzert, M., Fey, M., Hamilton, W. L., Lenssen, J. E., Rattan, G., & Grohe, M. (2019, July). Weisfeiler and leman go neural: Higher-order graph neural networks. In *Proceedings of the AAAI conference on artificial intelligence* (Vol. 33, No. 01, pp. 4602-4609).

- HyperGraph Convolution (HGConv) extends
 GCN by connecting multiple nodes via
 hyperedges, enabling richer interactions and
 higher-order relational learning
- Seen as a generalized form of GCN, it has gained attention in various applications.



Bai, S., Zhang, F., & Torr, P. H. (2021). Hypergraph convolution and hypergraph attention. *Pattern Recognition*, 110, 107637.

- However, prior research lacks a direct and systematic comparison of GCN and HGConv in terms of:
 - Structural generalization performance
 - Robustness to feature noise, perturbation,
 label noise



Ying, Z., Bourgeois, D., You, J., Zitnik, M., & Leskovec, J. (2019). Gnnexplainer: Generating explanations for graph neural networks. *Advances in neural information processing systems*, 32.

Research Goals

- Identify graph structures that support GCN and HGConv (1-hop, kNN)
 - Analyze performance across varying structures
- Evaluate the robustness of GCN and HGConv (1-hop)
 - Test models under feature/label noise, and structural perturbations

Methodology

- Message Passing Architecture
 - Graph Convolution

$$X^{l+1} = \sigma(\hat{A}X^lW)$$

HyperGraph Convolution

$$X^{l+1} = \sigma(D^{-\frac{1}{2}}HWB^{-1}H^TD^{-\frac{1}{2}}X^lP)$$

- Hyperedge construction for HGConv
 - 1-hop neighborhood grouping: Create a hyperedge for each node and its immediate neighbors

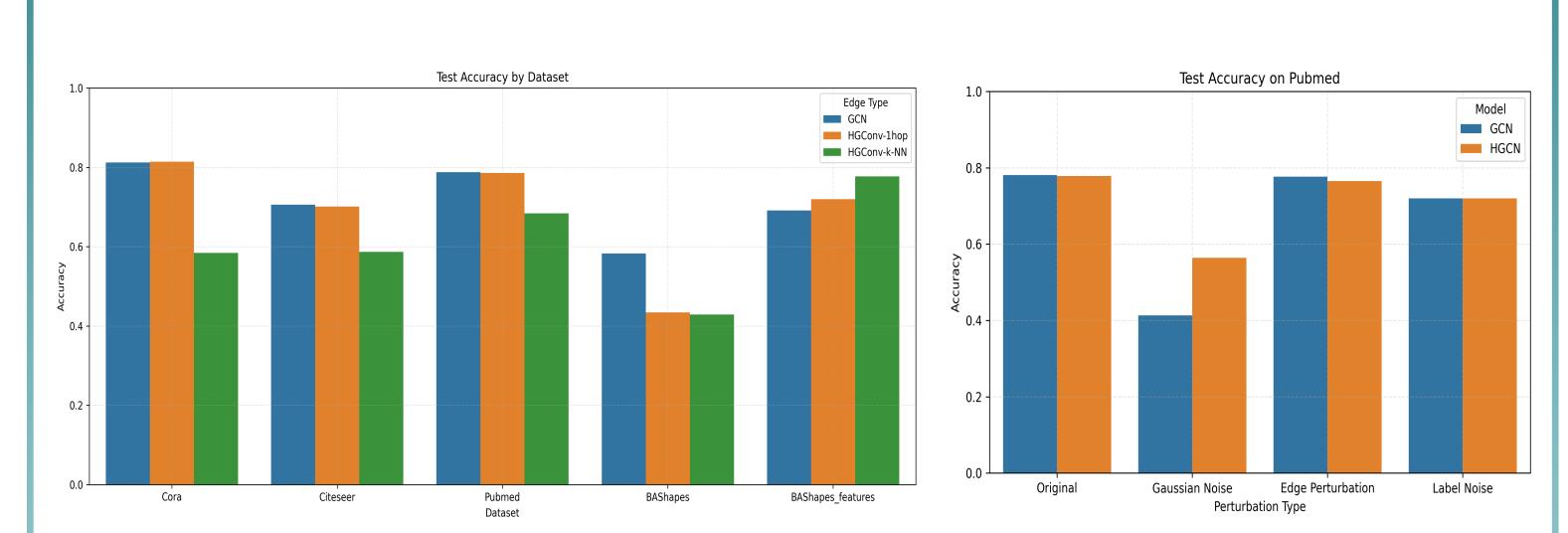
$$e_v = \{v\} \cup N(v) \text{ where } N(v) = \{u \in V | (v, u) \in E\}$$

• k-nearest neighbors grouping: Groups each node with its k most similar nodes based on cosine similarity

$$e_v = \{v\} \cup top_k(\{u \in V \setminus \{v\} \mid sim(X_v, X_u)\})$$

- Perturbation settings for robustness evaluation
 - Feature Noise: Gaussian Noise $N(0, \sigma^2)$ is added to input features to stimulate input corruption
 - Structural Perturbation: Randomly add or remove edges from the original graph structure to test the models' stability under topological changes
 - Label Noise: A fixed percentage of training node labels are randomly flipped to incorrect classes to assess classification robustness

Experiments



Experimental Setup

- Constructed 2-layer models using implementations from PyTorch
 Geometric (PyG)
- Evaluated on Cora, Citeseer, Pubmed, BAShapes, and a featureaugmented BAShapes dataset with class-wise shifted means
- Gaussian noise sigma 0.1, Edge perturbation 5%, Label noise 10%
- Key Results
 - On BAShapes with features, the performance followed the order:
 HGConv-kNN > HGConv-1hop > GCN
 - Under feature noise, HGConv model (1-hop) exhibited enhanced robustness

Concluding Remarks

- HGConv-kNN achieves the highest accuracy on BAShapes with features
 - Highlights the importance of hyperedge construction
- HGConv-1hop consistently outperforms GCN under feature-level noise
 - Demonstrates stronger robustness to feature noise across all datasets

GitHub

https://github.com/limlimlim00/FInal-Project_GCN-HGConv