

Question 3

```
# Prepare the data
df <- read.table("PS2Data/CARD.raw",
                 quote="\\"", comment.char="")

name_string <- "id   nearc2   nearc4   educ   age   fatheduc motheduc
weight momdad14 sinmom14 step14   reg661   reg662   reg663   reg664
reg665 reg666   reg667   reg668   reg669   south66   black   smsa   south
smsa66   wage   enroll   KWW   IQ   married   libcrd14   exper
lwage   expersq   "

name_string <- gsub("[\r\n]", " ", name_string)
name_string <- strsplit(name_string, " ")

name_vec <- vector()
for (i in name_string[[1]]) {
  if (i != "1" & i != ""){
    name_vec <- append(name_vec, i)
  }
}
colnames(df) <- name_vec
```

a

In the table below, the *iid* and *robust* standard errors are quite similar (*robust* standard errors are usually a little larger), so the inference (ttest and pvalue) is also quite similar.

The *iid* standard error assumes that the variance of the error term is constant and does not depend on independent variables. However, the *robust* standard error does not assume this, so it can work under both homoskedasticity and heteroskedasticity.

```
# Homoskedastic
homo <- feols(lwage ~ educ + exper + expersq + black + south + smsa + smsa66 +
              reg661 + reg662 + reg663 + reg664 + reg665 + reg666 + reg667 + reg668,
              se = "iid", df)

# Heteroskedastic
hetero <- feols(lwage ~ educ + exper + expersq + black + south + smsa + smsa66 +
                reg661 + reg662 + reg663 + reg664 + reg665 + reg666 + reg667 + reg668,
                se = "hc1", df)

out <- etable(homo, hetero, tex = TRUE, se.row = TRUE)
```

```
knitr::asis_output(c("\\begin{center}", out, "\\end{center}"))
```

Dependent Variable: Model:	(1)	lwage (2)
<i>Variables</i>		
(Intercept)	4.739*** (0.0715)	4.739*** (0.0746)
educ	0.0747*** (0.0035)	0.0747*** (0.0036)
exper	0.0848*** (0.0066)	0.0848*** (0.0068)
expersq	-0.0023*** (0.0003)	-0.0023*** (0.0003)
black	-0.1990*** (0.0182)	-0.1990*** (0.0182)
south	-0.1480*** (0.0260)	-0.1480*** (0.0280)
smsa	0.1364*** (0.0201)	0.1364*** (0.0192)
smsa66	0.0262 (0.0194)	0.0262 (0.0186)
reg661	-0.1186*** (0.0388)	-0.1186*** (0.0388)
reg662	-0.0222 (0.0283)	-0.0222 (0.0299)
reg663	0.0260 (0.0274)	0.0260 (0.0285)
reg664	-0.0635* (0.0357)	-0.0635* (0.0368)
reg665	0.0095 (0.0361)	0.0095 (0.0387)
reg666	0.0220 (0.0401)	0.0220 (0.0411)
reg667	-0.0006 (0.0394)	-0.0006 (0.0415)
reg668	-0.1750*** (0.0463)	-0.1750*** (0.0470)
<i>Fit statistics</i>		
Standard-Errors	IID	Heteroskedasticity-robust
Observations	3,010	3,010
R ²	0.29984	0.29984
Adjusted R ²	0.29633	0.29633

*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

b

There exists a practically and statistically significant partial correlation between *educ* and *nearc4*: the coefficient of *nearc4* is 0.32, which means individuals near 4 yr college have additional 0.32 years of schooling. It's significant under 1% level with both *iid* and *robust* standard errors.

For some variables, the *robust* standard error is a little larger, and for other variables, the *robust* standard error is a little smaller. But they are still quite similar and the inference (ttest and pvalue) gives same conclusions. For *near4*, the *robust* standard error is a little smaller, but the coefficient is both significant under 1% level.

```
reduce_homo <- feols(educ ~ nearc4 + exper + expersq + black + south + smsa + smsa66 +
                    reg661 + reg662 + reg663 + reg664 + reg665 + reg666 + reg667 + reg668,
                    se = "iid", df)

reduce_hetero <- feols(educ ~ nearc4 + exper + expersq + black + south + smsa + smsa66 +
                    reg661 + reg662 + reg663 + reg664 + reg665 + reg666 + reg667 + reg668,
                    se = "hc1", df)

out <- etable(reduce_homo, reduce_hetero, tex = TRUE, se.row = TRUE)

knitr::asis_output(c("\\begin{center}", out, "\\end{center}"))
```

Dependent Variable: Model:	(1)	educ (2)
<i>Variables</i>		
(Intercept)	16.85*** (0.2111)	16.85*** (0.1866)
nearc4	0.3199*** (0.0879)	0.3199*** (0.0851)
exper	-0.4125*** (0.0337)	-0.4125*** (0.0321)
expersq	0.0009 (0.0016)	0.0009 (0.0017)
black	-0.9355*** (0.0937)	-0.9355*** (0.0925)
south	-0.0516 (0.1354)	-0.0516 (0.1420)
smsa	0.4022*** (0.1048)	0.4022*** (0.1112)
smsa66	0.0255 (0.1058)	0.0255 (0.1106)
reg661	-0.2103 (0.2025)	-0.2103 (0.1994)
reg662	-0.2889** (0.1473)	-0.2889* (0.1513)
reg663	-0.2382* (0.1426)	-0.2382* (0.1431)
reg664	-0.0931 (0.1860)	-0.0931 (0.1799)
reg665	-0.4829** (0.1882)	-0.4829** (0.1951)
reg666	-0.5131** (0.2096)	-0.5131** (0.2090)
reg667	-0.4271** (0.2056)	-0.4271** (0.2110)
reg668	0.3136 (0.2417)	0.3136 (0.2338)
<i>Fit statistics</i>		
Standard-Errors	IID	Heteroskedasticity-robust
Observations	3,010	3,010
R ²	0.47712	0.47712
Adjusted R ²	0.47450	0.47450

*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

C

The IV estimate has wider CI and the lower bound is closer to 0, hence it's more conservative. However, the estimates from both IV and OLS are significant on 95% level since the lower bounds are both larger than 0.

```
iv_c <- feols(lwage ~ exper + expersq + black + south + smsa + smsa66 +  
              reg661 + reg662 + reg663 + reg664 + reg665 + reg666 + reg667 + reg668 |  
              educ ~ nearc4,  
              se = "hc1", df)
```

```
out <- etable(iv_c, hetero, tex = TRUE,  
              coefstat = c("confint"),  
              headers=list("IV" = 1, "OLS" = 1))
```

```
knitr::asis_output(c("\\begin{center}", out, "\\end{center}"))
```

Dependent Variable:	lwage	
Model:	IV (1)	OLS (2)
<i>Variables</i>		
(Intercept)	3.774*** [1.970; 5.578]	4.739*** [4.593; 4.886]
educ	0.1315** [0.0253; 0.2377]	0.0747*** [0.0675; 0.0818]
exper	0.1083*** [0.0624; 0.1542]	0.0848*** [0.0716; 0.0981]
expersq	-0.0023*** [-0.0030; -0.0017]	-0.0023*** [-0.0029; -0.0017]
black	-0.1468*** [-0.2497; -0.0438]	-0.1990*** [-0.2346; -0.1634]
south	-0.1447*** [-0.2018; -0.0875]	-0.1480*** [-0.2029; -0.0930]
smsa	0.1118*** [0.0507; 0.1729]	0.1364*** [0.0987; 0.1741]
smsa66	0.0185 [-0.0218; 0.0588]	0.0262 [-0.0102; 0.0627]
reg661	-0.1078*** [-0.1884; -0.0273]	-0.1186*** [-0.1946; -0.0425]
reg662	-0.0070 [-0.0733; 0.0592]	-0.0222 [-0.0809; 0.0365]
reg663	0.0404 [-0.0235; 0.1044]	0.0260 [-0.0299; 0.0818]
reg664	-0.0579 [-0.1350; 0.0192]	-0.0635* [-0.1357; 0.0087]
reg665	0.0385 [-0.0588; 0.1357]	0.0095 [-0.0664; 0.0853]
reg666	0.0551 [-0.0474; 0.1576]	0.0220 [-0.0586; 0.1025]
reg667	0.0268 [-0.0717; 0.1253]	-0.0006 [-0.0820; 0.0808]
reg668	-0.1909*** [-0.2905; -0.0912]	-0.1750*** [-0.2671; -0.0829]
<i>Fit statistics</i>		
Observations	3,010	3,010
R ²	0.23817	0.29984
Adjusted R ²	0.23435	0.29633

Heteroskedasticity-robust co-variance matrix, 95% confidence intervals in brackets
*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

d

The table below presents estimation results from the reduced form. After adding *nearc2*, the coefficient of *nearc4* is even a littler larger and the *se* is essentially the same. However, the coefficient of *nearc2* is way smaller than *nearc4* and not significant. Therefore, *nearc4* is more strongly related to *educ* than *nearc2*. After adding *nearc2*, the adjusted R square also increased a little - the independent variables can jointly explain more variation of *educ*.

```
reduce_d <- feols(educ ~ nearc2 + nearc4 + exper + expersq + black + south + smsa + smsa66 +  
                  reg661 + reg662 + reg663 + reg664 + reg665 + reg666 + reg667 + reg668,  
                  se = "hc1", df)  
  
out <- etable(reduce_d, reduce_hetero, tex = TRUE, se.row = TRUE)  
  
knitr::asis_output(c("\\begin{center}", out, "\\end{center}"))
```

Dependent Variable: Model:	educ	
	(1)	(2)
<i>Variables</i>		
(Intercept)	16.77*** (0.1940)	16.85*** (0.1866)
nearc2	0.1230 (0.0776)	
nearc4	0.3206*** (0.0850)	0.3199*** (0.0851)
exper	-0.4123*** (0.0320)	-0.4125*** (0.0321)
expersq	0.0008 (0.0017)	0.0009 (0.0017)
black	-0.9452*** (0.0925)	-0.9355*** (0.0925)
south	-0.0419 (0.1417)	-0.0516 (0.1420)
smsa	0.4014*** (0.1113)	0.4022*** (0.1112)
smsa66	7.82×10^{-5} (0.1118)	0.0255 (0.1106)
reg661	-0.1688 (0.2009)	-0.2103 (0.1994)
reg662	-0.2690* (0.1524)	-0.2889* (0.1513)
reg663	-0.1902 (0.1468)	-0.2382* (0.1431)
reg664	-0.0377 (0.1828)	-0.0931 (0.1799)
reg665	-0.4371** (0.1979)	-0.4829** (0.1951)
reg666	-0.5022** (0.2095)	-0.5131** (0.2090)
reg667	-0.3775* (0.2144)	-0.4271** (0.2110)
reg668	0.3820 (0.2381)	0.3136 (0.2338)
<i>Fit statistics</i>		
Standard-Errors	Heteroskedasticity-robust	
Observations	3,010	3,010
R ²	0.47756	0.47712
Adjusted R ²	0.47476	0.47450

Heteroskedasticity-robust standard-errors in parentheses
*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

After using two IV, the coefficient increases to 0.16, larger than former IV result (0.13) and the se is even smaller, so it does indicate a stronger relationship. The estimate is larger and we are more confident that it's significantly different from 0.

```
iv_d <- feols(lwage ~ exper + expersq + black + south + smsa + smsa66 +  
              reg661 + reg662 + reg663 + reg664 + reg665 + reg666 + reg667 + reg668 |  
              educ ~ nearc2 + nearc4,  
              se = "hc1", df)  
  
out <- etable(iv_d, iv_c, tex = TRUE,  
              headers=list("#IV:2" = 1, "#IV:1" = 1))  
  
knitr::asis_output(c("\\begin{center}", out, "\\end{center}"))
```

Dependent Variable:	lwage	
	#IV:2	#IV:1
Model:	(1)	(2)
<i>Variables</i>		
(Intercept)	3.340*** (0.8933)	3.774*** (0.9199)
educ	0.1571*** (0.0525)	0.1315** (0.0541)
exper	0.1188*** (0.0230)	0.1083*** (0.0234)
expersq	-0.0024*** (0.0004)	-0.0023*** (0.0003)
black	-0.1233** (0.0516)	-0.1468*** (0.0525)
south	-0.1432*** (0.0303)	-0.1447*** (0.0291)
smsa	0.1008*** (0.0314)	0.1118*** (0.0311)
smsa66	0.0151 (0.0212)	0.0185 (0.0206)
reg661	-0.1030** (0.0427)	-0.1078*** (0.0411)
reg662	-0.0002 (0.0346)	-0.0070 (0.0338)
reg663	0.0470 (0.0336)	0.0404 (0.0326)
reg664	-0.0554 (0.0410)	-0.0579 (0.0393)
reg665	0.0515 (0.0508)	0.0385 (0.0496)
reg666	0.0700 (0.0536)	0.0551 (0.0523)
reg667	0.0391 (0.0516)	0.0268 (0.0502)
reg668	-0.1980*** (0.0524)	-0.1909*** (0.0508)
<i>Fit statistics</i>		
Observations	3,010	3,010
R ²	0.17020	0.23817
Adjusted R ²	0.16605	0.23435

Heteroskedasticity-robust standard-errors in parentheses
*Signif. Codes: ***: 0.01, **: 0.05, *: 0.1*

e

IQ is significantly correlated with *nearc4*. Intuitively, *IQ* is also correlated with *education*, so *nearc4* might not be a valid IV for *education* since it does not satisfy the exclusion assumption. The previous IV estimations might be biased.

```
df$IQ <- as.numeric(df$IQ)
ols_e <- feols(IQ ~ nearc4, se = "hc1", df)
out <- etable(ols_e, tex = TRUE)

knitr::asis_output(c("\\begin{center}", out, "\\end{center}"))
```

Dependent Variable:	IQ
Model:	(1)
<i>Variables</i>	
(Intercept)	100.6*** (0.6331)
nearc4	2.596*** (0.7495)
<i>Fit statistics</i>	
Observations	2,061
R ²	0.00586
Adjusted R ²	0.00537
<i>Heteroskedasticity-robust standard-errors in parentheses</i>	
<i>Signif. Codes: ***: 0.01, **: 0.05, *: 0.1</i>	

f

After controlling for *region* variables, the coefficient of *nearc4* is not significant anymore. Therefore, after controlling for these *region* variables, *nearc4* can serve as a valid IV for *education* since we can exclude the bias led by *IQ*.

```
df$IQ <- as.numeric(df$IQ)
ols_f <- feols(IQ ~ nearc4 + smsa66 + reg661 + reg662 + reg669, se = "hcl", df)
out <- etable(ols_f, ols_e, tex = TRUE)

knitr::asis_output(c("\\begin{center}", out, "\\end{center}"))
```

Dependent Variable:	IQ	
Model:	(1)	(2)
<i>Variables</i>		
(Intercept)	99.38*** (0.7135)	100.6*** (0.6331)
nearc4	0.8681 (0.8183)	2.596*** (0.7495)
smsa66	1.355* (0.7904)	
reg661	4.768*** (1.423)	
reg662	5.808*** (0.8679)	
reg669	1.845 (1.142)	
<i>Fit statistics</i>		
Observations	2,061	2,061
R ²	0.03019	0.00586
Adjusted R ²	0.02783	0.00537
<i>Heteroskedasticity-robust standard-errors in parentheses</i>		
<i>Signif. Codes: ***: 0.01, **: 0.05, *: 0.1</i>		