

# ECE-GY 6303, PROBABILITY & STOCHASTIC PROCESSES

## Homework # 4

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### Problem 1

The random variable  $X$  is  $\mathcal{N}(5, 2)$  and  $Y = 2X + 4$ . Find the mean, variance of  $Y$  and  $f_Y(y)$ .

### Problem 2

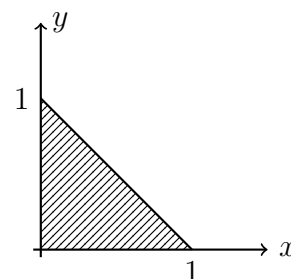
The random variable  $X$  is  $P(5)$  and  $Y = 2X + 4$ . Find the mean, variance of  $Y$  and  $f_Y(y)$ .

### Problem 3

- a. Given the joint probability density function  $f_{XY}(x, y)$  as,

$$f_{XY}(x, y) = \begin{cases} kxy, & (x, y) \in \text{shaded area} \\ 0 & \text{otherwise} \end{cases}$$

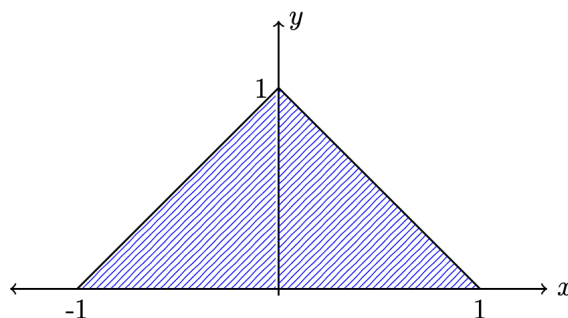
- a. Find  $k$ ,  $f_X(x)$  and  $f_Y(y)$ .  
b. Are  $X$  and  $Y$  independent?



### Problem 4

$X$  and  $Y$  are jointly distributed random variables with joint p.d.f

$$f_{XY}(x, y) = \begin{cases} e^{-x} & \infty > x > y > 0 \\ 0 & \text{otherwise} \end{cases}$$



- a. Find  $f_X(x)$  and  $f_Y(y)$ .
- b. Are  $X$  and  $Y$  independent?

## Problem 5

$X$  and  $Y$  are jointly distributed random variables with joint p.d.f

$$f_{XY}(x, y) = \begin{cases} k & 0 < x < y < a \\ 0 & \text{otherwise} \end{cases}$$

- a. Find  $k$ ,  $f_X(x)$  and  $f_Y(y)$ .
- b. Are  $X$  and  $Y$  independent?

## Problem 6

- a.  $X$  and  $Y$  are jointly distributed random variables with joint p.d.f

$$f_{XY}(x, y) = \begin{cases} e^{-(x+y)} & x \geq 0, y \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

Are  $X$  and  $Y$  independent?

- b. Given the joint probability density function  $f_{XY}(x, y)$  as

$$f_{XY}(x, y) = \frac{1}{2\pi} e^{-(x^2+y^2)/2}.$$

Show that  $X$  and  $Y$  are independent random variables