PA2 Report

● b10901059 林咏毅

Optimal substructure

• Reference:

https://ieeexplore.ieee.org/document/1270250

```
\begin{split} & \underbrace{\text{(https://ieeexplore.ieee.org/document/1270250)}} \\ & \text{IF } i \leq k \leq j-1 \\ & \text{ and } \big| \operatorname{MIS}(i,k-1) \big| + 1 + \big| \operatorname{MIS}(k+1,j-1) \big| > \big| \operatorname{MIS}(i,j-1) \big| \\ & \text{THEN } \operatorname{MIS}(i,j) \leftarrow \operatorname{MIS}(i,k-1) \cup \big\{ v_{kj} \big\} \cup \operatorname{MIS}(k+1,j-1) \\ & \text{ELSE } \operatorname{MIS}(i,j) \leftarrow \operatorname{MIS}(i,j-1) \end{split}
```

 Implement with recursion and dynamic programming

Data structures used

```
// save all the chords from input
1
2
      // chords[head] = tail
3
      // chords[tail] = head
4
      vector<int> chords(pivot_num, 0);
5
6
      // save chords used in answer
7
      vector<int> ans chords;
8
9
      // up-right half: number of available chords in partition chord_cnt[i][j]
10
      // bottom-left half: record the chord we want
      vector<vector<int>> chord_cnt(pivot_num, vector<int> (pivot_num, 0));
11
12
      for (int i=0; i<pivot_num; i++) {</pre>
13
          for (int j=0; j<pivot_num; j++) {</pre>
14
              if (j < i) {
15
                  chord_cnt[i][j] = -1;
16
17
          }
18 }
```

Observation

- In this assignment, we can see the huge difference in execution time between bottom-up and topdown method. Since I first try to implement with bottom-up method, I found it consumes more time than top-down method does, because it computes every result no matter it's useful or not.
- With dynamic programming, it can reduce a lot of time calculating the the recursion function everytime, below is the comparison using 1000 as

the input:

DP:

lin_1214@lin-1214:/mnt/c/Users/a0936/algo/PA2/b10901059_pa2\$./bin/mps ./inputs/1000.in ./outputs/1000.out
The total CPU time: 35.095ms

non-DP:

lin_1214@lin-1214:/mnt/c/Users/a0936/algo/PA2/b10901059_pa2\$./bin/mps ./inputs/1000.in ./outputs/1000.out

(seems it never ends...)