Homework 1 Due: 1002

1.

$\frac{d}{dt}a(t) = k_0 - k_1 a(t)b(t)$	$\frac{d}{dt}d(t) = k_1 a(t)b(t) - k_2 d(t)$	
$\frac{d}{dt}b(t) = -k_1a(t)b(t) + k_2d(t)$	$\frac{d}{dt} e(t) = k_s c(t) - k_q e(t)$	
$\frac{d}{dt}c(t) = k_1a(t)b(t) - k_3c(t)$	$\frac{d}{dt}f(t) = k_sc(t) - k_sf(t)$	
(2)	hts as fees	
state variables: act), (+), cct), o	ect) tit)	

2.

(a)

The three molecules are viral RNA, viral antigen and antibody

(b)

Inactive whole virus: When injected, the immune system recognizes the viral antigens and produces antibodies to fight the virus. These antibodies will be ready to respond to future exposures to the live virus.

Antigen proteins: The immune system identifies these proteins as foreign antigens and generates an immune response, including producing antibodies that recognize and neutralize the virus if encountered later.

mRNA(genetic instructions): The mRNA vaccines contain a small piece of the virus's genetic material that provides instructions for cells to make the spike protein found on the surface of SARS-CoV-2. Once cells produce this spike protein, the immune system detects it and generates a response, including the production of antibodies and memory cells to recognize the virus in the future.

DNA (genetic instructions): After being delivered into the body, cells take up the DNA, produce the spike protein, and display it on their surface. The immune system responds by producing antibodies and T cells, which prepare the body to fight the actual virus if it is encountered later.

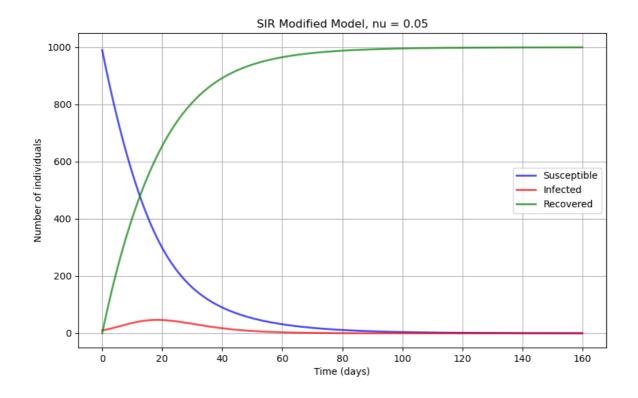
3.

(a)

Solution implemented in with Python in plot.py

```
# SIR model differential equations
Tabnine: Edit | Test | Explain | Document | Ask
def sir_model(y, t, beta, gamma, v, N):
    S, I, R = y
    dSdt = -beta * S * I / N - v * S
    dIdt = beta * S * I / N - gamma * I
    dRdt = gamma * I + v * S
    return [dSdt, dIdt, dRdt]
N = 1000 # Total population
IO, RO = 10, O # Initial number of infected and recovered individuals
S0 = N - I0 - R0 # Initial number of susceptible individuals
beta = 0.3 # Contact rate
gamma = 0.1 # Recovery rate
vs = [0.05, 0.00, 0.10, 0.30] # Vaccination rate
t = np.linspace(0, 160, 160) # Time grid
for v in vs:
    # Initial conditions vector
    y = [S0, I0, R0]
    # Solve the differential equations
    solution = odeint(sir_model, y, t, args=(beta, gamma, v, N))
    S, I, R = solution.T
```

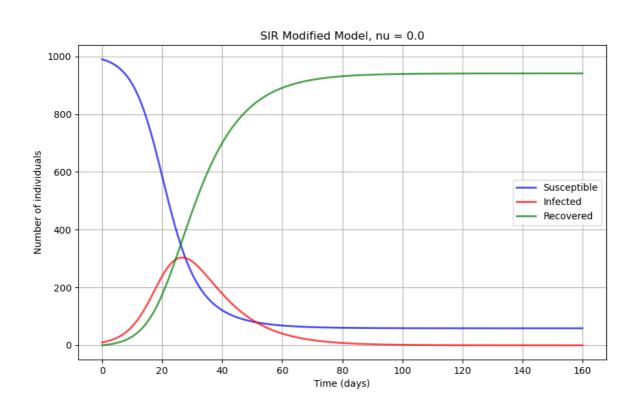
Result when u = 0.05



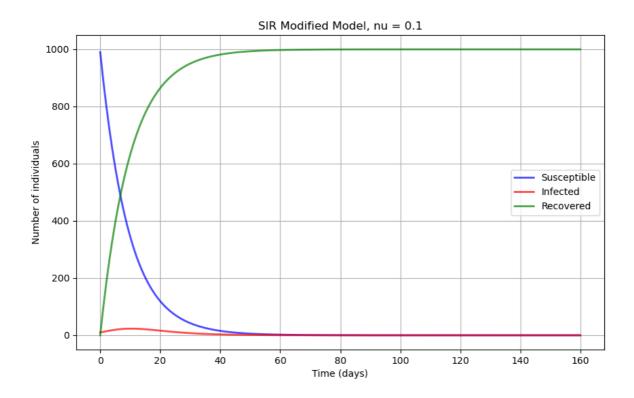
(b)

Compare result of different ν

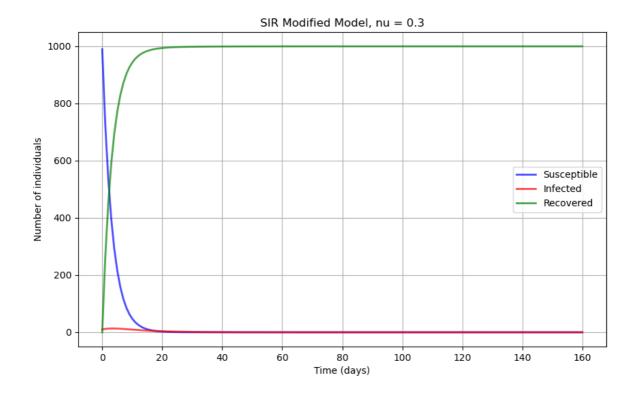
$$\nu = 0.0$$



 $\nu = 0.10$



 $\nu = 0.30$



By comparing the results of different ν , we can find that when ν increases, the number of susceptible individuals decreases faster, and the number of recovered individuals increases faster. This is because the vaccination rate ν reduces the number of susceptible individuals by vaccinating them, and also reduces the number of infected individuals by reducing the contact rate.

4. Souce Code

github