







MMSP 2nd Module – Lab1

Davide Salvi davide.salvi@polimi.it

Audio signal encoding

- 1. Load file 'pf.wav' and plot it. Check that its values are included between [-1,1].
- 2. Take only the first 60 sec. of the file and rescale its values between [0,255].
- 3. Convert each value into its binary representation over 8 bit.
- 4. Find the entropy of the binary source that has generated the above audio file.
- 5. Now consider the file as generated by a finite source whose alphabet is [0:255]. Plot the normalized histogram of the file and find the entropy of the above source.
- 6. Consider now the audio file as generated by a source with memory (let us suppose memory = 1). Find the conditional entropy.

- 1. Use audioread or wavread to read the audio file
- 1. Use **bi2de** for binary representation
- 1. Use **hist** to estimate pdf / pmf
- 2. Use **hist3** to estimate joint pdf / pmf
- 3. Pay attention to $log_2(0)$
- 4. Remember entropy properties (Venn diagram)

Image signal encoding

- 1. Load the image 'lena512color.tiff'. For each image component (R, G, B) display the histogram.
- 2. Approximate the pdf of each channel as the normalized histogram. Compute the entropy (in bpp) of each channel.
- 3. Let X be the source represented by the red channel and Y the source represented by the green channel. Compute and plot the joint pdf, p(X,Y).
- 4. Compute the joint entropy H(X,Y) and verify that $H(X,Y) \le H(X) + H(Y)$. Why the equality is not satisfied?
- 5. Suppose to encode Y with H(Y) bits and to send N = aX+b-Y instead of X, where 'a' and 'b' are obtained by linear regression (least squares on Y=aX+b). Compute the entropy of N and compare it with the conditional entropy H(X|Y) = H(X,Y) H(Y).

- 1. Use **imread** to load image files
- 2. Images are stored as **uint8**, consider casting to **double**
- 3. Remember how to solve a linear regression problem using least-squares

$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix} = \begin{bmatrix} x_1 & 1 \\ x_2 & 1 \\ \vdots \\ x_N & 1 \end{bmatrix} \cdot \begin{bmatrix} a \\ b \end{bmatrix}$$

Discrete memoryless source coding

Consider a discrete random sequence described by the following equation:

$$y(n) = \min(\max(0, \text{round}(\rho y(n-1) + w(n))), 15)$$

where w(n) is a Gaussian white noise of variance equal to 1 and ρ =0.95

- 1. Generate one realization of the process of length = 1,000,000
- 2. Determine the size of the alphabet of the source
- 3. Find the entropy H(Y) assuming that y(n) is a discrete memoryless source
- 4. Let K=py(n-1). Compute the joint PDF p(Y,K) and the joint entropy H(Y,K).
- 5. Compute the conditional entropy H(Y|K). Compare it with H(Y). How many bps are needed to represent the source exploiting inter-symbol redundancy?

Exam track (19th June 2006)

1. Generate N = 10000 samples of a AR(1) random process

$$\rho y(n-1) + w(n)$$

where w(n) is a Gaussian white noise of variance equal to 1 and ρ =0.99.

- 1. Clip the sample values in the range [-20,20] and round them to the nearest integer.
- 2. Compute the entropy H(y) of the source assuming that there is no memory. Compare H(y) with the maximum entropy of a source having the same alphabet.