

```

x<-c(1:10)
y<-c(11:20)#this is the 2D matrix .
k<- 2
center1<- c(x[1],y[1])
center2<-c(x[2],y[2])
dis<-matrix(nrow=length(x),ncol=k+1)
colnames(dis)<-c('dis_cen1',"dis_cen2","class")
c(x[3],y[3])

```

```
## [1] 3 13
```

```

while(TRUE){
  for(i in 1:length(x)){
    #calculate each value distance one by one and judge which center is shotest center
    dis[i,1]<- sqrt((x[i]-center1[1])^2+(y[i]-center2[2])^2)
    dis[i,2]<- ((x[i]-center2[1])^2+(y[i]-center2[2])^2)^0.5
    dis[i,3]<-which.min(dis[i,1:2])
  }
  dis
  #print("return boolean value")
  dis[,3]==1#return boolean value
  #print("find the new center1 and center2")
  (center1new<-c(mean(x[dis[,3]==1]),mean(y[dis[,3]==1])))
  (center2new<-c(mean(x[dis[,3]==2]),mean(y[dis[,3]==2])))
  if(sum(center1==center1new)+sum(center2==center2new)==4){
    break
  }
  center1<- center1new
  center2<- center2new
}

```

```

a<-c(1,2,3,4,5)
b<-c(1,1,1,1,1)
a<b

```

```
## [1] FALSE FALSE FALSE FALSE FALSE
```

we can apply function in a libaray to directly implement this effect

```

iris2<- iris
iris2$Species<- NULL
iris2

```

```

##      Sepal.Length Sepal.Width Petal.Length Petal.Width
## 1           5.1         3.5         1.4         0.2
## 2           4.9         3.0         1.4         0.2
## 3           4.7         3.2         1.3         0.2
## 4           4.6         3.1         1.5         0.2
## 5           5.0         3.6         1.4         0.2
## 6           5.4         3.9         1.7         0.4
## 7           4.6         3.4         1.4         0.3
## 8           5.0         3.4         1.5         0.2
## 9           4.4         2.9         1.4         0.2
## 10          4.9         3.1         1.5         0.1
## 11          5.4         3.7         1.5         0.2

```

## 12	4.8	3.4	1.6	0.2
## 13	4.8	3.0	1.4	0.1
## 14	4.3	3.0	1.1	0.1
## 15	5.8	4.0	1.2	0.2
## 16	5.7	4.4	1.5	0.4
## 17	5.4	3.9	1.3	0.4
## 18	5.1	3.5	1.4	0.3
## 19	5.7	3.8	1.7	0.3
## 20	5.1	3.8	1.5	0.3
## 21	5.4	3.4	1.7	0.2
## 22	5.1	3.7	1.5	0.4
## 23	4.6	3.6	1.0	0.2
## 24	5.1	3.3	1.7	0.5
## 25	4.8	3.4	1.9	0.2
## 26	5.0	3.0	1.6	0.2
## 27	5.0	3.4	1.6	0.4
## 28	5.2	3.5	1.5	0.2
## 29	5.2	3.4	1.4	0.2
## 30	4.7	3.2	1.6	0.2
## 31	4.8	3.1	1.6	0.2
## 32	5.4	3.4	1.5	0.4
## 33	5.2	4.1	1.5	0.1
## 34	5.5	4.2	1.4	0.2
## 35	4.9	3.1	1.5	0.2
## 36	5.0	3.2	1.2	0.2
## 37	5.5	3.5	1.3	0.2
## 38	4.9	3.6	1.4	0.1
## 39	4.4	3.0	1.3	0.2
## 40	5.1	3.4	1.5	0.2
## 41	5.0	3.5	1.3	0.3
## 42	4.5	2.3	1.3	0.3
## 43	4.4	3.2	1.3	0.2
## 44	5.0	3.5	1.6	0.6
## 45	5.1	3.8	1.9	0.4
## 46	4.8	3.0	1.4	0.3
## 47	5.1	3.8	1.6	0.2
## 48	4.6	3.2	1.4	0.2
## 49	5.3	3.7	1.5	0.2
## 50	5.0	3.3	1.4	0.2
## 51	7.0	3.2	4.7	1.4
## 52	6.4	3.2	4.5	1.5
## 53	6.9	3.1	4.9	1.5
## 54	5.5	2.3	4.0	1.3
## 55	6.5	2.8	4.6	1.5
## 56	5.7	2.8	4.5	1.3
## 57	6.3	3.3	4.7	1.6
## 58	4.9	2.4	3.3	1.0
## 59	6.6	2.9	4.6	1.3
## 60	5.2	2.7	3.9	1.4
## 61	5.0	2.0	3.5	1.0
## 62	5.9	3.0	4.2	1.5
## 63	6.0	2.2	4.0	1.0
## 64	6.1	2.9	4.7	1.4
## 65	5.6	2.9	3.6	1.3

## 66	6.7	3.1	4.4	1.4
## 67	5.6	3.0	4.5	1.5
## 68	5.8	2.7	4.1	1.0
## 69	6.2	2.2	4.5	1.5
## 70	5.6	2.5	3.9	1.1
## 71	5.9	3.2	4.8	1.8
## 72	6.1	2.8	4.0	1.3
## 73	6.3	2.5	4.9	1.5
## 74	6.1	2.8	4.7	1.2
## 75	6.4	2.9	4.3	1.3
## 76	6.6	3.0	4.4	1.4
## 77	6.8	2.8	4.8	1.4
## 78	6.7	3.0	5.0	1.7
## 79	6.0	2.9	4.5	1.5
## 80	5.7	2.6	3.5	1.0
## 81	5.5	2.4	3.8	1.1
## 82	5.5	2.4	3.7	1.0
## 83	5.8	2.7	3.9	1.2
## 84	6.0	2.7	5.1	1.6
## 85	5.4	3.0	4.5	1.5
## 86	6.0	3.4	4.5	1.6
## 87	6.7	3.1	4.7	1.5
## 88	6.3	2.3	4.4	1.3
## 89	5.6	3.0	4.1	1.3
## 90	5.5	2.5	4.0	1.3
## 91	5.5	2.6	4.4	1.2
## 92	6.1	3.0	4.6	1.4
## 93	5.8	2.6	4.0	1.2
## 94	5.0	2.3	3.3	1.0
## 95	5.6	2.7	4.2	1.3
## 96	5.7	3.0	4.2	1.2
## 97	5.7	2.9	4.2	1.3
## 98	6.2	2.9	4.3	1.3
## 99	5.1	2.5	3.0	1.1
## 100	5.7	2.8	4.1	1.3
## 101	6.3	3.3	6.0	2.5
## 102	5.8	2.7	5.1	1.9
## 103	7.1	3.0	5.9	2.1
## 104	6.3	2.9	5.6	1.8
## 105	6.5	3.0	5.8	2.2
## 106	7.6	3.0	6.6	2.1
## 107	4.9	2.5	4.5	1.7
## 108	7.3	2.9	6.3	1.8
## 109	6.7	2.5	5.8	1.8
## 110	7.2	3.6	6.1	2.5
## 111	6.5	3.2	5.1	2.0
## 112	6.4	2.7	5.3	1.9
## 113	6.8	3.0	5.5	2.1
## 114	5.7	2.5	5.0	2.0
## 115	5.8	2.8	5.1	2.4
## 116	6.4	3.2	5.3	2.3
## 117	6.5	3.0	5.5	1.8
## 118	7.7	3.8	6.7	2.2
## 119	7.7	2.6	6.9	2.3

```
## 120      6.0      2.2      5.0      1.5
## 121      6.9      3.2      5.7      2.3
## 122      5.6      2.8      4.9      2.0
## 123      7.7      2.8      6.7      2.0
## 124      6.3      2.7      4.9      1.8
## 125      6.7      3.3      5.7      2.1
## 126      7.2      3.2      6.0      1.8
## 127      6.2      2.8      4.8      1.8
## 128      6.1      3.0      4.9      1.8
## 129      6.4      2.8      5.6      2.1
## 130      7.2      3.0      5.8      1.6
## 131      7.4      2.8      6.1      1.9
## 132      7.9      3.8      6.4      2.0
## 133      6.4      2.8      5.6      2.2
## 134      6.3      2.8      5.1      1.5
## 135      6.1      2.6      5.6      1.4
## 136      7.7      3.0      6.1      2.3
## 137      6.3      3.4      5.6      2.4
## 138      6.4      3.1      5.5      1.8
## 139      6.0      3.0      4.8      1.8
## 140      6.9      3.1      5.4      2.1
## 141      6.7      3.1      5.6      2.4
## 142      6.9      3.1      5.1      2.3
## 143      5.8      2.7      5.1      1.9
## 144      6.8      3.2      5.9      2.3
## 145      6.7      3.3      5.7      2.5
## 146      6.7      3.0      5.2      2.3
## 147      6.3      2.5      5.0      1.9
## 148      6.5      3.0      5.2      2.0
## 149      6.2      3.4      5.4      2.3
## 150      5.9      3.0      5.1      1.8
```

```
(kmeans_result<-kmeans(iris2,3))
```

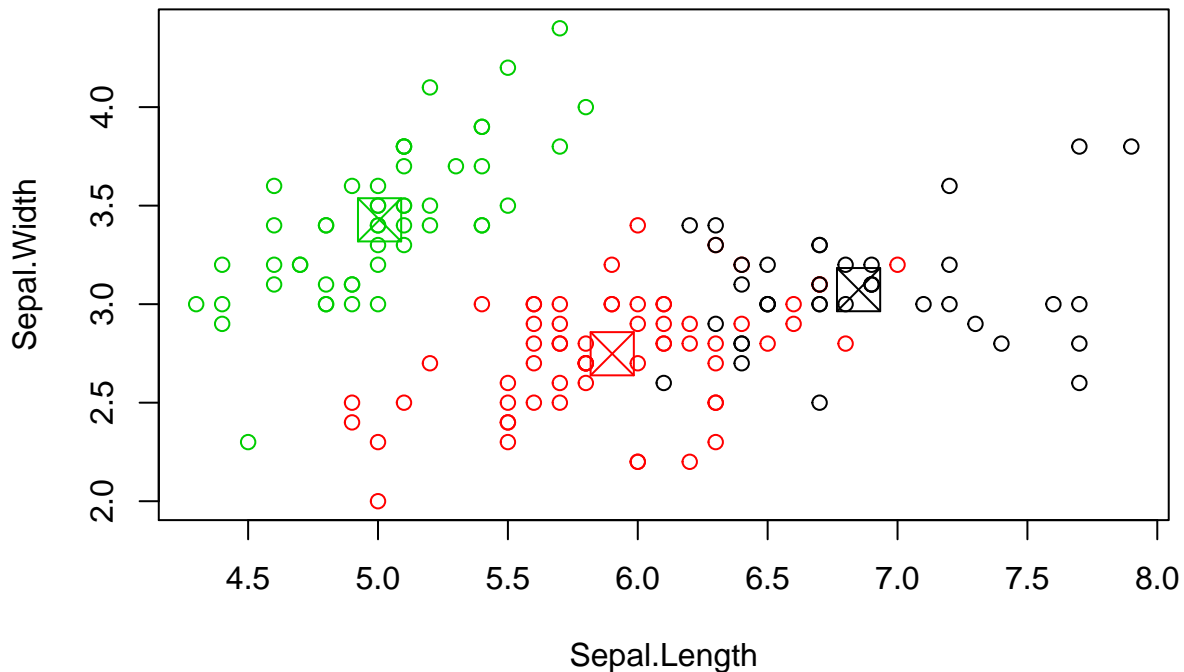
```
## K-means clustering with 3 clusters of sizes 38, 62, 50
##
## Cluster means:
##   Sepal.Length Sepal.Width Petal.Length Petal.Width
## 1    6.850000    3.073684    5.742105    2.071053
## 2    5.901613    2.748387    4.393548    1.433871
## 3    5.006000    3.428000    1.462000    0.246000
##
## Clustering vector:
##   [1] 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
##  [36] 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 2 2 1 2 2 2 2 2 2 2 2 2 2 2 2 2
##  [71] 2 2 2 2 2 2 2 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 1 2 1 1 1
## [106] 1 2 1 1 1 1 1 1 2 2 1 1 1 1 2 1 2 1 1 2 2 1 1 1 1 1 2 1 1 1 2 1
## [141] 1 1 2 1 1 1 2 1 1 2
##
## Within cluster sum of squares by cluster:
## [1] 23.87947 39.82097 15.15100
## (between_SS / total_SS =  88.4 %)
##
## Available components:
##
```

```
## [1] "cluster"      "centers"      "totss"       "withinss"
## [5] "tot.withinss" "betweenss"    "size"        "iter"
## [9] "ifault"
```

```
table(iris$Species,kmeans_result$cluster)
```

```
##
##           1  2  3
##  setosa    0  0 50
##  versicolor 2 48  0
##  virginica 36 14  0
```

```
plot(iris2[c("Sepal.Length", "Sepal.Width")],col=kmeans_result$cluster)
points(kmeans_result$centers[,c("Sepal.Length", "Sepal.Width")],col=1:3,pch=7,cex=3)
```



```
iris
```

```
##      Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1           5.1         3.5         1.4         0.2    setosa
## 2           4.9         3.0         1.4         0.2    setosa
## 3           4.7         3.2         1.3         0.2    setosa
## 4           4.6         3.1         1.5         0.2    setosa
## 5           5.0         3.6         1.4         0.2    setosa
## 6           5.4         3.9         1.7         0.4    setosa
## 7           4.6         3.4         1.4         0.3    setosa
## 8           5.0         3.4         1.5         0.2    setosa
## 9           4.4         2.9         1.4         0.2    setosa
## 10          4.9         3.1         1.5         0.1    setosa
## 11          5.4         3.7         1.5         0.2    setosa
## 12          4.8         3.4         1.6         0.2    setosa
## 13          4.8         3.0         1.4         0.1    setosa
## 14          4.3         3.0         1.1         0.1    setosa
## 15          5.8         4.0         1.2         0.2    setosa
## 16          5.7         4.4         1.5         0.4    setosa
```

## 17	5.4	3.9	1.3	0.4	setosa
## 18	5.1	3.5	1.4	0.3	setosa
## 19	5.7	3.8	1.7	0.3	setosa
## 20	5.1	3.8	1.5	0.3	setosa
## 21	5.4	3.4	1.7	0.2	setosa
## 22	5.1	3.7	1.5	0.4	setosa
## 23	4.6	3.6	1.0	0.2	setosa
## 24	5.1	3.3	1.7	0.5	setosa
## 25	4.8	3.4	1.9	0.2	setosa
## 26	5.0	3.0	1.6	0.2	setosa
## 27	5.0	3.4	1.6	0.4	setosa
## 28	5.2	3.5	1.5	0.2	setosa
## 29	5.2	3.4	1.4	0.2	setosa
## 30	4.7	3.2	1.6	0.2	setosa
## 31	4.8	3.1	1.6	0.2	setosa
## 32	5.4	3.4	1.5	0.4	setosa
## 33	5.2	4.1	1.5	0.1	setosa
## 34	5.5	4.2	1.4	0.2	setosa
## 35	4.9	3.1	1.5	0.2	setosa
## 36	5.0	3.2	1.2	0.2	setosa
## 37	5.5	3.5	1.3	0.2	setosa
## 38	4.9	3.6	1.4	0.1	setosa
## 39	4.4	3.0	1.3	0.2	setosa
## 40	5.1	3.4	1.5	0.2	setosa
## 41	5.0	3.5	1.3	0.3	setosa
## 42	4.5	2.3	1.3	0.3	setosa
## 43	4.4	3.2	1.3	0.2	setosa
## 44	5.0	3.5	1.6	0.6	setosa
## 45	5.1	3.8	1.9	0.4	setosa
## 46	4.8	3.0	1.4	0.3	setosa
## 47	5.1	3.8	1.6	0.2	setosa
## 48	4.6	3.2	1.4	0.2	setosa
## 49	5.3	3.7	1.5	0.2	setosa
## 50	5.0	3.3	1.4	0.2	setosa
## 51	7.0	3.2	4.7	1.4	versicolor
## 52	6.4	3.2	4.5	1.5	versicolor
## 53	6.9	3.1	4.9	1.5	versicolor
## 54	5.5	2.3	4.0	1.3	versicolor
## 55	6.5	2.8	4.6	1.5	versicolor
## 56	5.7	2.8	4.5	1.3	versicolor
## 57	6.3	3.3	4.7	1.6	versicolor
## 58	4.9	2.4	3.3	1.0	versicolor
## 59	6.6	2.9	4.6	1.3	versicolor
## 60	5.2	2.7	3.9	1.4	versicolor
## 61	5.0	2.0	3.5	1.0	versicolor
## 62	5.9	3.0	4.2	1.5	versicolor
## 63	6.0	2.2	4.0	1.0	versicolor
## 64	6.1	2.9	4.7	1.4	versicolor
## 65	5.6	2.9	3.6	1.3	versicolor
## 66	6.7	3.1	4.4	1.4	versicolor
## 67	5.6	3.0	4.5	1.5	versicolor
## 68	5.8	2.7	4.1	1.0	versicolor
## 69	6.2	2.2	4.5	1.5	versicolor
## 70	5.6	2.5	3.9	1.1	versicolor

## 71	5.9	3.2	4.8	1.8 versicolor
## 72	6.1	2.8	4.0	1.3 versicolor
## 73	6.3	2.5	4.9	1.5 versicolor
## 74	6.1	2.8	4.7	1.2 versicolor
## 75	6.4	2.9	4.3	1.3 versicolor
## 76	6.6	3.0	4.4	1.4 versicolor
## 77	6.8	2.8	4.8	1.4 versicolor
## 78	6.7	3.0	5.0	1.7 versicolor
## 79	6.0	2.9	4.5	1.5 versicolor
## 80	5.7	2.6	3.5	1.0 versicolor
## 81	5.5	2.4	3.8	1.1 versicolor
## 82	5.5	2.4	3.7	1.0 versicolor
## 83	5.8	2.7	3.9	1.2 versicolor
## 84	6.0	2.7	5.1	1.6 versicolor
## 85	5.4	3.0	4.5	1.5 versicolor
## 86	6.0	3.4	4.5	1.6 versicolor
## 87	6.7	3.1	4.7	1.5 versicolor
## 88	6.3	2.3	4.4	1.3 versicolor
## 89	5.6	3.0	4.1	1.3 versicolor
## 90	5.5	2.5	4.0	1.3 versicolor
## 91	5.5	2.6	4.4	1.2 versicolor
## 92	6.1	3.0	4.6	1.4 versicolor
## 93	5.8	2.6	4.0	1.2 versicolor
## 94	5.0	2.3	3.3	1.0 versicolor
## 95	5.6	2.7	4.2	1.3 versicolor
## 96	5.7	3.0	4.2	1.2 versicolor
## 97	5.7	2.9	4.2	1.3 versicolor
## 98	6.2	2.9	4.3	1.3 versicolor
## 99	5.1	2.5	3.0	1.1 versicolor
## 100	5.7	2.8	4.1	1.3 versicolor
## 101	6.3	3.3	6.0	2.5 virginica
## 102	5.8	2.7	5.1	1.9 virginica
## 103	7.1	3.0	5.9	2.1 virginica
## 104	6.3	2.9	5.6	1.8 virginica
## 105	6.5	3.0	5.8	2.2 virginica
## 106	7.6	3.0	6.6	2.1 virginica
## 107	4.9	2.5	4.5	1.7 virginica
## 108	7.3	2.9	6.3	1.8 virginica
## 109	6.7	2.5	5.8	1.8 virginica
## 110	7.2	3.6	6.1	2.5 virginica
## 111	6.5	3.2	5.1	2.0 virginica
## 112	6.4	2.7	5.3	1.9 virginica
## 113	6.8	3.0	5.5	2.1 virginica
## 114	5.7	2.5	5.0	2.0 virginica
## 115	5.8	2.8	5.1	2.4 virginica
## 116	6.4	3.2	5.3	2.3 virginica
## 117	6.5	3.0	5.5	1.8 virginica
## 118	7.7	3.8	6.7	2.2 virginica
## 119	7.7	2.6	6.9	2.3 virginica
## 120	6.0	2.2	5.0	1.5 virginica
## 121	6.9	3.2	5.7	2.3 virginica
## 122	5.6	2.8	4.9	2.0 virginica
## 123	7.7	2.8	6.7	2.0 virginica
## 124	6.3	2.7	4.9	1.8 virginica

## 125	6.7	3.3	5.7	2.1	virginica
## 126	7.2	3.2	6.0	1.8	virginica
## 127	6.2	2.8	4.8	1.8	virginica
## 128	6.1	3.0	4.9	1.8	virginica
## 129	6.4	2.8	5.6	2.1	virginica
## 130	7.2	3.0	5.8	1.6	virginica
## 131	7.4	2.8	6.1	1.9	virginica
## 132	7.9	3.8	6.4	2.0	virginica
## 133	6.4	2.8	5.6	2.2	virginica
## 134	6.3	2.8	5.1	1.5	virginica
## 135	6.1	2.6	5.6	1.4	virginica
## 136	7.7	3.0	6.1	2.3	virginica
## 137	6.3	3.4	5.6	2.4	virginica
## 138	6.4	3.1	5.5	1.8	virginica
## 139	6.0	3.0	4.8	1.8	virginica
## 140	6.9	3.1	5.4	2.1	virginica
## 141	6.7	3.1	5.6	2.4	virginica
## 142	6.9	3.1	5.1	2.3	virginica
## 143	5.8	2.7	5.1	1.9	virginica
## 144	6.8	3.2	5.9	2.3	virginica
## 145	6.7	3.3	5.7	2.5	virginica
## 146	6.7	3.0	5.2	2.3	virginica
## 147	6.3	2.5	5.0	1.9	virginica
## 148	6.5	3.0	5.2	2.0	virginica
## 149	6.2	3.4	5.4	2.3	virginica
## 150	5.9	3.0	5.1	1.8	virginica

```
(centers<- kmeans_result$centers[kmeans_result$cluster,])
```

[illegible]

[illegible]

[illegible]

```
## 2      5.901613      2.748387      4.393548      1.433871
## 1      6.850000      3.073684      5.742105      2.071053
## 1      6.850000      3.073684      5.742105      2.071053
## 1      6.850000      3.073684      5.742105      2.071053
## 1      6.850000      3.073684      5.742105      2.071053
## 2      5.901613      2.748387      4.393548      1.433871
## 1      6.850000      3.073684      5.742105      2.071053
## 1      6.850000      3.073684      5.742105      2.071053
## 1      6.850000      3.073684      5.742105      2.071053
## 2      5.901613      2.748387      4.393548      1.433871
## 1      6.850000      3.073684      5.742105      2.071053
## 1      6.850000      3.073684      5.742105      2.071053
## 1      6.850000      3.073684      5.742105      2.071053
## 2      5.901613      2.748387      4.393548      1.433871
## 1      6.850000      3.073684      5.742105      2.071053
## 1      6.850000      3.073684      5.742105      2.071053
## 2      5.901613      2.748387      4.393548      1.433871
```

```
(distance<-sqrt(rowSums((iris2-centers)^2)))
```

```
##      [1] 0.14135063 0.44763825 0.41710910 0.52533799 0.18862662 0.67703767
##      [7] 0.41518670 0.06618157 0.80745278 0.37627118 0.48247280 0.25373214
##     [13] 0.50077939 0.91322505 1.01409073 1.20481534 0.65420180 0.14415270
##     [19] 0.82436642 0.38933276 0.46344363 0.32860310 0.64029681 0.38259639
##     [25] 0.48701129 0.45208406 0.20875823 0.21536016 0.21066561 0.40838707
##     [31] 0.41373905 0.42565244 0.71552778 0.91977171 0.34982853 0.35039977
##     [37] 0.52685861 0.25686572 0.76077592 0.11480418 0.18541845 1.24803045
##     [43] 0.66901420 0.38675574 0.60231221 0.48205809 0.41034132 0.47199576
##     [49] 0.40494444 0.14959947 1.22697525 0.68414100 1.01903626 0.73153652
##     [55] 0.63853451 0.26937898 0.76452634 1.58388575 0.75582717 0.85984838
##     [61] 1.53611907 0.32426175 0.80841374 0.39674141 0.87269542 0.87306498
##     [67] 0.41229163 0.53579956 0.63676390 0.71254917 0.70937310 0.46349013
##     [73] 0.69373966 0.43661144 0.54593856 0.74313017 0.98798453 0.84636259
##     [79] 0.21993519 1.02437260 0.86396528 0.97566381 0.55763082 0.73395781
##     [85] 0.57500396 0.68790275 0.92700552 0.61459444 0.50830256 0.62911910
##     [91] 0.48790256 0.38266958 0.49185351 1.54856350 0.38560870 0.44284695
##     [97] 0.34498790 0.37241653 1.66064034 0.38393196 0.77731871 0.85382472
##    [103] 0.30610139 0.65293923 0.38458885 1.14225684 1.07101875 0.78573677
##    [109] 0.65454939 0.84355960 0.74552218 0.75289837 0.25958095 0.88917352
##    [115] 1.20227628 0.68288333 0.50991553 1.47791217 1.52971038 0.82617494
##    [121] 0.26952816 0.81891975 1.31149299 0.74269596 0.27627819 0.52766931
##    [127] 0.62526165 0.70228926 0.54629196 0.59428255 0.73126650 1.43802246
##    [133] 0.56055720 0.81536685 1.12133058 0.95311851 0.73306362 0.57903109
##    [139] 0.61011676 0.34794609 0.38934920 0.68403844 0.85382472 0.30952112
##    [145] 0.50939919 0.61173881 0.89747884 0.65334214 0.83572418 0.83452741
```

```
(outliers<-order(distance,decreasing = T)[1:5])
```

```
## [1] 99 58 94 61 119
```

```
print (outliers)
```

```
## [1] 99 58 94 61 119
```

```
print(iris2[outliers,])
```

```
##      Sepal.Length Sepal.Width Petal.Length Petal.Width
```

## 99	5.1	2.5	3.0	1.1
## 58	4.9	2.4	3.3	1.0
## 94	5.0	2.3	3.3	1.0
## 61	5.0	2.0	3.5	1.0
## 119	7.7	2.6	6.9	2.3