

1. $x=[2,2,2]$, $h=[2,2,2]$ 做卷積，另依下側條件各做一次卷積。

- 試改變 x ，再觀察 y 。
- 試改變 h ，再觀察 y 。

問題

- 問輸出為何? (3 組答案) (8 分)
- 請將輸出畫圖。(3 張圖) (4 分)
- 將數學推導詳細列出。(由題目那組推導) (4 分)
- 輸出的長度與 x , h 之間的長度有何關係? (9 分)

```
x=[2,2,2]
```

```
x = 1×3  
    2    2    2
```

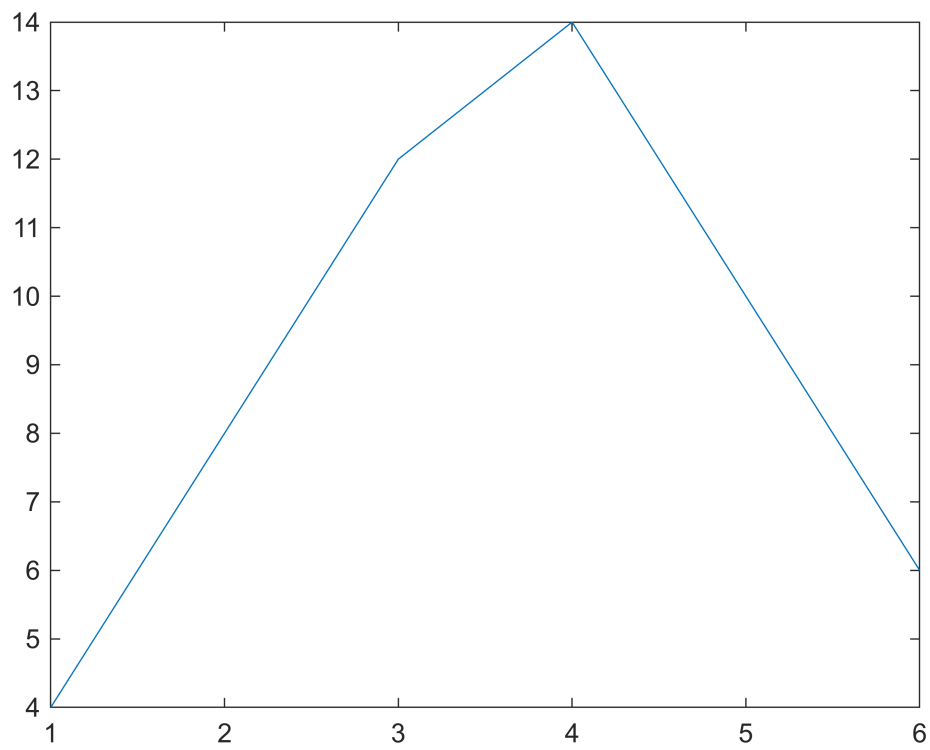
```
h=[2,2,2,3]
```

```
h = 1×4  
    2    2    2    3
```

```
c=conv(x,h)
```

```
c = 1×6  
    4    8   12   14   10    6
```

```
plot(c)
```



```
x=[2,2,2]
```

```
x = 1×3
     2     2     2
```

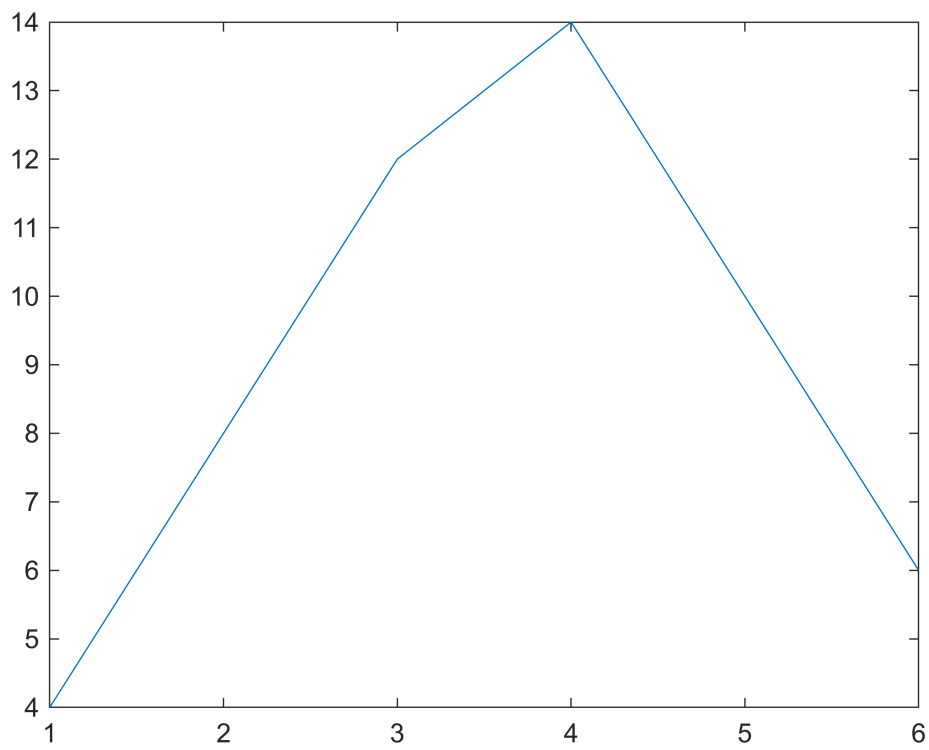
```
h=[2,2,2,3]
```

```
h = 1×4
     2     2     2     3
```

```
c=conv(x,h)
```

```
c = 1×6
     4     8    12    14    10     6
```

```
plot(c)
```



```
x=[2,2,4]
```

```
x = 1×3
     2     2     4
```

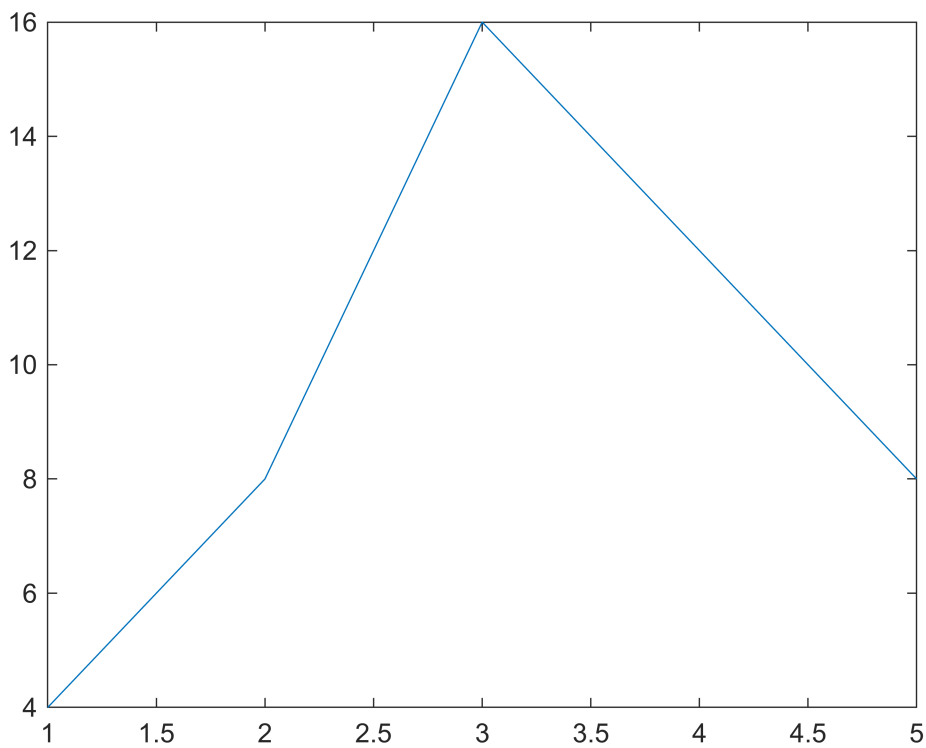
```
h=[2,2,2]
```

```
h = 1×3
     2     2     2
```

```
c=conv(x,h)
```

```
c = 1×5
     4     8    16    12     8
```

```
plot(c)
```



%X 與 h 是因為 h 反轉再重合相乘
%兩個 vector 的長度相加減一

2.請問下列卷積後輸出為何？

- $x = \cos(2\pi f \cdot \text{time})$ [Lab 3 FFT 範例], $h = [1, 1, 1]$ (15 分)
- $x = [2 \ 1; \ 3 \ 2]$, $h = [-1 \ 1; \ 2 \ 1]$ (10 分)

N=256

N = 256

fs=8000

fs = 8000

freqStep=fs/N

freqStep = 31.2500

time=(0:N-1)/fs

time = 1×256
0 0.0001 0.0003 0.0004 0.0005 0.0006 0.0008 0.0009 ...

f=10*freqStep

```
f = 312.5000
```

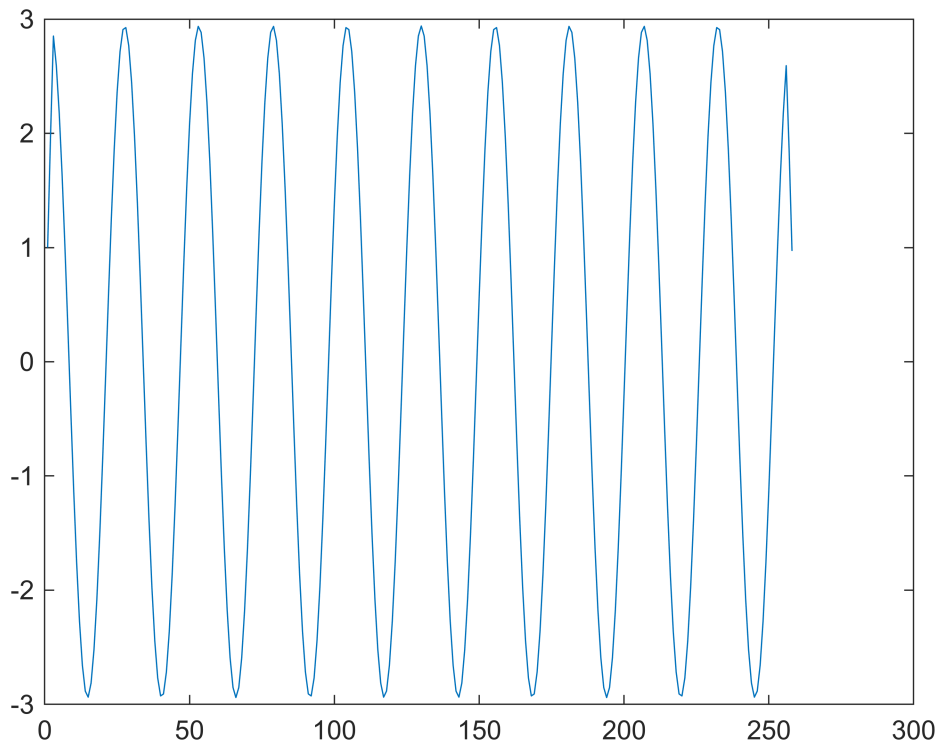
```
x= cos(2*pi*f*time)
```

```
x = 1×256  
1.0000    0.9700    0.8819    0.7410    0.5556    0.3369    0.0980   -0.1467 ...
```

```
h=[1,1,1]
```

```
h = 1×3  
1    1    1
```

```
imp = [1; zeros(49,1)];  
plot(conv(x,h))
```



```
x=[2 1; 3 2 ]
```

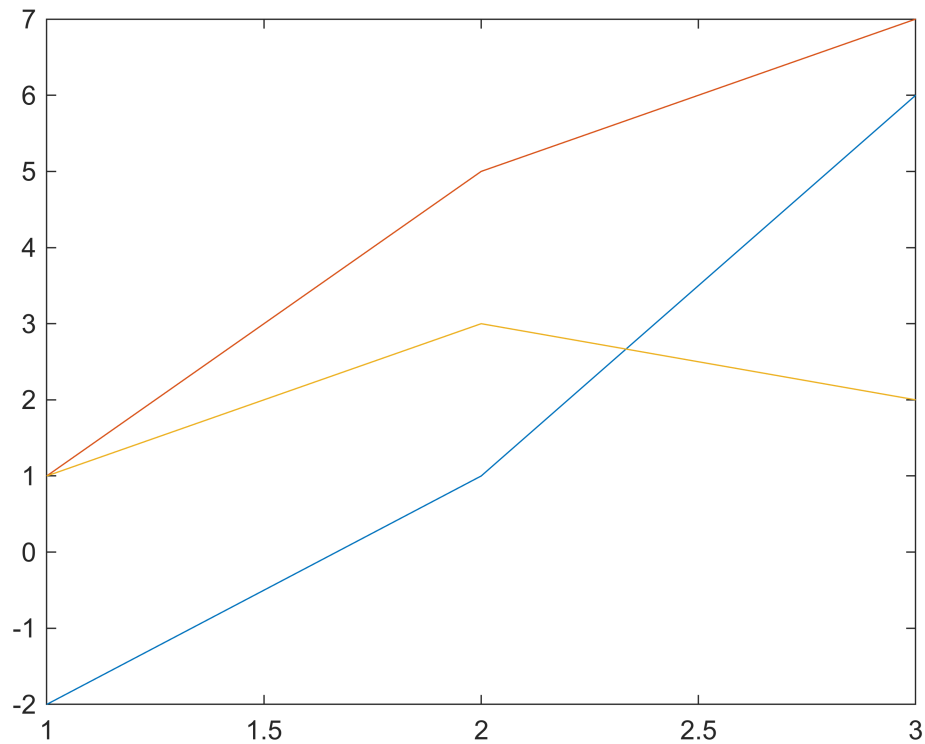
```
x = 2×2  
2    1  
3    2
```

```
h=[-1 1; 2 1]
```

```
h = 2×2  
-1    1  
2    1
```

```
plot(conv2(x,h))
```

```
axis tight
```



3.兩個系統皆具有脈衝響應(impulse responses), 並使用 MATLAB 指令繪製階躍響應(step responses)後的結果。(25%)

```
t=-5:1:5
```

```
t = 1×11  
    -5    -4    -3    -2    -1     0     1     2     3     4     5
```

```
h1=[0.25 0.25 0.25 0.25 zeros(1,6)]
```

```
h1 = 1×10  
    0.2500    0.2500    0.2500    0.2500         0         0         0         0 ...
```

```
h2=[0.25 -0.25 -0.25 0.25 zeros(1,6)]
```

```
h2 = 1×10  
    0.2500   -0.2500   -0.2500    0.2500         0         0         0         0 ...
```

```
x=conv(h1,heaviside(t))
```

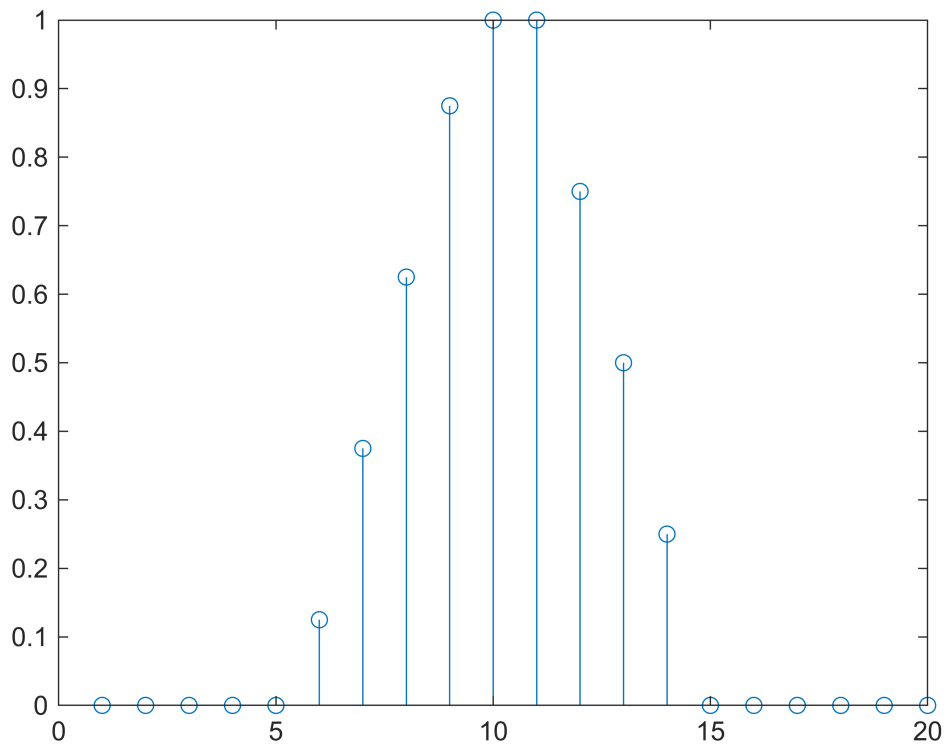
```
x = 1×20  
     0         0         0         0         0    0.1250    0.3750    0.6250 ...
```

```
x1=conv(h2,heaviside(t))
```

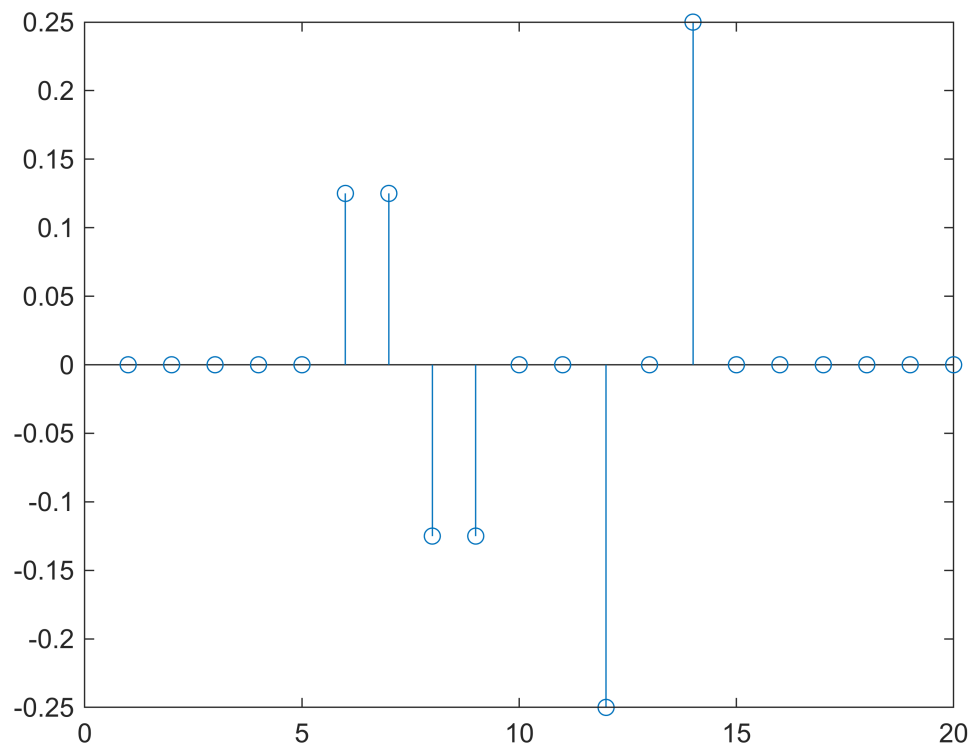
```
x1 = 1×20
```

```
0      0      0      0      0      0.1250      0.1250      -0.1250 ...
```

```
stem(x)
```



```
stem(x1)
```



4.使用 MATLAB 指令，繪製以下捲積圖，

$y(t) = (e^{-at} \cdot u(t)) * (\cos(2\pi f t) \cdot u(t))$ ，其中從 $t=0$ 到 3、 $a=2$ 、 $f=20$

繪製 $y(t)$ 整段訊號。 (25 分)

- 給定 t and $u(t)$ ， $\Delta t = 0.1$ 。
- 使用函式: $x1 = e^{-at} \cdot u(t)$
- 使用函式: $x2 = \cos(2\pi f t) \cdot u(t)$
- 使用函式: $y = x1 * x2$

```
t= 0:0.1:3
```

```
t = 1x31
    0    0.1000    0.2000    0.3000    0.4000    0.5000    0.6000    0.7000 ...
```

```
a=2
```

```
a = 2
```

```
f=20
```



```
f = 20
```

```
%x1=(exp())  
x1 = exp(-a*t).*heaviside(t)
```

```
x1 = 1×31  
    0.5000    0.8187    0.6703    0.5488    0.4493    0.3679    0.3012    0.2466 ...
```

```
x2 = cos(2*pi*f*t).*heaviside(t)
```

```
x2 = 1×31  
    0.5000    1.0000    1.0000    1.0000    1.0000    1.0000    1.0000    1.0000 ...
```

```
y=conv(x1,x2)
```

```
y = 1×61  
    0.2500    0.9094    1.6539    2.2635    2.7625    3.1711    3.5057    3.7796 ...
```

```
stem(y)
```

