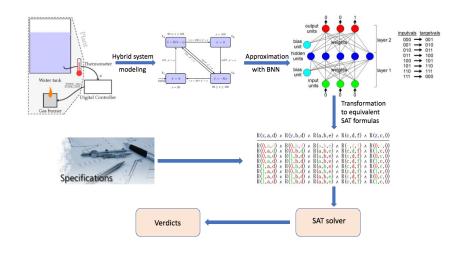
Leveraging SAT and BNN to Design safety-critical systems (LSBD)

05 March 2021

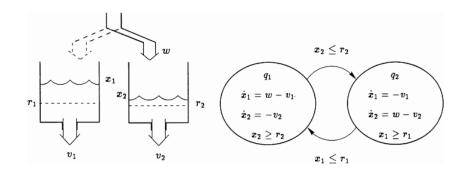
### Simple Illustration



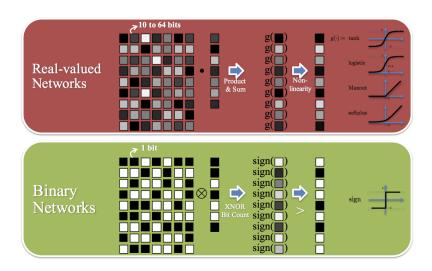
#### Primary Elements of LSBD

- Differential equation solution approximated by (binary) NN
  - ► One recent very popular NN for this is called PINN (next slides)
  - Several possibilities for our case: adapt PINN that will be approximated further by BNN; or directly approximate ODE (PDE) by BNN (no related work)
  - Trade-off between accuracy and complexity
- Interaction between continuous and discrete aspects (formulate an explicit jump relation)
  - Very few works on this from machine learning community
  - ▶ It seems that neural networks are not suitable to classify the system states with regard to the occurrence of an event (imbalanced data). (see [4])
  - Other techniques? (directly encoded in SMT?)
- From BNN to SAT (see [5])

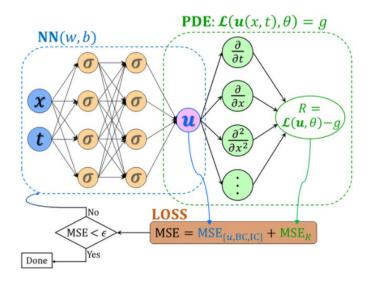
# Hybrid Systems [6]



# BNN vs. DNN [1, 2]



# Physics-informed neural networks (PINN)[3]



#### Useful references

- Matthieu Courbariaux, Yoshua Bengio, BinaryNet: Training Deep Neural Networks with Weights and Activations Constrained to +1 or -1 (https://arxiv.org/pdf/1602.02830v1.pdf)
- 4 Haotong Qin, Ruihao Gong, Xianglong Liu, Xiao Bai, Jingkuan Song, Nicu Sebe, Binary Neural Networks: A Survey (https://arxiv.org/pdf/2004.03333.pdf)
- Maziar Raissi, Paris Perdikaris, George Em Karniadakis, Physics-Informed Neural Networks: A Deep Learning Framework for Solving Forward and Inverse Problems Involving Nonlinear Partial Differential Equations
- Stefanie Nadine Winkler, Felix Breitenecker, Neural Network Application for Event Detection in Hybrid Dynamical Systems
- Nina Narodytska, Shiva Prasad Kasiviswanathan, Leonid Ryzhyk, Mooly Sagiv, Toby Walsh, Verifying Properties of Binarized Deep Neural Networks
- Radoslav Ivanov, James Weimer, Rajeev Alur, George J. Pappas, Insup Lee, Verisig: verifying safety properties of hybrid systems with neural network controllers (https://arxiv.org/pdf/1811.01828.pdf)

#### Benchmark collection site

https://ths.rwth-aachen.de/research/projects/hypro/benchmarks-of-continuous-and-hybrid-systems/hypro/benchmarks-of-continuous-and-hybrid-systems/hypro/bench

## **Expenses**

- GPU (NVIDIA GeForce RTX 3090)?
- Else for now?