

midtermrain-lina.R

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Mon Oct 19 22:15:56 2015

```
## read data in loops
library(dplyr)

library(ggplot2)
raw<-NULL
Y<-c("00","01","02","03","04")
M<-c("01","02","03","04","05","06","07","08","09","10","11","12")
for(i in 1:5)
{
  for(j in 1:12)
  {
    name<-paste("L-",Y[i], "-",M[j], ".txt", sep="")
    raw<-rbind(raw, read.csv(name, skip=2, stringsAsFactors = F, header=T))
  }
}

## data cleaning
raw<-raw[,2:25]
dim(raw)

## [1] 1827    24

## let T=0, other strange data=-1
raw[raw=="T"]<-0
raw[raw=="----"]<-(-1)
raw[raw=="M"]<-(-1)
raw[raw=="T  "]<-0
raw[raw=="M  "]<-(-1)

class(raw[1,1])

## [1] "character"

test<-as.matrix(raw)
data<-as.numeric(t(test))## trans the matrix and make it into a vector
length(data)

## [1] 43848

## count the rain.
rain<-NULL
temp<-0
k=1
```

```

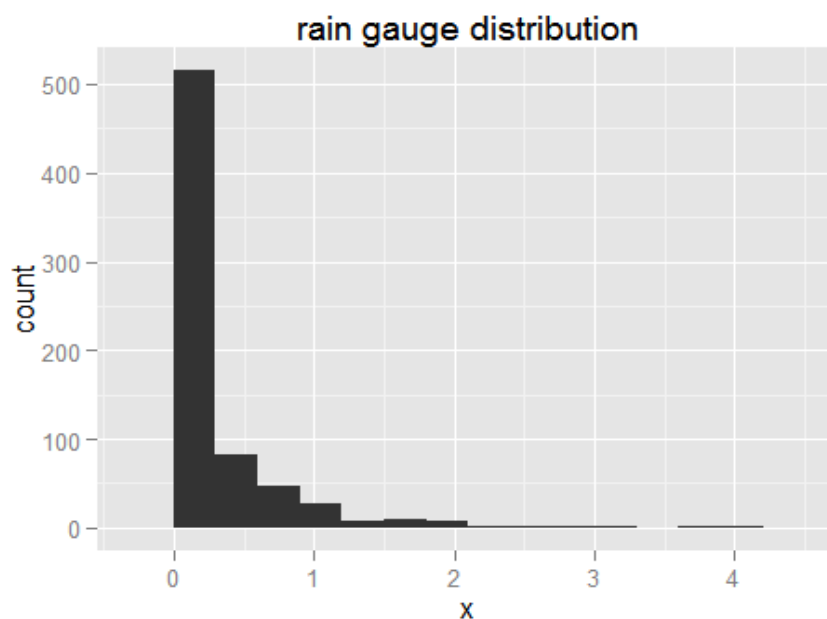
while(k<length(data))
{
  if(data[k]>=0)
  {
    while(data[k]>=0)
    {
      temp=temp+data[k]
      k=k+1
    }
    rain<-c(rain,temp)
    temp=0
  }
  else{k=k+1}
}
rain

## MEM MLE
data1<-data.frame(x=rain)
data1<-subset(data1,data1$x!=0.00)
head(data1)

##      x
## 1 0.03
## 3 0.03
## 4 0.01
## 5 0.01
## 6 0.97
## 7 0.06

ggplot(data=data1)+geom_histogram(aes(x),binwidth=.3)+labs(title="rain
gauge distribution")

```



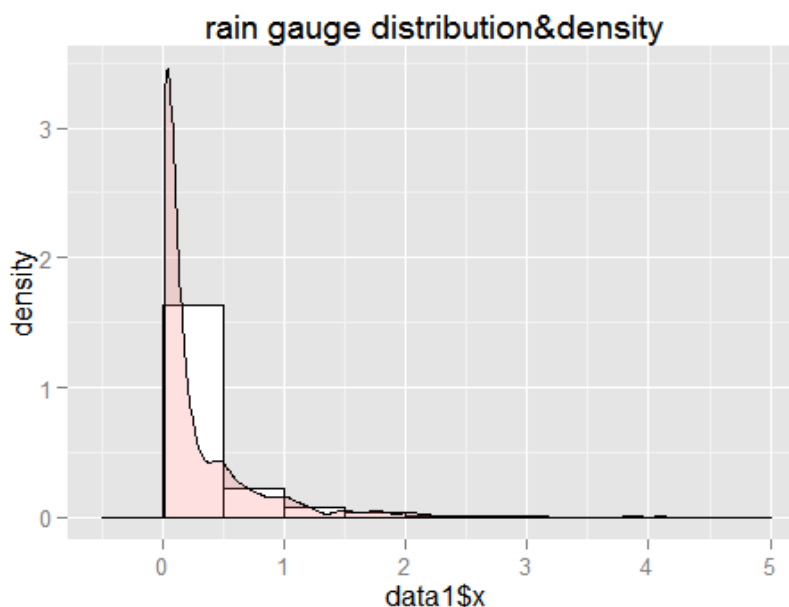
```

mean(data1$x)
## [1] 0.2831108
var(data1$x)
## [1] 0.2218382
## 2 parameters
alpha <- mean(data1$x)^2/var(data1$x)
lambda <- mean(data1$x)/var(data1$x)
## plot HW1
gam<-function(x)
{
  gamm<-(lambda^alpha)*x^(alpha-1)*exp(-lambda*x)/gamma(alpha)
  return(gamm)
}
data1$ga<-gam(data1$x)
head(data1)

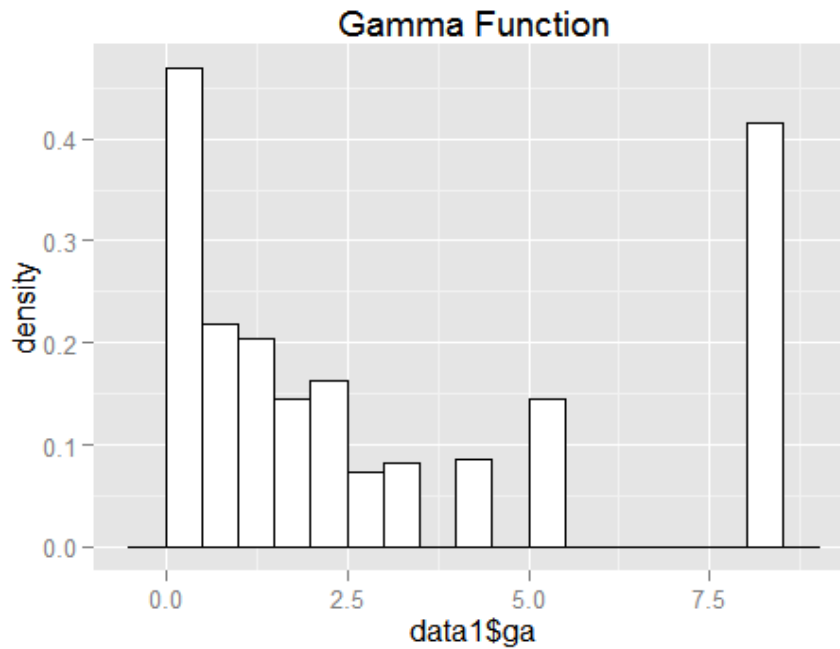
##      x      ga
## 1 0.03 4.0063483
## 3 0.03 4.0063483
## 4 0.01 8.2902504
## 5 0.01 8.2902504
## 6 0.97 0.1310848
## 7 0.06 2.4765980

## plot of density & count
ggplot(data1,aes(x=data1$x))+geom_histogram(aes(y=..density..),binwidth
=.5,colour="black",fill="white")+labs(title="rain gauge distribution&de
nsity")+geom_density(alpha=.2,fill="#FF6666")

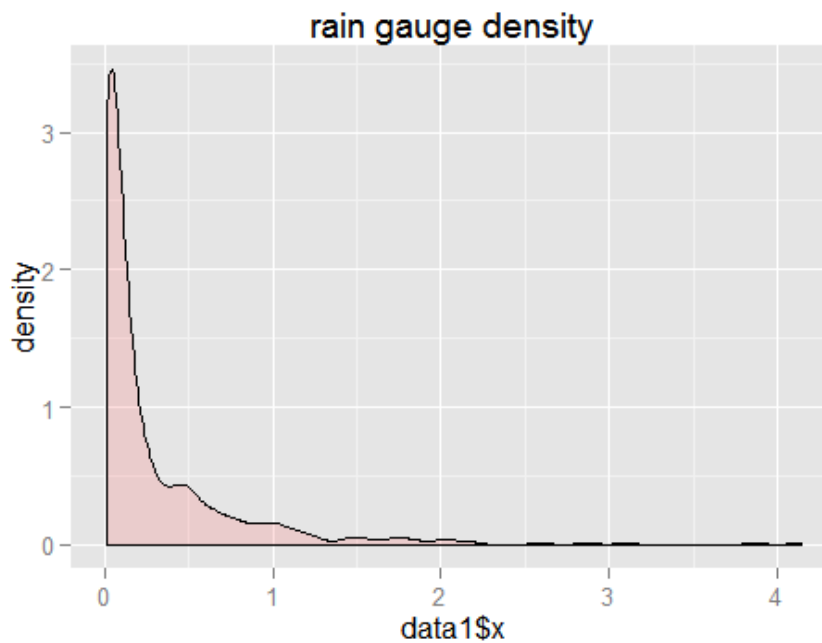
```



```
## plot of density function
ggplot(data1,aes(x=data1$ga))+geom_histogram(aes(y=..density..),binwidth
h=.5,colour="black",fill="white")+labs(title="Gamma Function")
```



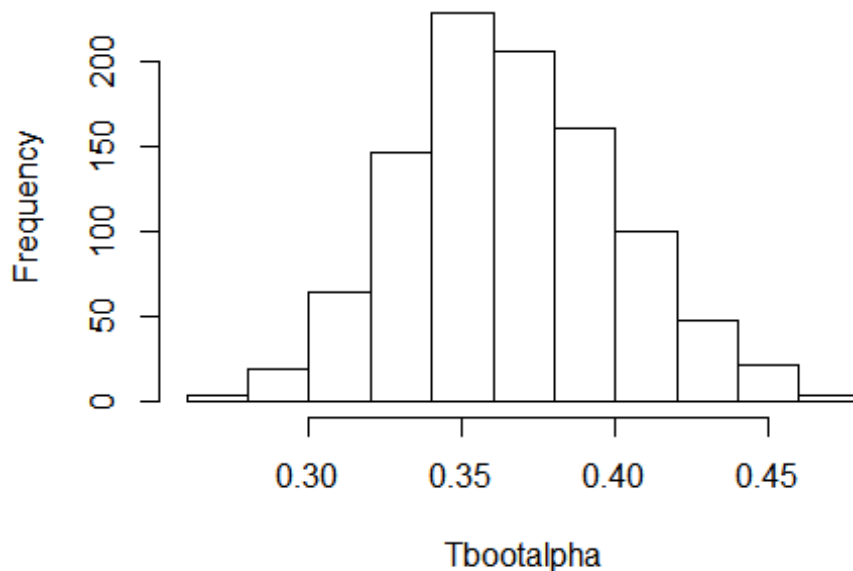
```
## plot of density
ggplot(data1,aes(x=data1$x))+geom_density(alpha=0.2,fill="#FF6666")+lab
s(title="rain gauge density")
```



```
## bootstrap HW2
n<-length(data1$x)
B<-1000
Tbootalpha<-rep(0,B)
Tbootlambda<-rep(0,B)
for(i in 1:B){
  al.s<-sample(data1$x,n,replace=TRUE)
  lam.s<-sample(data1$x,n,replace=TRUE)
  Tbootalpha[i]<-mean(al.s)^2/var(al.s)
  Tbootlambda[i]<-mean(lam.s)/var(lam.s)
}
## standrad error for alpha
seal<-sqrt(var(Tbootalpha))
seal

## [1] 0.03557355
hist(Tbootalpha)
```

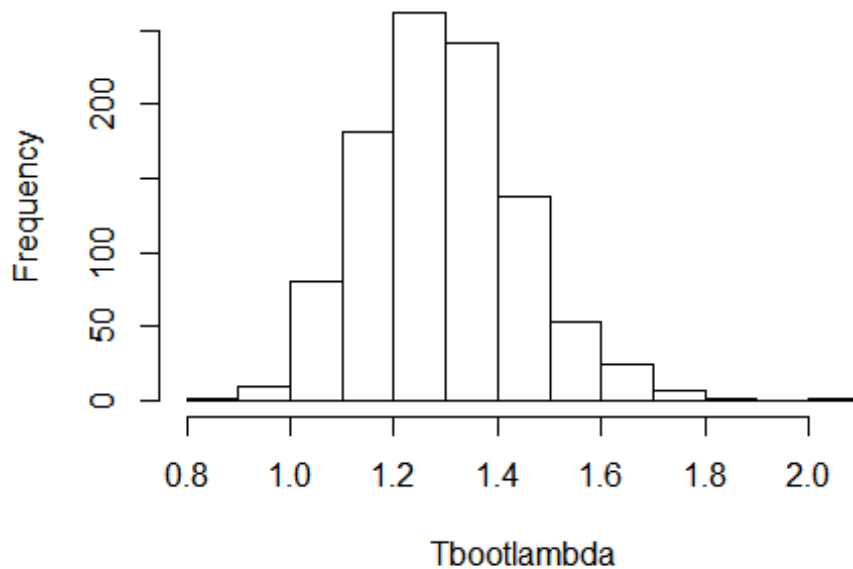
Histogram of Tbootalpha



```
## standrad error for lambda
selam<-sqrt(var(Tbootlambda))
selam

## [1] 0.1504287
hist(Tbootlambda)
```

Histogram of Tbootlambda



```
## MLE
theta <- c(alpha,lambda)
minus.likelihood <- function(theta) {-(n*theta[1]*log(theta[2])-n*lgamma(theta[1])+(theta[1]-1)*sum(log(data1$x))-theta[2]*sum(data1$x))}
max.likelihood <- nlminb(start=c(alpha,lambda), obj = minus.likelihood)
theta

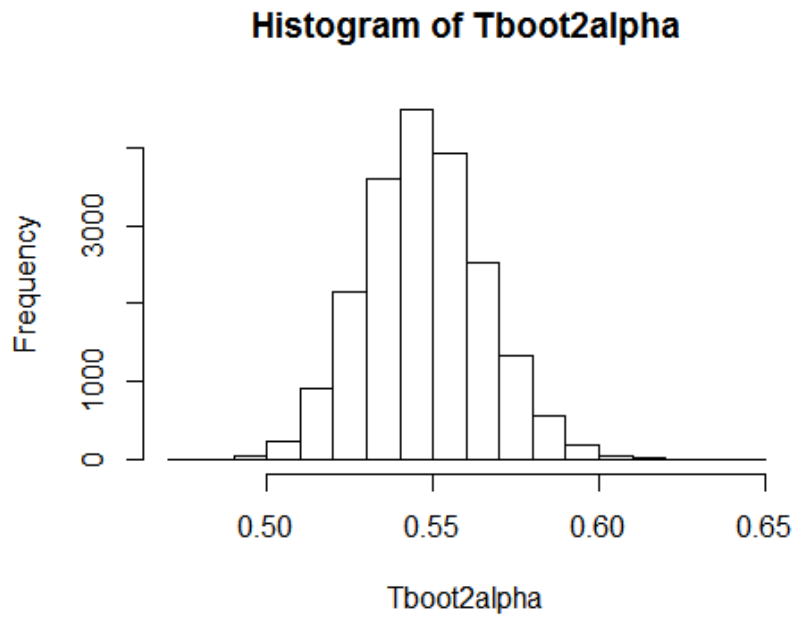
## [1] 0.3613071 1.2762037

max.likelihood$par

## [1] 0.5461541 1.9291179

## bootstrap MLE
B2<-20000
Tboot2alpha<-rep(0,B2)
Tboot2lambda<-rep(0,B)
minus.likelihood2 <- function(theta) {-(n*theta[1]*log(theta[2])-n*lgamma(theta[1])+(theta[1]-1)*sum(log(boot))-theta[2]*sum(boot))}
for(i in 1:B2)
{ boot <- sample(data1$x, n, replace=TRUE)
  mle <- nlminb(start=c(.1794, 1.1062), obj = minus.likelihood2)
  Tboot2alpha[i]<-mle$par[1]
  Tboot2lambda[i]<-mle$par[2]
}
## standard error for alpha in mle
se2a1<-sd(Tboot2alpha)
se2a1
```

```
## [1] 0.017941  
hist(Tboot2alpha)
```



```
## standard error for lambda in mem  
se2la<-sd(Tboot2lambda)  
se2la  
## [1] 0.1584769  
hist(Tboot2lambda)
```

