

## Task 1

part a:

A have 8 values and each  $B_1, B_2 \dots B_{10}$  have 5 values

$$\text{so } 8 \times 5^{10} = 8 \times 9765625 = 78125000$$

part b:

Each  $B_i$  is conditionally independent of all other  $\{B_j\}$  variables

$$\text{so } 8 \times 5 \times 10 = 400$$

part c:

Yes, this scenario follow the Naive-Bayes model

## Task 2.

Q. C C C C C L

$$\begin{aligned} c \quad P(c) &= 0.1 \times 1 + 0.2 \times 0.75 + 0.4 \times 0.5 + 0.2 \times 0.25 + 0.1 \times 0 \\ &= 0.5 \end{aligned}$$

$$P(h_1) = \frac{0.1 \times 1}{0.5} = 0.2 \quad P(h_2) = \frac{0.2 \times 0.75}{0.5} = 0.3$$

$$P(h_3) = \frac{0.4 \times 0.5}{0.5} = 0.4 \quad P(h_4) = \frac{0.2 \times 0.25}{0.5} = 0.1$$

$$P(h_5) = \frac{0.1 \times 0}{0.5} = 0$$

$$C \quad P(c) = 0.2 \times 1 + 0.3 \times 0.75 + 0.4 \times 0.5 + 0.1 \times 0.25 + 0 \times 0 \\ = 0.65$$

$$P(h_1) = \frac{0.2 \times 1}{0.65} = 0.30769 \quad P(h_2) = \frac{0.3 \times 0.75}{0.65} = 0.34615$$

$$P(h_3) = \frac{0.4 \times 0.5}{0.65} = 0.30769 \quad P(h_4) = \frac{0.1 \times 0.25}{0.65} = 0.03846$$

$$P(h_5) = \frac{0 \times 0}{0.65} = 0$$

$$C \quad P(c) = 0.30769 \times 1 + 0.34615 \times 0.75 + 0.30769 \times 0.5 + 0.03846 \times 0.25 + 0 \times 0 \\ = 0.73077$$

$$P(h_1) = \frac{0.30769 \times 1}{0.73077} = 0.42105 \quad P(h_2) = \frac{0.34615 \times 0.75}{0.73077} = 0.35526$$

$$P(h_3) = \frac{0.30769 \times 0.5}{0.73077} = 0.21053 \quad P(h_4) = \frac{0.03846 \times 0.25}{0.73077} = 0.01316$$

$$P(h_5) = \frac{0 \times 0}{0.73077} = 0$$

$$C \quad P(c) = 0.42105 \times 1 + 0.35526 \times 0.75 + 0.21053 \times 0.5 + 0.01316 \times 0.25 + 0 \times 0 \\ = 0.79605$$

$$P(h_1) = \frac{0.42105 \times 1}{0.79605} = 0.52893 \quad P(h_2) = \frac{0.35526 \times 0.75}{0.79605} = 0.33471$$

$$P(h_3) = \frac{0.21053 \times 0.5}{0.79605} = 0.13223 \quad P(h_4) = \frac{0.01316 \times 0.25}{0.79605} = 0.00413$$

$$P(h_5) = \frac{0 \times 0}{0.79605} = 0$$

$$C \quad P(c) = 0.52893 \times 1 + 0.33471 \times 0.75 + 0.13223 \times 0.5 + 0.00413 \times 0.25 + 0 \times 0 \\ = 0.84711$$

$$P(h_1) = \frac{0.52893 \times 1}{0.84711} = 0.62439 \quad P(h_2) = \frac{0.33471 \times 0.75}{0.84711} = 0.29634$$

$$P(h_3) = \frac{0.13223 \times 0.5}{0.84711} = 0.07805 \quad P(h_4) = \frac{0.00413 \times 0.25}{0.84711} = 0.00122$$

$$P(h_5) = \frac{0 \times 0}{0.84711} = 0$$

$$L \quad P(L) = 0.62439 \times 0 + 0.29634 \times 0.25 + 0.07805 \times 0.5 + 0.00122 \times 0.75 + 0 \times 1 \\ = 0.11402$$

$$P(h_1) = \frac{0.62439 \times 0}{0.11402} = 0 \quad P(h_2) = \frac{0.29634 \times 0.25}{0.11402} = 0.64973$$

$$P(h_3) = \frac{0.07805 \times 0.5}{0.11402} = 0.34225 \quad P(h_4) = \frac{0.00122 \times 0.75}{0.11402} = 0.00802$$

$$P(h_5) = \frac{0 \times 1}{0.11402} = 0$$

b. CL CL CL

$$C \quad P(c) = 0.1 \times 1 + 0.2 \times 0.75 + 0.4 \times 0.5 + 0.2 \times 0.25 + 0.1 \times 0 \\ = 0.5$$

$$P(h_1) = \frac{0.1 \times 1}{0.5} = 0.2 \quad P(h_2) = \frac{0.2 \times 0.75}{0.5} = 0.3$$

$$P(h_3) = \frac{0.4 \times 0.5}{0.5} = 0.4 \quad P(h_4) = \frac{0.2 \times 0.25}{0.5} = 0.1$$

$$P(h_5) = \frac{0.1 \times 0}{0.5} = 0$$

$$L \quad P(L) = 0.2 \times 0 + 0.3 \times 0.25 + 0.4 \times 0.5 + 0.1 \times 0.75 + 0 \times 1 \\ = 0.35$$

$$P(h_1) = \frac{0.2 \times 0}{0.35} = 0 \quad P(h_2) = \frac{0.3 \times 0.25}{0.35} = 0.21429$$

$$P(h_3) = \frac{0.4 \times 0.5}{0.35} = 0.57143 \quad P(h_4) = \frac{0.1 \times 0.75}{0.35} = 0.21429$$

$$P(h_5) = \frac{0 \times 1}{0.35} = 0$$

$$C \quad P(c) = 0.1 + 0.21429 \times 0.75 + 0.57143 \times 0.5 + 0.21429 \times 0.25 + 0 \times 0 \\ = 0.58020$$

$$P(h_1) = \frac{0.1}{0.58020} = 0 \quad P(h_2) = \frac{0.21429 \times 0.75}{0.58020} = 0.32143$$

$$P(h_3) = \frac{0.57143 \times 0.5}{0.58020} = 0.57143 \quad P(h_4) = \frac{0.21429 \times 0.25}{0.58020} = 0.10714$$

$$P(h_5) = \frac{0 \times 0}{0.44643} = 0$$

L  $P(L) = 0 \times 0 + 0.32143 \times 0.25 + 0.57143 \times 0.5 + 0.10714 \times 0.75 + 0 \times 1$   
 $= 0.44643$

$$P(h_1) = \frac{0 \times 0}{0.44643} = 0$$

$$P(h_2) = \frac{0.32143 \times 0.25}{0.44643} = 0.18000$$

$$P(h_3) = \frac{0.57143 \times 0.5}{0.44643} = 0.64000 \quad P(h_4) = \frac{0.10714 \times 0.75}{0.44643} = 0.18000$$

$$P(h_5) = \frac{0 \times 1}{0.44643} = 0$$

C  $P(C) = 0 \times 1 + 0.18000 \times 0.75 + 0.64000 \times 0.5 + 0.18000 \times 0.25 + 0 \times 0$   
 $= 0.50000$

$$P(h_1) = \frac{0 \times 1}{0.50000} = 0$$

$$P(h_2) = \frac{0.18000 \times 0.75}{0.50000} = 0.27000$$

$$P(h_3) = \frac{0.64000 \times 0.5}{0.50000} = 0.64000$$

$$P(h_4) = \frac{0.18000 \times 0.25}{0.50000} = 0.09000$$

$$P(h_5) = \frac{0 \times 0}{0.50000} = 0$$

L  $P(L) = 0 \times 0 + 0.27000 \times 0.25 + 0.64000 \times 0.5 + 0.09000 \times 0.75 + 0 \times 1$   
 $= 0.45500$

$$P(h_1) = \frac{0 \times 0}{0.45500} = 0$$

$$P(h_2) = \frac{0.27000 \times 0.25}{0.45500} = 0.14835$$

$$P(h_3) = \frac{0.64000 \times 0.5}{0.45500} = 0.70330$$

$$P(h_4) = \frac{0.09000 \times 0.75}{0.45500} = 0.14835$$

$$P(h_5) = \frac{0 \times 1}{0.45500} = 0$$

C. C C C L L L

C  $P(C) = 0.1 \times 1 + 0.2 \times 0.75 + 0.4 \times 0.5 + 0.2 \times 0.25 + 0.1 \times 0$   
 $= 0.5$

$$P(h_1) = \frac{0.1 \times 1}{0.5} = 0.2 \quad P(h_2) = \frac{0.2 \times 0.75}{0.5} = 0.3$$

$$P(h_3) = \frac{0.4 \times 0.5}{0.5} = 0.4 \quad P(h_4) = \frac{0.2 \times 0.25}{0.5} = 0.1$$

$$P(h_5) = \frac{0.1 \times 0}{0.5} = 0$$

C  $P(C) = 0.2 \times 1 + 0.3 \times 0.75 + 0.4 \times 0.5 + 0.1 \times 0.25 + 0 \times 0$   
 $= 0.65$

$$P(h_1) = \frac{0.2 \times 1}{0.65} = 0.30769 \quad P(h_2) = \frac{0.3 \times 0.75}{0.65} = 0.34615$$

$$P(h_3) = \frac{0.4 \times 0.5}{0.65} = 0.30769 \quad P(h_4) = \frac{0.1 \times 0.25}{0.65} = 0.03846$$

$$P(h_5) = \frac{0 \times 0}{0.65} = 0$$

C  $P(C) = 0.30769 \times 1 + 0.34615 \times 0.75 + 0.30769 \times 0.5 + 0.03846 \times 0.25 + 0 \times 0$   
 $= 0.73077$

$$P(h_1) = \frac{0.30769 \times 1}{0.73077} = 0.42105 \quad P(h_2) = \frac{0.34615 \times 0.75}{0.73077} = 0.35526$$

$$P(h_3) = \frac{0.30769 \times 0.5}{0.73077} = 0.21053 \quad P(h_4) = \frac{0.03846 \times 0.25}{0.73077} = 0.01316$$

$$P(h_5) = \frac{0 \times 0}{0.73077} = 0$$

L  $P(L) = 0.42105 \times 0 + 0.35526 \times 0.25 + 0.21053 \times 0.5 + 0.01316 \times 0.75 + 0 \times 1$   
 $= 0.20395$

$$P(h_1) = \frac{0.45105 \times 0}{0.20395} = 0$$

$$P(h_2) = \frac{0.35526 \times 0.25}{0.20395} = 0.43548$$

$$P(h_3) = \frac{0.24053 \times 0.5}{0.20395} = 0.51613 \quad P(h_4) = \frac{0.01316 \times 0.75}{0.20395} = 0.04839$$

$$P(h_5) = \frac{0 \times 1}{0.20395} = 0$$

L  $P(L) = 0 \times 0 + 0.43548 \times 0.25 + 0.51613 \times 0.5 + 0.04839 \times 0.75 + 0 \times 1$   
 $= 0.40323$

$$P(h_1) = \frac{0 \times 0}{0.40323} = 0$$

$$P(h_2) = \frac{0.43548 \times 0.25}{0.40323} = 0.27000$$

$$P(h_3) = \frac{0.51613 \times 0.5}{0.40323} = 0.64000 \quad P(h_4) = \frac{0.04839 \times 0.75}{0.40323} = 0.09000$$

$$P(h_5) = \frac{0 \times 1}{0.40323} = 0$$

L  $P(L) = 0 \times 0 + 0.27000 \times 0.25 + 0.64000 \times 0.5 + 0.09000 \times 0.75 + 0 \times 1$   
 $= 0.45500$

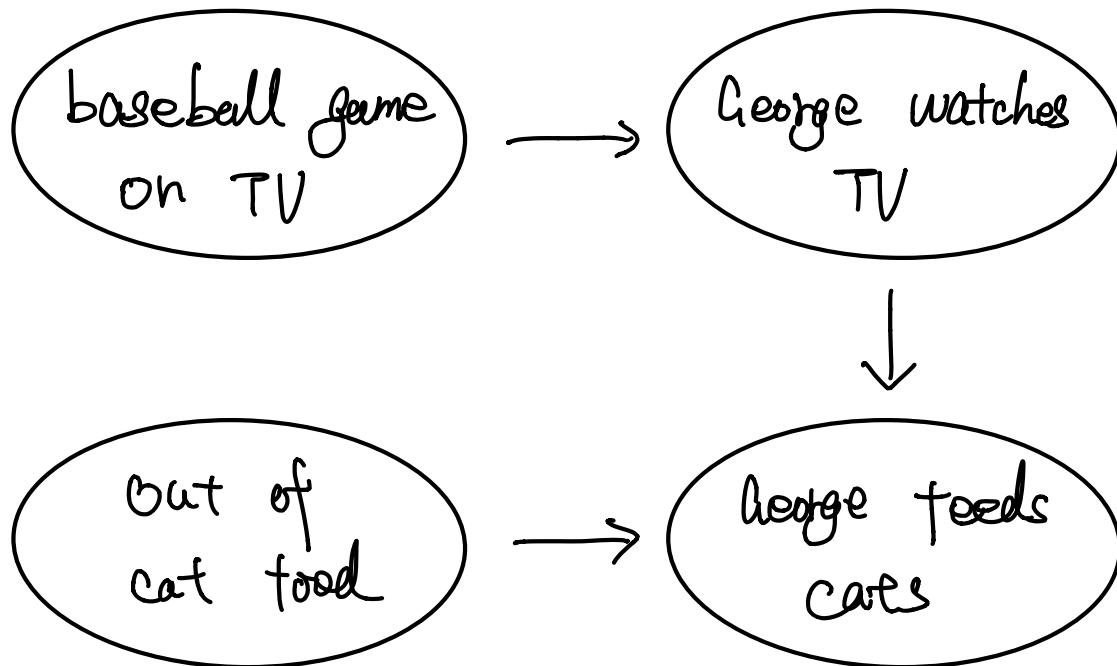
$$P(h_1) = \frac{0 \times 0}{0.45500} = 0$$

$$P(h_2) = \frac{0.27000 \times 0.25}{0.45500} = 0.14835$$

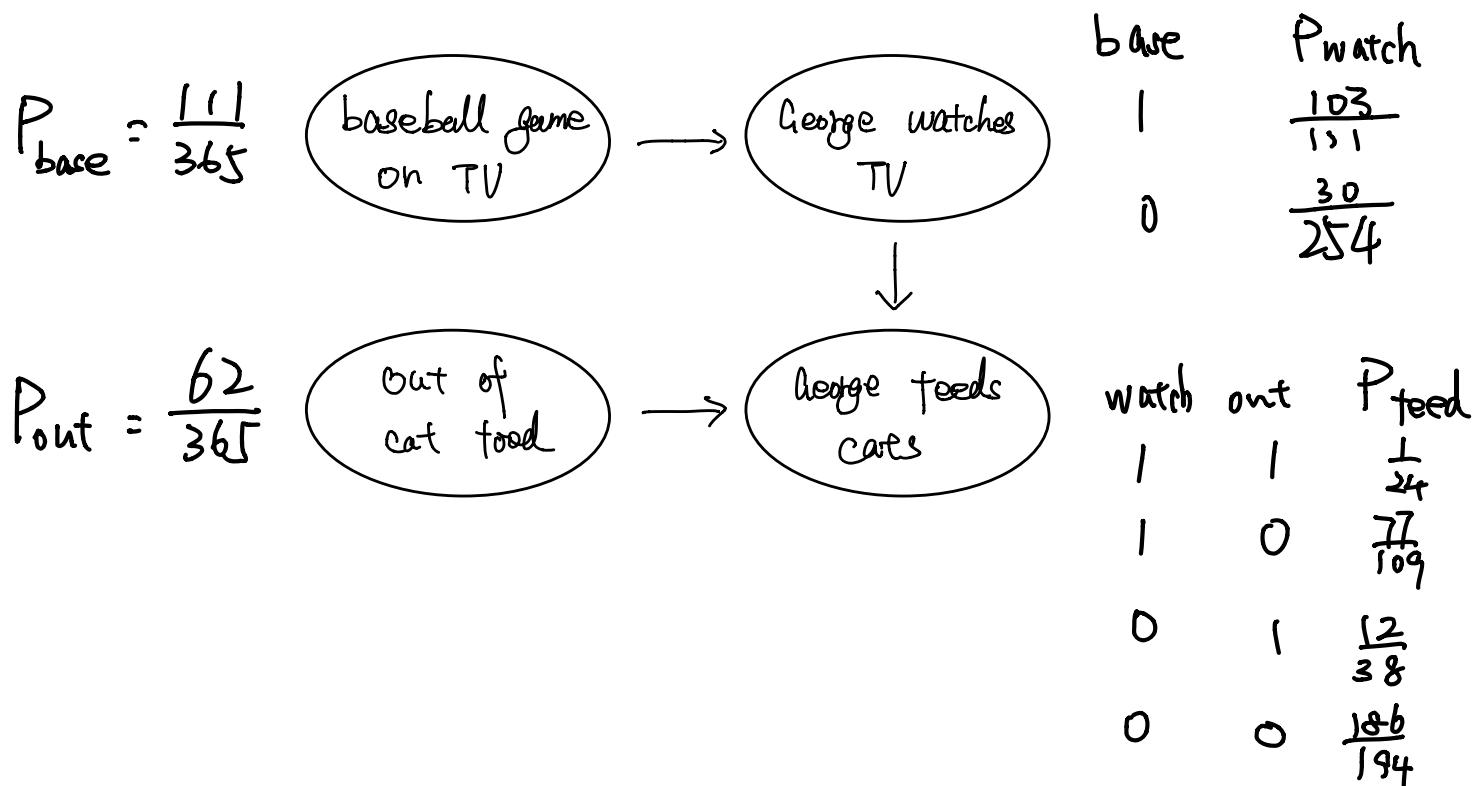
$$P(h_3) = \frac{0.64000 \times 0.5}{0.45500} = 0.70330 \quad P(h_4) = \frac{0.09000 \times 0.75}{0.45500} = 0.14835$$

$$P(h_5) = \frac{0 \times 1}{0.45500} = 0$$

## Task 3



## Task 4



## Task 5

$$P(\text{hot feed} \mid \text{baseball})$$

$$= \frac{P(\text{not feed, baseball})}{P(\text{baseball})}$$

for  $P(\text{not feed, baseball})$ :

$$\begin{aligned} &= P(\text{not feed} \mid \text{watch, out}) \cdot p(\text{watch} \mid \text{baseball}) p(\text{out}) p(\text{baseball}) + \\ &\quad P(\text{not feed} \mid \text{not watch, out}) p(\text{not watch} \mid \text{baseball}) p(\text{out}) p(\text{baseball}) + \\ &\quad P(\text{not feed} \mid \text{watch, not out}) p(\text{watch} \mid \text{baseball}) p(\text{not out}) p(\text{baseball}) + \\ &\quad P(\text{not feed} \mid \text{not watch, not out}) p(\text{not watch} \mid \text{baseball}) p(\text{not out}) p(\text{baseball}) + \\ &= 0.11801 \end{aligned}$$

$$P(\text{not feed} \mid \text{baseball})$$

$$= 0.38804$$

## Task 6

a. node C (parent)

node P, node Q (children)

node K node M (children's parents)

$$b. P(C, H) = P(H|C) \cdot P(C)$$

$$= 0.6 \times 0.6$$

$$= 0.36$$

It is derived from  $P(C)$  and  $P(H|C)$

$$c. P(O | \text{not}(J), \bar{G}) = \frac{P(O, \text{not}(J), \bar{G})}{P(\text{not}(J), \bar{G})}$$

$$= \frac{P(O|\text{not}(J)) \cdot P(\text{not}(W)|\bar{G}) \cdot P(\bar{G})}{P(\text{not}(J) | \bar{G}) - P(\bar{G})}$$

$$= 0.8$$

It is derived from  $P(O|\text{not}(J)) \cdot P(\text{not}(J)|\bar{G}) \cdot P(\bar{G})$