

See the Assessment Guide for information on how to interpret this report.

## ASSESSMENT SUMMARY

Compilation: PASSED (0 errors, 2 warnings)  
API: PASSED

Spotbugs: PASSED  
PMD: FAILED (1 warning)  
Checkstyle: PASSED

Correctness: 44/45 tests passed  
Memory: 134/134 tests passed  
Timing: 193/193 tests passed

Aggregate score: 98.67%

[Compilation: 5%, API: 5%, Spotbugs: 0%, PMD: 0%, Checkstyle: 0%, Correctness: 60%, Memory: 10%, Timing: 20%]

## ASSESSMENT DETAILS

The following files were submitted:

-----  
3.7K Jul 6 06:35 Deque.java  
924 Jul 6 06:35 Permutation.java  
3.2K Jul 6 06:35 RandomizedQueue.java

\*\*\*\*\*  
\* COMPILING  
\*\*\*\*\*

% javac Deque.java

% javac RandomizedQueue.java

-----  
RandomizedQueue.java:20: warning: [unchecked] unchecked cast  
s = (Item[]) new Object[1];  
                  ^  
required: Item[]  
found: Object[]  
where Item is a type-variable:  
Item extends Object declared in class RandomizedQueue  
RandomizedQueue.java:34: warning: [unchecked] unchecked cast  
Item[] copy = (Item[]) new Object[capacity];  
                  ^  
required: Item[]  
found: Object[]  
where Item is a type-variable:  
Item extends Object declared in class RandomizedQueue  
2 warnings

% javac Permutation.java

-----  
Checking the APIs of your programs.

\*  
Deque:

RandomizedQueue:

Permutation:

-----  
\*\*\*\*\*  
\* CHECKING STYLE AND COMMON BUG PATTERNS  
\*\*\*\*\*

% spotbugs \*.class

-----  
% pmd .

-----  
RandomizedQueue.java:79: The private instance (or static) variable 'random' can be made 'final'; it is initialized only in the declaration or construction.  
PMD ends with 1 warning.

-----  
% checkstyle \*.java

% custom checkstyle checks for Deque.java

% custom checkstyle checks for RandomizedQueue.java

% custom checkstyle checks for Permutation.java

-----  
\*\*\*\*\*  
\* TESTING CORRECTNESS  
\*\*\*\*\*

Testing correctness of Deque

\*-----  
Running 17 total tests.

Tests 1-6 make random calls to addFirst(), addLast(), removeFirst(), removeLast(), isEmpty(), and size(). The probabilities of each operation are (p1, p2, p3, p4, p5, p6), respectively.

Test 1: check random calls to addFirst(), addLast(), and size()

\* 5 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2)  
\* 50 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2)  
\* 500 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2)  
\* 1000 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2)  
==> passed

Test 2: check random calls to addFirst(), removeFirst(), and isEmpty()

\* 5 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0)  
\* 50 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0)  
\* 500 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0)  
\* 1000 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0)  
\* 5 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0)  
\* 50 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0)  
\* 500 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0)  
\* 1000 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0)  
==> passed

Test 3: check random calls to addFirst(), removeLast(), and isEmpty()

\* 5 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0)  
\* 50 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0)  
\* 500 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0)  
\* 1000 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0)  
\* 5 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0)  
\* 50 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0)  
\* 500 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0)  
\* 1000 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0)  
==> passed

Test 4: check random calls to addLast(), removeLast(), and isEmpty()

\* 5 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0)  
\* 50 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0)  
\* 500 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0)  
\* 1000 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0)  
\* 5 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0)  
\* 50 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0)  
\* 500 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0)  
\* 1000 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0)  
==> passed

Test 5: check random calls to addLast(), removeFirst(), and isEmpty()

\* 5 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0)  
\* 50 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0)  
\* 500 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0)  
\* 1000 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0)  
\* 5 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0)  
\* 50 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0)  
\* 500 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0)  
\* 1000 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0)  
==> passed

Test 6: check random calls to addFirst(), addLast(), removeFirst(), removeLast(), isEmpty(), and size()

\* 5 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.1)  
\* 50 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.1)  
\* 500 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.1)  
\* 1000 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.1)  
\* 5 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1)  
\* 50 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1)  
\* 500 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1)  
\* 1000 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1)  
==> passed

Test 7: check removeFirst() and removeLast() from an empty deque

\* removeFirst()  
\* removeLast()  
==> passed

Test 8: check whether two Deque objects can be created at the same time

\* n = 10  
\* n = 1000  
==> passed

Test 9: check iterator() after n calls to addFirst()

\* n = 10  
\* n = 50  
==> passed

Test 10: check iterator() after each of m intermixed calls to addFirst(), addLast(), removeFirst(), and removeLast()

\* m = 20  
\* m = 50  
\* m = 100  
\* m = 1000  
==> passed

Test 11: create two nested iterators to same deque

\* n = 10  
\* n = 50  
==> passed

Test 12: create two parallel iterators to same deque

==> passed

Test 13: create an iterator and check calls to next() and hasNext()

\* 10 consecutive calls to hasNext() on a deque of size 10  
\* 10 consecutive calls to next() on a deque of size 10  
\* 50 random intermixed calls to next() and hasNext() on a deque of size 10  
\* 1000 random intermixed calls to next() and hasNext() on a deque of size 100  
==> passed

Test 14: create Deque objects of different parameterized types

==> passed

Test 15: call addFirst() and addLast() with null argument  
 ==> passed

Test 16: check that remove() and next() throw the specified exceptions in iterator()  
 ==> passed

Test 17: call iterator() when the deque is empty  
 ==> passed

Total: 17/17 tests passed!

=====

Testing correctness of RandomizedQueue

-----

Running 19 total tests.

Tests 1-4 make random calls to enqueue(), dequeue(), sample(), isEmpty(), and size(). The probabilities of each operation are (p1, p2, p3, p4, p5), respectively.

Test 1: check random calls to enqueue() and size()  
 \* 5 random calls (0.8, 0.0, 0.0, 0.0, 0.2)  
 \* 50 random calls (0.8, 0.0, 0.0, 0.0, 0.2)  
 \* 500 random calls (0.8, 0.0, 0.0, 0.0, 0.2)  
 \* 1000 random calls (0.8, 0.0, 0.0, 0.0, 0.2)  
 ==> passed

Test 2: check random calls to enqueue() and dequeue()  
 \* 5 random calls (0.7, 0.1, 0.0, 0.1, 0.1)  
 \* 50 random calls (0.7, 0.1, 0.0, 0.1, 0.1)  
 \* 500 random calls (0.7, 0.1, 0.0, 0.1, 0.1)  
 \* 1000 random calls (0.7, 0.1, 0.0, 0.1, 0.1)  
 \* 5 random calls (0.1, 0.7, 0.0, 0.1, 0.1)  
 \* 50 random calls (0.1, 0.7, 0.0, 0.1, 0.1)  
 \* 500 random calls (0.1, 0.7, 0.0, 0.1, 0.1)  
 \* 1000 random calls (0.1, 0.7, 0.0, 0.1, 0.1)  
 ==> passed

Test 3: check random calls to enqueue(), sample(), and size()  
 \* 5 random calls (0.8, 0.0, 0.1, 0.0, 0.1)  
 \* 50 random calls (0.8, 0.0, 0.1, 0.0, 0.1)  
 \* 500 random calls (0.8, 0.0, 0.1, 0.0, 0.1)  
 \* 1000 random calls (0.8, 0.0, 0.1, 0.0, 0.1)  
 \* 5 random calls (0.1, 0.0, 0.8, 0.0, 0.1)  
 \* 50 random calls (0.1, 0.0, 0.8, 0.0, 0.1)  
 \* 500 random calls (0.1, 0.0, 0.8, 0.0, 0.1)  
 \* 1000 random calls (0.1, 0.0, 0.8, 0.0, 0.1)  
 ==> passed

Test 4: check random calls to enqueue(), dequeue(), sample(), isEmpty(), and size()  
 \* 5 random calls (0.6, 0.1, 0.1, 0.1, 0.1)  
 \* 50 random calls (0.6, 0.1, 0.1, 0.1, 0.1)  
 \* 500 random calls (0.6, 0.1, 0.1, 0.1, 0.1)  
 \* 1000 random calls (0.6, 0.1, 0.1, 0.1, 0.1)  
 \* 5 random calls (0.1, 0.6, 0.1, 0.1, 0.1)  
 \* 50 random calls (0.1, 0.6, 0.1, 0.1, 0.1)  
 \* 500 random calls (0.1, 0.6, 0.1, 0.1, 0.1)  
 \* 1000 random calls (0.1, 0.6, 0.1, 0.1, 0.1)  
 ==> passed

Test 5: call dequeue() and sample() from an empty randomized queue  
 \* dequeue()  
 \* sample()  
 ==> passed

Test 6: create multiple randomized queue objects at the same time  
 \* n = 10  
 \* n = 100  
 ==> passed

Test 7: check that iterator() returns correct items after a sequence of n enqueue() operations  
 \* n = 10  
 \* n = 50  
 ==> passed

Test 8: check that iterator() returns correct items after sequence of m enqueue() and dequeue() operations  
 \* m = 10  
 \* m = 1000  
 ==> passed

Test 9: create two nested iterators over the same randomized queue  
 \* n = 10  
 \* n = 50  
 ==> passed

Test 10: create two parallel iterators over the same randomized queue  
 \* n = 10  
 \* n = 50  
 ==> passed

Test 11: create two iterators over different randomized queues  
 ==> passed

Test 12: create an iterator and check calls to next() and hasNext()  
 \* 10 consecutive calls to hasNext() on a deque of size 10  
 \* 10 consecutive calls to next() on a deque of size 10  
 \* 50 random intermixed calls to next() and hasNext() on a deque of size 10  
 \* 1000 random intermixed calls to next() and hasNext() on a deque of size 100  
 ==> passed

Test 13: create RandomizedQueue objects of different parameterized types  
 ==> passed

Test 14: check randomness of sample() by enqueueing n items, repeatedly calling sample(), and counting the frequency of each item  
 \* n = 3, trials = 12000  
 \* n = 5, trials = 12000

```

* n = 8, trials = 12000
* n = 10, trials = 12000
==> passed

Test 15: check randomness of dequeue() by enqueueing n items, dequeueing n items,
and seeing whether each of the n! permutations is equally likely
* n = 2, trials = 12000
* n = 3, trials = 12000
* n = 4, trials = 12000
* n = 5, trials = 12000
==> passed

Test 16: check randomness of iterator() by enqueueing n items, iterating over those
n items, and seeing whether each of the n! permutations is equally likely
* n = 2, trials = 12000
* n = 3, trials = 12000
* n = 4, trials = 12000
* n = 5, trials = 12000
==> passed

Test 17: call enqueue() with a null argument
==> passed

Test 18: check that remove() and next() throw the specified exceptions in iterator()
- throws wrong exception when calling next() when iterator is exhausted
- throws a java.lang.ArrayIndexOutOfBoundsException
- should throw a java.util.NoSuchElementException

==> FAILED

Test 19: call iterator() when randomized queue is empty
==> passed

Total: 18/19 tests passed!

```

```

=====
*****
* TESTING CORRECTNESS (substituting reference RandomizedQueue and Deque)
*****

```

```

Testing correctness of Permutation
*-----
Tests 1-5 call the main() function directly, resetting standard input
before each call.

```

Running 9 total tests.

```

Test 1a: check formatting for sample inputs from assignment specification
% java Permutation 3 < distinct.txt
G
H
D

```

```

% java Permutation 3 < distinct.txt
H
I
C

```

```

% java Permutation 8 < duplicates.txt
AA
BB
CC
BB
CC
BB
BB
BB

```

==> passed

```

Test 1b: check formatting for other inputs
% java Permutation 8 < mediumTale.txt
it
times
of
it
it
foolishness
of
age

% java Permutation 0 < distinct.txt
[no output]

```

==> passed

```

Test 2: check that main() reads all data from standard input
* filename = distinct.txt, k = 3
* filename = distinct.txt, k = 3
* filename = duplicates.txt, k = 8
* filename = mediumTale.txt, k = 8
==> passed

```

```

Test 3a: check that main() prints each item from the sequence at most once
(for inputs with no duplicate strings)
* filename = distinct.txt, k = 3
* filename = distinct.txt, k = 1
* filename = distinct.txt, k = 9
* filename = permutation6.txt, k = 6
* filename = permutation10.txt, k = 10
==> passed

```

```

Test 3b: check that main() prints each item from the sequence at most once
(for inputs with duplicate strings)
* filename = duplicates.txt, k = 8
* filename = duplicates.txt, k = 3
* filename = permutation8.txt, k = 6
* filename = permutation8.txt, k = 2
* filename = tinyTale.txt, k = 10
==> passed

```

```

Test 3c: check that main() prints each item from the sequence at most once
        (for inputs with newlines)
* filename = mediumTale.txt, k = 10
* filename = mediumTale.txt, k = 20
* filename = tale.txt, k = 10
* filename = tale.txt, k = 50
==> passed

```

```

Test 4: check main() when k = 0
* filename = distinct.txt, k = 0
* filename = distinct.txt, k = 0
==> passed

```

```

Test 5a: check that permutations are uniformly random
        (for inputs with no duplicate strings)
* filename = permutation4.txt, k = 1
* filename = permutation4.txt, k = 2
* filename = permutation4.txt, k = 3
* filename = permutation4.txt, k = 4
* filename = permutation6.txt, k = 2
==> passed

```

```

Test 5b: check that permutations are uniformly random
        (for inputs with duplicate strings)
* filename = permutation5.txt, k = 1
* filename = permutation5.txt, k = 2
* filename = permutation5.txt, k = 3
* filename = duplicates.txt, k = 3
* filename = permutation8.txt, k = 2
==> passed

```

Total: 9/9 tests passed!

```

=====
*****
* TIMING (substituting reference RandomizedQueue and Deque)
*****

```

Timing Permutation

```

*-----
Running 23 total tests.

```

```

Test 1: count calls to methods in StdIn
* java Permutation 5 < distinct.txt
* java Permutation 10 < permutation10.txt
* java Permutation 1 < mediumTale.txt
* java Permutation 20 < tale.txt
* java Permutation 100 < tale.txt
* java Permutation 16412 < tale.txt
==> passed

```

```

Test 2: count calls to methods in Deque and RandomizedQueue
* java Permutation 5 < distinct.txt
* java Permutation 10 < permutation10.txt
* java Permutation 1 < mediumTale.txt
* java Permutation 20 < tale.txt
* java Permutation 100 < tale.txt
* java Permutation 16412 < tale.txt
==> passed

```

```

Test 3: count calls to methods in StdRandom
* java Permutation 5 < distinct.txt
* java Permutation 10 < permutation10.txt
* java Permutation 1 < mediumTale.txt
* java Permutation 20 < tale.txt
* java Permutation 100 < tale.txt
* java Permutation 16412 < tale.txt
==> passed

```

Test 4: Time main() with k = 5, for inputs containing n random strings

```

        n  seconds
-----
=> passed      1000    0.00
=> passed      2000    0.00
=> passed      4000    0.00
=> passed      8000    0.00
=> passed     16000    0.01
=> passed     32000    0.01
=> passed     64000    0.03
=> passed    128000    0.05
=> passed    256000    0.08
=> passed    512000    0.17
==> 10/10 tests passed

```

Test 5: Time main() with k = 1000, for inputs containing n random strings

```

        n  seconds
-----
=> passed      1000    0.00
=> passed      2000    0.00
=> passed      4000    0.00
=> passed      8000    0.00
=> passed     16000    0.01
=> passed     32000    0.01
=> passed     64000    0.02
=> passed    128000    0.04
=> passed    256000    0.09
=> passed    512000    0.20
==> 10/10 tests passed

```

Total: 23/23 tests passed!

```

=====

```

```
*****
* MEMORY
*****
```

Analyzing memory of Permutation

```
*****
```

Running 2 total tests.

Test 1: check that only one Deque or RandomizedQueue object is created

```
* filename = distinct.txt, n = 9, k = 1
* filename = distinct.txt, n = 9, k = 2
* filename = distinct.txt, n = 9, k = 4
* filename = tinyTale.txt, n = 12, k = 10
* filename = tale.txt, n = 138653, k = 50
==> passed
```

Test 2: check that the maximum size of any Deque or RandomizedQueue object created is between k and n

```
* filename = distinct.txt, n = 9, k = 1
* filename = distinct.txt, n = 9, k = 2
* filename = distinct.txt, n = 9, k = 4
* filename = tinyTale.txt, n = 12, k = 10
* filename = tale.txt, n = 138653, k = 5
* filename = tale.txt, n = 138653, k = 50
* filename = tale.txt, n = 138653, k = 500
* filename = tale.txt, n = 138653, k = 5000
* filename = tale.txt, n = 138653, k = 50000
==> passed
```

Test 3 (bonus): check that maximum size of any or Deque or RandomizedQueue object created is equal to k

```
* filename = tale.txt, n = 138653, k = 5
- max size of RandomizedQueue object = 138653

* filename = tale.txt, n = 138653, k = 50
- max size of RandomizedQueue object = 138653

* filename = tale.txt, n = 138653, k = 500
- max size of RandomizedQueue object = 138653

* filename = tale.txt, n = 138653, k = 5000
- max size of RandomizedQueue object = 138653

* filename = tale.txt, n = 138653, k = 50000
- max size of RandomizedQueue object = 138653
```

==> FAILED

Total: 2/2 tests passed!

```
=====
```

```
*****
* MEMORY
*****
```

Analyzing memory of Deque

```
*****
```

For tests 1-4, the maximum amount of memory allowed for a Deque containing n items is  $48n + 192$ .

Running 48 total tests.

Test 1a-1i: total memory usage after inserting n items,  
where n is a power of 2

	n	bytes
=> passed	32	1576
=> passed	64	3112
=> passed	128	6184
=> passed	256	12328
=> passed	512	24616
=> passed	1024	49192
=> passed	2048	98344
=> passed	4096	196648
=> passed	8192	393256

==> 9/9 tests passed

Memory:  $48.00 n + 40.00$  ( $R^2 = 1.000$ )

Test 2a-2i: Total memory usage after inserting n items,  
when n is one more than a power of 2.

	n	bytes
=> passed	33	1624
=> passed	65	3160
=> passed	129	6232
=> passed	257	12376
=> passed	513	24664
=> passed	1025	49240
=> passed	2049	98392
=> passed	4097	196696
=> passed	8193	393304

==> 9/9 tests passed

Memory:  $48.00 n + 40.00$  ( $R^2 = 1.000$ )

Test 3a-3i: Total memory usage after inserting  $2n-1$  items, and then deleting  $n-1$  items, when n is one more than a power of 2.

	n	bytes
=> passed	33	1624
=> passed	65	3160
=> passed	129	6232

```
=> passed      257      12376
=> passed      513      24664
=> passed     1025      49240
=> passed     2049      98392
=> passed     4097     196696
=> passed     8193     393304
==> 9/9 tests passed
```

Memory: 48.00 n + 40.00 (R^2 = 1.000)

Test 4a-4e: Total memory usage after inserting n items,  
and then deleting all but one item  
(should not grow with n or be too large of a constant).

	n	bytes
=> passed	32	88
=> passed	64	88
=> passed	128	88
=> passed	256	88
=> passed	512	88
=> passed	1024	88
=> passed	2048	88
=> passed	4096	88
=> passed	8192	88

==> 9/9 tests passed

Memory: 88.00 (R^2 = 1.000)

Test 5a-5e: Total memory usage of iterator after inserting n items  
(should not grow with n or be too large of a constant).

	n	bytes
=> passed	32	32
=> passed	64	32
=> passed	128	32
=> passed	256	32
=> passed	512	32
=> passed	1024	32
=> passed	2048	32
=> passed	4096	32
=> passed	8192	32

==> 9/9 tests passed

Memory: 32.00 (R^2 = 1.000)

Test 6a: Insert n strings; delete them one at a time, checking for  
loitering after each deletion. The probabilities of addFirst()  
and addLast() are (p1, p2), respectively. The probabilities of  
removeFirst() and removeLast() are (q1, q2), respectively.

- \* 100 random insertions (1.0, 0.0) and 100 random deletions (1.0, 0.0)
- \* 100 random insertions (1.0, 0.0) and 100 random deletions (0.0, 1.0)
- \* 100 random insertions (0.0, 1.0) and 100 random deletions (1.0, 0.0)
- \* 100 random insertions (0.0, 1.0) and 100 random deletions (0.0, 1.0)
- \* 100 random insertions (0.5, 0.5) and 100 random deletions (0.5, 0.5)

==> passed

Test 6b: Perform random operations, checking for loitering after  
each operation. The probabilities of addFirst(), addLast(),  
removeFirst(), and removeLast() are (p1, p2, p3, p4),  
respectively.

- \* 100 random operations (0.8, 0.0, 0.2, 0.0)
- \* 100 random operations (0.8, 0.0, 0.0, 0.2)
- \* 100 random operations (0.0, 0.8, 0.2, 0.0)
- \* 100 random operations (0.0, 0.8, 0.0, 0.2)
- \* 100 random operations (0.4, 0.4, 0.1, 0.1)
- \* 100 random operations (0.2, 0.2, 0.3, 0.3)

==> passed

Test 7: worst-case constant memory allocated or de-allocated  
per deque operation?

- \* 128 random operations
- \* 256 random operations
- \* 512 random operations

==> passed

Min observed memory for Deque: 48.00 n + 40.00 (R^2 = 1.000)  
Max observed memory for Deque: 48.00 n + 40.00 (R^2 = 1.000)

Total: 48/48 tests passed!

=====

Analyzing memory of RandomizedQueue

\*-----  
For Tests 1-5, the maximum amount of memory allowed for  
a RandomizedQueue containing n items is 48n + 192.

For Test 6, the maximum amount of memory allowed for  
a RandomizedQueue iterator over n items is 8n + 72.

Test 1a-1i: Total memory usage after inserting n items  
when n is a power of 2.

	n	bytes
=> passed	32	312
=> passed	64	568
=> passed	128	1080
=> passed	256	2104
=> passed	512	4152
=> passed	1024	8248
=> passed	2048	16440
=> passed	4096	32824

```
=> passed      8192      65592
==> 9/9 tests passed
```

Memory: 8.00 n + 56.00 (R^2 = 1.000)

Test 2a-2i: Total memory usage after inserting n items,  
when n is one more than a power of 2.

	n	bytes
=> passed	33	568
=> passed	65	1080
=> passed	129	2104
=> passed	257	4152
=> passed	513	8248
=> passed	1025	16440
=> passed	2049	32824
=> passed	4097	65592
=> passed	8193	131128

```
==> 9/9 tests passed
```

Memory: 16.00 n + 40.00 (R^2 = 1.000)

Test 3a-3i: Total memory usage after inserting 2n-1 items, and then  
deleting n-1 items, when n is one more than a power of 2.

	n	bytes
=> passed	33	1080
=> passed	65	2104
=> passed	129	4152
=> passed	257	8248
=> passed	513	16440
=> passed	1025	32824
=> passed	2049	65592
=> passed	4097	131128
=> passed	8193	262200

```
==> 9/9 tests passed
```

Memory: 32.00 n + 24.00 (R^2 = 1.000)

Test 4a-4i: Total memory usage after inserting n items, deleting n items,  
then inserting n times, when n is a power of 2.

	n	bytes
=> passed	32	312
=> passed	64	568
=> passed	128	1080
=> passed	256	2104
=> passed	512	4152
=> passed	1024	8248
=> passed	2048	16440
=> passed	4096	32824
=> passed	8192	65592

```
==> 9/9 tests passed
```

Memory: 8.00 n + 56.00 (R^2 = 1.000)

Test 5a-5i: Total memory usage after inserting n items,  
and then deleting all but one item.

	n	bytes
=> passed	32	72
=> passed	64	72
=> passed	128	72
=> passed	256	72
=> passed	512	72
=> passed	1024	72
=> passed	2048	72
=> passed	4096	72
=> passed	8192	72

```
==> 9/9 tests passed
```

Memory: 72.00 (R^2 = 1.000)

Test 6a-6i: Total memory usage of iterator after inserting n items.

	n	bytes
=> passed	32	192
=> passed	64	320
=> passed	128	576
=> passed	256	1088
=> passed	512	2112
=> passed	1024	4160
=> passed	2048	8256
=> passed	4096	16448
=> passed	8192	32832

```
==> 9/9 tests passed
```

Memory: 4.00 n + 64.00 (R^2 = 1.000)

Test 7a: Insert 100 strings; delete them one at a time, checking  
for loitering after each deletion.

```
==> passed
```

Test 7b: Perform random operations, checking for loitering after  
each operation. The probabilities of enqueue(), dequeue(),  
and sample() are (p1, p2, p3), respectively.

```
* 200 random operations (0.8, 0.2, 0.0)
* 200 random operations (0.2, 0.8, 0.0)
* 200 random operations (0.6, 0.2, 0.2)
* 200 random operations (0.2, 0.4, 0.4)
==> passed
```



Test 8: Insert T items into queue; then iterate over queue and check that worst-case constant memory is allocated or deallocated per iterator operation.

```
* T = 64
* T = 128
* T = 256
==> passed
```

Test 9: Total memory usage after inserting n items, seeking to identify values of n where memory usage is minimized as a function of n.

	n	bytes
=> passed	8	120
=> passed	16	184
=> passed	32	312
=> passed	64	568
=> passed	128	1080
=> passed	256	2104
=> passed	512	4152
=> passed	1024	8248
=> passed	2048	16440
=> passed	8	120
=> passed	16	184
=> passed	32	312
=> passed	64	568
=> passed	128	1080
=> passed	256	2104
=> passed	512	4152
=> passed	1024	8248
=> passed	2048	16440

==> 18/18 tests passed

Memory: 8.00 n + 56.00 (R^2 = 1.000)

Test 10: Total memory usage after inserting 4096 items, then successively deleting items, seeking values of n where memory usage is maximized as a function of n

	n	bytes
=> passed	2049	65592
=> passed	1025	32824
=> passed	513	16440
=> passed	257	8248
=> passed	129	4152
=> passed	65	2104
=> passed	33	1080
=> passed	17	568
=> passed	9	312

==> 9/9 tests passed

Memory: 32.00 n + 24.00 (R^2 = 1.000)

Min observed memory for RandomizedQueue: 8.00 n + 56.00 (R^2 = 1.000)

Max observed memory for RandomizedQueue: 32.00 n + 24.00 (R^2 = 1.000)

Running 84 total tests.

Total: 84/84 tests passed!

=====

\*\*\*\*\*  
\* TIMING  
\*\*\*\*\*

Timing Deque

\*-----  
Running 103 total tests.

Test 1a-1k: make n calls to addFirst() followed by n calls to removeFirst()

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.00
=> passed	256000	0.00
=> passed	512000	0.01
=> passed	1024000	0.02

==> 11/11 tests passed

Test 2a-2k: make n calls to addLast() followed by n calls to removeLast()

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.00
=> passed	256000	0.00
=> passed	512000	0.01
=> passed	1024000	0.03

==> 11/11 tests passed

Test 3a-3k: make n calls to addFirst() followed by n calls to removeLast()

```

n seconds
-----
=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.00
=> passed    128000      0.00
=> passed    256000      0.01
=> passed    512000      0.01
=> passed   1024000      0.03
==> 11/11 tests passed

```

Test 4a-4k: make n calls to addLast() followed by n calls to removeFirst()

```

n seconds
-----

```

```

=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.00
=> passed    128000      0.00
=> passed    256000      0.01
=> passed    512000      0.01
=> passed   1024000      0.02
==> 11/11 tests passed

```

Test 5a-5g: make n random calls to addFirst(), removeFirst(), isEmpty(), and size() with probabilities (0.7, 0.1, 0.1, 0.1)

```

n seconds
-----
=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.00
=> passed    128000      0.01
=> passed    256000      0.01
=> passed    512000      0.02
=> passed   1024000      0.03
=> passed   2048000      0.06
==> 12/12 tests passed

```

Test 6a-6g: make n random calls to addLast(), removeLast(), isEmpty(), and size(), with probabilities (0.7, 0.1, 0.1, 0.1)

```

n seconds
-----
=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.00
=> passed    128000      0.01
=> passed    256000      0.01
=> passed    512000      0.02
=> passed   1024000      0.04
=> passed   2048000      0.07
==> 12/12 tests passed

```

Test 7a-7g: make n random calls to addFirst(), addLast(), removeFirst(), removeLast(), isEmpty(), and size() with probabilities (0.3, 0.3, 0.1, 0.1, 0.1, 0.1)

```

n seconds
-----
=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.00
=> passed    128000      0.01
=> passed    256000      0.01
=> passed    512000      0.04
=> passed   1024000      0.04
=> passed   2048000      0.07
==> 12/12 tests passed

```

Test 8a-8g: make n calls to addFirst(); iterate over the n items by calling next() and hasNext()

```

n seconds
-----
=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.00
=> passed    128000      0.01
=> passed    256000      0.01
=> passed    512000      0.01
=> passed   1024000      0.02
=> passed   2048000      0.23
==> 12/12 tests passed

```

Test 9a-9k: make n calls to addFirst()/addLast(); interleave n calls each to removeFirst(), removeLast(), addFirst(), and addLast()

	n	seconds
=> passed	1025	0.00
=> passed	2049	0.00
=> passed	4097	0.00
=> passed	8193	0.00
=> passed	16385	0.00
=> passed	32769	0.00
=> passed	65537	0.01
=> passed	128001	0.01
=> passed	256001	0.02
=> passed	512001	0.05
=> passed	1024001	0.15

==> 11/11 tests passed

Total: 103/103 tests passed!

Timing RandomizedQueue

Running 67 total tests.

Test 1: make n calls to enqueue() followed by n calls to dequeue();  
count calls to StdRandom

\* n = 10  
\* n = 100  
\* n = 1000  
==> passed

Test 2: make n calls to enqueue() followed by n calls to sample();  
count calls to StdRandom

\* n = 10  
\* n = 100  
\* n = 1000  
==> passed

Test 3: make n calls to enqueue() and iterate over the n items;  
count calls to StdRandom

\* n = 10  
\* n = 100  
\* n = 1000  
==> passed

Test 4a-k: make n calls to enqueue() followed by n calls to dequeue()

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.01
=> passed	256000	0.01
=> passed	512000	0.02
=> passed	1024000	0.07

==> 11/11 tests passed

Test 5a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.2, 0.2, 0.2, 0.2, 0.2)

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.01
=> passed	128000	0.01
=> passed	256000	0.02
=> passed	512000	0.04
=> passed	1024000	0.11

==> 11/11 tests passed

Test 6a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.6, 0.1, 0.1, 0.1, 0.1)

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.01
=> passed	256000	0.02
=> passed	512000	0.05
=> passed	1024000	0.10

==> 11/11 tests passed

Test 7a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.1, 0.1, 0.6, 0.1, 0.1)

```

      n  seconds
-----
=> passed      1024    0.00
=> passed      2048    0.00
=> passed      4096    0.00
=> passed      8192    0.00
=> passed     16384    0.00
=> passed     32768    0.00
=> passed     65536    0.01
=> passed    128000    0.01
=> passed    256000    0.03
=> passed    512000    0.06
=> passed   1024000    0.13
==> 11/11 tests passed

```

Test 8a-k: make n calls to enqueue() followed by n calls each to next() and hasNext().

```

      n  seconds
-----
=> passed      1024    0.00
=> passed      2048    0.00
=> passed      4096    0.00
=> passed      8192    0.00
=> passed     16384    0.00
=> passed     32768    0.00
=> passed     65536    0.00
=> passed    128000    0.01
=> passed    256000    0.01
=> passed    512000    0.03
=> passed   1024000    0.06
==> 11/11 tests passed

```

Test 9a-i: make 100 calls to enqueue; 99 calls to dequeue; n calls to enqueue(); then call dequeue() three times, followed by enqueue() three times, and repeat n times.

```

      n  seconds
-----
=> passed      1024    0.00
=> passed      2048    0.00
=> passed      4096    0.00
=> passed      8192    0.00
=> passed     16384    0.00
=> passed     32768    0.00
=> passed     65536    0.01
=> passed    128000    0.02
=> passed    256000    0.06
==> 9/9 tests passed

```

Total: 67/67 tests passed!

=====