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1. Proof by contradiction

We return result as a maximum value

\therefore result is either

① not an element of inputs

② has an element $\text{input}[i]$ such that
 $\text{max} < \text{input}[i]$

\rightarrow we see that result is assigned to the elements of input
 so ① is contradicted

After n -iteration of the for-loop, $\text{result} \geq \text{input}[n]$, result only increases
 which contradicts ②

\therefore result is always the maximum value

2. Github: <https://github.com/linchen1010/>

Stackoverflow: <https://stackoverflow.com/users/12746413/linchen1010>

3.

```
double Solution::FindMedian(std::vector<double> &inputs) {
    if (inputs.size() == 0) {
        return -1;
    }
    else if (inputs.size() % 2 != 0) { // odd numbers
        return inputs[inputs.size()/2];
    }
    else if (inputs.size() % 2 == 0) { // even numbers
        double result = INT32_MIN;
        result = ( inputs[inputs.size()/2 - 1] + inputs[inputs.size()/2] ) / 2 ;
        return result ;
    }
}
```

Runtime:

There is no loop in the function, therefore, $T(n) = O(1)$

Result:

```
INFO: Elapsed time: 9.935s, Critical Path: 0.04s
INFO: 0 processes.
INFO: Build completed successfully, 1 total action
INFO: Build completed successfully, 1 total action
inputs: {1, 2, 3, 4, 5}, output: 3
inputs: {1, 2, 3, 4, 5, 6}, output: 3.5
inputs: {}, output: -1
linchen@Bende-MBP find_median %
```

```
TEST (FindMedianTest, HandleOddNumber) {
    Solution solution;
    std::vector<double> inputs = {1,2,3,4,5};
    EXPECT_EQ(solution.FindMedian(inputs), 3);
}

TEST (FindMedianTest, HandleEvenNumber) {
    Solution solution;
    std::vector<double> inputs = {1,2,3,4,5,6};
    EXPECT_EQ(solution.FindMedian(inputs), 3.5);
}

TEST (FindMedianTest, HandlesEmptyVector) {
    Solution solution;
    std::vector<double> inputs = {};
    EXPECT_EQ(solution.FindMedian(inputs), -1);
}
```

Test-case include empty set, odd-number set and even-number set!

4.

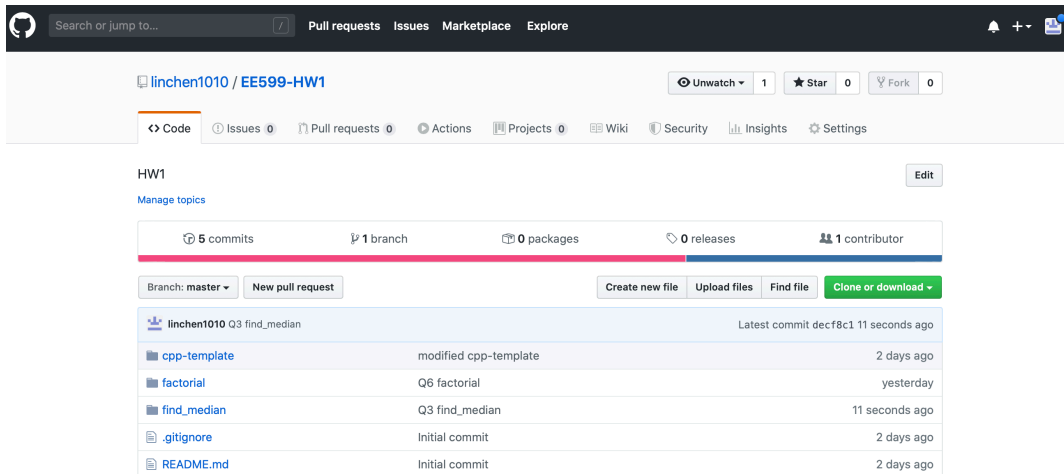
-f >> --force

Override the up-to-date check

-r

Allow recursive removal when a leading directory name is given

```
Target //src/main:main up-to-date:
  bazel-bin/src/main/main
INFO: Elapsed time: 8.716s, Critical Path: 0.04s
INFO: 0 processes.
INFO: Build completed successfully, 1 total action
INFO: Build completed successfully, 1 total action
Name: Shi-Lin Chen / Email: shilinch@usc.edu
linchen@Bende-MBP cpp-template %
```



5. Time complexity

1.

The outer for-loop is $O(\log n)$

The inner for-loop is controlled by $\log n$

\therefore The time complexity should be $O(\log^2 n)$

2. $\log n$

since the while-loop is controlled by n

1st iteration $\Rightarrow X = n/2$

2nd iteration $\Rightarrow X = n/4$

\vdots

$k \quad \quad \quad \Rightarrow X = n/2^k = 1$

$\therefore k = \log_2 n \quad \therefore O(\log n)$

6.

Code is included in the folder

```

int Solution::Factorial(int n) {
    if (n == 0) {
        return 1;
    }

    else if (n < 0) {
        return -1;
    }
    else {
        int result = 1;
        for(; n > 0 ;n--) {
            result = result*n;
        }

        return result;
    }
}

```

```

int Solution::FactorialRecursive(int n) {
    int result=1;
    result *= n;
    if(n == 0) {
        return 1;
    }
    else if (n < 0) {
        return -1;
    }
    else {
        return result * FactorialRecursive(n - 1);
    }
}

```

b.

Non-recursive

since there is one for-loop controlled by n
 \therefore the time complexity should be $O(n)$

Recursive:

it only does constant time and then the function return itself
 \therefore the time complexity is $O(1)$

6.5

we can use proof by introduction.

1. Assume $n = k$ is true, and $k > 0$

By the function code I wrote.

$$\text{Factorial}(k) = k * (k-1) * (k-2) \dots 2 * 1 = k! = \text{Factorial}(n)$$

2. Induction part, we want to show $n = k+1$ is also true

If $n = k + 1$

$$\text{Factorial}(k+1) = (k+1) * k * (k-1) * (k-2) * \dots * 2 * 1 = (k+1)! = \text{Factorial}(n)$$

Therefore,

$\text{Factorial}(n) = n!$ QED

Result:

```
INFO: Found 1 target...
Target //src/main:main up-to-date:
  bazel-bin/src/main/main
INFO: Elapsed time: 0.106s, Critical Path: 0.00s
INFO: 0 processes.
INFO: Build completed successfully, 1 total action
INFO: Build completed successfully, 1 total action
(Calculate n!) >> Please enter n:-1
n should be greater or equal to 0!
linchen@Bende-MacBook-Pro factorial %
```

```
INFO: Analyzed target //src/main:main (0 packages loaded, 0 targets)
INFO: Found 1 target...
Target //src/main:main up-to-date:
  bazel-bin/src/main/main
INFO: Elapsed time: 0.250s, Critical Path: 0.02s
INFO: 0 processes.
INFO: Build completed successfully, 1 total action
INFO: Build completed successfully, 1 total action
(Calculate n!) >> Please enter n:5
(Non Recursive) 5! = 120
(Recursive) 5! = 120
linchen@Bende-MacBook-Pro factorial %
```

Test cases include $n < 0$, $n=0$, $n > 0$