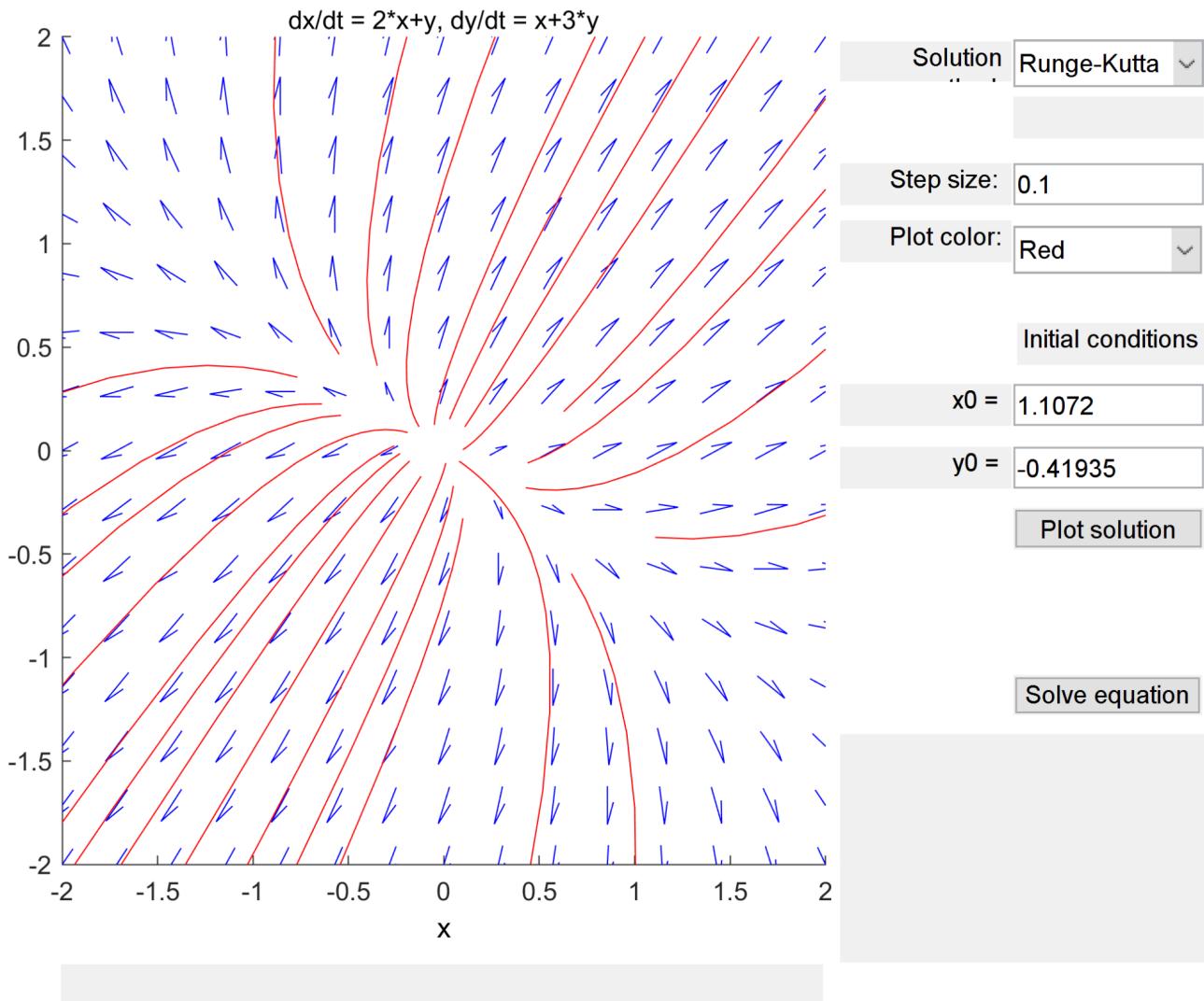


1. $\mathbf{dx/dt} = [2 \ 1; 1 \ 3] \mathbf{x}$

a. Phase Portrait



b. Equilibrium:

- **Asymptotic stability:** Unstable
- **Behaviour:** Nodal source
- **Clockwise/Counterclockwise:** N/A

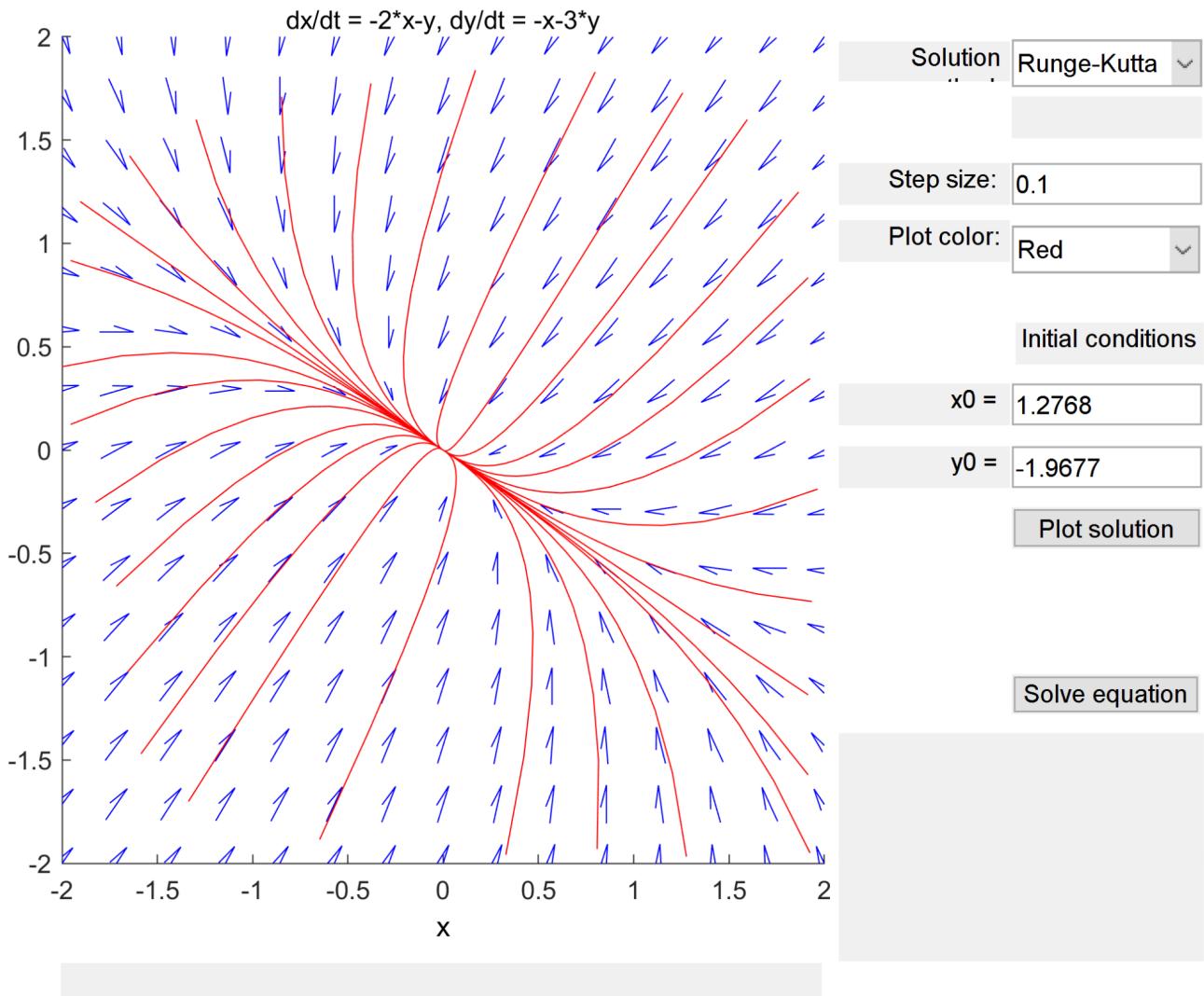
c. Eigenvalues:

i. $\lambda_1 = \frac{5 + \sqrt{5}}{2}, \lambda_2 = \frac{5 - \sqrt{5}}{2}$

- ii. **Justification:** The eigenvalues for the system are real, positive, and distinct. Therefore $(0,0)$ is an unstable nodal source.

2. $\frac{dx}{dt} = [-2 \ -1; \ -1 \ -3] x$

a. Phase Portrait



b. Equilibrium:

- **Asymptotic stability:** Asymptotically stable
- **Behaviour:** Nodal sink
- **Clockwise/Counterclockwise:** N/A

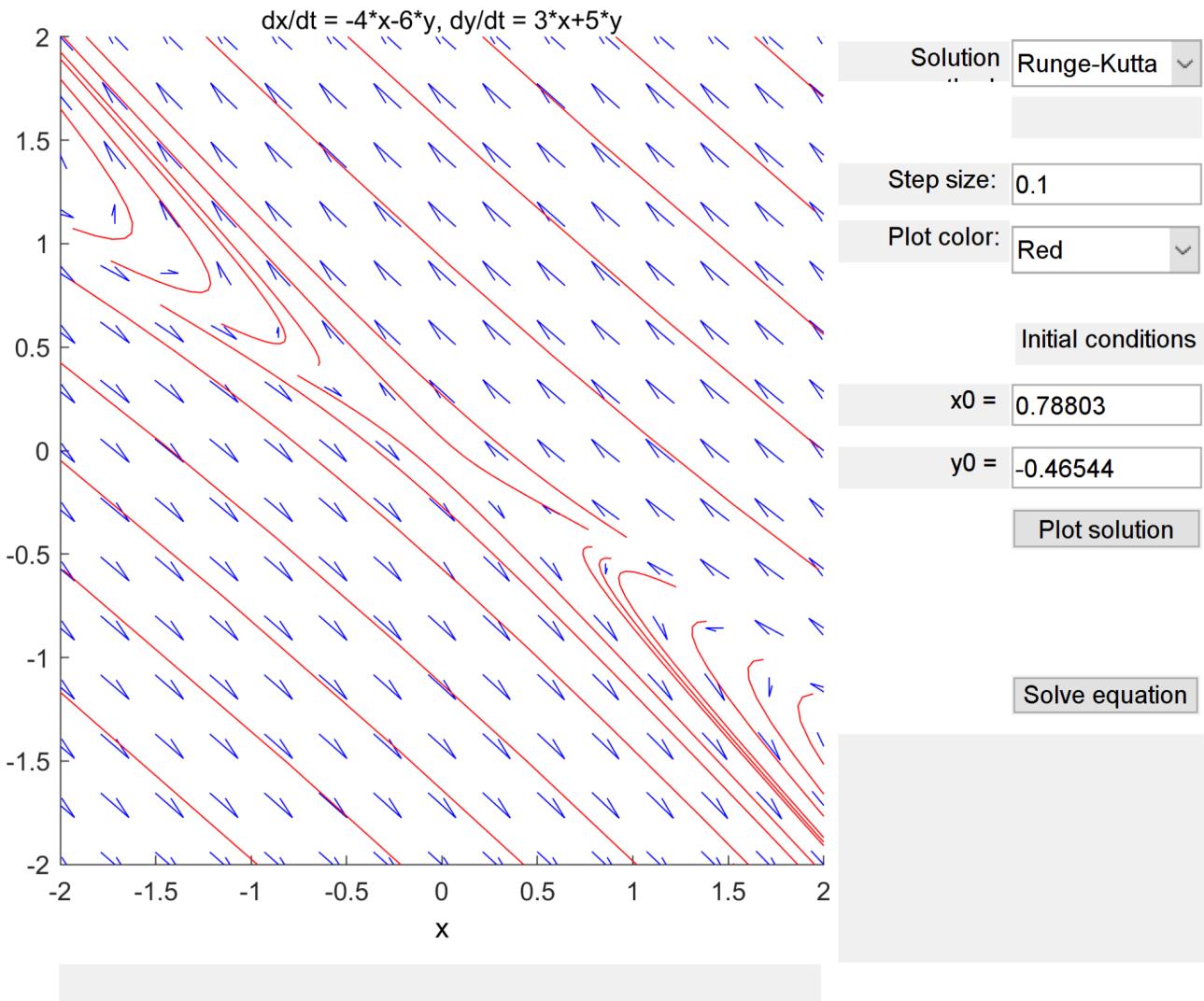
c. Eigenvalues:

i. $\lambda_1 = \frac{-5 + \sqrt{5}}{2}, \lambda_2 = \frac{-5 - \sqrt{5}}{2}$

- ii. **Justification:** The eigenvalues for the system are real, negative, and distinct. Therefore (0,0) is an asymptotically stable nodal sink.

3. $\frac{dx}{dt} = [-4 \ -6; \ 3 \ 5] x$

a. Phase Portrait



b. Equilibrium:

- **Asymptotic stability:** Unstable
- **Behaviour:** Saddle
- **Clockwise/Counterclockwise:** N/A

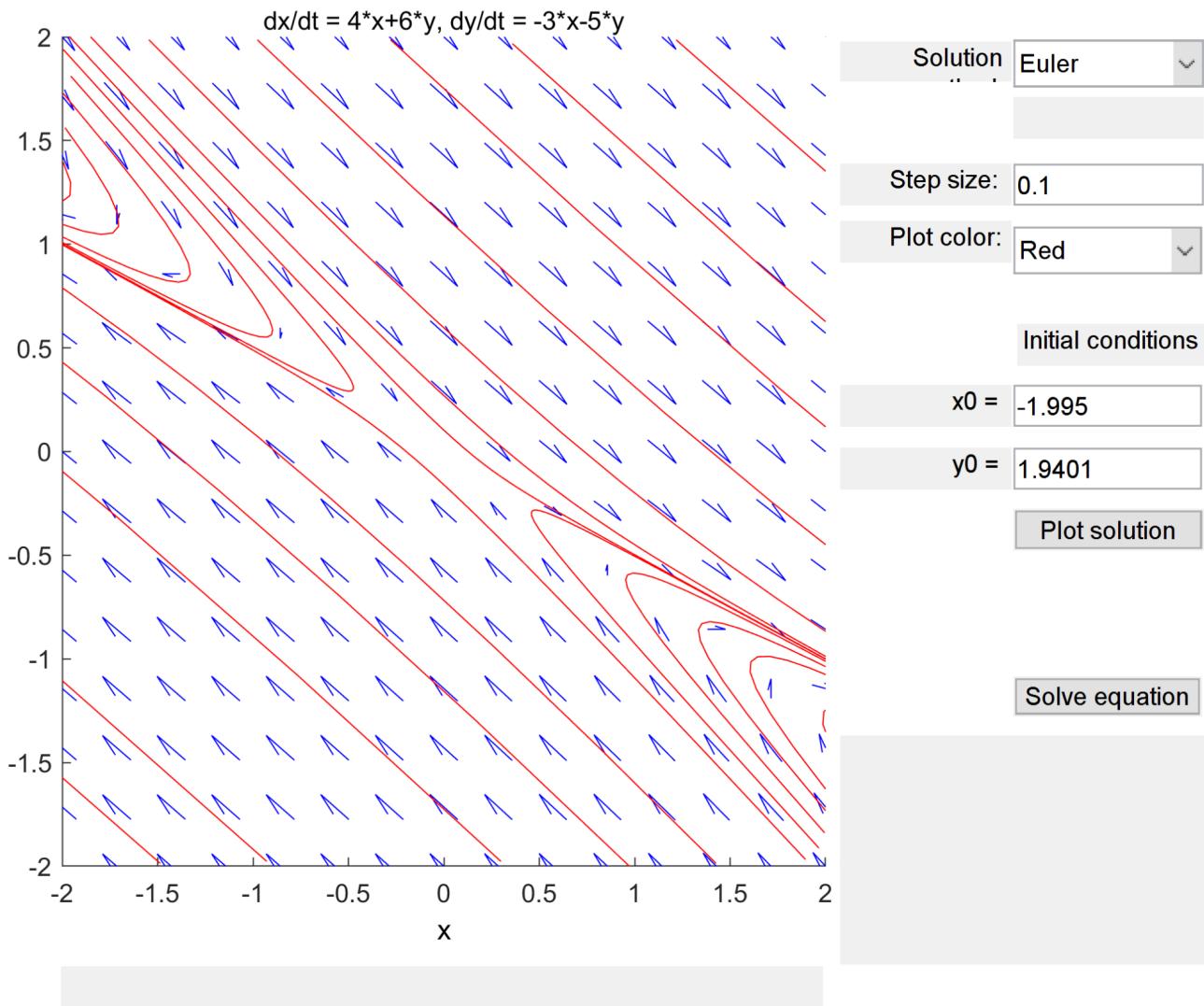
c. Eigenvalues:

i. $\lambda_1 = 2, \lambda_2 = -1$

- ii. **Justification:** The eigenvalues for the system are real and distinct, and have opposite signs. Therefore $(0,0)$ is an unstable saddle point.

4. $\frac{dx}{dt} = [4 \ 6; -3 \ -5] x$

a. Phase Portrait



b. Equilibrium:

- **Asymptotic stability:** Unstable
- **Behaviour:** Saddle
- **Clockwise/Counterclockwise:** N/A

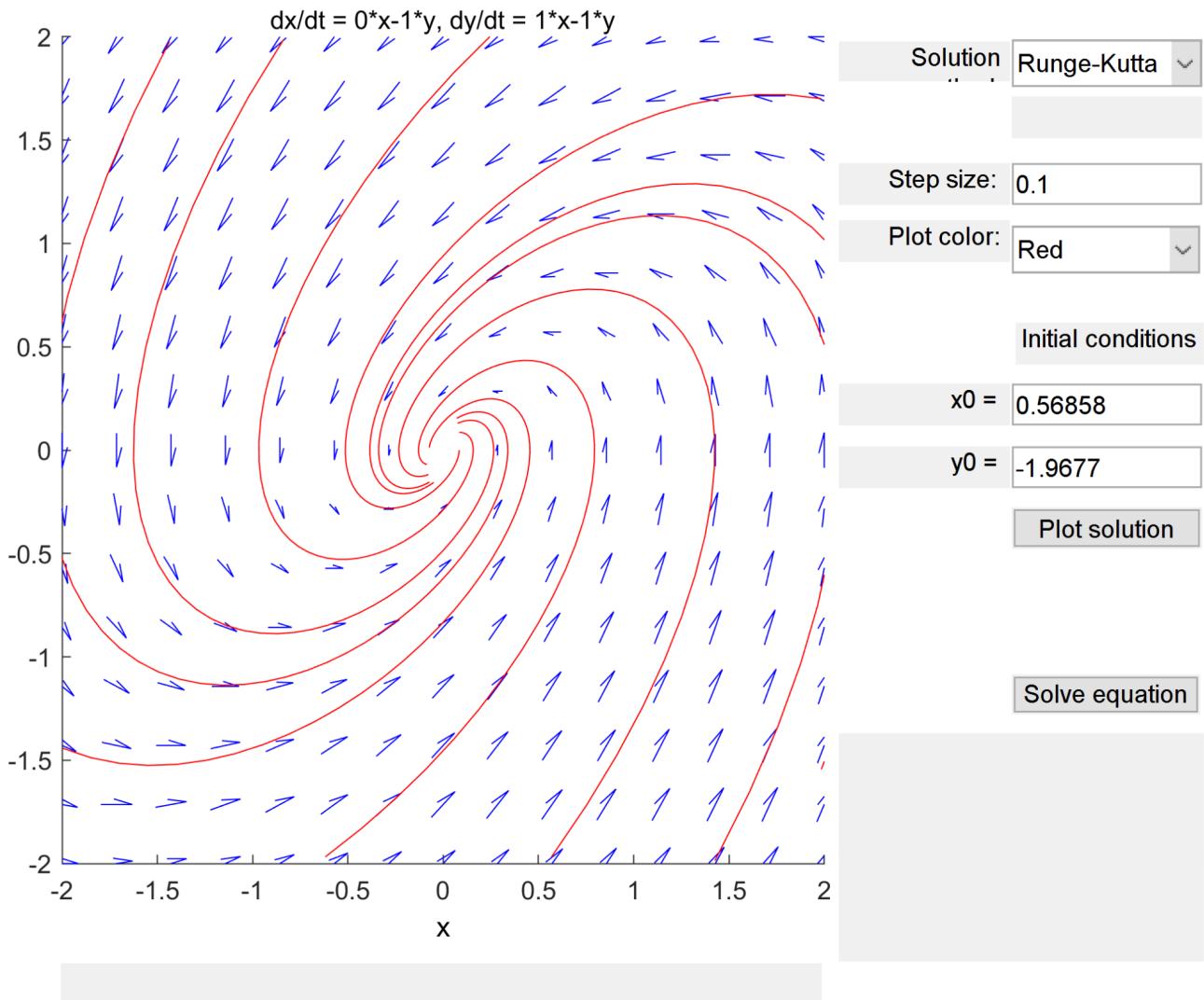
c. Eigenvalues:

i. $\lambda_1 = -2, \lambda_2 = 1$

- ii. **Justification:** The eigenvalues for the system are real and distinct, and have opposite signs. Therefore (0,0) is an unstable saddle point.

5. $\mathbf{dx/dt} = [0 \ -1; 1 \ -1] \mathbf{x}$

a. Phase Portrait



b. Equilibrium:

- **Asymptotic stability:** Asymptotically stable
- **Behaviour:** Spiral sink
- **Clockwise/Counterclockwise:** Counter-clockwise

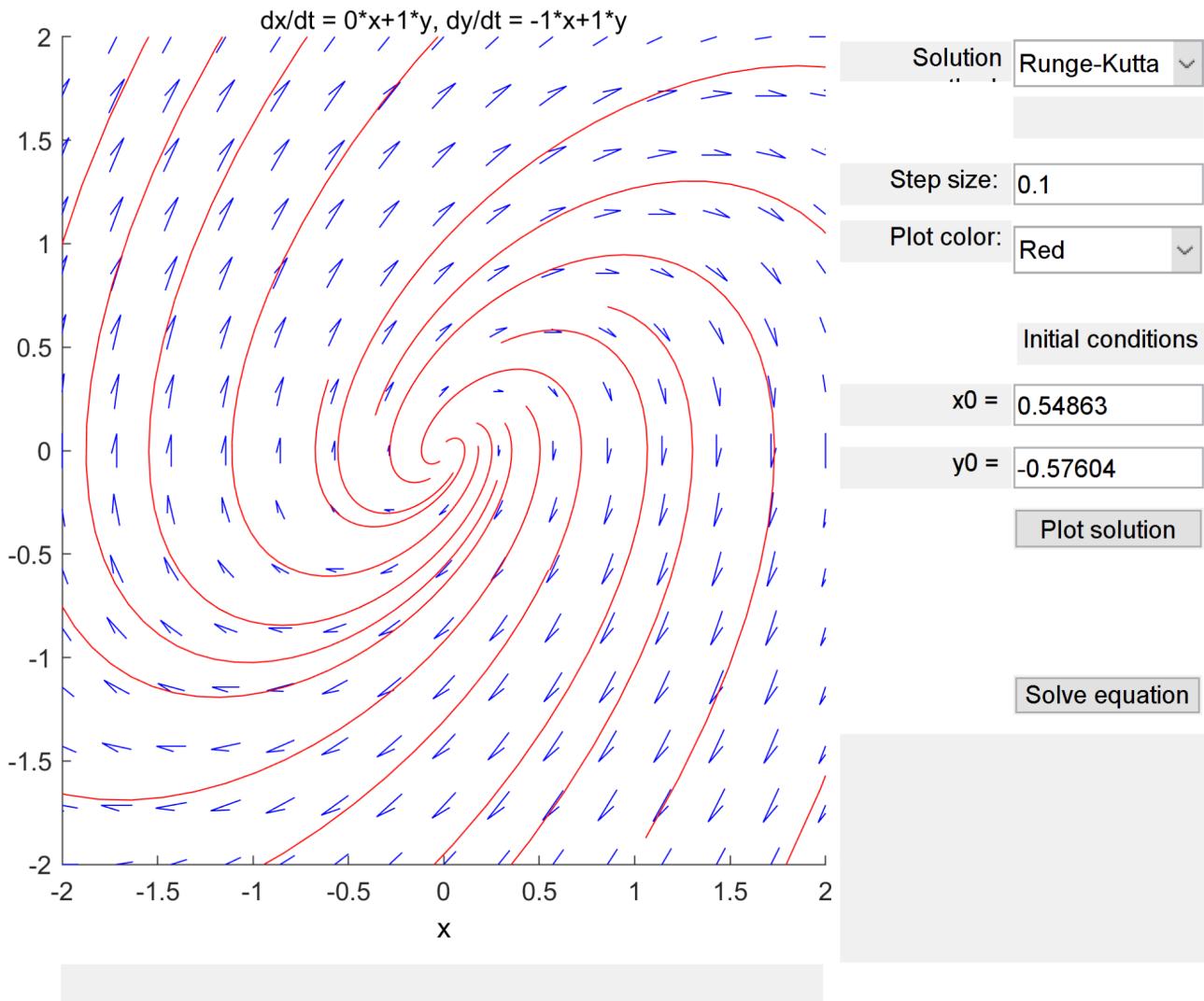
c. Eigenvalues:

i. $\lambda_1 = \frac{-1 + i\sqrt{3}}{2}, \lambda_2 = \frac{-1 - i\sqrt{3}}{2}$

- ii. **Justification:** Both eigenvalues are complex, and the real components of the eigenvalues are less than zero. Therefore (0,0) is a stable spiral sink.

6. $\mathbf{dx/dt} = [0 \ 1; -1 \ 1] \mathbf{x}$

a. Phase Portrait



b. Equilibrium:

- **Asymptotic stability:** Unstable
- **Behaviour:** Spiral source
- **Clockwise/Counterclockwise:** Clockwise

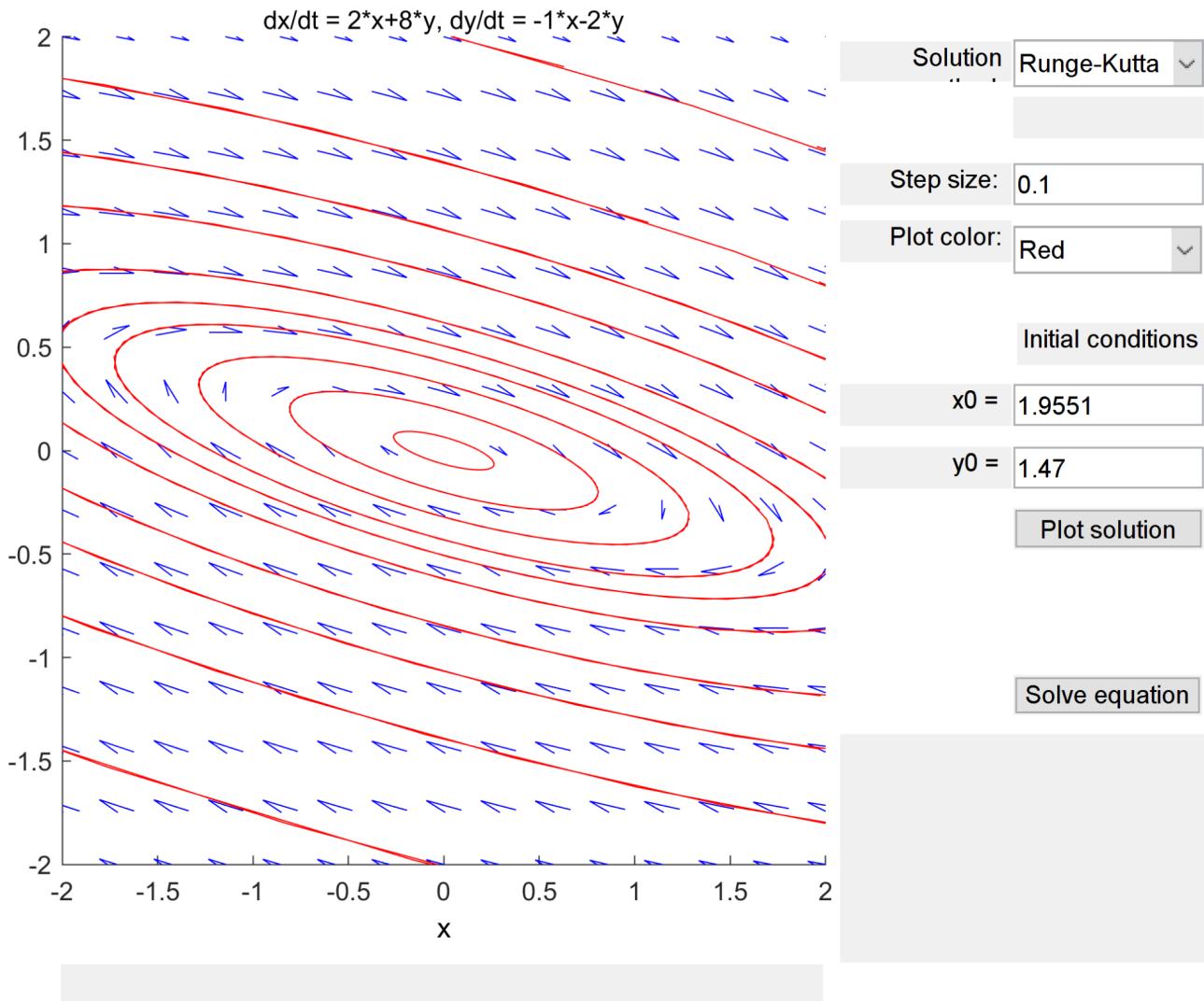
c. Eigenvalues:

i. $\lambda_1 = \frac{1+i\sqrt{3}}{2}, \lambda_2 = \frac{1-i\sqrt{3}}{2}$

- ii. **Justification:** Both eigenvalues are complex, and the real components of the eigenvalues are greater than zero. Therefore (0,0) is an unstable spiral source.

7. $\mathbf{dx/dt} = [2 \ 8; -1 \ -2] \mathbf{x}$

a. Phase Portrait



b. Equilibrium:

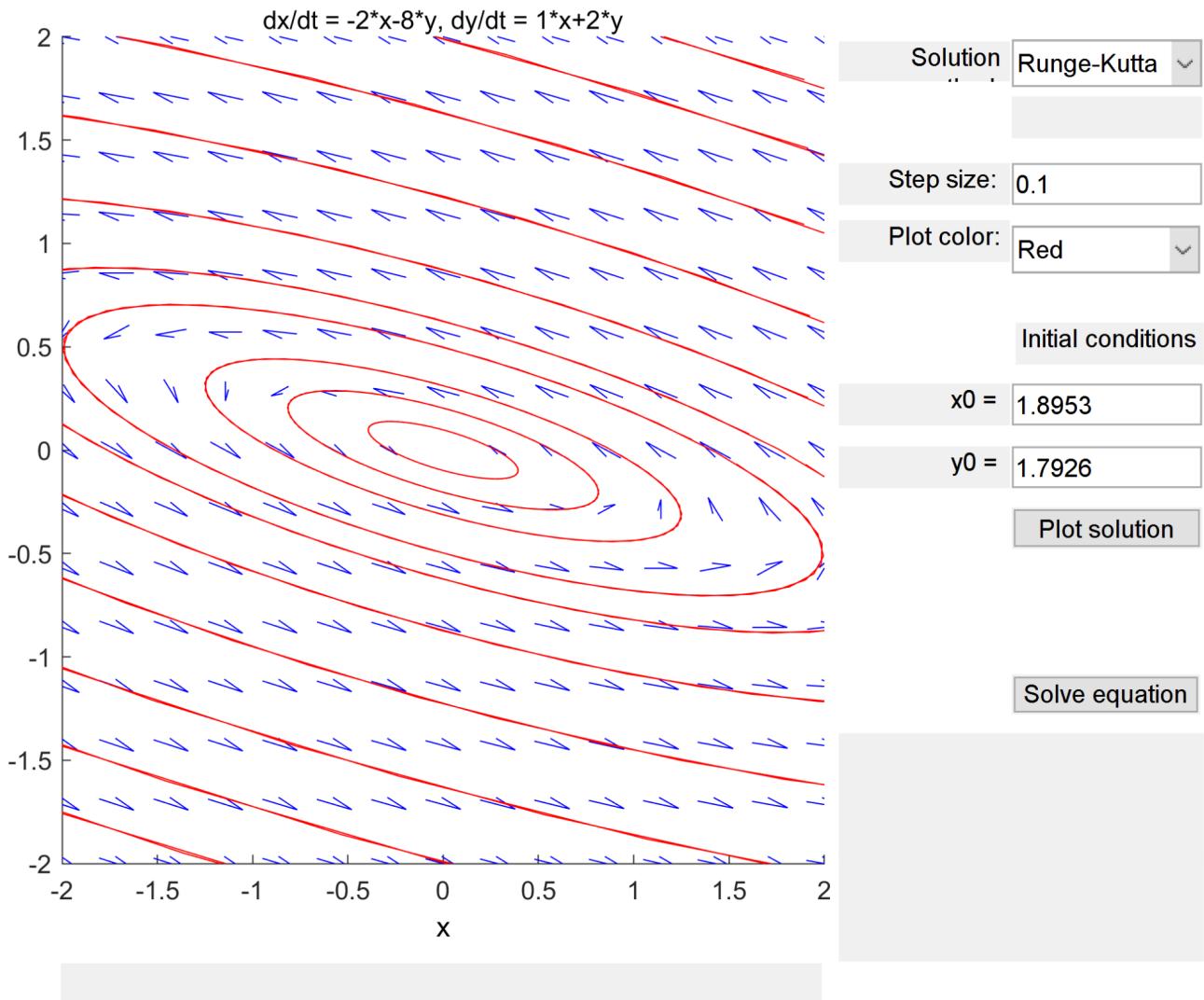
- **Asymptotic stability:** Stable
- **Behaviour:** Center
- **Clockwise/Counterclockwise:** Clockwise

c. Eigenvalues:

- $\lambda_1 = 2i, \lambda_2 = -2i$
- Justification:** The real components of the eigenvalues are equal to zero (eigenvalues are imaginary). Therefore $(0,0)$ is a stable center.

8. $\frac{dx}{dt} = [-2 \ -8; 1 \ 2] x$

a. Phase Portrait



b. Equilibrium:

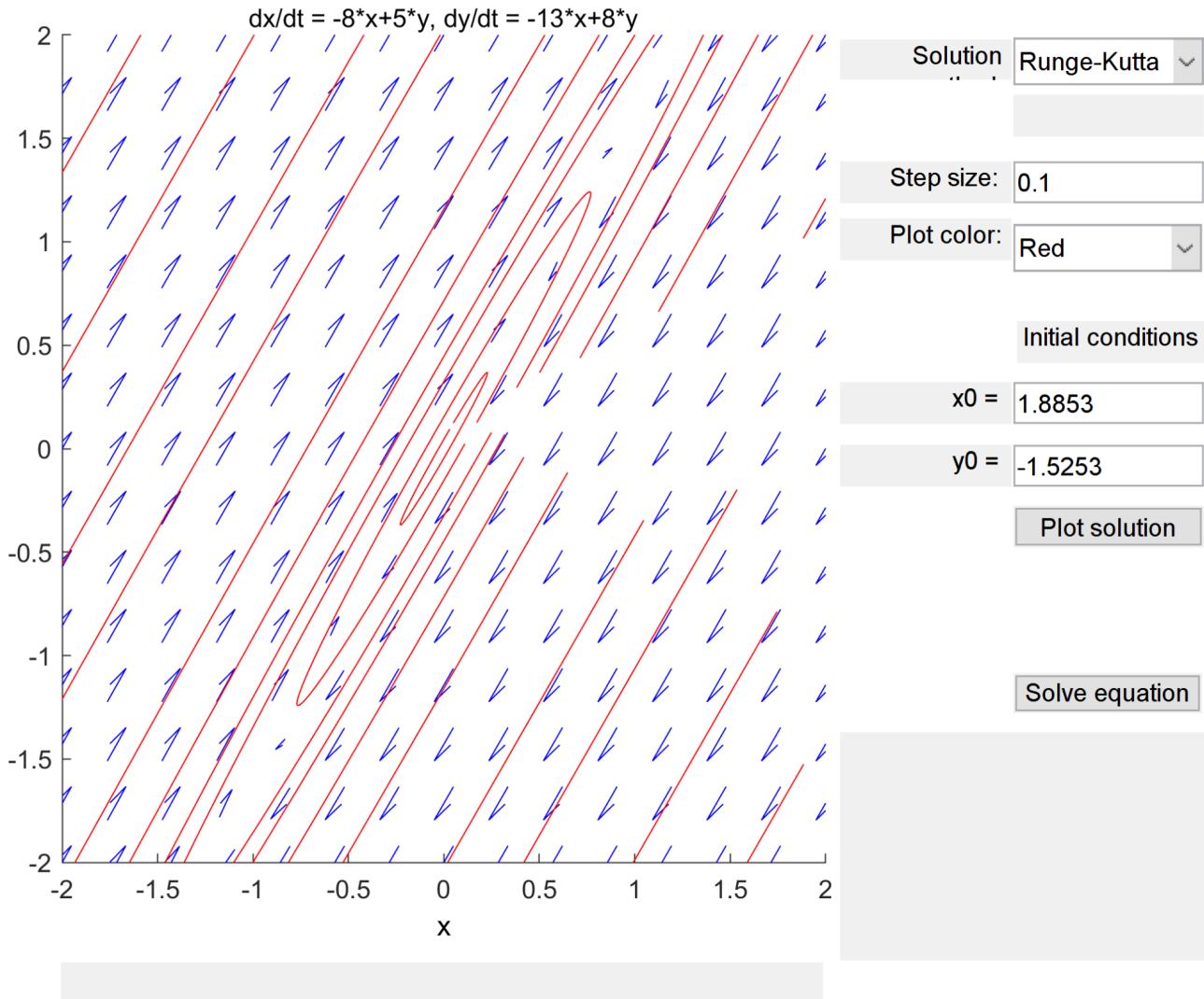
- **Asymptotic stability:** Stable
- **Behaviour:** Center
- **Clockwise/Counterclockwise:** Counter-clockwise

c. Eigenvalues:

- $\lambda_1 = 2i, \lambda_2 = -2i$
- Justification:** The real components of the eigenvalues are equal to zero (eigenvalues are imaginary). Therefore (0,0) is a stable center.

9. $\frac{dx}{dt} = [-8 \ 5; -13 \ 8] x$

a. Phase Portrait



b. Equilibrium:

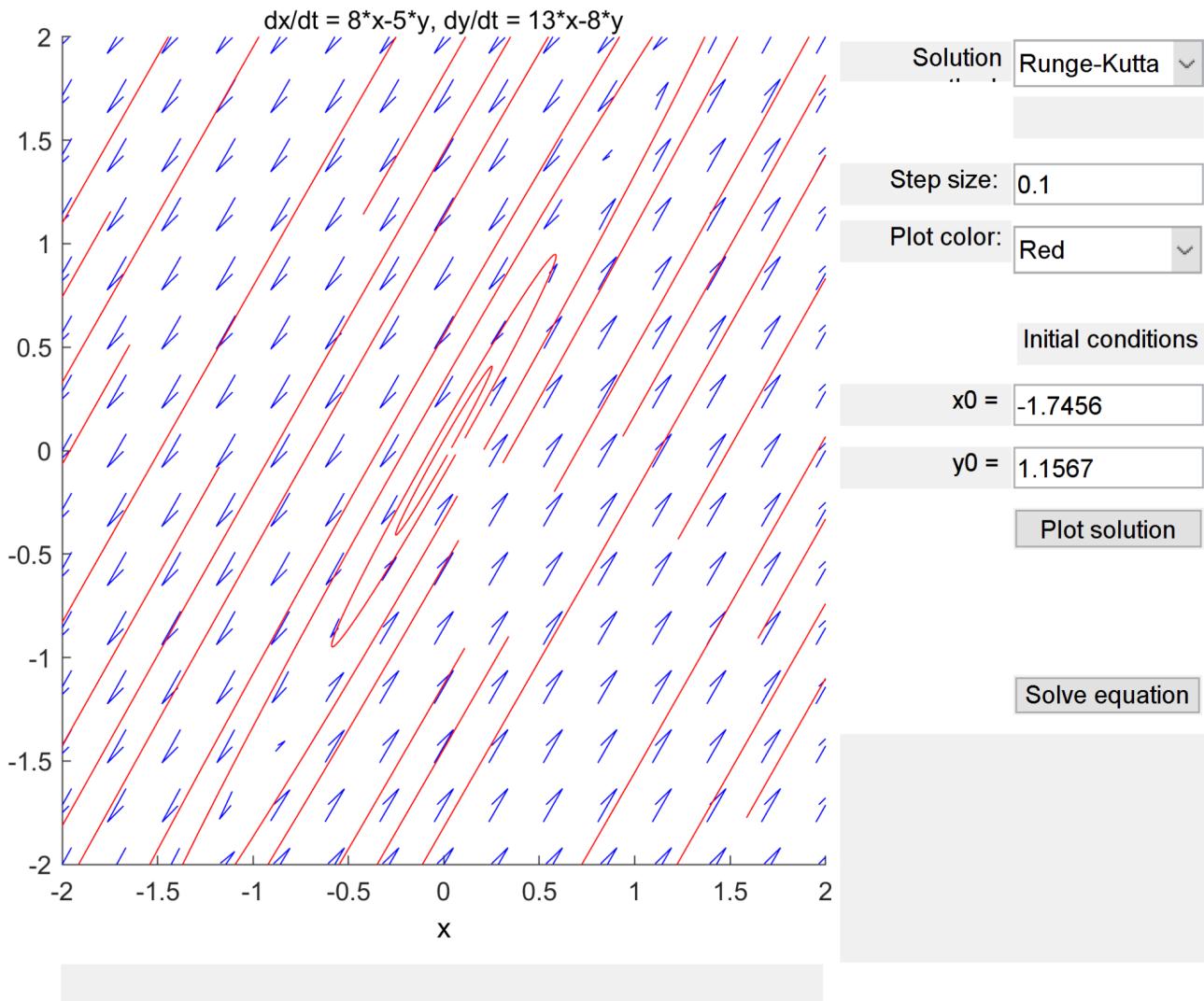
- **Asymptotic stability:** Stable
- **Behaviour:** Center
- **Clockwise/Counterclockwise:** Clockwise

c. Eigenvalues:

- i. $\lambda_1 = i, \lambda_2 = -i$
- ii. **Justification:** The real components of the eigenvalues are equal to zero (eigenvalues are imaginary). Therefore (0,0) is a stable center.

10. $\mathbf{dx/dt} = [8 -5; 13 -8] \mathbf{x}$

a. Phase Portrait



b. Equilibrium:

- **Asymptotic stability:** Stable
- **Behaviour:** Center
- **Clockwise/Counterclockwise:** Counter-clockwise

c. Eigenvalues:

- $\lambda_1 = i, \lambda_2 = -i$
- Justification:** The real components of the eigenvalues are equal to zero (eigenvalues are imaginary). Therefore (0,0) is a stable center.