

$$\tilde{J} = \frac{1}{N} \sum R_i$$

calculated using  $x_i$  &  $w_i$  &  $b_i$

for now.  
incorporate

$$\frac{\partial L}{\partial w_j} = (y - t) x_j$$

$$\nabla_w \tilde{J} = \frac{\partial \tilde{J}}{\partial \underline{w}} = \left( \frac{\partial \tilde{J}}{\partial w_1}, \frac{\partial \tilde{J}}{\partial w_2}, \dots, \frac{\partial \tilde{J}}{\partial w_D} \right)$$

weight matrix  
not a scalar

$$\underline{w} \leftarrow \underline{w} - \underset{\downarrow}{a} \frac{\partial \tilde{J}}{\partial \underline{w}} = \underline{w} - a \sum_{i=0}^N \frac{\partial L_i}{\partial w_i}$$

$$\underline{w} \leftarrow \underline{w} - \underset{\text{learning rate}}{a} \sum_{i=0}^N (y^i - t^i) x^i$$

how GD update the weight matrix, after each iteration

$$\text{optimal} = \frac{\partial \tilde{J}}{\partial \underline{w}} = 0. \quad \xrightarrow{\text{learning rate}} \frac{\partial \tilde{J}}{\partial \underline{w}} = 0$$

calculate the euclidean distance given a vector

$$R = \frac{1}{2} \|\underline{w}\|_2^2 \leadsto l_2 \text{ regularization}$$

constant Euclid. dist  
a tunable hyperparameter

$$\underline{w} \leftarrow \underline{w} - a \frac{\partial \tilde{J} + \lambda R}{\partial \underline{w}}$$

$$\underline{w} - a \left( \frac{\partial \tilde{J}}{\partial \underline{w}} + \frac{\partial \lambda R}{\partial \underline{w}} \right) \Leftrightarrow \underline{w} - a \left( \frac{\partial \tilde{J}}{\partial \underline{w}} + \lambda \frac{\partial R}{\partial \underline{w}} \right) \xrightarrow{\underline{w}} \underline{w} - a \lambda \underline{w}$$

$$\underline{w} \leftarrow \underline{w} - a \left( \frac{\partial \tilde{J}}{\partial \underline{w}} + \lambda \underline{w} \right)$$

$$\underline{w} \leftarrow (1 - a \lambda) \underline{w} - a \frac{\partial \tilde{J}}{\partial \underline{w}}$$

$\theta = \text{Config. of parameters} = (w, b)$

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$$\underline{J(\theta)} = \frac{1}{N} \sum_{i=1}^N L^{(i)} = \frac{1}{N} \sum_{i=1}^N L(y(x^{(i)}, \theta), t^{(i)})$$

$$\frac{\partial J}{\partial \theta} = \frac{1}{N} \sum \frac{\partial L^{(i)}}{\partial \theta} \quad \text{impractical.}$$

$\downarrow$  cb

$$W = \begin{bmatrix} \underline{1} & w \end{bmatrix}$$

$\downarrow$   
dummy index

$$w \approx \theta - \alpha \frac{\partial L^{(i)}}{\partial \theta}$$

$\uparrow$  0,  $\uparrow$  w

