Introduction to Machine Learning

Support Vector Machines & Kernels

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Overview

- Prediction
 - Why might predictions be wrong?
- Support vector machines
 - Do really well with linear models
- Kernels
 - Making the non-linear linear

Why Might Predictions be Wrong?

- True non-determinism
 - Flip a biased coin
 - $p(\text{heads}) = \theta$
 - Estimate θ
 - If $\theta > 0.5$, predict "heads", else "tails"
- Lots of ML research on problems like this:
 - Learn a model
 - Do the best you can in expectation

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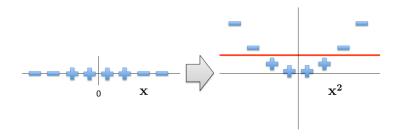
Why Might Predictions be Wrong?

- Partial observability
 - Something needed to predict y is missing from observation x
 - *N*-bit parity problem
 - Determine the parity (even or odd) of a sequence of N binary bits.
 - The goal is to build a model that can correctly predict the parity of any given N-bit sequence.
- Noise in the observation x
 - Measurement error
 - Instrument limitations
- Representational bias
- Algorithmic bias
- Bounded resources

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Representational Bias

• Having the right features for x is crucial



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Support Vector Machines

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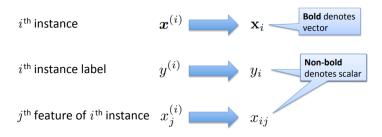
Strengths of SVMs

- Good generalization
 - in theory
 - in practice
- Works well with frew training instances
- Find globally best model
- Efficient algorithms
- Amenable to the kernel trick

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Minor Notation Change

- To better match notations used in SVMs and to make matrix formulas simpler
- We will drop using superscripts for the i^{th} instance



Minor Notation Change

- Training instances: $\mathbf{x} \in \mathbb{R}^{d+1}, x_0 = 1, y \in -1, 1$
- Model parameters: $\theta \in \mathbb{R}^{d+1}$
- Hyperplane: $\theta^{\mathsf{T}} x = \langle \theta, x \rangle = 0$
 - the vectors are orthogonal to each other
- Recall the inner (dot) product:

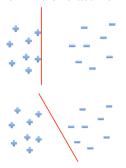
$$\langle \boldsymbol{\theta}, \boldsymbol{x} \rangle = \boldsymbol{\theta} \cdot \boldsymbol{x} = \boldsymbol{\theta}^{\top} \boldsymbol{x} = \sum_{i} \theta_{i} x_{i}$$
 (1)

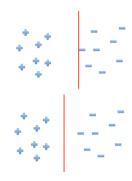
• Decision function: $h(x) = sign(\theta^{T}x) = sign(\langle \theta, x \rangle)$

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Intuition

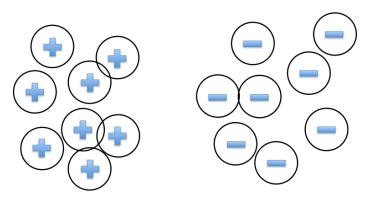
• Which line or classifier is better?





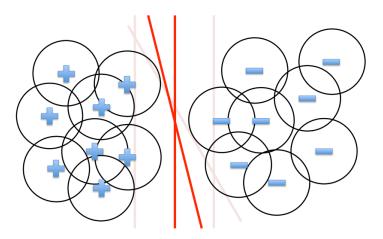
Noise in the observations

- Each circle denotes the "noise" that can happen when the sample is observed (e.g. faulty measuring equipment)
- A sample's actual reading, in terms of features, can fall anywhere in the circle around the "true" values



More Noise; Ruling Out Some Seperators

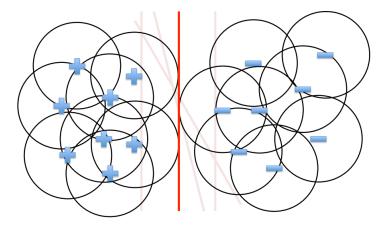
• When the readings (the values of features) become noisier, we can rule out some separators or classifiers



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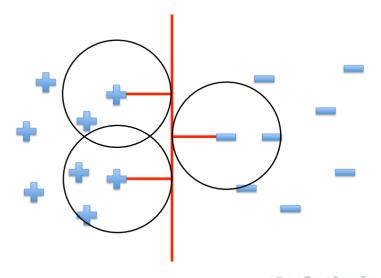
Only One Separator Remains

 Assuming that the values of the features are as noisy as they can get, provided that the samples are still linearly separable in the feature space.



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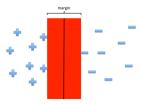
Maximizing the Margin



"Wide" Separators

• We want the separators as "wide" as possible, to allow for more noise in the features of the samples.





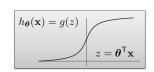
Why Maximize Margin

- Increasing margin reduces capacity
 - i.e. fewer possible models
- Lesson from Learning Theory:
 - If the following holds:
 - H is sufficiently constrained in size
 - and/or the size of the training dataset *N* is large
 - Then low training error is likely to be evidence of low generalization error

Alternative View of Logistic Regression

- if y = 1 we want $h_{\theta} \approx 1, \theta^{\top} x \gg 0$
- if y = 0 we want $h_{\theta} \approx 0, \theta^{\top} x \ll 0$

$$h_{\theta}(x) = \frac{1}{1 + e^{-\theta^{\top} x}} \tag{2}$$



• We want to minimize the cross-entropy cost, by finding the θ summing the losses across the classifications on all the samples

$$\mathcal{J}(\boldsymbol{\theta}) = -\sum_{i=1}^{N} \left[y_i \log h_{\boldsymbol{\theta}}(\boldsymbol{x}_i) + (1 - y_i) \log(1 - h_{\boldsymbol{\theta}}(\boldsymbol{x}_i)) \right]$$
(3)

- $cost_1(\theta^\top x_i) \iff log h_\theta(x_i)$
- $cost_0(\theta^{\top} x_i) \iff log(1 h_{\theta}(x_i))$

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Alternative View of Logistic Regression

• Cost of one sample:

$$\mathcal{L}(\theta) = -y_i \log h_{\theta}(\mathbf{x}_i) + (1 - y_i) \log(1 - h_{\theta}(\mathbf{x}_i))$$
 (4)

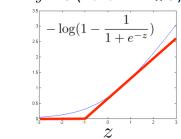
$$h_{\theta}(x) = \frac{1}{1 + e^{-\theta^{\mathsf{T}}x}} \tag{5}$$

$$z = \boldsymbol{\theta}^{\top} \boldsymbol{x} \tag{6}$$

If y = 1 (want $\boldsymbol{\theta}^\mathsf{T} \mathbf{x} \gg 0$):

 $-\log \frac{1}{1 + e^{-z}}$

If y=0 (want ${\boldsymbol{\theta}}^{\mathsf{T}}\mathbf{x}\ll 0$):



Logistic Regression to SVMs

Logistic Regression:

$$\min_{\theta} - \sum_{i=1}^{N} [y_i \log h_{\theta}(\mathbf{x}_i) + (1 - y_i) \log(1 - h_{\theta}(\mathbf{x}_i))] + \frac{\lambda}{2} \sum_{j=1}^{d} \theta_j^2$$
 (7)

Support Vector Machines:

$$\min_{\theta} C \sum_{i=1}^{N} [y_i \text{cost}_1(\theta^{\top} x_i) + (1 - y_i) \text{cost}_0(\theta^{\top} x_i)] + \frac{1}{2} \sum_{j=1}^{d} \theta_j^2$$
 (8)

• C is a constant, a tunable hyperparameter. You can imagine it as similar to $\frac{1}{4}$

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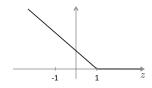
The Hinge Loss

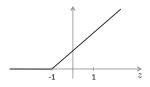
• Support Vector Machines:

$$\min_{\boldsymbol{\theta}} C \sum_{i=1}^{N} [y_i \operatorname{cost}_1(\boldsymbol{\theta}^{\mathsf{T}} \boldsymbol{x}_i) + (1 - y_i) \operatorname{cost}_0(\boldsymbol{\theta}^{\mathsf{T}} \boldsymbol{x}_i)] + \frac{1}{2} \sum_{j=1}^{d} \theta_j^2$$
 (9)

If
$$y=1$$
 (want ${m heta}^\intercal {f x} \geq 1$):

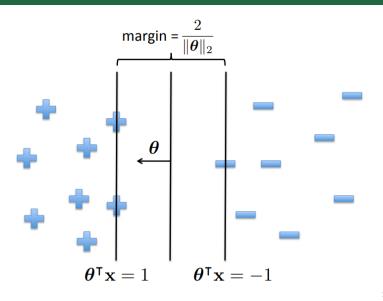
If
$$y = 1$$
 (want $\theta^{\mathsf{T}} \mathbf{x} \ge 1$): If $y = 0$ (want $\theta^{\mathsf{T}} \mathbf{x} \le -1$):





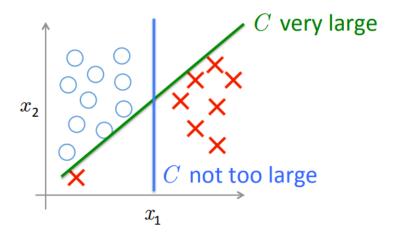
$$\ell_{\text{hinge}} = \max(0, 1 - y \cdot h(x)) \tag{10}$$

Maximum Margin Hyperplane





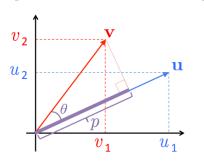
Large Margin Classifier in Presence of Outliers



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Vector Inner Product

• Some quick review on the vector inner product:



$$u = \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} \qquad v = \begin{bmatrix} v_1 \\ v_2 \end{bmatrix}$$

$$\|\mathbf{u}\|_2 = \operatorname{length}(\mathbf{u}) \in \mathbb{R}$$

= $\sqrt{u_1^2 + u_2^2}$

Vector Inner Product

• Continued from the previous slide:

$$\boldsymbol{u}^{\top}\boldsymbol{v} = \boldsymbol{v}^{\top}\boldsymbol{u} \tag{11}$$

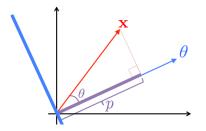
$$\boldsymbol{u}^{\top}\boldsymbol{v} = u_1v_1 + u_2v_2 \tag{12}$$

$$\boldsymbol{u}^{\top}\boldsymbol{v} = ||\boldsymbol{u}||_2||\boldsymbol{v}||_2\cos\theta \tag{13}$$

$$\boldsymbol{u}^{\top} \boldsymbol{v} = p||\boldsymbol{u}||_2$$
, where $p = ||\boldsymbol{v}||_2 \cos\theta$ (14)

Understanding the Hyperplane

• The hyperplane is orthogonal to the vector θ :



$$\boldsymbol{\theta}^{\mathsf{T}} \mathbf{x} = \|\boldsymbol{\theta}\|_2 \underbrace{\|\mathbf{x}\|_2 \cos \theta}_p$$

$$= p\|\boldsymbol{\theta}\|_2$$

• Assume $\theta_0 = 0$ so that the hyperplane is centered at the origin, and that d = 2 for it to be visually rendered in 2D. All for the purpose of simplicity of the demo.

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Understanding the Hyperplane

• Support Vector Machines objective to minimize:

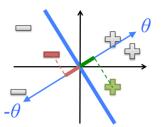
$$\min_{\boldsymbol{\theta}} C \sum_{i=1}^{N} [y_i \text{cost}_1(\boldsymbol{\theta})^{\top} \boldsymbol{x}_i + (1 - y_i) \text{cost}_0(\boldsymbol{\theta})^{\top} \boldsymbol{x}_i] + \frac{1}{2} \sum_{j=1}^{d} \theta_j^2$$
 (15)

- Suppose that C is set to an arbitrarily large value \iff the first term becomes 0, for simplicity
- Now we are just minimizing the second term $\frac{1}{2} \sum_{j=1}^{d} \theta_{j}^{2}$
- Recall that $\theta^{\top} x_i \ge 1$ when $y_i = 1$ and $\theta^{\top} x_i \le -1$ when $y_i = -1$

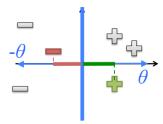
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Maximizing the Margin

• Let p_i be the projection of x_i onto the vector θ



Since p is small, therefore $\|\theta\|_2$ must be large to have $p\|\theta\|_2 \ge 1$ (or \le -1)



Since p is larger, $\| \boldsymbol{\theta} \|_2$ can be smaller in order to have $p \| \boldsymbol{\theta} \|_2 \geq 1$ (or \leq -1)

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The SVN Dual Problem

• The primal SVM problem was given as

$$\frac{1}{2} \sum_{j=1}^{d} \theta_j^2, \text{ s.t. } y_i(\boldsymbol{\theta}^\top \boldsymbol{x}_i + b) \ge 1, \forall i$$
 (16)

- Can be solved more efficiently by taking the Lagrangian dual
 - Duality is a common idea in optimization
 - It transforms a difficult optimization problem into a simpler one
 - ullet Key idea: introduce slack variables α_i for each constraint
 - α_i indicates how important a particular constraint is to the solution

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The Lagragian

- The Lagrangian dual refers to the dual formulation of an optimization problem using the Lagrange duality theory.
- It transforms a primal optimization problem into its dual problem
 - which can sometimes provide useful insights or computational advantages.
- The Lagrange duality theory is based on the concept of Lagrange multipliers
 - which are introduced to incorporate constraints into an optimization problem.
- By introducing these multipliers, the problem is transformed into a new formulation that involves maximizing or minimizing a function called the Lagrangian
 - which incorporates both the objective function and the constraints.

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The SVM Dual Problem

• The Lagrangian is given as, s.t. $\alpha_i \ge 0 \ \forall i$:

$$\frac{1}{2} \sum_{j=1}^{d} \theta_j^2 - \sum_{i=1}^{n} \alpha_i (y_i(\boldsymbol{\theta}^{\top} x_i + b) - 1)$$
 (17)

- We must minimize over θ and maximize over α
- At optimal solution, partials w.r.t. θ 's are 0



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The SVM Dual Representation

• After solving a bunch of linear algebra and calculus, want to maximize:

$$\mathcal{J}(\alpha) = \sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j \langle \mathbf{x}_i, \mathbf{x}_j \rangle$$
 (18)

Such that $\sum_i a_j y_j = 0$, s.t. $\alpha_i \ge 0$, $\forall i$

• The decision function is given by:

$$h(\mathbf{x}) = \operatorname{sign}\left(\sum_{i \in SV} \alpha_i y_i \langle \mathbf{x}, \mathbf{x}_i \rangle + b\right)$$
 (19)

$$b = \frac{1}{|SV|} \sum_{i \in SV} \left(y_i - \sum_{j \in SV} \alpha_j y_j \langle \boldsymbol{x}_i, \boldsymbol{x}_j \rangle \right)$$
 (20)

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Understanding the Dual

- We have $\alpha_i \geq 0, \forall i$
 - Constaint weights (α_i 's cannot be negative)
- We have $\sum_i \alpha_i y_i = 0$
 - Balances between the weight of constraints for different classes

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Understanding the Dual

After solving a bunch of linear algebra and calculus, want to maximize:

$$\mathcal{J}(\alpha) = \sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j \langle \mathbf{x}_i, \mathbf{x}_j \rangle$$
 (21)

Such that $\sum_i a_j y_j = 0$, s.t. $\alpha_i \ge 0$, $\forall i$

- $\langle x_i, x_j \rangle$ measures the similarity between the points
- Points with different labels increase the sum $\frac{1}{2}\sum_{i=1}^{n}\sum_{j=1}^{n}\alpha_{i}\alpha_{j}y_{i}y_{j}\langle x_{i},x_{j}\rangle$, while points with the same label decrease the sum

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Understanding the Dual

• After solving a bunch of linear algebra and calculus, want to maximize:

$$\mathcal{J}(\alpha) = \sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j \langle \mathbf{x}_i, \mathbf{x}_j \rangle$$
 (22)

Such that $\sum_i a_j y_j = 0$, s.t. $\alpha_i \ge 0$, $\forall i$

- $a_i \ge 0$ and the constraint is tight $y_i(\theta^\top x_i) = 1$
 - Point is a support vector
- $a_i = 0$
 - Point is not a support vector



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What if Data Are Not Linearly Separable?

- Cannot find θ that satisfies $y_i(\theta^T x_i) \ge 1, \forall i$
- Introduce the slack variable ξ_i

$$y_i(\boldsymbol{\theta}^{\top} \boldsymbol{x}_i) \ge 1 - \xi_i, \forall i$$
 (23)

• New problem, s. t. $y_i(\theta^\top x_i) \ge 1 - \xi_i, \forall i$:

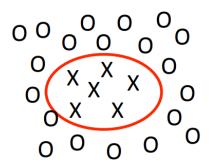
$$\min_{\theta} \frac{1}{2} \sum_{j=1}^{d} \theta_j^2 + C \sum_{i} \xi_i$$
 (24)

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Strengths of SVMs

- Good generalization in theory
- Good generalization in practice
- Work well with few training instances
- Find the globally best model
- Efficient algorithms
- Amenable to the kernel trick ...

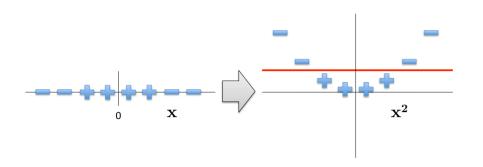
What is the Decision Boundary Is Not Linear?





Kernel Methods: Making the Non-Linear Linear

When Linear Separators Fail



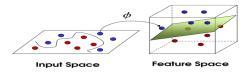
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Mapping into a New Feature Space

• For example, with $x_i \in \mathbb{R}^2$:

$$\Phi([x_{i1}, x_{i2}]) = [x_{i1}, x_{i2}, x_{i1}x_{i2}, x_{i1}^2, x_{i2}^2]$$
 (25)

- Rather than running SVM on x_i , run it on $\Phi(x_i)$
 - Find non-linear separator in input space
- What if $\Phi(x_i)$ is really big?
- Use kernels to compute it implicitly!



$$\Phi: \mathcal{X} \to \hat{\mathcal{X}} = \Phi(\mathbf{x}) \tag{26}$$

Kernels

• Find kernels K such that:

$$K(\mathbf{x}_i, \mathbf{x}_j) = \langle \Phi(\mathbf{x}_i), \Phi(\mathbf{x}_j) \rangle \tag{27}$$

- Compute $K(x_i, x_j)$ should be efficient, much more so than computing $\Phi(x_i)$ and $\Phi(x_j)$
- Use $K(x_i, x_j)$ in the SVM algorithm rather than $\langle x_i, x_j \rangle$



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The Polynomial Kernel

- Let $x_i = [x_{i1}, x_{i2}]$ and $x_j = [x_{j1}, x_{j2}]$
- Consider the following function:

$$K(\mathbf{x}_i, \mathbf{x}_j) = \langle \mathbf{x}_i, \mathbf{x}_j \rangle^2 \tag{28}$$

$$K(\mathbf{x}_i, \mathbf{x}_j) = (x_{i1}x_{j1} + x_{i2}x_{j2})^2$$
 (29)

$$K(\mathbf{x}_i, \mathbf{x}_j) = (x_{i1}^2 x_{j1}^2 + x_{i2}^2 x_{j2}^2 + 2x_{i1} x_{i2} x_{j1} x_{j2})$$
(30)

$$K(\mathbf{x}_i, \mathbf{x}_j) = \langle \Phi(\mathbf{x}_i), \Phi(\mathbf{x}_j) \rangle \tag{31}$$

where

$$\Phi(\mathbf{x}_i) = [x_{i1}^2, x_{i2}^2, \sqrt{2}x_{i1}x_{i2}]$$
 (32)

$$\Phi(\mathbf{x}_j) = [x_{j1}^2, x_{j2}^2, \sqrt{2}x_{j1}x_{j2}]$$
(33)

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The Kernel Trick

- Given an algorithm that is formulated in terms of a positive definite kernel K_1 , one can construct an alternative algorithm by replacing K_1 with another positive definite kernel K_2
- SVMs can use the kernel trick

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Incorporating Kernels into SVMs

• Originally we have:

$$\mathcal{J}(\alpha) = \sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j \langle \mathbf{x}_i, \mathbf{x}_j \rangle$$
 (34)

Such that $\sum_i a_i y_i = 0$, s.t. $\alpha_i \ge 0$, $\forall i$

• After we incorporate the kernel, it becomes:

$$\mathcal{J}(\alpha) = \sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j K(\boldsymbol{x}_i, \boldsymbol{x}_j)$$
(35)

Such that $\sum_i a_j y_j = 0$, s.t. $\alpha_i \ge 0$, $\forall i$

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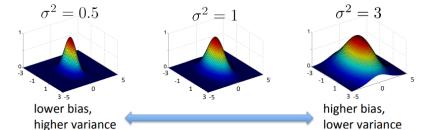
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The Gaussian Kernel

Also called Radial Basis Function (RBF) kernel

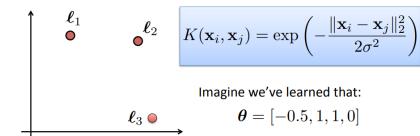
$$K(x_i, x_j) = \exp\left(-\frac{||x_i - x_j||_2^2}{2\sigma^2}\right)$$
 (36)

- Has value 1 when $x_i = x_i$
- Value falls off to 0 with increasing distance
- Note: Need to do feature scaling before using the Gaussian kernel



• Assume that we want to predict +1 or positive if:

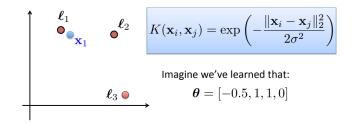
$$\theta_0 + \theta_1 K(\boldsymbol{x}, \boldsymbol{\ell}_1) + \theta_2 K(\boldsymbol{x}, \boldsymbol{\ell}_2) + \theta_3 K(\boldsymbol{x}, \boldsymbol{\ell}_3) \ge 0 \tag{37}$$



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• Assume that we want to predict +1 or positive if:

$$\theta_0 + \theta_1 K(\boldsymbol{x}, \boldsymbol{\ell}_1) + \theta_2 K(\boldsymbol{x}, \boldsymbol{\ell}_2) + \theta_3 K(\boldsymbol{x}, \boldsymbol{\ell}_3) \ge 0 \tag{38}$$



• for x_1 , we have $K(x_1, \ell_1) \approx 1$, other similarities ≈ 0

$$\theta_0 + \theta_1(1) + \theta_2(0) + \theta_3(0) = 0.5 \ge 0$$
 (39)

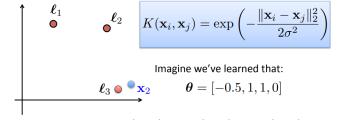
• so, predict +1 or positive



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• Assume that we want to predict +1 or positive if:

$$\theta_0 + \theta_1 K(\boldsymbol{x}, \boldsymbol{\ell}_1) + \theta_2 K(\boldsymbol{x}, \boldsymbol{\ell}_2) + \theta_3 K(\boldsymbol{x}, \boldsymbol{\ell}_3) \ge 0 \tag{40}$$



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• for x_2 , we have $K(x_2, \ell_3) \approx 1$, other similarities ≈ 0

$$\theta_0 + \theta_1(0) + \theta_2(0) + \theta_3(1) = -0.5 \le 0$$
 (41)

• so, predict -1 or negative

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• Assume that we want to predict +1 or positive if:

$$\theta_0 + \theta_1 K(\boldsymbol{x}, \boldsymbol{\ell}_1) + \theta_2 K(\boldsymbol{x}, \boldsymbol{\ell}_2) + \theta_3 K(\boldsymbol{x}, \boldsymbol{\ell}_3) \geq 0$$

$$\vdots$$

$$K(\mathbf{x}_i, \mathbf{x}_j) = \exp\left(-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|_2^2}{2\sigma^2}\right)$$

$$\vdots$$

$$\theta = [-0.5, 1, 1, 0]$$

$$\theta = [-0.5, 1, 1, 0]$$

(42)

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Here's the graph sketch of the decision boundary when projected into the 2D space

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Other Kernels

Sigmoid Kernel

$$K(\mathbf{x}_i, \mathbf{x}_j) = \tanh(\alpha \mathbf{x}_i^{\mathsf{T}} \mathbf{x}_j + c) \tag{43}$$

- Neural networks use sigmoid as an activation function
- SVM with a sigmoid kernel is equivalent to a 2-layer perceptron
- Cosine Similarity Kernel

$$K(x_i, x_j) = \frac{x_i^{\top} x_j}{||x_i|| ||x_j||}$$
(44)

- Popular choice for measuring the similarity of text documents
- L^2 norm projects vectors onto the unit sphere; their dot product is the cosine of the angle between the vectors

Other Kernels

Chi-squared Kernel

$$K(\mathbf{x}_i, \mathbf{x}_j) = \exp\left(-\gamma \sum_k \frac{(x_{ik} - x_{jk})^2}{x_{ik} + x_{jk}}\right)$$
(45)

- Widely used in computer vision applications
- Chi-squared measures the distance between probability distributions
- Data is issued to be non-negative, often with L^1 norm
- String kernels
- Tree kernels
- Graph kernels



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Conclusion

- The SVM finds the optimal linear separator
- The kernel trick makes SVMs learn non-linear decision surfaces
- Strengths of SVMs:
 - Good theoretical and empirical performance
 - Supports many types of kernels
- Weaknesses of SVMs:
 - "Slow" to train and predict for huge datasets (although relatively fast...)
 - The kernel needs to be wisely chosen and its parameters need to be tuned