

Homework 3

1. Create problems and solutions on the course training wiki: http://gragg.math.kth.se/sf2524/merge_group_pages2.php?name=97359. At least one problem and solution has to be in block 3. Further problems and solutions can be in any block of the course. This task is optional but can increase your bonus. Individual task (do work in groups). See how the work influences your bonus points under http://kth.instructure.com/courses/17791/pages/homework-slash-bonus-points-rules.

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- 2. FFT algorithm
 - a) Carry out FFT (by hand) on the vector.

$$b = \begin{bmatrix} 1 \\ 1 \\ 2 \\ 2 \end{bmatrix}$$

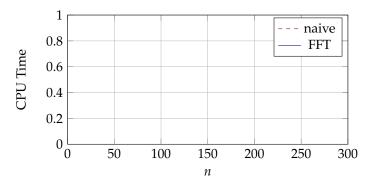
In a), you may want to keep an eye out for any structures that can simplify the computation. It will be needed in problem d).

b) Implement the recursive FFT algorithm (Algorithm 1 in block3.pdf or Algorithm 1.8.1 in Björck) and apply it to the vector

c) Make a CPU-time comparison between your FFT-implementation and the naive matrix vector multiplication consisting of forming the entire F_N -matrix and computing FN*b. (Creating the matrix should not seen as a part of the computation.) Provide a figure like below. Use sizes $nv=2.^(1:p)$ and increase p until you see what you expect. Use a random b-vector.

It is difficult to do good CPU-timing in MATLAB. Use the technique in: CANVAS \rightarrow SF2526 \rightarrow Pages \rightarrow View all pages \rightarrow CPU comparisons





d) Improve the FFT algorithm for vectors of the following form using what you may have observed in a):

$$b = \begin{bmatrix} y_1 \\ y_1 \\ y_2 \\ y_2 \\ \vdots \\ y_s \\ y_s \end{bmatrix}$$

where $y \in \mathbb{R}^s$ and $s = 2^{p-1}$. How much better is it in theory? Present one comparison simulation (or add another plot in figure in c).

3. Download the audio file from CANVAS course page

hw3_terrible_sound_with_hidden_message.ogg.

(Turn down the volume of your speaker before listening.) Use MAT-LAB commands audioread and sound to load and play the sound.

- (a) Use FFT and inverse FFT to remove (at least some) of the annoying sound, by setting some frequencies to zero. Hint: The noice frequencies are equidistant in the frequency (with distance 100 units). What is the hidden message?
- (b) With the naive DFT, how large problems can you solve on your computer (with say approx 30 min computation time)? Is it possible to solve the problem in this case?
- 4. Do "Homework 3 quiz: structured matrices" on CANVAS. This is mandatory and should be done individually (not in a group).
- 5. Download the files build_bisection_tree.m and smatrix_skeleton.m. You will use these to construct your own matrix vector product.
 - (a) In the first lines of code in smatrix_skeleton.m a matrix is created. Why is this a semiseparable matrix?

Numerics for data science

Homework 3 - SF2526



- (b) ** This will be added in an updated version of the PDF **
- (c) ** This will be added in an updated version of the PDF **