## R code to implement the power calculation method

```
# Source the R functions needed
source('FUNCTIONS.R')
# Design parameters for the illustrative example
I <- 96
         # number of clusters
n <- 40
           # number of participants per cluster per period
T <- 5
             # number of time periods
p0 <- 0.08 # prevalence under control
p1 <- 0.064 # prevalence under intervention
theta_star \leftarrow log(p1/(1-p1))-log(p0/(1-p0)) # log odds ratio
sig <- 0.05 # alpha significance level</pre>
rho <- 0.1 # inter-cluster correlation
# Power from equation 3 and 5
linear_no_time <- function(p0,p1,rho,n,T,I,sig){</pre>
  sigma_sq \leftarrow (p1*(1-p1)+p0*(1-p0))/2
  var <- 12*sigma_sq*(1-rho)*(1-rho+n*T*rho)/(n*I*T*(3*(1-rho)+2*n*rho*(T+1)))
  test_stat <- abs((p1-p0)/sqrt(var))</pre>
  power <- pnorm(test_stat-qnorm(1-sig/2))</pre>
  return(power)
}
linear_no_time(p0,p1,rho,n,T,I,sig)
## [1] 0.982436
# Power from equation 4 and 6
logistic_no_time <- function(p0,p1,theta_star,rho,n,T,I,sig){</pre>
  a \leftarrow sqrt(p0*(1-p0))
  b \leftarrow sqrt(p1*(1-p1))
  var < -(6*(1-rho)*(a^2+b^2)+2*n*rho*(T+1)*(a-b)^2)*(1-rho+n*T*rho)/
          (n*I*T*a^2*b^2*(3*(1-rho)+2*n*rho*(T+1)))
  test_stat <- abs(theta_star/sqrt(var))</pre>
  power <- pnorm(test_stat-qnorm(1-sig/2))</pre>
  return(power)
logistic_no_time(p0,p1,theta_star,rho,n,T,I,sig)
## [1] 0.9775285
# Power from equation 2 and 7
linear_time <- function(p0,p1,rho,n,T,I,sig){</pre>
  sigma_sq \leftarrow (p1*(1-p1)+p0*(1-p0))/2
   var <- 12*sigma_sq*(T-1)*(1-rho)*(1-rho+n*T*rho)/(n*I*T*(T-2)*(2*(1-rho)+n*rho*(T+1))) 
  test_stat <- abs((p1-p0)/sqrt(var))</pre>
  power <- pnorm(test_stat-qnorm(1-sig/2))</pre>
  return(power)
linear_time(p0,p1,rho,n,T,I,sig)
## [1] 0.7096853
# Power from equation 8 and 9
logistic_time <- function(beta,theta_star,R,n,T,I,sig){</pre>
  invR <- solve(R)</pre>
  trtSeq <- matrix(0,T-1,T)</pre>
```

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trtSeq[upper.tri(trtSeq)] <- 1</pre>
  Z_part <- kronecker(diag(T),rep(1,n))</pre>
  q < -I/(T-1)
  var <- var.logistic(I,T,q,beta,theta_star,trtSeq,n,invR,Z_part)</pre>
  test_stat <- abs(theta_star/sqrt(var))</pre>
  power <- pnorm(test_stat - qnorm(1-sig/2))</pre>
  return(power)
}
R_exch <- (1-rho)*diag(n*T) + rho*matrix(1,nrow=n*T,ncol=n*T) # exchangeable correlation matrix
beta <-c(log(p0/(1-p0))), # decrease in probability of an event only at step 1 (then maintained)
          rep(log(p0/(1-p0))-0.15,T-1))
logistic_time(beta,theta_star,R_exch,n,T,I,sig)
## [1] 0.6442509
# Power from equation 9 and 10
rho1 <- 0.1 # within-period correlation</pre>
rho2 <- 0.01 # inter-period correlation</pre>
R nest \leftarrow (1-rho1)*diag(n*T) +
           (rho1-rho2)* kronecker(diag(T), matrix(1, nrow=n, ncol=n)) +
          rho2*matrix(1,nrow=n*T,ncol=n*T) # nested exchangeable correlation matrix
logistic_time(beta,theta_star,R_nest,n,T,I,sig)
## [1] 0.2397403
# Power from equation 9 and 11
tau <- 0.1 # within-period correlation
rho <- 0.56 # decay parameter
times \leftarrow 1:T
varrho <- rho^abs(outer(times,times,"-"))</pre>
R_{exp} \leftarrow (1-tau)*diag(n*T) +
          kronecker(tau*varrho,matrix(1,nrow=n,ncol=n)) # exponential decay correlation matrix
logistic_time(beta,theta_star,R_exp,n,T,I,sig)
## [1] 0.264653
# Power from equation 9 and 12
logistic_trt_het_time <- function(beta,theta_star,rho1,rho2,rho3,n,T,I,sig){</pre>
  trtSeq <- matrix(0,T-1,T)</pre>
  trtSeq[upper.tri(trtSeq)] <- 1</pre>
  Z_part <- kronecker(diag(T),rep(1,n))</pre>
  q < -I/(T-1)
  var <- var.logistic.trt.het(I,T,q,beta,theta_star,trtSeq,n,rho1,rho2,rho3,Z_part)</pre>
  test_stat <- abs(theta_star/sqrt(var))</pre>
  power <- pnorm(test_stat - qnorm(1-sig/2))</pre>
  return(power)
rho1 <- 0.1 # inter-cluster correlation (control, control)
rho2 <- 0.02 # inter-cluster correlation (control, treatment)
rho3 <- 0.08 # inter-cluster correlation (treatment, treatment)
logistic_trt_het_time(beta,theta_star,rho1,rho2,rho3,n,T,I,sig)
## [1] 0.2484286
# Varying cluster sizes
n_{mod} \leftarrow c(62,63,64,65,65,66,67,68,
            35,36,37,38,39,40,41,42,43,44,45,46,47,rep(48,6),49,50,51,52,53,54,55,56,57,58,59,60,61,
            32,33,34,35,36,37,38,rep(35,10),rep(30,14),rep(40,14),
            14,15,16,17,18,19,20,21,22,23,24) # moderate cluster size variation
mean(n_mod)
```

## [1] 40

```
sd(n_mod)/mean(n_mod)
## [1] 0.3196215
n_{\text{lar}} \leftarrow c(70,74,76,92,134,172,213,302,
            35,36,37,38,38,39,39,40,40,41,42,43,44,45,46,47,rep(48,3),49,50,51,52,53,54,55,56,57,58,
            59,60,61,
            12,15,18,19,20,20,21,21,22,22,23,25,25,25,25,26,27,28,30,31,31,31,34,35,37,38,39,39,39,
            rep(35,2),rep(30,3),rep(40,3),45,
            1,2,2,2,3,3,3,4,4,4,5,6,7,8,10,10,10,11) # large cluster size variation
mean(n lar)
## [1] 40
sd(n lar)/mean(n lar)
## [1] 1.036403
# Design parameters
rho <- 0.1
q < -I/(T-1)
trtSeq <- matrix(0,T-1,T)</pre>
trtSeq[upper.tri(trtSeq)] <- 1</pre>
X.ij <- kronecker(trtSeq,rep(1,q))</pre>
# Power from equation 15 and 16
set.seed(3656)
M <- 1000 # Number of randomization sequences to be used
power <- matrix(NA,M,2)</pre>
colnames(power) <- c("moderate","large")</pre>
for (m in 1:M) {
  first <- sample(1:I,q)</pre>
  second <- sample((1:I)[-first],q)</pre>
  third <- sample((1:I)[-c(first, second)],q)
  fourth <- (1:I) [-c(first, second, third)]</pre>
  S.ij <- X.ij[c(first, second, third, fourth),]</pre>
                                                    # randomization sequence
  var <- var.logistic.vary(I,T,q,beta,theta_star,S.ij,n_mod,rho)</pre>
  test_stat <- abs(theta_star/sqrt(var))</pre>
  power[m,1] <- pnorm(test_stat - qnorm(1-sig/2))</pre>
  var <- var.logistic.vary(I,T,q,beta,theta_star,S.ij,n_lar,rho)</pre>
  test_stat <- abs(theta_star/sqrt(var))</pre>
  power[m,2] <- pnorm(test_stat - qnorm(1-sig/2))</pre>
colMeans(power) # mean power
## moderate
                  large
## 0.6433369 0.6402897
apply(power,2,min) # minimum power
## moderate
                  large
## 0.6342235 0.6178242
apply(power,2,max) # maximum power
## moderate
                  large
## 0.6479599 0.6489909
```