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2 **Automated surface feature selection using SALSA2D: Assessing**
3 **distribution of Elephant carcasses in Etosha National Park**

4 L.A.S Scott-Hayward^a, M.L. Mackenzie^a, C.G. Walker^b, G. Shatumbu^c, W. Kilian^c
5 and P. du Preez^d

6 ^aSchool of Mathematics and Statistics, University of St Andrews, KY16 9LZ, Fife, Scotland;

7 ^bDepartment of Engineering Science, University of Auckland, 70 Symonds Street, Auckland,

8 New Zealand; ^cEtosha Ecological Institute, PO Box 6, Okaukuejo via Outjo, Ministry of

9 Environment, Forestry and Tourism, Namibia; ^dAfrican Wildlife Conservation Trust, PO

10 box 97401, Windhoek, Namibia

11 ^aORCID: LSH (0000-0003-3402-533X), MLM (0000-0002-8505-6585)

12 **ARTICLE HISTORY**

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14 **Open Research Statement**

15 The data and code are provided as private-for-peer review but can be made pub-

16 lic if accepted for publication. The files can be found at the github site of the

17 first/corresponding author: <https://github.com/lindesaysh/Carcass-paper>.

18 Additionally, the data file will be made public and permanently archived in the St

19 Andrews PURE repository.

20 **KEYWORDS**

21 CReSS (Complex Region Spatial Smoother); Spatially Adaptive; SALSA; spline;

22 point process; GAM; regression

ABSTRACT

This paper describes the development of an automated knot selection method (selecting number and location of knots) for bivariate splines in a pure regression framework (SALSA2D). To demonstrate this approach we use carcass location data from Etosha National Park (ENP), Namibia to assess the spatial distribution of elephant deaths. Elephant mortality is an important component of understanding population dynamics, the overall increase or decline in populations and for disease monitoring.

The presence only carcass location data were modelled using a downweighted Poisson regression (equivalent to a point-process model) and using developed method, SALSA2D, for knot selection. The result was a more realistic local/clustered intensity surface compared with an existing model averaging approach.

Using the new algorithm, the carcass location data were modelled using additional environmental covariates (annual rainfall, distance to water and roads). The results showed high carcass intensity close to water holes ($<3\text{km}$) and roads ($<2\text{km}$) and in areas of the park with average rainfall ($\sim 450\text{mm}$ annually). Some high risk areas were identified particularly in the north east of the park and the risk of death does not always coincide with elephant distribution across the park. These findings are an important component in understanding population dynamics and drivers for population and park management. Particularly for controlling elephant numbers and/or mitigation of anthrax or other disease outbreaks.

45 Introduction

46 Spline based regression is a well established method for estimating relationships
47 when the functional form between an expected response and a set of covariates is
48 unknown and non-linear. Splines are restrictive enough to benefit from parametric
49 estimation and general enough to approximate a wide range of smooth functions.
50 Within the parametric estimation framework, there are two main approaches to es-
51 timating these functional forms, a penalised or un-penalised approach. In the for-
52 mer, a penalty term which includes a smoothing parameter is used to determine the
53 wiggleness of the spline and in the latter approach the appropriate wiggleness is de-
54 termined by judicious placement and number of knots. While penalised approaches
55 are covered extensively, for example in Wood [1] or Eilers and Marx [2], this paper
56 focuses on methods for judicious placement and number of knots, the un-penalised
57 approach.

58 Walker et al. [3] presented an algorithm for adaptively placing knots called SALSA
59 - Spatially Adaptive Local Smoothing Algorithm. It is an adaptive knot selection
60 approach, with the number and location of the knots being determined by the so-
61 lution process. The algorithm is not an all possible subsets approach but combines
62 a local-search strategy with a restricted forward/backward regression approach to
63 significantly reduce the number of models evaluated at each iteration. The paper
64 demonstrated SALSA for univariate splines and found it to be an “intuitive solution
65 that is naturally able to accommodate local changes smoothness”.

66 Scott-Hayward et al. [4] developed the CReSS (Complex Region Spatial Smoother)
67 approach to allow bivariate smooths to cope with complex topographies to respect
68 the natural boundaries encountered by animals, e.g. complex coastlines or lakes.
69 This approach does not choose the number and location of knots for a bivariate
70 spline but achieves spatially adaptive surfaces via a judicious weighting (model aver-
71 aging) of a variety of candidate surfaces. Each model uses a set of exponential basis
72 functions located at a fixed number of ‘space-filled’ knots [5] and fixed radius to de-
73 termine the influence of each basis. These models result in surfaces ranging from the
74 very simplistic (via small numbers of knots with basis functions with a relatively

75 global influence) to very complex (via large numbers of knots with basis functions
76 with a relatively localised influence).

77 This approach (CReSS with model averaging) has been shown to perform well
78 against other model-based alternatives developed for data sets with internal exclu-
79 sion zones (such as coastlines and island systems) and is finding use in a range of
80 ecological applications [6–8].

81 However, while this approach has been shown to produce reliable results in many
82 cases [4], this procedure can be complicated, in terms of model handling and difficult
83 to assess model fit and to provide confidence intervals. A paper by Dormann et al.
84 [9] highlights some of the limitations of a model averaging approach. Namely, the
85 authors show that estimating model weights introduces unknown and unaccounted
86 for uncertainty and that confidence intervals for model-averaged predictions rarely
87 achieve nominal coverage. They also state that model-averaging is most useful when
88 the predictive error of contributing model predictions is dominated by variance (as
89 opposed to bias), and if the covariance between models is low. We argue that ecolog-
90 ical data, including the carcass data seen here, is often highly variable with limited
91 covariates and thus could result in prediction errors dominated by variance. Addi-
92 tionally, given the CReSS with model averaging approach averages models with the
93 same covariates but different parameterisations, there is also likely to be high co-
94 variance between competing models, rendering the model averaging approach less
95 appropriate.

96 Further, when the spatial patterns are particularly unusual (e.g. stripe-like features
97 or local hotspots are genuinely present) we have found that a model-averaging ap-
98 proach can result in overly smooth surfaces which mask these unusual, but impor-
99 tant, patterns. This may result for a variety of reasons: under the original CReSS
100 approach the space-filled knots are fixed in position for a given knot number, and
101 the extent that each basis function is local (or global) is fixed (and the same) for all
102 knots in that candidate surface.

103 This paper uses the principals of SALSA (for univariate splines) and the CReSS ba-
104 sis to present a spatially adaptive local smoothing algorithm for bivariate splines

105 (SALSA2D). To demonstrate this approach we use carcass location data from
 106 Etosha National Park (ENP), Namibia to assess the spatial distribution of elephant
 107 deaths.

108 The African Savannah Elephant (*Loxodonta africana*) occurs across 37 African coun-
 109 tries with Southern Africa holding the largest number of elephants on the continent
 110 [10]. It is the largest living terrestrial mammal, social, intelligent, an ecosystem en-
 111 gineer, a species of great conservation concern, and has been studied extensively.
 112 However, continental African elephant populations are declining rapidly - so much
 113 so that in the 2021-1 IUCN Red List of Threatened species these elephants have
 114 been reclassified as Endangered [11]. Reasons for this decline include poaching, habi-
 115 tat fragmentation and loss, unsustainable bushmeat harvesting, conflict with hu-
 116 mans, and scarcity of food and water linked to frequent severe droughts or civil war
 117 [12, 13].

118 Elephant mortality is an important component of understanding the population dy-
 119 namics, the overall increase or decline in populations and for disease monitoring.

120 Poaching has been the major focus of elephant mortality studies [14–16] with other
 121 causes such as human-elephant conflicts, accidents and natural processes (e.g. dis-
 122 ease) less studied. With no natural predators, natural elephant mortality is often as
 123 a consequence of food scarcity and water stress during drought [17] or diseases such
 124 as Anthrax. Recently, Mukeka et al. [17] highlighted that despite the considerable
 125 inter-annual and spatial variation in elephant mortality in Kenya, the impact of this
 126 variation on population dynamics has not yet been widely assessed.

127 The Monitoring the Illegal Killing of Elephants (MIKE; [https://cites.org/eng/](https://cites.org/eng/prog/mike/index.php/portal)
 128 [prog/mike/index.php/portal](https://cites.org/eng/prog/mike/index.php/portal)) programme is an international collaboration that
 129 collects and monitors trends related to the illegal killing of elephants from across
 130 Africa and Asia [18]. The MIKE project also seeks to monitor the effectiveness of
 131 field conservation efforts and is part of the Convention on International Trade in
 132 Endangered Species of Wild Fauna and Flora (CITES) initiative. MIKE operates
 133 in over 80 sites, across 43 elephant range states across Africa and Asia and rigor-
 134 ous protocols have been developed as part of this initiative to collect, analyse and

135 build the capacity to better enforce the law and to reduce illegal elephant killings.
 136 The overall goal of MIKE is to provide information needed for elephant range states
 137 to make appropriate management and enforcement decisions, and to build institu-
 138 tional capacity within the range states for the long-term management of their ele-
 139 phant populations. In particular, they report PIKE (Proportion of Illegally Killed
 140 Elephants) for every range state.

141 In contrast to much of Africa, there has been little to no poaching of elephants in
 142 Etosha National Park (ENP) and the population of elephants in Namibia is actually
 143 increasing [19]. Despite the limited poaching activity in Namibia, the MIKE project
 144 has been active in ENP in Namibia for over a decade, and substantial resources
 145 are used to collect relevant abundance and mortality data by dedicated aerial sur-
 146 veys under strict survey protocols. As part of routine park activities, opportunistic
 147 data on carcass information is also recorded. Together these form the African ele-
 148 phant mortality database for ENP. To date these data have only been reported to
 149 the MIKE project and not analysed spatially.

150 Statistical modelling of these data is necessary since the park is very large ($\sim 23,000$
 151 km^2) and regardless of the survey regime, the observed counts will undoubtedly
 152 comprise a subset of a larger number of deaths. Reliable modelling results which
 153 accurately estimate the magnitude and location of elephant mortality in ENP are
 154 also not guaranteed and require the careful consideration of at least the following
 155 two points, 1) most wildlife, including elephant, rarely traverse a large salt pan:
 156 there is little vegetation to be found in the pan and the sometimes boggy terrain
 157 prevents travel for large animals such as elephant; 2) the spatial patterns of mortal-
 158 ity are likely to be localised and patchy: the abundance of elephant in the park is far
 159 from homogeneous and the reasons for death (natural or otherwise) are also likely to
 160 vary across the park. Failing to account for the possibly unusual spatial patterns in
 161 these data and/or assuming points across the pan are as closely linked as equidistant
 162 points without a physical barrier, can unwittingly lead to false conclusions about the
 163 magnitude and location of elephant deaths in the park.

164 The Complex Region Spatial Smoother (CReSS) is a regression spline based sta-

165 tistical modelling method equipped to address both aspects of these data [4]. Eu-
 166 clidean or geodesic ('around the salt pan') distances can be used to underpin the
 167 smoothed surface and the method is spatially adaptive enabling the targeting of sur-
 168 face flexibility to accommodate any particularly patchy trends and/or local surface
 169 features. While appropriate, the currently published CReSS method [4] undertakes
 170 the, crucially important, model selection process using a model-averaging of predic-
 171 tions approach which can be computationally intensive. We have also found after
 172 extensive use that this can mask unusually shaped spatial patterns when these are
 173 observed. In this paper, we propose using CReSS with an automated model selec-
 174 tion approach, as an alternative to model-averaging, which enables atypical spatial
 175 patterns to be deduced from the data - patterns which have implications for park
 176 management in this case, and produces one model which is easier to handle.
 177 In much of the grey literature the methods described here have been applied in a
 178 Poisson or Binomial generalised additive model framework (GAM). Here we have
 179 chosen to showcase the versatility of the SALSA algorithms and apply them to a
 180 presence only data set, where the primary interest are the spatial locations of pres-
 181 ence points (carcass locations).
 182 This paper begins by describing the original CReSS method in more detail and then
 183 introduces the SALSA2D algorithm. The first analysis presented focuses solely on
 184 spatial variation to compare the SALSA2D method to the original model averaging
 185 one. Lastly, using only the SALSA2D method for the spatial variation, environmen-
 186 tal covariates are also added to the model to assess how carcass intensity varies with
 187 location, annual rainfall, distance to water and distance to roads.

188 **Methodology**

189 *The Complex Region Spatial Smoother(CReSS)*

190 The CReSS approach fits pure spatial regression models to a set of coordinates \mathbf{x} of
 191 the form:

$$g(\mathbf{y}) = \eta = \beta_0 + s(\mathbf{x}) \quad (1)$$

where g is the link function and η the linear predictor. \mathbf{s} is a two dimensional surface approximated by a linear combination of exponential basis functions bE . The formula for this basis function at observation i and knot location k is:

$$bE_{ki} = \exp(-h_{ki}/r_k^2) \quad (2)$$

where r_k dictates the extent of the decay of this exponential function with distance between points, and thus the extent of its local nature. Notably h_{ki} indicates a geodesic or Euclidean distance (for some observation i and the k -th knot location). Parameter r_k takes values such that if r_k is small the model will have a set of relatively local basis functions and if r_k is large the model will have a set of relatively global basis functions. The exact values of r_k are dependent upon the range and units of the spatial covariates.

After the choice of distance metric, the CReSS with model averaging procedure fits multiple models with each model evaluated at one of a variety of parameter values for the number of knots (K) and the effective range parameter (r). According to Scott-Hayward et al. [4] model selection is achieved using AIC_c [20] weights and averaging those models with $\Delta AIC_c < 10$ to produce weighted predictions.

We have also extended the suite of CReSS basis functions that can be used for the two-dimensional smoothing. This is useful since SALSA2D is agnostic about the basis function used but relies instead on an objective fit criteria for execution.

As part of recent work, we have expanded the CReSS approach to include a Gaussian radial basis to the choice of basis functions available for selection. The two bases have different shapes, with the exponential being more peaked at the centre.

These choices allow for more nuanced model fitting, akin to link function or distance

metric choice. The Gaussian radial basis, bG , is specified as:

$$bG_{ki} = \exp^{-(h_{ki}r_k)^2} \quad (3)$$

where r_k and h_{ki} are as defined for the exponential (Equation 2) except that for the Gaussian basis, a small value for r_k returns a relatively global basis and a large r_k value returns a relatively local basis.

The new basis and SALSA2D algorithm are all implemented inside the MRSea R package [21, 22] for easy use by practitioners.

Spatially Adaptive Local Smoothing Algorithm for at least two dimensions (SALSA2D)

SALSA2D uses the same model framework as for model averaging (see Equation 1) but where the knot locations, k , are chosen using an iterative three step procedure. The algorithm works in (at least) two dimensions and begins with space-filled knots to facilitate spatial coverage and then adaptively moves, adds and drops knots into, or from, locations in line with poor model fit (evidenced by large residuals) and an objective fit criteria. At each stage, the global/local extent of each basis function via the r_k value employed can also be revised as part of the search for a more appropriate surface. So, unlike the model averaging approach, SALSA2D returns one model with specifically selected k and r_k enabling standard methods for assessment of fit and uncertainty estimation.

The algorithm that drives SALSA2D has an iterative 3-step structure. After an initialisation step, there are three repeated steps: the first is a simplification step to reduce the number of estimated parameters which is achieved by allowing for the removal of columns from the design matrix (reduction in knot number). The second and third steps (exchange and improve) are designed to efficiently search the model space (all possible number and locations of knots). The exchange step allows for the possibility of moving away from a local optimum or addition of columns to

239 the design matrix (a new knot) and the improvement step attempts to make local
 240 improvements in knot location. The outcome of each of these steps is determined by
 241 an objective fit criterion and repeated until no improvements are made (or an iteration limit is reached). The structure of the algorithm is given in the pseudo code in
 242 Box 1 and the next sections describe the steps in detail.

SALSA2D:

Given an n -dimensional set K_l of possible knot locations over the region of interest.

Initialise

Initialise knots, K_s within the points of K_l

Check for convergence

244

Repeat

Repeat Simplification step *while* ($K > K_{\min}$ and fit measure improves)

Repeat Exchange step *while* ($K < K_{\max}$ and fit measure improves)

Repeat Improvement step *while* (fit measure improves)

While (an improvement in fit measure is made by one of the above steps)

245 Box 1: Pseudo-code outlining the structure of SALSA2D [adapted from Figure 1, 3],
 where K is the number of knots used for fitting.

246 *Initialisation*

247 Each observed location, i , is considered a possible location for a knot position. To
 248 avoid estimation issues, only unique knot locations are considered giving K_l legal
 249 knot locations. The user specifies a starting number of knots, K_s , where $K_s < K_l$,
 250 and these are selected from K_l using a space-filling algorithm [5]. This method provides
 251 good coverage across the spatial region as a starting position for SALSA2D.

252 Additionally, the minimum number of knots, K_{\min} ($2 \leq K_{\min} < K_s$) and maximum
 253 number K_{\max} ($K_s < K_{\max} \leq K_l$) are specified.

254 To evaluate the basis function, the r_k -value for each basis must also be chosen. The
 255 SALSA2D algorithm selects from R possible options for r_k which range from a very
 256 local basis to a globally acting basis. The middle option which is neither very local

257 or very global, is chosen to initialise the first model.

258 To ensure that the initial model fit has converged, there is a drop step compo-
259 nent that is activated if the variance of the initialised first model exceeds that of
260 the simpler input model (the variance should not increase with additional parame-
261 ters/flexibility in the model). If this occurs, knot locations with the largest contribu-
262 tions to the variance are removed one by one until the overall variance of the more
263 complex model is lower than the input model.

264 *The simplify step*

265 Using the fit criteria specified, the simplify step compares the current model with all
266 models obtained by removing an existing knot (as long as this is at least K_{\min}). At
267 each iteration, the model with the best fitness measure is retained and the process
268 repeated until there is no further improvement in the fitness measure. This step can
269 be carried out by fixing r_k or by choosing r_k for each basis as each knot is dropped
270 for comparison.

271 *The exchange step*

272 The exchange step increases the extent of the search of model space by enabling a
273 move away from a local minima (of the fit criterion). It uses the maximum Pearson
274 residual from the current fitted model to identify a possible candidate location for
275 a new knot (although in theory other types of residuals could be chosen and we use
276 an alternative metric for the point process models in the next sections). The algo-
277 rithm then compares the objective fit criteria for these models that result when each
278 of the existing knots in the current model is moved to this new location, and also
279 the fit criteria from the model that results when an additional knot at this location
280 is added to the current model (if this does not exceed K_{\max}). The model with the
281 best fitness measure is retained in this step if it has a better fitness measure than
282 the current model. Evaluation of each of these models can be very quick to return
283 but this process is naturally more computationally expensive, if r_k is also chosen
284 for each basis function for each candidate model. In practice, the algorithm uses the

285 knot locations of the five largest residuals as candidates for an exchange or move.

286 *The improve step*

287 The improve steps allows a more nuanced search of the local minima by allowing
288 small adjustments to the location of each knot. Using the fit criteria specified, the
289 improve step compares the current model with all models obtained by moving an ex-
290 isting knot to one of its five nearest neighbours (determined by the distance metric
291 employed: geodesic or Euclidean). At each iteration, the model with the best fitness
292 measure is retained. As with the exchange step, alternative choices for the r_k param-
293 eter may be considered when fitting each new model and this process is likely to be
294 swift at this stage.

295 *Determining r_k*

296 This routine considers incrementing or decrementing r_k values in the sequence of
297 R possible values, where the sequence is selected using the method from 4. It can
298 be evaluated either once at the end of the exchange, improve and simplify steps or
299 as part of every decision taken during these steps. The process is done by consid-
300 ering each of the radial basis columns in turn, and incrementing or decrementing
301 the r_k values in the index until there is no improvement in the fitness measure. At
302 each step the r_k -values for the other basis columns are maintained at the current
303 solution. The best of these models is selected as the new current model, and the
304 process iterates until no improvement is made. This process can have a large com-
305 putational overhead and may significantly prolong the procedure but constitutes a
306 broader search of the model space.

307 This algorithm is implemented in the MRSea package which can be found at [http:](http://lindesaysh.github.io/MRSea/)
308 [//lindesaysh.github.io/MRSea/](http://lindesaysh.github.io/MRSea/) [21].

309 **Methods comparison**

310 This section compares the performance of the CReSS with model-averaging ap-
311 proach to CReSS with SALSA2D for model selection. The methods are compared
312 numerically using log-likelihood, while the practical consequences of using each are
313 assessed visually and contextualised using surface features in Etosha National Park,
314 Namibia.

315 ***Data specification***

316 To appreciate the numerical and practical benefits of this methodological develop-
317 ment, the MIKE data was used for the method comparison and for the subsequent
318 analysis in full [18]. These data consists of 320 carcass locations observed between
319 February 2000 and March 2017 in Etosha National Park (ENP). The observed fa-
320 talities are recorded as being due to: anthrax, natural (age-related) causes, poaching
321 and unknown. While a substantial proportion of the carcasses are recorded as be-
322 ing for ‘unknown’ reasons (54%) the largest known cause of death is from Anthrax
323 (27.8%; 12.5% confirmed cases and 15% suspected). Less than 1% of the carcasses
324 were confirmed as poached. All reported carcasses were used in the analysis regard-
325 less of type. Disregarding 2017 as it was only a partial year, 2006, 2013 and 2014
326 had the fewest recorded carcasses (7-8), whilst 2002, 2003, 2005 and 2011 had the
327 highest recorded (27-28). As there were a relatively small number of observations
328 per year, no guarantee the deaths occurred in the year of detection and no obvious
329 changes in the spatial pattern of observations, the data were pooled across years.
330 The longitude and latitude coordinates were converted to Universal Transverse Mer-
331 cator (UTM) zone 33S and the study region was extended beyond the ENP bound-
332 ary by 20 km to allow for the inclusion of carcasses just outside the park. Addition-
333 ally, the large salt pan was reduced in size by 2 km to allow inclusion of carcasses
334 found near the edge of the pan. The data show that carcasses generally seem to oc-
335 cur near roads (or, at least, are more commonly observed near roads) and water-
336 holes (Figure 1). It is possible that these patterns are due to opportunistic reporting

337 of carcasses as a result of park vehicles moving along the roads, however the data
 338 were from both opportunistic and dedicated surveys, which are carried out with-
 339 out reference to roads. Furthermore, collared elephant in ENP have been shown to
 340 utilise roads/tracks and fire breaks extensively and are known to frequent waterholes
 341 [23, 24]. Deaths as a result of anthrax appear to be particularly well correlated with
 342 waterholes (Figure 1).

343 [Figure 1 about here.]

344 In this data set, the link back to the original survey effort (where surveys were un-
 345 dertaken) is not available so we are left with only the carcass locations and no ab-
 346 sence locations. Warton and Shepherd [25] showed the link between logistic regres-
 347 sion and an inhomogeneous Poisson point process model (PPM) and here we use
 348 both this link and the downweighted Poisson regression method [26] to fit a Pois-
 349 son PPM using a pure regression GAM framework. In this case, the intensity is the
 350 number of presence records (carcass sightings) per unit area and is modelled as a
 351 function of covariates measured throughout the study region. It is a relative measure
 352 and gives the expected abundance of carcass sightings for a given area.

353 Pseudo-absences in the regression setting play the same role as quadrature points
 354 in point process modelling and we used the point process framework to choose the
 355 number and location of these points. The pseudo-absence points were selected as a
 356 regular grid and the number based on convergence of the likelihood [26].

357 Lastly, to determine areas of poor fit, the exchange step requires the calculation of
 358 residuals. This was achieved by creating a neighbourhood around each knot location
 359 (k) and comparing the observed number of points with the sum of the estimated
 360 intensities in the same area. For more details, see Section 1 of the Appendix S1.

361 *Model specification*

362 To compare the performance of SALSA2D with model averaging as a model selec-
 363 tion approach, models with a two dimensional smoother-based term for geographic
 364 locations were fitted to the MIKE data. The comparison involved either the pub-

lished CReSS method which employs model averaging [4] or model selection using
SALSA2D to determine knot number and location. Here we model the the loca-
tions of the carcasses jointly with the pseudo-absences by maximising the following
weighted Poisson log-pseudolikelihood [27]:

$$l(\beta; \mathbf{X}) = \sum_{i=1}^N w_i (y_i \log(\lambda(\mathbf{X}_i)) - \lambda(\mathbf{X}_i)) \quad (4)$$

where $\lambda(\mathbf{X}_i)$ is the intensity at location i , \mathbf{X}_i represents the design matrix at lo-
cation i , N is the total number of points (presence and pseudo-absence), $\mathbf{w} =$
 $\{w_1, \dots, w_N\}$ are quadrature weights.

$$y_i = \begin{cases} \frac{1}{w_i} & \text{if } i \text{ is a presence location} \\ 0 & \text{if } i \text{ is a pseudo-absence location} \end{cases}$$

The log-pseudolikelihood in Equation 4 [27] is a re-expression of the Poisson PPM
log-likelihood [28], which means that models can be fitted using standard GLM soft-
ware. Here we model the expected number of carcasses per square kilometre and
so the weights for the pseudo-absence points are specified as the area of the study
region, 37,872 km² (ENP plus the 20 km buffer) divided by the number of pseudo-
absences. The weights for presence points are set to some small value (10⁻⁶).
Likelihood convergence was used to determine the the number of pseudo-absences
which was estimated to be 9644 (a grid spacing of 2 km). For more details see Sec-
tion 2 of Appendix S1.
For this method comparison section, we model the intensity as a function of coordi-
nates, \mathbf{x} , only.

$$\log(\lambda(\mathbf{X}_i)) = \eta_i = \beta_0 + s(\mathbf{x}) = \mathbf{X}_i^T \boldsymbol{\beta} \quad (5)$$

where η_i is the linear predictor, consisting of the intercept, β_0 , and a smooth function of coordinates, $s(\mathbf{x})$. The smooth function is either the exponential or Gaussian basis function.

For both the model averaging and SALSA2D methods, the following specifications were used to return the columns of the design matrix \mathbf{X} in Equation 5:

- Two basis options: Exponential (bE_{ki} ; Equation 2) or Gaussian (bG_{ki} ; Equation 3)
- Two distance measures (Euclidean or geodesic) to calculate h in the basis equations; the geodesic distances are calculated using Floyds algorithm [29] and for more details see [4]. In this study, geodesic distances are “around the salt pan” distances.
- 12 choices of fixed knot number (for the model-averaging approach) and 12 choices of starting knot numbers, K_s for the SALSA2D approach. In each case, the fixed/starting knot set was: [5, 10, 15, ..., 55, 60]. A total of 285 legal knot positions (K_l) were considered. These consisted of all non-duplicated carcass locations (n=245) and 50 space-filled pseudo-absence locations ($\sim 20\%$ of all K_l).
- 10 choices of r_k (also specified as part of Equations 2 and 3)

Additionally, for SALSA2D, K_{\min} and K_{\max} were set to 2 and 100 respectively, for all model specifications.

Model comparison

In keeping with Scott-Hayward et al. [21], the model-averaging CReSS method was governed by AIC_c weights which were used to choose which models to average ($\Delta AIC_c \leq 10$) and their relative contribution to the overall averaged model. In keeping with Walker et al. [3], the BIC was used to govern SALSA2D model selection regarding the choice of knot number and their locations across the range of combinations of basis type, distance metric, starting knot number and r_k choices [30]. In all cases, the log-likelihood score (Equation 4) was calculated for each model

411 to enable comparison between model selection strategies.

412 **Results**

413 *Numerical comparison*

414 The log-likelihood scores returned for the model averaging method were fairly close
415 (maximum difference 14 points) regardless of the basis function and distance metric
416 used in each model (Table 1, Method: ‘Model averaging’). The geodesic-exponential
417 combination scored the best (largest log-likelihood) of the 4 combinations trialled.
418 Interestingly, this combination chose 11 models with which to average over to obtain
419 this solution, compared with some options that chose far fewer models to use as part
420 of the average calculation. In general, geodesic distances were preferred to Euclidean
421 regardless of basis.

422 [Table 1 about here.]

423 The log-likelihood scores for the SALSA2D based selection are shown for the model
424 with the highest log-likelihood for each of the basis/distance metric combinations
425 (Table 1, Method: SALSA2D). Across the four combinations, the scores were less
426 homogeneous than for the model averaging results and the exponential-Euclidean
427 SALSA2D model (using 41 knots) was the best of all trialled here. In contrast to the
428 averaging approach, there was a preference for the exponential basis with the dis-
429 tance metric secondary. In reality, the user may prefer to select the best model using
430 BIC (as was used for k/r selection). In this case, the order of the four parameteri-
431 sations was the same (exponential-Euclidean the best and Gaussian-Euclidean the
432 worst) and the best model using BIC was the same as in Table 1 when log-likelihood
433 was used (see Section 3 of Appendix S1 for an expanded version of Table 1).
434 Using the “best” SALSA2D models only, for all but one combination of basis type
435 and distance metric used, all SALSA2D models produced better scores than the
436 model averaging method – sometimes reducing the log-likelihood score by as much

437 as 10%. However, if SALSA2D initialises with too few knots, the algorithm may get
 438 stuck in local minima. So long as a large enough number of starting knot locations
 439 was selected ($\sim \geq 40$), SALSA2D-based selection resulted in superior scores over
 440 the model-averaging alternative (Figure 2). This demonstrates that the SALSA2D
 441 model selection method can return improved results and at worst, SALSA2D results
 442 were almost indistinguishable from the best model averaging-based result.

443 [Figure 2 about here.]

444 *Visual comparison*

445 Results for the model-averaging based model (Figure 3a) signalled that the inten-
 446 sity of carcasses was highest in the north-east of the park (where most the observed
 447 deaths occurred) and along the southern edge of the large salt pan, which is consis-
 448 tent with the observed data. The carcass intensity is very low near the south-west
 449 and south-eastern borders of ENP.

450 Whilst the model averaging results show a smooth intensity surface, the SALSA2D
 451 method produces a more clustered intensity surface (Figure 3b). The surface shows
 452 more local effects, particularly the centre west and below the salt pan and the high-
 453 est intensity at these spots was nearly three times that of the model-averaging re-
 454 sult. These effects, match well with the carcass location data and frequently occur at
 455 the confluence of several roads and some waterholes.

456 [Figure 3 about here.]

457 Figure 4 shows the selected knot locations and equivalent r parameter from the 11
 458 averaged models (Figure 4a) and the one best SALSA2D model (Figure 4b). The
 459 averaged knot locations are more difficult to represent but it can be seen that there
 460 are multiple r values (ranging from global to very local) across the same locations
 461 and occasionally a location where the sign of the coefficient changes between mod-
 462 els. The SALSA2D result is more nuanced with very few knot locations selected to
 463 the west of the park. For the 41 selected locations, a variety of r 's were chosen. It is
 464 interesting that the SALSA2D approach found the Euclidean distance metric to be

best and it is possible that the more local knots chosen under this method negate
the need for the geodesic distances by limiting the possible leakage across the pan.

[Figure 4 about here.]

468 **Application: Analysis of Elephant mortality in Etosha National Park**

469 Model

470 *Data available*

471 The intensity of elephant carcasses, based on the observed carcass locations and
472 pseudo-absences, was modelled using four candidate covariate terms: distance from
473 the nearest road, distance from the nearest water point, mean annual rainfall and a
474 spatial term based on spatial coordinates (in km, UTM zone 33S).

475 The distance from nearest road and nearest waterhole metrics were calculated us-
476 ing shape files supplied by the Ministry of Environment, Forestry and Tourism
477 (Namibia). These metrics were considered as candidates in the model to reflect pos-
478 sibly differential mortality rates near roads and waterholes, regardless of their spa-
479 tial location in the park.

480 The mean annual rainfall was based on rainfall data collected from 168 rain gauges
481 distributed across Etosha National Park which are visited annually, when possible.
482 Annual rainfall was not available for every gauge for every year, due to logistical dif-
483 ficulties reaching remote areas in some years, and so this metric was averaged across
484 years for each gauge before interpolation to indicate areas in ENP with persistently
485 high or low rainfall. The interpolation was achieved using a high dimensional pe-
486 nalisised spline ($df = 150$) to allow for interpolation to the carcass data locations and
487 to the pseudo-absence grid. Details on the rainfall interpolation can be found in Sec-
488 tion 4 of Appendix S1.

489 The proximity to waterholes was included as a candidate since elephant frequent wa-
490 ter holes throughout the year, particularly in the dry season; roughly May to Octo-
491 ber [23] and have been shown to have increased habitat use with proximity to water.
492 [31].

493 While natural deaths might occur in line with their distributional patterns it is
494 thought Anthrax-related deaths may be related to the use of water holes [32]. The
495 relationship with waterholes was found to be very stepped and so this variable was

496 converted to a 2 level factor; $< 3\text{km}$ and $\geq 3\text{km}$ (cutoffs of 1-5km were trialled and
 497 assessed using BIC).

498 The reasons for including proximity to roads as a candidate might seem less obvious,
 499 but the attraction or repulsion to roads by elephants might also be evident in their
 500 mortality patterns, and the model comparison work demonstrated that some roads
 501 are important (Figure 3b). This could be due to elephant preference to be found
 502 near roads, which is possible owing to their extensive use of roads/tracks for travel
 503 [23], but can only be confirmed by a dedicated analysis of survey data or that the
 504 detection of carcasses is higher near roads (e.g. easier to observe).

505 The spatial term was considered for inclusion in this model to represent the spatial
 506 patterns in mortality that are not adequately explained by proximity to roads, water
 507 holes or annual mean rainfall. The role of this term in this model is crucial in this
 508 case - correctly identifying systematic spatial patterns in mortality might provide in-
 509 sights about other park features not currently considered to be related to mortality
 510 and overlooking these features prevents the mitigation of future elephant mortalities,
 511 particularly those related to poaching.

512 *Model specification*

513 We are interested in modelling the intensity of elephant carcass locations as a func-
 514 tion of distance to water, roads, mean annual rainfall and as a spatially adaptive
 515 smooth function of spatial coordinates. The model specification was:

$$\begin{aligned}\log(\lambda(\mathbf{X}_i)) &= \eta_i \\ &= \beta_0 + \text{distWater}_i + s_1(\text{rainfall}_i) \\ &\quad + s_2(\text{distRoads}_i) + s_3(\mathbf{x}) \\ &= \mathbf{X}_i^T \boldsymbol{\beta}\end{aligned}$$

516 In this case, $\lambda(\mathbf{X}_i)$ is the intensity at location i and \mathbf{X}_i represents the coordinates
 517 and environmental covariates. s_1 and s_2 represent one-dimensional basis functions,

518 while $s_3(\mathbf{x})$ represents a two-dimensional exponential basis function for the spatial
 519 coordinates. β is a vector of model parameters associated with all columns of the
 520 design matrix, \mathbf{X} . The columns of \mathbf{X} comprise the intercept (1), water $\geq 3\text{km}$ (0,1),
 521 B -spline bases for rainfall and roads and the exponential radial basis for the spatial
 522 term.
 523 Specifically, quadratic B -splines with SALSA based knot selection [3] were used
 524 to implement the one dimensional smooth terms for rainfall and roads. The two-
 525 dimensional spline basis function was determined using Equation 2 (exponential ba-
 526 sis) and based on Euclidean distances. Knot number, their locations and r_k values
 527 were chosen using the SALSA2D algorithm. The starting parameters were based on
 528 the best result from the simulation study; $k_s = 41$, $k_{\min} = 2$ and $k_{\max} = 100$. The
 529 BIC was used to govern model selection in all cases.

530 ***Results***

531 The results show that carcass intensity is highest near to water holes and roads
 532 (Figures 5 & 6) and locations where the annual rainfall is approximately 450mm
 533 (Figure 7). Specifically, intensity decreases steeply with the distance from road until
 534 approximately 1km when the relationship subsides.

535 [Figure 5 about here.]

536 [Figure 6 about here.]

537 [Figure 7 about here.]

538 The addition of distance from roads and mean annual rainfall to the spatial term,
 539 improved model results when compared with model results based on a SALSA2D-
 540 based spatial term alone (Models 2 and 3 Table 2); the BIC scores substantially im-
 541 proved from 2980 to 2848.

542 The spatial term also contributed positively to the model, despite the extra parame-
 543 ters incurred (Table 2); the BIC score decreased from 3084 for the univariate model
 544 (Model 1) to 2848 when the spatial term was included (Model 2). The practical con-
 545 sequences of its inclusion was clearly evidenced by tempering the ‘global’ effect of

546 roads and water which was implicit in the model that included the additional vari-
 547 ables (Figure 8a). In some cases the road and water effects diminished altogether
 548 where carcasses were not seen in the data. Crucially, this spatial term also better
 549 accommodates carcass locations which are not explained by only their proximity to
 550 water, distance to roads or average annual rainfall. Figure 9 shows that in Model 1,
 551 the water hole relationship dominates with a peak of intensity at each one. When
 552 the spatial term is added, the waterhole peak is suppressed at a number of water-
 553 holes and even increased at others. The peak in intensity is shifted to the north
 554 which is in keeping with the high number of carcasses observed there. The knot lo-
 555 cations are similar to Model 3 but with fewer in the west and a higher proportion
 556 of smaller r (Figure 9b). Overall, the modelling shows that most, but not all, wa-
 557 terholes and some roads have high carcass intensity. Figure 8b shows the top 5%
 558 highest carcass intensity areas which form the highest risk areas in the park.

559 [Table 2 about here.]

560 [Figure 8 about here.]

561 [Figure 9 about here.]

562 Discussion

563 Using SALSA2D for model selection provided better results and the ability to have
564 a more realistic local/clustered intensity surface compared with the existing model
565 averaging approach. There are clear numerical and practical benefits to SALSA2D-
566 based model selection compared with a model averaging approach in this case and
567 while the benefits of doing so might be less stark in cases where spatial patterns are
568 more smooth, it needs to be possible to identify clusters and irregular patterns, such
569 as those observed here, when they exist.

570 Simply including proximity to water and roads in the model as part of this
571 analysis did not reveal genuine patterns in all areas of the park, since not all
572 roads/waterholes have been associated with carcasses. The addition of the spatial
573 term with spatially adaptive knot selection was able to suppress/enhance the global
574 relationships with the environmental covariates in particular areas. This resulted in
575 the identification of some critical areas of the park which is important for effective
576 park management, both in terms of disease outbreak, which after ‘unknown’ was the
577 largest category, and poaching, which although small in this data set ($<1\%$ of car-
578 casses), is increasing in the park.

579 It is impossible to patrol such a large area at random and the areas of the park
580 identified here (particularly those accessed by a subset of roads/waterholes) appear
581 to require more monitoring efforts than others. Elephants are highly mobile and so
582 early detection of carcasses, in particular anthrax related deaths, are important to
583 identify spread of disease across the park [33]. The area of high intensity of carcasses
584 to the south of the main pan matches well to the area of high anthrax risk identi-
585 fied by Dougherty et al. [34]. This is also the area where the majority of anthrax
586 or suspected anthrax cases were found in our database. Specifically, we show here
587 that within this anthrax risk area the highest intensity of carcasses is near the wa-
588 terholes.

589 In the critical high carcass intensity area identified in the north-east of the park, the
590 cause of death is less clear as the majority of carcasses were of unknown cause. How-
591 ever, it is interesting to note that the water sources in Etosha are a mix of boreholes

592 and springs but the north east corner is mostly springs. It is possible that in this
 593 region, there is higher water stress during drought which plays a role in mortality.
 594 Whilst the density of elephant across the park is shown to be fairly constant [19], we
 595 have found that the density of carcasses is not. Mortality is one of the key compo-
 596 nents in population dynamics models and the effects of spatial and temporal hetero-
 597 geneity must be accounted for to have accurate predictive models for use in manage-
 598 ment and conservation [35].
 599 Therefore it is important to understand the changes in the spatial distribution of
 600 mortality across the park to have a better understanding of the population dynamics
 601 and drivers for population management. For example, it is well known that surface
 602 water availability drives the distribution and abundance of elephants and that arti-
 603 ficial manipulation of water availability is one of the tools available for the manage-
 604 ment of elephant populations [24]. Closing waterholes is an option for managers to
 605 control elephant numbers should the numbers in Etosha continue to rise. One might
 606 base this decision on a number of factors including knowledge of which waterholes
 607 have a high density but low mortality.
 608 If the deaths are natural and, for instance, disease-related (e.g. anthrax) then this
 609 provides valuable information about the prevalence and locale of disease in the park.
 610 Endemic anthrax occurs in Etosha annually [36] and plays an important role in ele-
 611 phant population regulation/limitation. The monitoring of the prevalence of anthrax
 612 in elephant is important, because it advances our knowledge of a top down factor
 613 limiting a mega-herbivore.
 614 Even though the poaching of elephants in ENP is low (20 deaths reported to MIKE
 615 in 2018 and none poached), the general trend in more recent years is increasing
 616 (*pers. comm.* Etosha Ecological Institute). As the number of poached elephants in-
 617 creases it is very useful knowledge to have a baseline distribution of natural deaths.
 618 It is also very important in light of the mass death events seen in Botswana in 2020
 619 and 2021 [37]. Having a sense of “normal” places of natural death may provide in-
 620 sights should such events ever occur in Etosha.
 621 Critchlow et al. [38] developed a method for improving the efficiency of ranger pa-

622 trols using ranger collected monitoring data. Ranger patrols are not just important
623 for law enforcement but also the conservation of key species. With limited resource
624 available for patrols, the key is to ensure that the patrol effort is efficient with re-
625 spect to the activity one wishes to combat. The starting point for the method pre-
626 sented by Critchlow et al. [38] is a least one geographical map of illegal activity oc-
627 currence. However, the activity does not need to be an illegal one and in this case
628 the activity of interest could be risk of disease outbreak. Along with a map of exist-
629 ing ranger effort, the carcass intensity maps presented here could be used to assess
630 and improve the existing ranger effort in the park without the need for increased
631 resources.

632 Furthermore, should poaching increase in Etosha, then the methods presented here
633 can provide necessary information about the prevalence, locale and patterns of these
634 deaths. Additionally, should poaching occur in regions not common to find natu-
635 ral deaths, then increased/targeted mitigation measures can be efficiently actioned.
636 Practically, understanding both the magnitude and spatial patterns of elephant
637 deaths in ENP may assist in adapting patrol efforts in and around the park to track
638 the anthrax disease and/or combat any poaching activities.

639 This extended CReSS approach using SALSA2D model selection presented in this
640 paper is of immediate and practical value to a wide range of users of statistical mod-
641 elling methods. SALSA2D is implemented inside the MRSea R package and it can
642 automatically select knots based on two user-defined types of two-dimensional spline
643 bases (Gaussian and exponential) and distance calculation (Euclidean or geodesic)
644 based on a range of objective fitness criteria, chosen by the user. Notably, exclusion
645 zones and non-Euclidean distances can be included to model more complex spatial
646 regions [as seen in 4, 21] and adaptations have been made to allow for the fitting of
647 Poisson PPMs using the downweighted Poisson regression method. By using pres-
648 ence only data in this paper, as opposed to the more traditional Binomial or Poisson
649 GAMs, we have demonstrated the flexibility of this approach for a wide variety of
650 settings.

651 **Supplementary Material**

652 See Appendix S1 for information on residual calculation, pseudo-absence selection,
653 expanded results of the methods comparison and details of rainfall interpolation.

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656 with PPM queries and reading a draft of the paper.

657 ***Notes on contributors***

- 658 • LSH, MLM and CGW contributed to method development, analysis and pa-
659 per writing
- 660 • GS, WK and PdP contributed to data collection and local information

661 ***Conflict of Interest***

662 There are no competing interests.

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771 List of Tables

772	1	Table showing the results of the model averaging and SALSA2D	
773		methods of model selection for a given basis type and distance met-	
774		ric used. The ‘No. Models’ indicates the number of models chosen to	
775		carry out the model averaging in each case, and the ‘No. Knots’ indi-	
776		cates the number of knots chosen for each model using the SALSA2D	
777		selection method. The star indicates the model with the largest log-	
778		likelihood (LL) score, and thus the chosen model based on the LL in	
779		each case.	32
780	2	Table showing the results for the model based on one dimensional	
781		smoother-based relationships only (model 1) and the model with both	
782		one and two dimensional smoothers (model 2). For reference, model 3	
783		is the model with only a two dimensional smooth (see Table 1).	33

Table 1.: Table showing the results of the model averaging and SALSA2D methods of model selection for a given basis type and distance metric used. The ‘No. Models’ indicates the number of models chosen to carry out the model averaging in each case, and the ‘No. Knots’ indicates the number of knots chosen for each model using the SALSA2D selection method. The star indicates the model with the largest log-likelihood (LL) score, and thus the chosen model based on the LL in each case.

Method	Basis	Distance Measure	No. Models	No. Knots	Log-Likelihood
MA	Exponential*	Geodesic	11	-	-1432.0
	Gaussian	Geodesic	2	-	-1441.5
	Exponential	Euclidean	1	-	-1443.4
	Gaussian	Euclidean	8	-	-1446.3
SALSA2D	Exponential	Geodesic	-	32	-1369.7
	Gaussian	Geodesic	-	32	-1408.3
	Exponential*	Euclidean	-	41	-1301.6
	Gaussian	Euclidean	-	47	-1541.6

Table 2.: Table showing the results for the model based on one dimensional smoother-based relationships only (model 1) and the model with both one and two dimensional smoothers (model 2). For reference, model 3 is the model with only a two dimensional smooth (see Table 1).

Model	Term	df	χ^2 p -value	Log-Likelihood	BIC
1	s(rainfall)	3	$p < 0.0001$	-1505.4	3084.4
	s(distRoads)	3	$p < 0.0001$		
	Near water	1	$p < 0.0001$		
2	s(rainfall)	3	$p < 0.0001$	-1221.3	2848.0
	s(distRoads)	3	$p < 0.0001$		
	Near water	1	$p < 0.0001$		
	s(xcoord, ycoord)	36	$p < 0.0001$		
3	s(xcoord, ycoord)	41	$p < 0.0001$	-1301.6	2980.1

784 List of Figures

785	1	Figure showing the study area (Etosha National Park) with the carcass locations. The green triangles show confirmed or suspected anthrax cases and grey/black all other types. As there are duplicate locations, the darker the shape, the more presence locations. The study area (park boundary plus 20km buffer) is outlined in black. The blue polygon is the Etosha salt pan, the red lines are park roads and the blue crosses are waterholes. The outermost red line is also the park fence.	36
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793	2	Figure showing the model identification number (increasing start knots) and the negative log-likelihood score for each of the SALSA2D models resulting from a different start knot number, K_s . The horizontal lines are the scores for the equivalent model averaging result. (Euc - Euclidean, Geo - Geodesic, Exp - Exponential and Gau - Gaussian) .	37
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798	3	Figure showing the intensity of carcass locations throughout Etosha using the model averaging (top) and SALSA2D (bottom). Note: to ensure detail can be seen, the two images have differing intensity scales. The carcass locations are shown as black circles. The blue polygon is the Etosha salt pan and the lines are the roads within the park.	38
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804	4	Figure showing the knot locations and r (effective range of basis function) from the best model averaging (top) and SALSA2D (bottom) models. Yellow is for a positive model coefficient and purple a negative one. The size of the coloured circles is a visual representation of the size of the r parameter. Note that in (a) the concentric rings are from models had the same knot locations with different r . In (b) the colours overlap but each k is in a different location. The carcass locations are shown as grey/black circles. The blue polygon is the Etosha salt pan.	39
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813	5	Figure showing the estimated relationship of distance to the nearest waterhole to carcass intensity (when distance to roads = 1.5km and mean annual rainfall = 420mm). The red line area is a 95% confidence interval about the estimated relationship.	40
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817	6	Figure showing the estimated relationship of distance to roads to carcass intensity (when mean annual rainfall = 420mm and distance to waterhole is ≥ 3 km). The red shaded area is a 95% confidence interval about the estimated relationship. The tick marks top and bottom show the values of the covariate in the original data which were presence locations (1's) and absences (0's).	41
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823	7	Figure showing the estimated relationship of mean annual rainfall to carcass intensity (when distance to road = 1.5km and distance to waterhole is ≥ 3 km). The red shaded area is a 95% confidence interval about the estimated relationship. The tick marks top and bottom show the values of the covariate in the original data which were presences (1's) and absences (0's).	42
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829	8	Figure showing the estimated carcass intensity throughout the study	
830		area using SALSA and SALSA2D-based model selection and both one	
831		and two dimensional spline based terms (a). Figure showing the top	
832		5% intensity areas. The carcass locations are shown as black circles,	
833		the blue polygon is the Etosha salt pan, the blue crosses are water-	
834		holes and the black lines are roads.	43
835	9	Figure showing the estimated carcass intensity for the north-east part	
836		of the study area for (a) Model 1, (b) Model 2 and (c) the location	
837		of k and associated r for model 2. The carcass locations are shown as	
838		black circles, the blue polygon is the Etosha salt pan, the blue crosses	
839		are waterholes and the black lines are roads	44

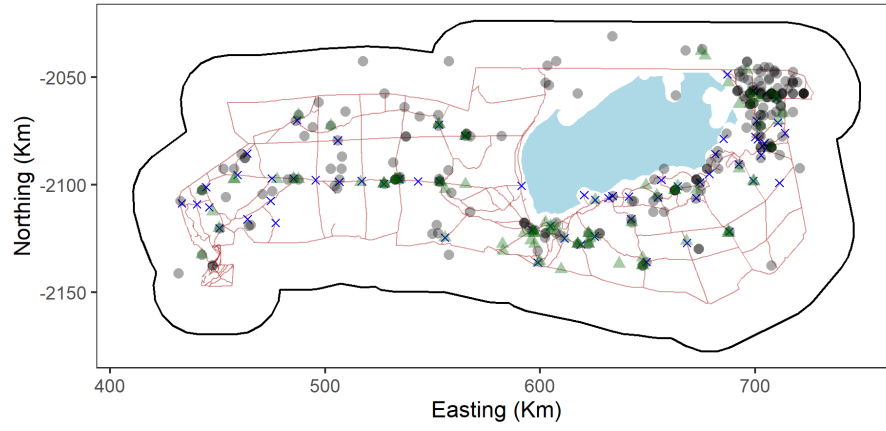


Figure 1.: Figure showing the study area (Etosha National Park) with the carcass locations. The green triangles show confirmed or suspected anthrax cases and grey/black all other types. As there are duplicate locations, the darker the shape, the more presence locations. The study area (park boundary plus 20km buffer) is outlined in black. The blue polygon is the Etosha salt pan, the red lines are park roads and the blue crosses are waterholes. The outermost red line is also the park fence.

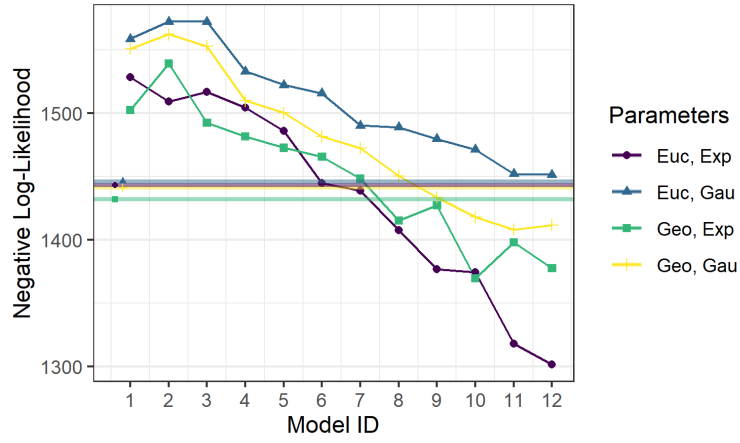


Figure 2.: Figure showing the model identification number (increasing start knots) and the negative log-likelihood score for each of the SALSA2D models resulting from a different start knot number, K_s . The horizontal lines are the scores for the equivalent model averaging result. (Euc - Euclidean, Geo - Geodesic, Exp - Exponential and Gau - Gaussian)

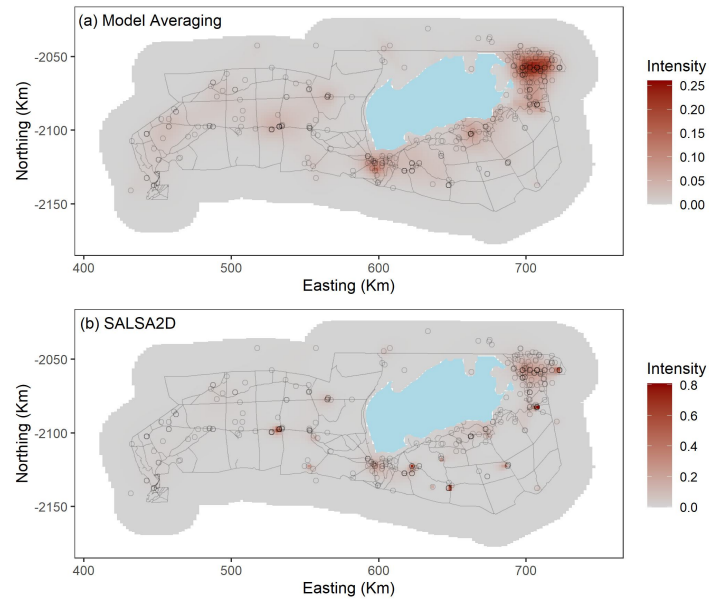


Figure 3.: Figure showing the intensity of carcass locations throughout Etosha using the model averaging (top) and SALSA2D (bottom). Note: to ensure detail can be seen, the two images have differing intensity scales. The carcass locations are shown as black circles. The blue polygon is the Etosha salt pan and the lines are the roads within the park.

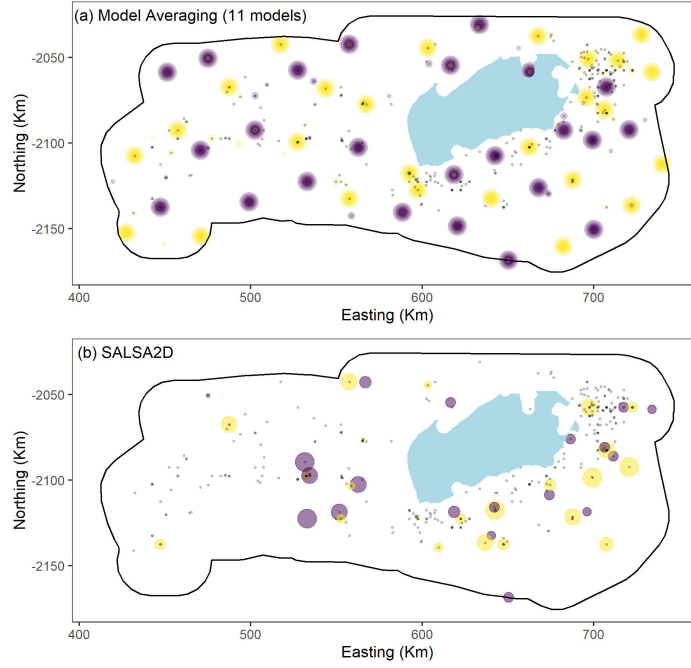


Figure 4.: Figure showing the knot locations and r (effective range of basis function) from the best model averaging (top) and SALSA2D (bottom) models. Yellow is for a positive model coefficient and purple a negative one. The size of the coloured circles is a visual representation of the size of the r parameter. Note that in (a) the concentric rings are from models had the same knot locations with different r . In (b) the colours overlap but each k is in a different location. The carcass locations are shown as grey/black circles. The blue polygon is the Etosha salt pan.

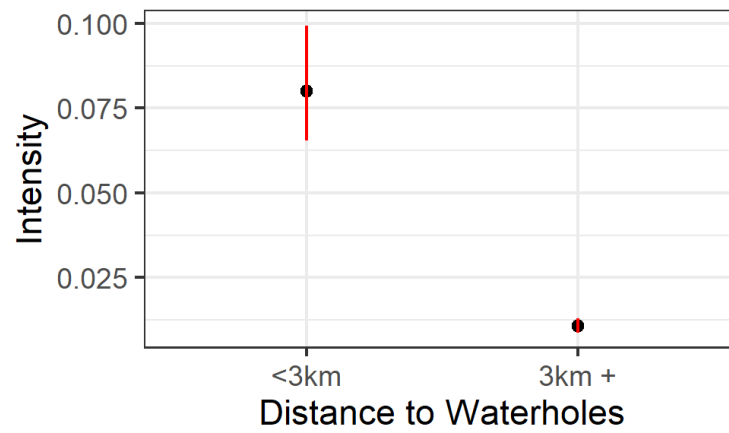


Figure 5.: Figure showing the estimated relationship of distance to the nearest waterhole to carcass intensity (when distance to roads = 1.5km and mean annual rainfall = 420mm). The red line area is a 95% confidence interval about the estimated relationship.

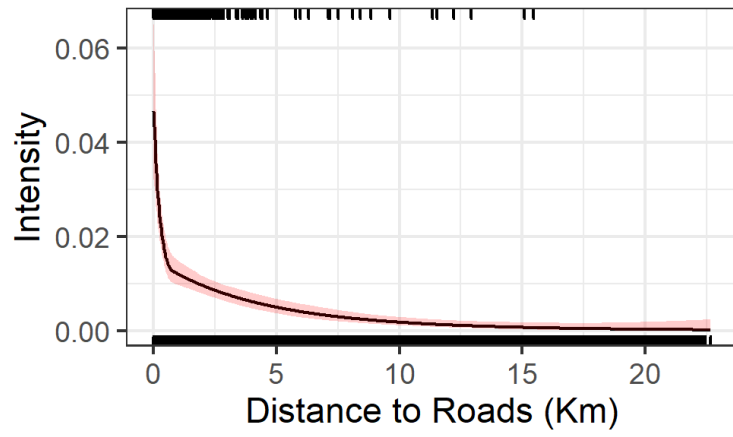


Figure 6.: Figure showing the estimated relationship of distance to roads to carcass intensity (when mean annual rainfall = 420mm and distance to waterhole is ≥ 3 km). The red shaded area is a 95% confidence interval about the estimated relationship. The tick marks top and bottom show the values of the covariate in the original data which were presence locations (1's) and absences (0's).

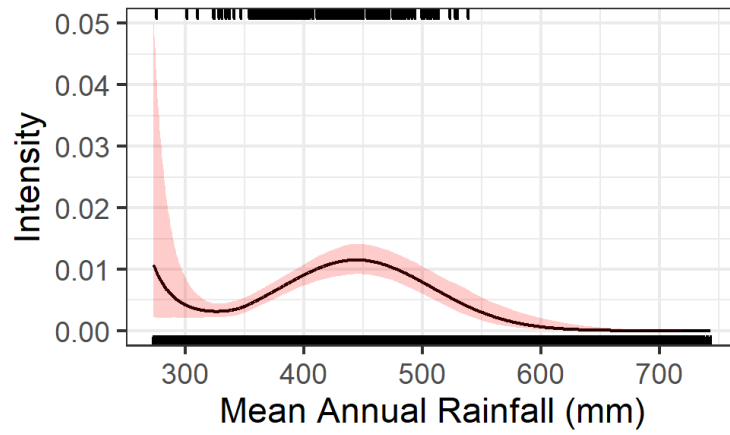


Figure 7.: Figure showing the estimated relationship of mean annual rainfall to carcass intensity (when distance to road = 1.5km and distance to waterhole is ≥ 3 km). The red shaded area is a 95% confidence interval about the estimated relationship. The tick marks top and bottom show the values of the covariate in the original data which were presences (1's) and absences (0's).

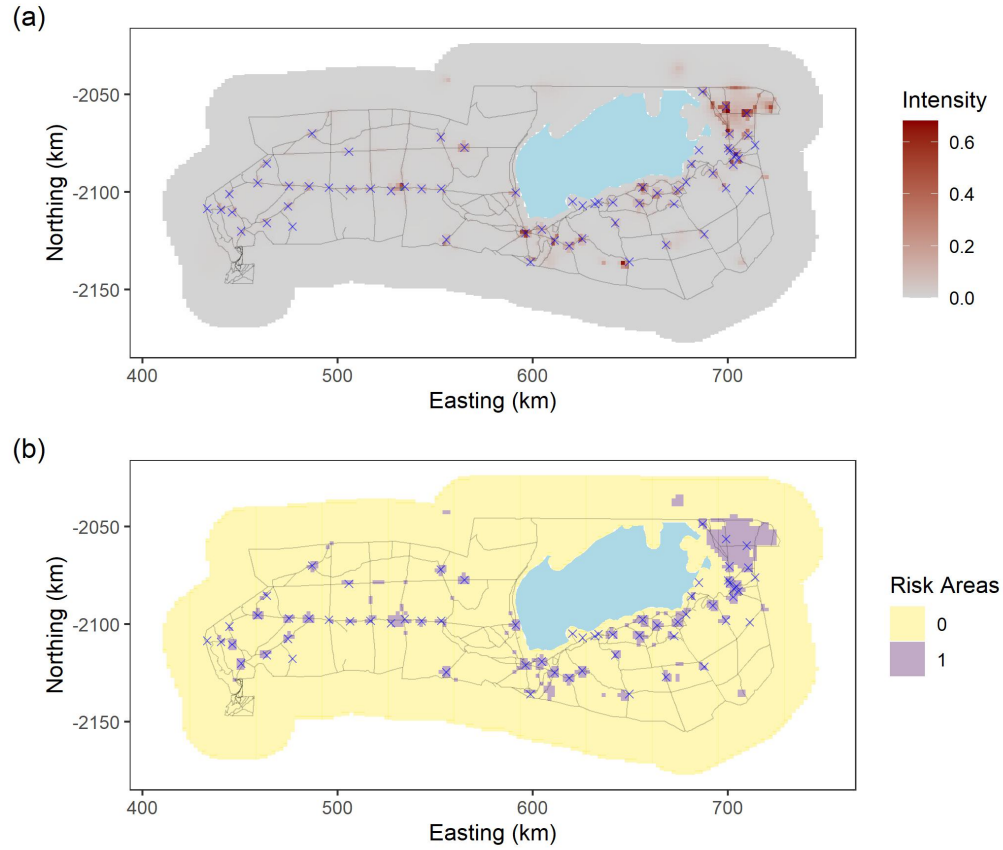


Figure 8.: Figure showing the estimated carcass intensity throughout the study area using SALSA and SALSA2D-based model selection and both one and two dimensional spline based terms (a). Figure showing the top 5% intensity areas. The carcass locations are shown as black circles, the blue polygon is the Etosha salt pan, the blue crosses are waterholes and the black lines are roads.

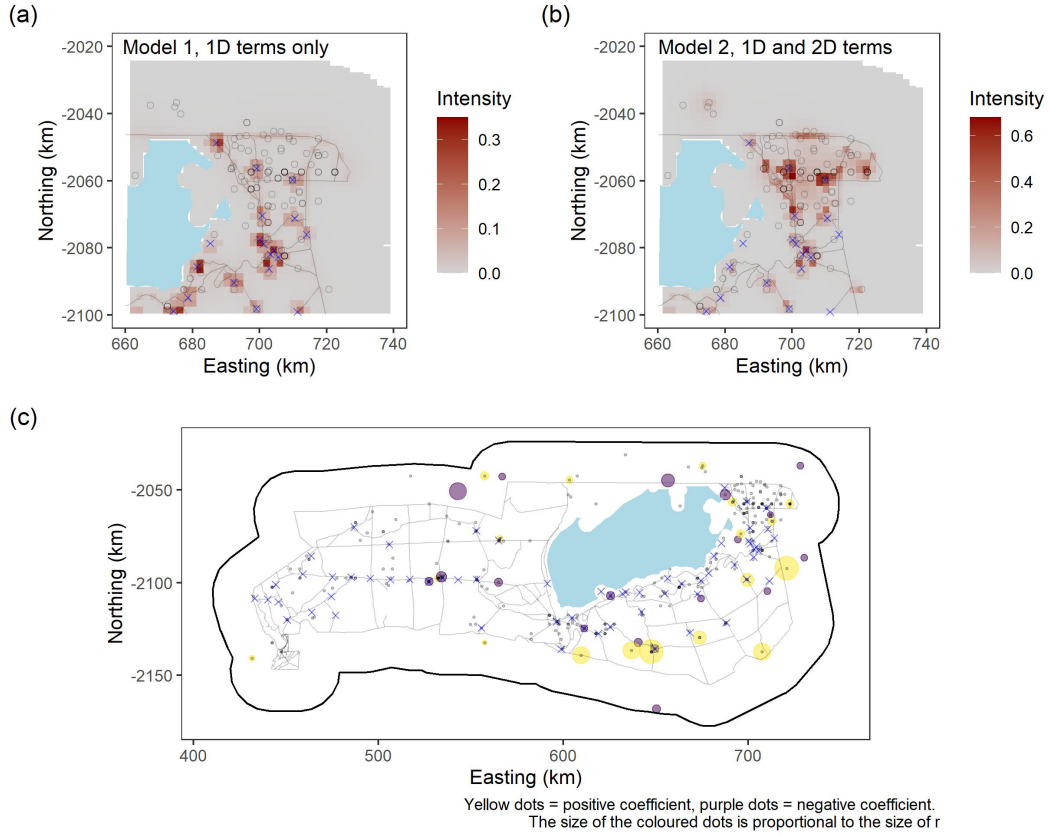


Figure 9.: Figure showing the estimated carcass intensity for the north-east part of the study area for (a) Model 1, (b) Model 2 and (c) the location of k and associated r for model 2. The carcass locations are shown as black circles, the blue polygon is the Etosha salt pan, the blue crosses are waterholes and the black lines are roads