Runs Test Paper

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Simulated Data

Make some simulated toy data using the following equation:

$$y = \beta_0 + \beta_1 X_1$$

where $\beta_0 = 1$ and $\beta_1 = 0.3$

```
dat<-makeToyData(200, length.panels=5)
head(dat)</pre>
```

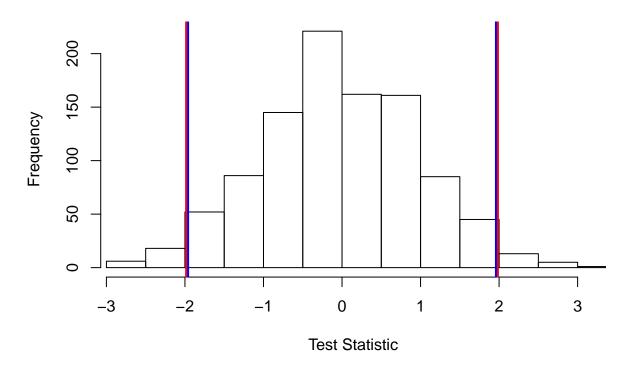
	x	evph	mu	panelid
1	1.000000	0	3.669297	1
2	1.090909	0	3.770746	1
3	1.181818	0	3.874999	1
4	1.272727	0	3.982135	1
5	1.363636	0	4.092234	1
6	1.454545	0	4.205376	2

Uncorrelated data

1000 sets of noisy data are simulated from this truth using a Poisson distribution.

```
newdat<-generateNoise(nsim, dat$mu, family='poisson', d=1)</pre>
To test, fit a glm to one of the sets of data.
init_glm<-glm(newdat[,1] ~ x, data=dat, family='quasipoisson')</pre>
summary(init_glm)
Call:
glm(formula = newdat[, 1] ~ x, family = "quasipoisson", data = dat)
Deviance Residuals:
     Min
                10
                       Median
                                      30
                                                Max
-3.13421 -0.69426
                      0.02305
                                           2.06863
                                0.57711
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.956845
                        0.057000 16.79
                                            <2e-16 ***
            0.306386
                        0.007401
                                    41.40
                                            <2e-16 ***
Х
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for quasipoisson family taken to be 1.013624)
    Null deviance: 2270.5 on 199 degrees of freedom
Residual deviance: 204.9 on 198 degrees of freedom
AIC: NA
Number of Fisher Scoring iterations: 4
Models were fitted to all datasets generated above and the runs test was evaluated for each one. The
distribution of the test statistics is returned. A plot is also produced, which shows the lower 2.5% and upper
97.5\% critical values of the empirical distribution (red) and from the Normal (N(0,1)) distribution.
empdistribution<-getRunsCritVals(n.sim = nsim, simData=newdat,</pre>
                                   model = init_glm, data = dat, plot=TRUE,
                                   returnDist = TRUE)
```

Empirical Distribution: Runs Test Statistic



Use the data generated to assess the 5% error rate for this test when using the Normal distribution or the empirical distribution generated above.

```
newdat<-generateNoise(nsim, dat$mu, family='poisson', d=1)
ps<-matrix(NA, nrow=nsim, ncol=2)

for(i in 1:nsim){
    sim_glm<-glm(newdat[,i] ~ x , data=dat, family='quasipoisson')
    # find both the empirical and Normal p-values
    ps[i,1]<-runs.test(residuals(sim_glm, type='pearson'), critvals = empdistribution)$p.value
    ps[i,2]<-runs.test(residuals(sim_glm, type='pearson'))$p.value
}

(length(which(ps[,1]<0.05))/nsim)*100

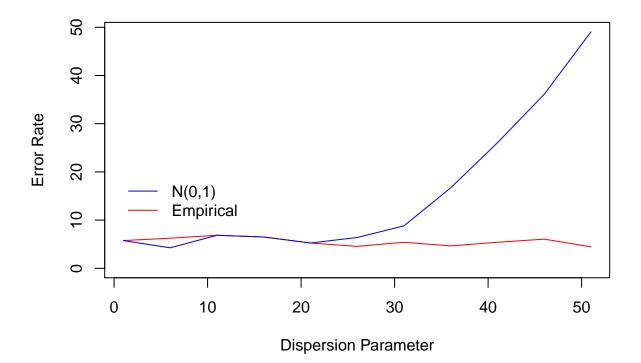
[1] 6.9
(length(which(ps[,2]<0.05))/nsim)*100</pre>
```

[1] 6.9

How does this change if we vary the dispersion parameter for the data?

```
nphi=seq(1,51, by=5)
errrate<-matrix(NA, nrow=length(nphi), ncol=2)
counter=1
nsim=2000
for(p in nphi){
   newdat<-generateNoise(nsim, dat$mu, family='poisson', d=p)</pre>
```

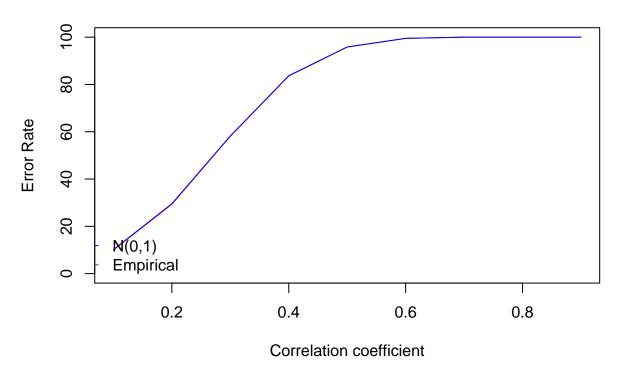
```
plot(nphi, errrate[,1], type='l', col='red', ylim=c(0, range(errrate)[2]), ylab='Error Rate', xlab='Dis
lines(nphi, errrate[,2], col='blue')
legend(0, 20, legend = c('N(0,1)', 'Empirical'), col = c('blue', 'red'), lty = c(1,1), bty = 'n')
```



Correlated data

```
dat<-makeToyData(200, length.panels=5)</pre>
head(dat)
        x evph
                      mu panelid
1 1.000000 0 3.669297
2 1.090909
           0 3.770746
                               1
4 1.272727 0 3.982135
                               1
6 1.454545
             0 4.205376
                               2
nsim=2000
newdat<-generateNoise(nsim, dat$mu, family='poisson', d=1)</pre>
rho = seq(0.1, 0.9, by = 0.1)
errrate<-matrix(NA, nrow=length(rho), ncol=2)</pre>
counter=1
for(r in rho){
  newdatcorr<-generateIC.toy(dat, c(1, r, r^2, r^3, r^4), 'panelid', newdat, ncol(newdat), dots=FALSE)
  # for each change in phi, update the empirical distribution
  empdistribution<-getRunsCritVals(n.sim = nsim, simData=newdat,</pre>
                                   model = init_glm, data = dat, plot=FALSE,
                                   returnDist = TRUE, dots=FALSE)
  ps<-matrix(NA, nrow=nsim, ncol=2)</pre>
  for(i in 1:nsim){
   sim_glm<-glm(newdatcorr[,i] ~ x , data=dat, family='quasipoisson')</pre>
    \# find both the empirical and Normal p-values
   ps[i,1] <-runs.test(residuals(sim_glm, type='pearson'), critvals = empdistribution)$p.value
   ps[i,2]<-runs.test(residuals(sim_glm, type='pearson'))$p.value</pre>
  errrate[counter,1]<-(length(which(ps[,1]<0.05))/nsim)*100
  errrate[counter,2]<-(length(which(ps[,2]<0.05))/nsim)*100</pre>
  counter=counter+1
}
plot(rho, errrate[,1], type='l', col='red', ylim=c(0, range(errrate)[2]), ylab='Error Rate', xlab='Corr
lines(rho, errrate[,2], col='blue')
legend(0, 20, legend = c('N(0,1)', 'Empirical'), col = c('blue', 'red'), lty = c(1,1), bty = 'n')
```

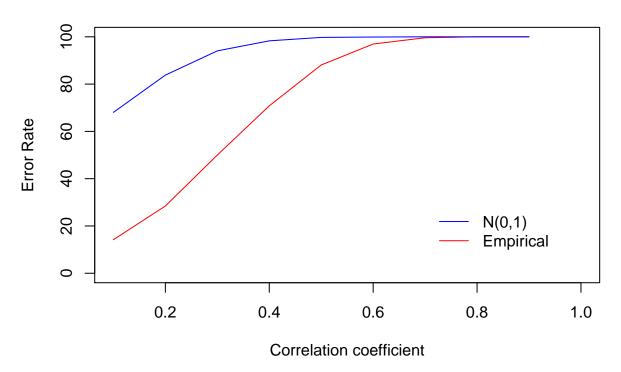
Dispersion = 1



```
nsim=2000
newdat<-generateNoise(nsim, dat$mu, family='poisson', d=50)</pre>
rho=seq(0.1, 0.9, by=0.1)
errrate<-matrix(NA, nrow=length(rho), ncol=2)</pre>
counter=1
for(r in rho){
  newdatcorr<-generateIC.toy(dat, c(1, r, r^2, r^3, r^4), 'panelid', newdat, ncol(newdat), dots=FALSE)
  # for each change in phi, update the empirical distribution
  empdistribution<-getRunsCritVals(n.sim = nsim, simData=newdat,</pre>
                                     model = init_glm, data = dat, plot=FALSE,
                                     returnDist = TRUE, dots=FALSE)
  ps<-matrix(NA, nrow=nsim, ncol=2)</pre>
  for(i in 1:nsim){
    sim_glm<-glm(newdatcorr[,i] ~ x , data=dat, family='quasipoisson')</pre>
    # find both the empirical and Normal p-values
    ps[i,1] <-runs.test(residuals(sim_glm, type='pearson'), critvals = empdistribution) $p.value
    ps[i,2]<-runs.test(residuals(sim_glm, type='pearson'))$p.value</pre>
  \verb|errrate| [counter, 1] < -(length(which(ps[, 1] < 0.05)) / nsim) * 100|
  errrate[counter,2]<-(length(which(ps[,2]<0.05))/nsim)*100
  counter=counter+1
```

```
plot(rho, errrate[,1], type='l', col='red', ylim=c(0, range(errrate)[2]), xlim=c(0.1,1), ylab='Error Ra
lines(rho, errrate[,2], col='blue')
legend(0.7, 30, legend = c('N(0,1)', 'Empirical'), col = c('blue', 'red'), lty = c(1,1), bty = 'n')
```

Dispersion = 50



As expected, when the dispersion in the data is high, there is a greater discrepancy between the N(0,1) and empirical distributions.

What does all this mean for power analysis?

If data are assumed to be correlated, then a correlation structure is chosen and GEE - type model fitted. If the independent working correlation structure is specified, then robust standard errors are used for inference. Does this machinery still work when there is actually no correlation present in the data?

Question:

- 1. Are robust standard errors the same as raw standard errors when no correlation is present?
- 2. What happens when a blocking structure is chosen that is not necessary. i.e. does the answer to question 1 vary with differing block structures?
- 3. Is the power to detect change affected by using robust standard errors when not necessary?

Make data but add an impact. Here we repeat the data but have a 50% decline in the response for the second set.

```
50\% decline, \phi = 50
datimp<-makeToyData(200, length.panels=5, changecoef.link = log(0.5))
head(datimp)
                     mu panelid
        x evph
1 1.000000 0 3.669297
2 1.090909
             0 3.770746
3 1.181818
             0 3.874999
4 1.272727
            0 3.982135
1
6 1.454545
             0 4.205376
Generate independent noisy data with a high dispersion, e.g. \phi = 50
newdat<-generateNoise(nsim, datimp$mu, family='poisson', d=50)</pre>
init_impglm<-glm(newdat[,1] ~ x + as.factor(evph), data=datimp, family='quasipoisson')</pre>
summary(init_impglm)
Call:
glm(formula = newdat[, 1] ~ x + as.factor(evph), family = "quasipoisson",
   data = datimp)
Deviance Residuals:
    Min
               10
                   Median
                                   30
                                           Max
-10.6337 -4.4825 -2.7733 -0.0955
                                       26.7367
Coefficients:
                Estimate Std. Error t value Pr(>|t|)
                  (Intercept)
                                      6.290 2.01e-09 ***
                  0.3567
                             0.0567
as.factor(evph)1 -0.7526
                             0.2539 -2.964 0.00341 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for quasipoisson family taken to be 54.75764)
   Null deviance: 9692.4 on 199 degrees of freedom
Residual deviance: 6460.4 on 197 degrees of freedom
AIC: NA
Number of Fisher Scoring iterations: 7
Get the empirical distribution critical values:
empdistribution<-getRunsCritVals(n.sim = nsim, simData=newdat,</pre>
                                model = init_impglm, data = datimp, plot=FALSE,
```

Emp Norm

apply(runspowsim out\$rawrob, 2, sum)/nsim

runspowsim_out<-runsPowerSim(newdat, init_impglm, empdistribution, nsim, powercoefid = 3)

returnDist = TRUE, dots=FALSE)

```
0.0665 0.8280
(length(which(runspowsim_out$imppvals[,1]<=0.05))/nsim)*100</pre>
[1] 73.1
(length(which(runspowsim_out$imppvals[,2]<=0.05))/nsim)*100</pre>
[1] 73.85
25\% decline, \phi = 50
  Emp Norm
0.066 0.609
[1] 23.45
[1] 26
0% decline, \phi = 50
   Emp
         Norm
0.0510 0.4485
[1] 5.15
[1] 5.85
It seems that when the Normal distribution is used to test for correlation, consistently the power to detect
change is higher than when the empirical distribution is used to choose which standard errors to use.
Test: Repeat for 50% decline to get a range of power values. Check to see if the discrepancy is consistent.
50% decline, \phi = 50, multiruns
wilcox.test(x = runspower[,1], runspower[,2], paired = T)
    Wilcoxon signed rank test with continuity correction
data: runspower[, 1] and runspower[, 2]
V = 0, p-value < 2.2e-16
alternative hypothesis: true location shift is not equal to 0
wilcox.test(x = power[,1], power[,2], paired = T)
    Wilcoxon signed rank test with continuity correction
data: power[, 1] and power[, 2]
V = 12, p-value < 2.2e-16
alternative hypothesis: true location shift is not equal to 0
apply(power, 2, mean)
```

[1] 72.9140 74.0305

```
apply(runspower, 2, mean)
```

[1] 0.059565 0.834885

Statistically we have a significant difference between the power calculated from raw/robust s.e. but the real world significance in this toy example is minimal. The mean difference is one percentage point (with raw giving a higher power).

```
25% decline, \phi = 50, multiruns
```

```
Wilcoxon signed rank test with continuity correction
```

```
data: runspower[, 1] and runspower[, 2]
V = 0, p-value < 2.2e-16
alternative hypothesis: true location shift is not equal to 0
Wilcoxon signed rank test with continuity correction

data: power[, 1] and power[, 2]
V = 0, p-value < 2.2e-16
alternative hypothesis: true location shift is not equal to 0
[1] 23.6045 25.3685
[1] 0.057965 0.620265</pre>
```

Toy data with smaller mean

The Falls of Warness data has a very small mean (1.01) compared with the toy data used so far. Here we reduce the mean of the toy data inline with that seen in the Falls of Warness data to see if we can replicate results

```
datlow<-makeToyData(200, length.panels=5, b0=-2)
head(datlow)</pre>
```

```
x evph
                       mu panelid
1 1.000000
              0 0.1826835
                                 1
2 1.090909
              0 0.1877344
                                 1
3 1.181818
              0 0.1929248
                                 1
4 1.272727
              0 0.1982588
                                 1
5 1.363636
              0 0.2037403
                                 1
6 1.454545
              0 0.2093733
                                 2
```

```
mean(datlow$mu)
```

```
[1] 0.9442818
```

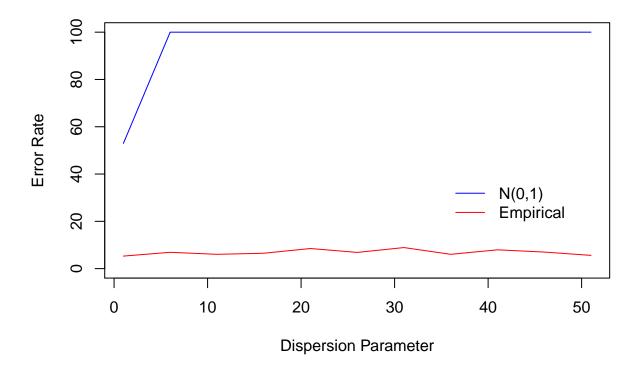
```
init_glm<-glm(newdat[,1] ~ x, data=datlow, family='quasipoisson')
summary(init_glm)</pre>
```

```
Call:
```

```
glm(formula = newdat[, 1] ~ x, family = "quasipoisson", data = datlow)
```

Deviance Residuals:

```
Median
              1Q
                                3Q
-8.1861 -4.3997 -3.1320 -0.0988 26.8324
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
                        0.42226 3.019 0.00287 **
(Intercept) 1.27496
                        0.05738 3.971 0.00010 ***
х
             0.22782
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for quasipoisson family taken to be 55.17751)
   Null deviance: 6956.7 on 199 degrees of freedom
Residual deviance: 5994.9 on 198 degrees of freedom
AIC: NA
Number of Fisher Scoring iterations: 6
nphi=seq(1,51, by=5)
errrate<-matrix(NA, nrow=length(nphi), ncol=2)
counter=1
nsim=2000
for(p in nphi){
 newdat<-generateNoise(nsim, datlow$mu, family='poisson', d=p)</pre>
  # for each change in phi, update the empirical distribution
  empdistribution <- getRunsCritVals(n.sim = nsim, simData=newdat,
                                   model = init_glm, data = datlow, plot=FALSE,
                                   returnDist = TRUE, dots=FALSE)
  ps<-matrix(NA, nrow=nsim, ncol=2)</pre>
  for(i in 1:nsim){
    sim_glm<-glm(newdat[,i] ~ x + as.factor(evph), data=datlow,</pre>
                 family='quasipoisson')
    # find both the empirical and Normal p-values
   ps[i,1] <-runs.test(residuals(sim_glm, type='pearson'), critvals = empdistribution)$p.value
   ps[i,2]<-runs.test(residuals(sim_glm, type='pearson'))$p.value</pre>
  errrate[counter,1]<-(length(which(ps[,1]<0.05))/nsim)*100
  errrate[counter,2]<-(length(which(ps[,2]<0.05))/nsim)*100
  counter=counter+1
}
plot(nphi, errrate[,1], type='l', col='red', ylim=c(0, range(errrate)[2]), ylab='Error Rate', xlab='Dis
lines(nphi, errrate[,2], col='blue')
legend(35, 40, legend = c('N(0,1)', 'Empirical'), col = c('blue', 'red'), lty = c(1,1), bty = 'n')
```



25% decline, $\phi = 50$, multiruns

Wilcoxon signed rank test with continuity correction

data: runspower[, 1] and runspower[, 2]

V = 0, p-value < 2.2e-16

alternative hypothesis: true location shift is not equal to 0

Wilcoxon signed rank test with continuity correction

data: power[, 1] and power[, 2]

V = 0, p-value < 2.2e-16

alternative hypothesis: true location shift is not equal to ${\tt 0}$

[1] 9.2585 22.5115

[1] 0.078355 1.000000

25% decline, $\phi = 1$, multiruns

Wilcoxon signed rank test with continuity correction

data: runspower[, 1] and runspower[, 2]

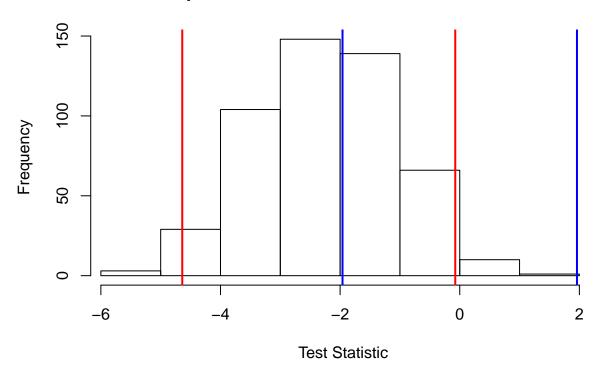
```
V = 0, p-value < 2.2e-16
alternative hypothesis: true location shift is not equal to 0
   Wilcoxon signed rank test with continuity correction
data: power[, 1] and power[, 2]
V = 0, p-value < 2.2e-16
alternative hypothesis: true location shift is not equal to 0
[1] 44.5755 47.3495
[1] 0.056925 0.695025
Real Data: Falls of Warness
init_glm<-glm(response ~ TideState + WindStrength + SeaState + SimpPrecipitation + CloudCover, data=da</pre>
nsim=500
newdat<-generateNoise(nsim, fitted(init_glm), family='poisson', d=1)</pre>
500 sets of noisy data are simulated from this truth using a Poisson distribution.
To test, fit a glm to one of the sets of data.
fowsim_glm<-glm(newdat[,1] ~ TideState + WindStrength + SeaState + SimpPrecipitation + CloudCover, dat</pre>
summary(fowsim_glm)
Call:
glm(formula = newdat[, 1] ~ TideState + WindStrength + SeaState +
   SimpPrecipitation + CloudCover, family = quasipoisson, data = dat)
Deviance Residuals:
             1Q Median
   Min
                             3Q
                                     Max
-2.6583 -1.2134 -0.1304 0.5300
                                  3.9991
Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
(Intercept)
                       TideState
WindStrength
                       SeaState
                        0.394730
                                 0.012600 31.327 < 2e-16 ***
SimpPrecipitationHEAVY
                        0.167996
                                 0.084613 1.985
                                                   0.0471 *
SimpPrecipitationLIGHT
                        0.880236
                                 0.053269 16.524 < 2e-16 ***
SimpPrecipitationNONE
                        0.311551
                                 0.048875 6.374 1.87e-10 ***
SimpPrecipitationSHOWERS 0.846511
                                  0.049402 17.135 < 2e-16 ***
CloudCover
                        0.102456
                                 0.002971 34.484 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for quasipoisson family taken to be 1.003368)
   Null deviance: 34848 on 26334 degrees of freedom
Residual deviance: 29566 on 26326 degrees of freedom
```

Number of Fisher Scoring iterations: 5

Runs Test Check

Models were fitted to all datasets generated above and the runs test was evaluated for each one. The distribution of the test statistics is returned. A plot is also produced, which shows the lower 2.5% and upper 97.5% critical values of the empirical distribution (red) and from the Normal (N(0,1)) distribution.

Empirical Distribution: Runs Test Statistic

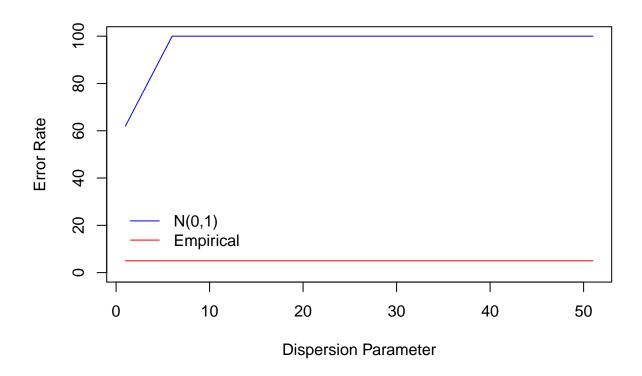


Use the data generated to assess the 5% error rate for this test when using the Normal distribution or the empirical distribution generated above.

```
newdat<-generateNoise(nsim, fitted(init_glm), family='poisson', d=1)
ps<-matrix(NA, nrow=nsim, ncol=2)

for(i in 1:nsim){
    sim_glm<-update(fowsim_glm, newdat[,i]~.)
    # find both the empirical and Normal p-values
    ps[i,1]<-runs.test(residuals(sim_glm, type='pearson'), critvals = empdistribution)$p.value
    ps[i,2]<-runs.test(residuals(sim_glm, type='pearson'))$p.value</pre>
```

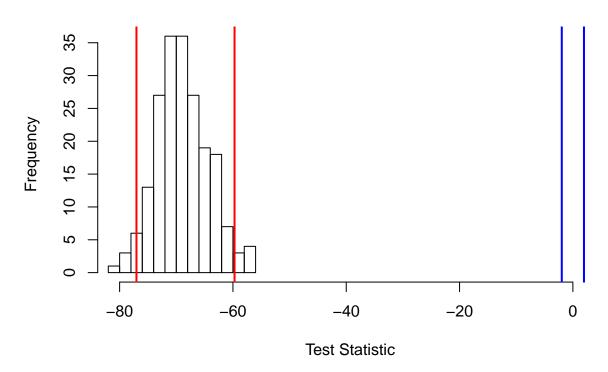
```
(length(which(ps[,1]<0.05))/nsim)*100
[1] 5.6
(length(which(ps[,2]<0.05))/nsim)*100
[1] 62.6
How does this change if we vary the dispersion parameter for the data?
nphi=seq(1,51, by=5)
errrate<-matrix(NA, nrow=length(nphi), ncol=2)</pre>
counter=1
nsim=500
for(p in nphi){
  newdat<-generateNoise(nsim, fitted(init_glm), family='poisson', d=p)</pre>
  # for each change in phi, update the empirical distribution
  empdistribution <- getRunsCritVals(n.sim = nsim, simData=newdat,
                                    model = init_glm, data = dat, plot=FALSE,
                                    returnDist = TRUE, dots=FALSE)
  ps<-matrix(NA, nrow=nsim, ncol=2)</pre>
  for(i in 1:nsim){
    sim_glm<-update(fowsim_glm, newdat[,i]~.)</pre>
    # find both the empirical and Normal p-values
    ps[i,1] <-runs.test(residuals(sim_glm, type='pearson'), critvals = empdistribution)$p.value
    ps[i,2]<-runs.test(residuals(sim_glm, type='pearson'))$p.value</pre>
  errrate[counter,1]<-(length(which(ps[,1]<0.05))/nsim)*100</pre>
  errrate[counter,2]<-(length(which(ps[,2]<0.05))/nsim)*100
  counter=counter+1
}
plot(nphi, errrate[,1], type='l', col='red', ylim=c(0, range(errrate)[2]), ylab='Error Rate', xlab='Dis
lines(nphi, errrate[,2], col='blue')
legend(0, 30, legend = c('N(0,1)', 'Empirical'), col = c('blue', 'red'), lty = c(1,1), bty = 'n')
```



Assessing the effect on Power

0% decline, dispersion = 50

Empirical Distribution: Runs Test Statistic



```
runspowsim_out<-runsPowerSim(newdat, fowsim_glm, empdistribution, nsim, powercoefid = length(coef(fowsim_apply(runspowsim_out$rawrob, 2, sum)/nsim

Emp Norm
0.055 1.000
(length(which(runspowsim_out$imppvals[,1]<=0.05))/nsim)*100

[1] 5.5
(length(which(runspowsim_out$imppvals[,2]<=0.05))/nsim)*100

[1] 5.5

Multiple runs of power test: 0% decline, dispersion=50
wilcox.test(x = runspower[,1], runspower[,2], paired = T)

Wilcoxon signed rank test with continuity correction

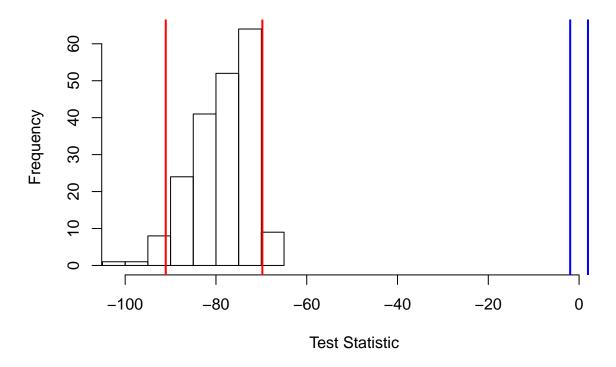
data: runspower[, 1] and runspower[, 2]
V = 0, p-value < 2.2e-16
alternative hypothesis: true location shift is not equal to 0
wilcox.test(x = power[,1], power[,2], paired = T)</pre>
```

Wilcoxon signed rank test with continuity correction

```
data: power[, 1] and power[, 2]
V = 372, p-value = 0.00302
alternative hypothesis: true location shift is not equal to 0
apply(power, 2, mean)
[1] 5.385 5.290
apply(runspower, 2, mean)
[1] 0.055 1.000
```

25% decline, dispersion = 50

Empirical Distribution: Runs Test Statistic



runspowsim_out<-runsPowerSim(newdat, fowsim_glm, empdistribution, nsim, powercoefid = length(coef(fowsim_glm, empdistribution, nsim, empdistribution, empdistribut

```
apply(runspowsim_out$rawrob, 2, sum)/nsim
  Emp Norm
0.055 1.000
(length(which(runspowsim_out$imppvals[,1]<=0.05))/nsim)*100</pre>
[1] 99
(length(which(runspowsim_out$imppvals[,2]<=0.05))/nsim)*100</pre>
[1] 99
Multiple runs of power test: 25% decline, dispersion=50
wilcox.test(x = runspower[,1], runspower[,2], paired = T)
   Wilcoxon signed rank test with continuity correction
data: runspower[, 1] and runspower[, 2]
V = 0, p-value < 2.2e-16
alternative hypothesis: true location shift is not equal to 0
wilcox.test(x = power[,1], power[,2], paired = T)
   Wilcoxon signed rank test with continuity correction
data: power[, 1] and power[, 2]
V = 36, p-value = 0.008334
alternative hypothesis: true location shift is not equal to 0
apply(power, 2, mean)
[1] 99.580 99.535
apply(runspower, 2, mean)
[1] 0.055 1.000
Multiple runs of power test: 10\% decline, dispersion=50
wilcox.test(x = runspower[,1], runspower[,2], paired = T)
   Wilcoxon signed rank test with continuity correction
data: runspower[, 1] and runspower[, 2]
V = 0, p-value = 0.001904
alternative hypothesis: true location shift is not equal to 0
wilcox.test(x = power[,1], power[,2], paired = T)
   Wilcoxon signed rank test with continuity correction
data: power[, 1] and power[, 2]
```

```
V = 0, p-value = NA
alternative hypothesis: true location shift is not equal to 0
apply(power, 2, mean)
[1] 36.4 36.4
apply(runspower, 2, mean)
[1] 0.06 1.00
Multiple runs of power test: 10% decline, dispersion=80
wilcox.test(x = runspower[,1], runspower[,2], paired = T)
   Wilcoxon signed rank test with continuity correction
data: runspower[, 1] and runspower[, 2]
V = 0, p-value = 0.001904
alternative hypothesis: true location shift is not equal to 0
wilcox.test(x = power[,1], power[,2], paired = T)
   Wilcoxon signed rank test with continuity correction
data: power[, 1] and power[, 2]
V = 7.5, p-value = 0.4237
alternative hypothesis: true location shift is not equal to 0
apply(power, 2, mean)
[1] 28.6 28.2
apply(runspower, 2, mean)
[1] 0.06 1.00
```