```
in[*]:= (*Clear any existing symbol definitions*)ClearAll[e, s, n, w];
        (*Define rules*)+
        rules = {
            (*Combine terms in the same direction*)
            e[x_] * e[y_] \Rightarrow e[x + y],
            S[X_] * S[Y_] \Rightarrow S[X + Y],
            n[x_{-}] * n[y_{-}] \Rightarrow n[x + y],
            W[X_{-}] * W[Y_{-}] \Rightarrow W[X + Y],
            (*Power rules*)
            e[x_]^n_: \rightarrow e[x*n],
            s[x_]^n_ : s[x * n],
            n[x_]^n_:\rightarrow n[x*n],
            W[x_]^n_:\rightarrow W[x*n],
            (*Commutative property for multiplication*)
            e[x_] * s[y_] \Rightarrow s[y] * e[x],
            e[x_] * n[y_] \Rightarrow n[y] * e[x],
            e[x_] *w[y_] \Rightarrow w[y] *e[x],
            s[x_] * n[y_] \Rightarrow n[y] * s[x],
            S[X_] * W[Y_] \Rightarrow W[Y] * S[X],
            n[x_] *w[y_] \Rightarrow w[y] *n[x]
           };
        (*Example expression*)
        expr = e[1] * s[1] + e[1] * e[1] * s[1];
        (*Apply rules*)
        simplifiedExpr = expr //. rules
Out[0]=
        (e[1] + e[2]) s[1]
```

```
In[*]:= (*Clear any existing definitions*)
        ClearAll[e, s, n, w];
        (*Basic rules:handle multiplication and addition*)
        rules = {
            (*Combine terms in the same direction*)
            e[x_] * e[y_] \Rightarrow e[x + y],
            s[x_] * s[y_] \Rightarrow s[x + y],
            e[x_]^n_ : e[x * n],
            s[x_]^n_ : s[x*n],
            (*Commutative property*)
            e[x_] * s[y_] \Rightarrow s[y] * e[x],
            (*Factor out common terms*)
            a_* * s[x_] + b_* * s[x_] \Rightarrow s[x] * (a + b) ;
        (*Example expression*)
        expr = e[1] * s[1] + e[1] * e[1] * s[1];
        (*Apply the rules to simplify*)
        simplifiedExpr = expr //. rules
Out[0]=
        (e[1] + e[2]) s[1]
 In[*]:= (*Example expression*)
        expr = e[1] \times e[1] * s[1] + e[1] * e[1] * s[2] + e[2] * s[3] + s[2] + s[2] * e[1];
        (*Apply the rules to simplify*)
        simplifiedExpr = expr //. rules
Out[0]=
        e\,[\,2\,]\,\times\,s\,[\,1\,]\,\,+\,\,(\,1\,+\,e\,[\,1\,]\,+\,e\,[\,2\,]\,\,)\,\,\,s\,[\,2\,]\,+\,e\,[\,2\,]\,\times\,s\,[\,3\,]
```