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# IT4272E-COMPUTER SYSTEMS

## Chapter 5: Large and Fast: Exploiting Memory Hierarchy

[with materials from *Computer Organization and Design, 4<sup>th</sup> Edition*,  
Patterson & Hennessy, © 2008, MK]

# Memory Technology

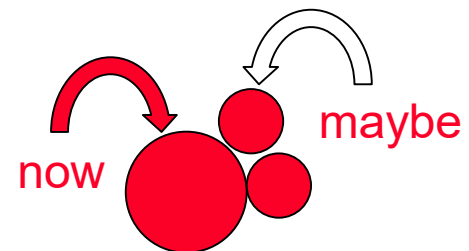
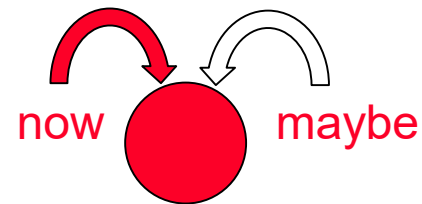
- ❑ Static RAM (SRAM)
  - | 0.5ns – 2.5ns, \$2000 – \$5000 per GB
- ❑ Dynamic RAM (DRAM)
  - | 50ns – 70ns, \$20 – \$75 per GB
- ❑ Magnetic disk
  - | 5ms – 20ms, \$0.20 – \$2 per GB
- ❑ Ideal memory
  - | Access time of SRAM
  - | Capacity and cost/GB of disk

*Ideal* [ai'diəl] tiêu chuẩn

# Principle of Locality

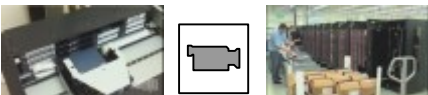
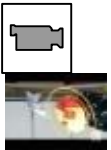
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- ❑ Programs access a small proportion of their address space at any time
- ❑ Temporal locality /'tempərəl/ thời gian
  - | Items accessed recently are likely to be accessed again soon
  - | e.g., instructions in a loop, induction variables
- ❑ Spatial locality /'speɪʃəl/ không gian
  - | Items near those accessed recently are likely to be accessed soon
  - | E.g., sequential instruction access, array data



# Taking Advantage of Locality

- ❑ Memory hierarchy
- ❑ Store everything on disk
- ❑ Copy recently accessed (and nearby) items from disk to smaller DRAM memory
  - | Main memory
- ❑ Copy more recently accessed (and nearby) items from DRAM to smaller SRAM memory
  - | Cache memory attached to CPU



# Memory Hierarchy Levels

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- ❑ Block (aka line): unit of copying

- | May be multiple words

- ❑ If accessed data is present in upper level

- | Hit: access satisfied by upper level

- Hit ratio: hits/accesses

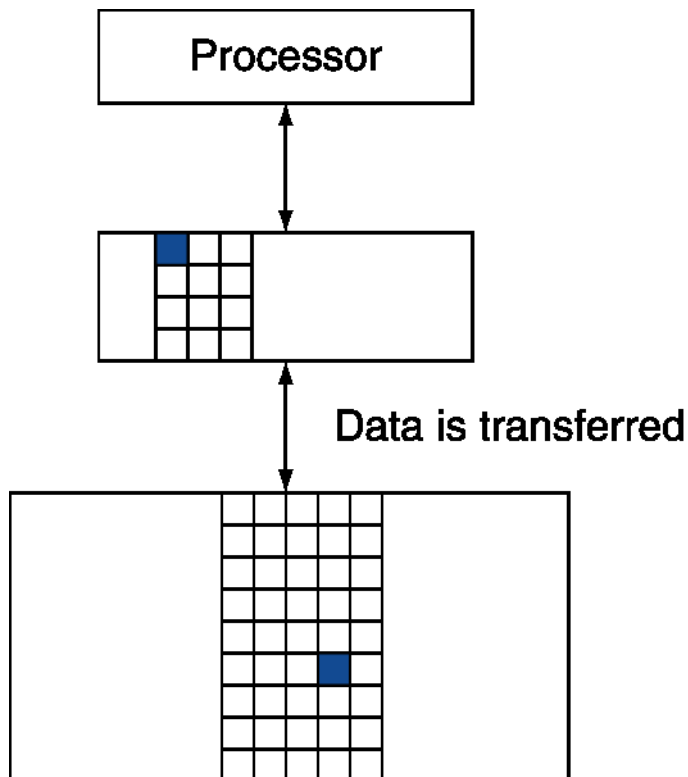
- ❑ If accessed data is absent

- | Miss: block copied from lower level

- Time taken: miss penalty

- Miss ratio: misses/accesses  
=  $1 - \text{hit ratio}$

- | Then accessed data supplied from upper level



# Cache Memory

- ❑ Cache memory
  - | The level of the memory hierarchy closest to the CPU
- ❑ Given accesses  $X_1, \dots, X_{n-1}, X_n$

$X_4$
$X_1$
$X_{n-2}$
$X_{n-1}$
$X_2$
$X_3$

a. Before the reference to  $X_n$ 

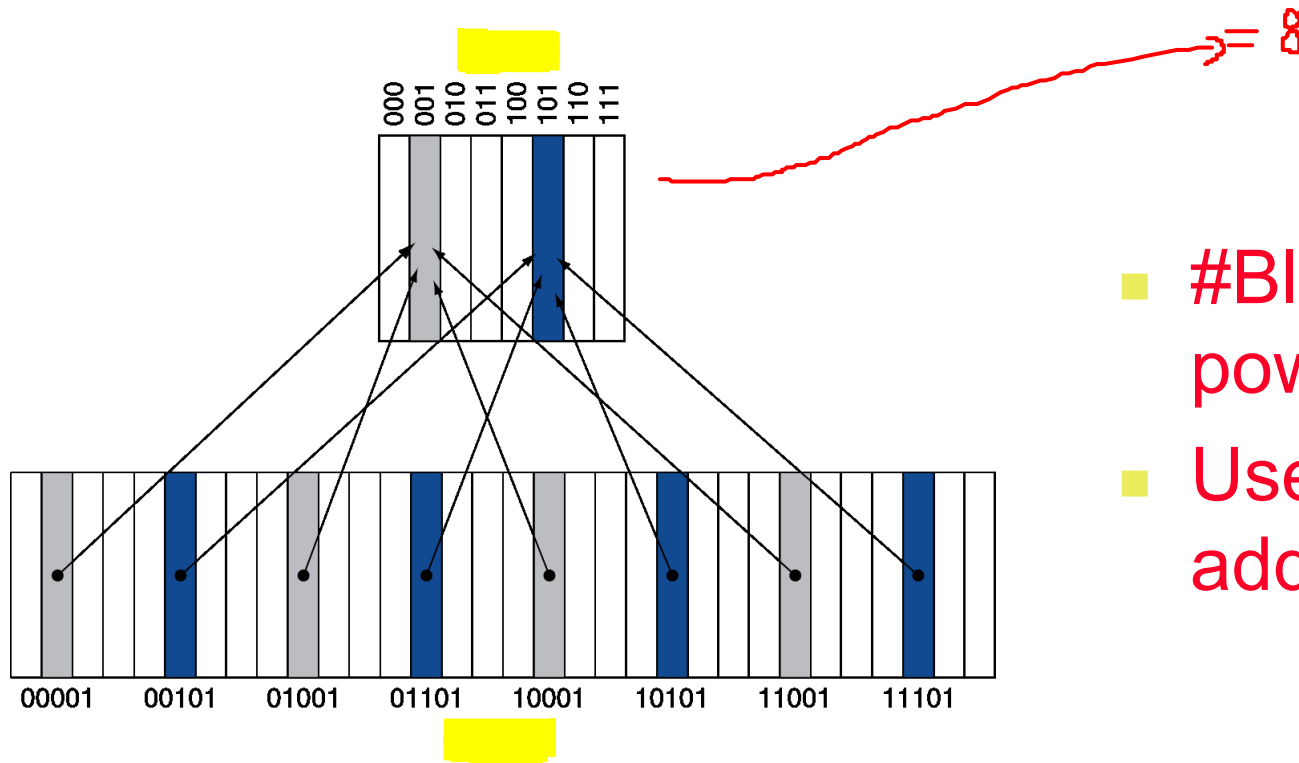
$X_4$
$X_1$
$X_{n-2}$
$X_{n-1}$
$X_2$
$X_n$
$X_3$

b. After the reference to  $X_n$ 

- How do we know if the data is present?
- Where do we look?

# Direct Mapped Cache

- ❑ Location determined by address
- ❑ Direct mapped: only one choice
  - | **(Block address) modulo (#Blocks in cache)**

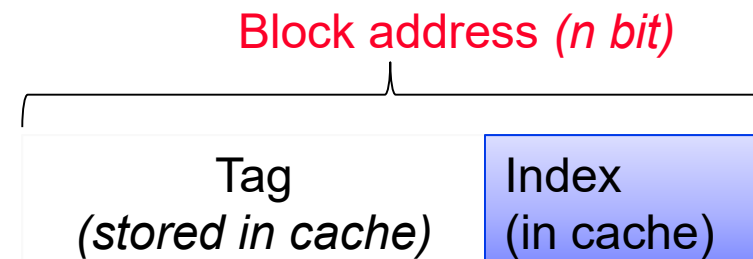
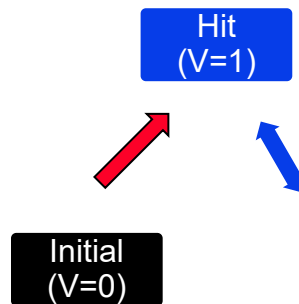


- #Blocks is a power of 2
- Use low-order address bits

Block Number 11

# Tags and Valid Bits

- ❑ How do we know which particular block is stored in a cache location?
  - | Store block address as well as the data
  - | Actually, only need the high-order bits
  - | Called the tag
- ❑ What if there is no data in a location?
  - | Valid bit: 1 = present, 0 = not present
  - | Initially 0





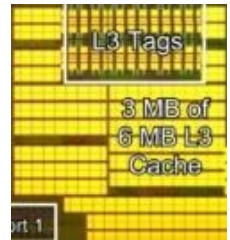
# Cache Example

- ❑ 8-blocks, 1 word/block, direct mapped
- ❑ Initial state

Address Bits  
of Cache

High Address Bits of Mem,  
but stored in Cache

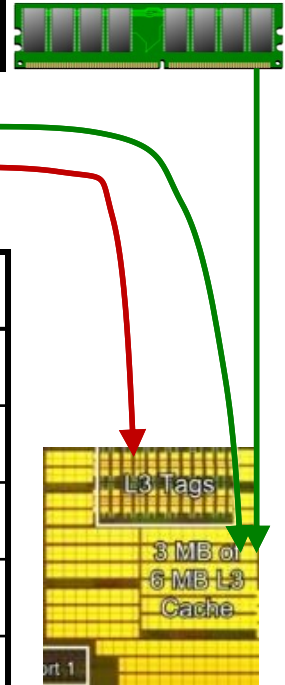
Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	N		
111	N		



# Cache Example

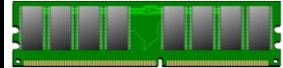
Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Miss	110

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

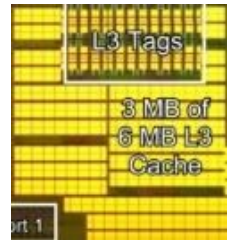


# Cache Example

Word addr	Binary addr	Hit/miss	Cache block
26	11 010	Miss	010

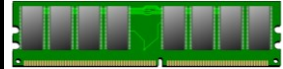


Index	V	Tag	Data
000	N		
001	N		
010	Y	11	Mem[11010]
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

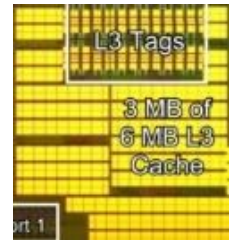


# Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Hit	110
26	11 010	Hit	010

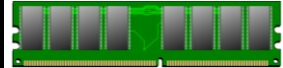


Index	V	Tag	Data
000	N		
001	N		
010	Y	11	Mem[11010]
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

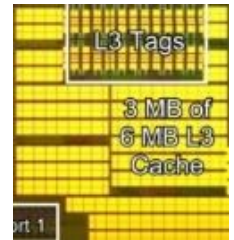


# Cache Example

Word addr	Binary addr	Hit/miss	Cache block
16	10 000	Miss	000
3	00 011	Miss	011
16	10 000	Hit	000

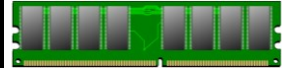


Index	V	Tag	Data
000	Y	10	Mem[10000]
001	N		
010	Y	11	Mem[11010]
011	Y	00	Mem[00011]
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

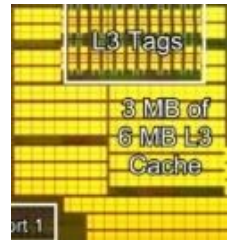


# Cache Example

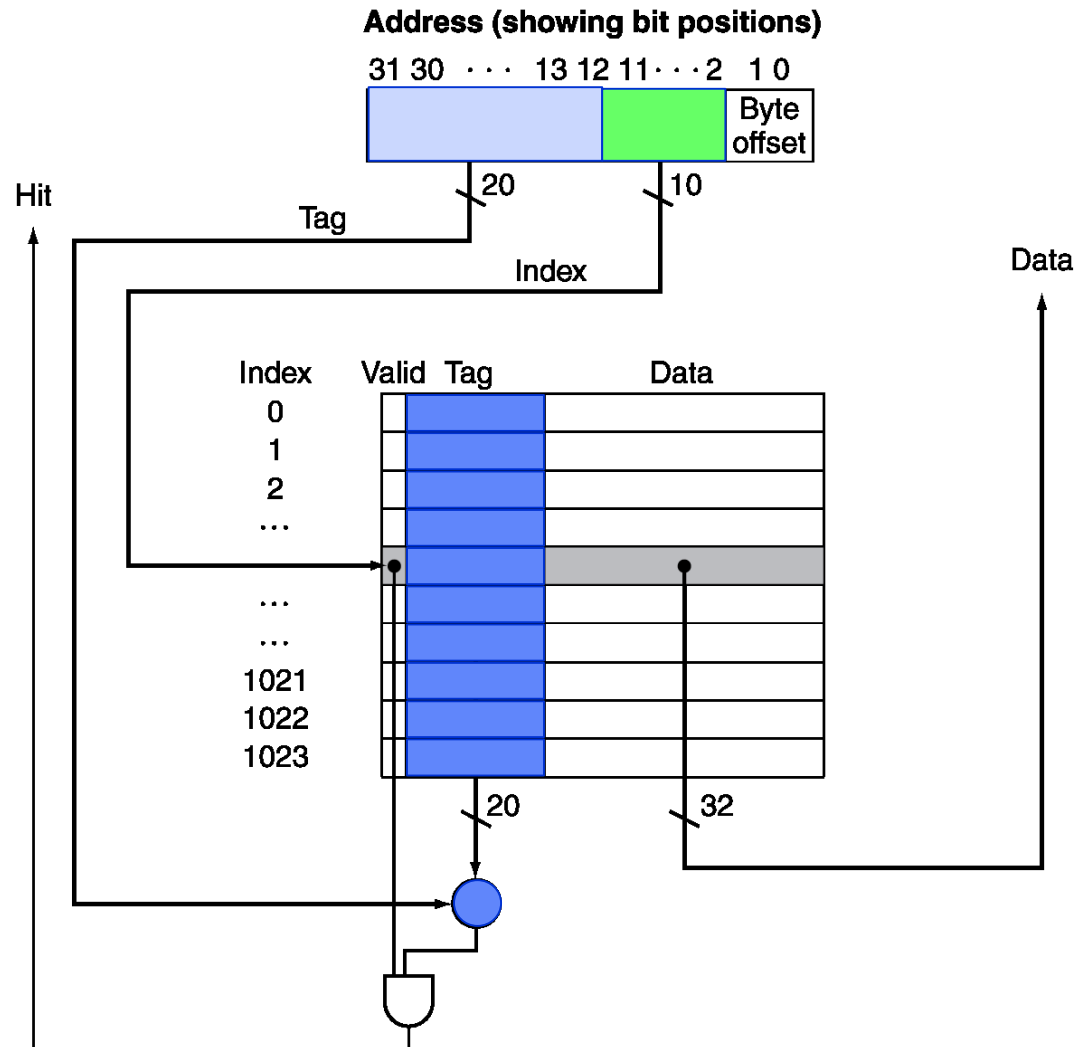
Word addr	Binary addr	Hit/miss	Cache block
18	10 010	Miss	010



Index	V	Tag	Data
000	Y	10	Mem[10000]
001	N		
010	Y	10	Mem[10010]
011	Y	00	Mem[00011]
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

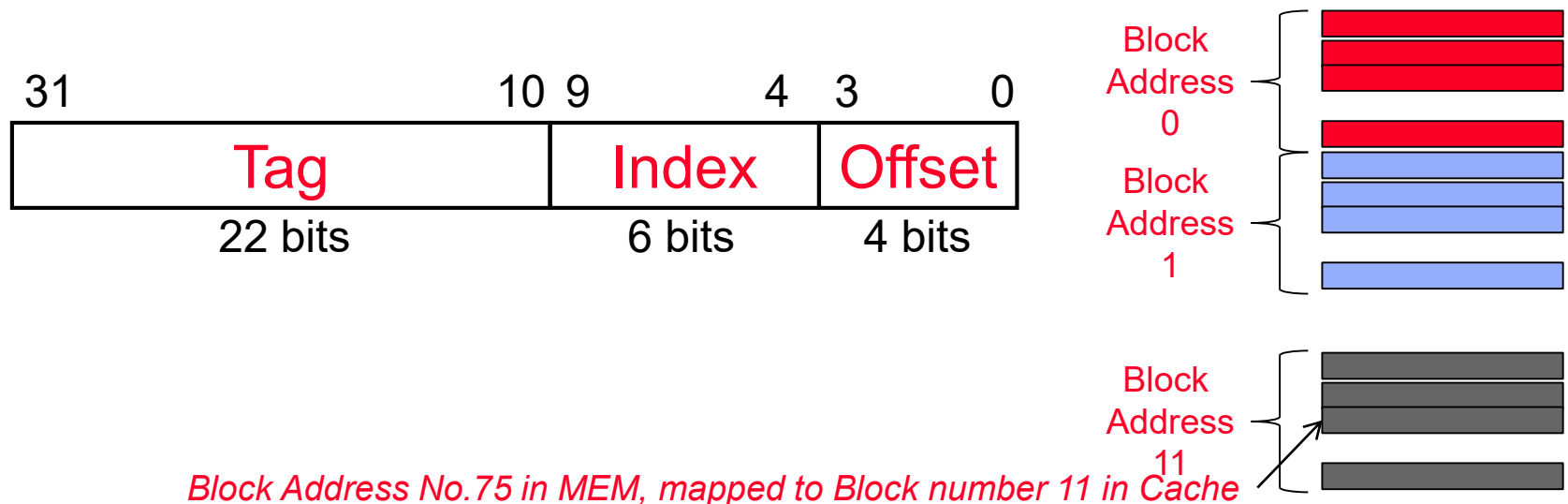


# Address Subdivision



## Example: Larger Block Size

- Cache has 64 blocks, 16 bytes/block
  - To what block number does address 1200 map?
- Block address =  $\lfloor 1200/16 \rfloor = 75$
- Block number =  $75 \text{ modulo } 64 = 11$





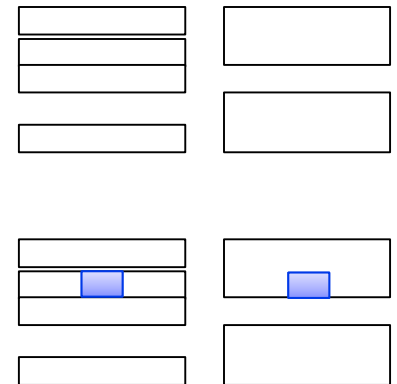
# Block Size Considerations

## ❑ Larger blocks should reduce miss rate

- | Due to spatial locality

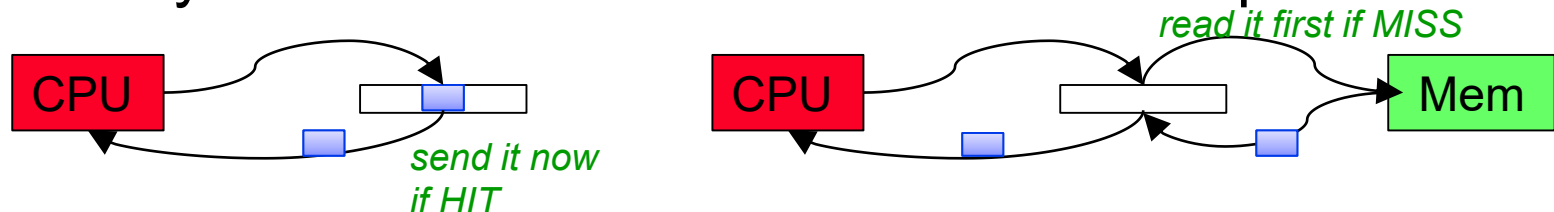
## ❑ But in a fixed-sized cache

- | Larger blocks  $\Rightarrow$  fewer of them
  - More competition  $\Rightarrow$  increased miss rate
- | Larger blocks  $\Rightarrow$  pollution



## ❑ Larger miss penalty

- | Can override benefit of reduced miss rate
- | Early restart and critical-word-first can help



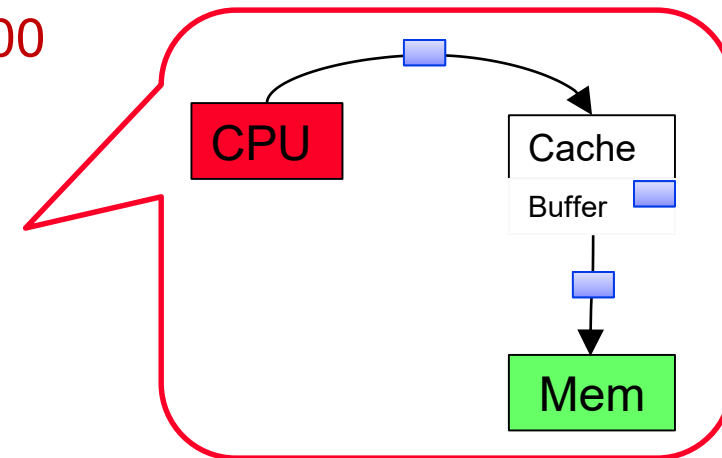
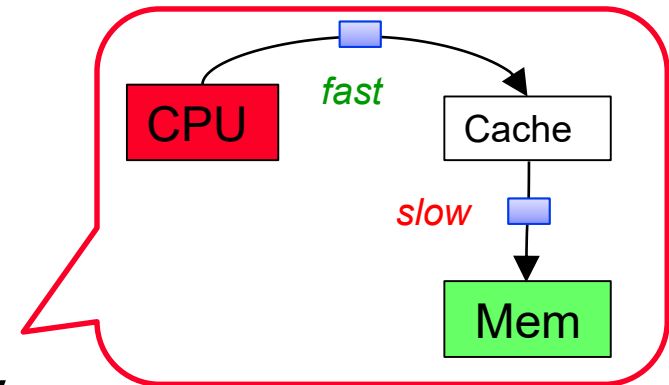
# Cache Misses

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- ❑ On cache hit, CPU proceeds normally
- ❑ On cache miss
  - | Stall the CPU pipeline
  - | Fetch block from next level of hierarchy
  - | Instruction cache miss
    - Restart instruction fetch
  - | Data cache miss
    - Complete data access

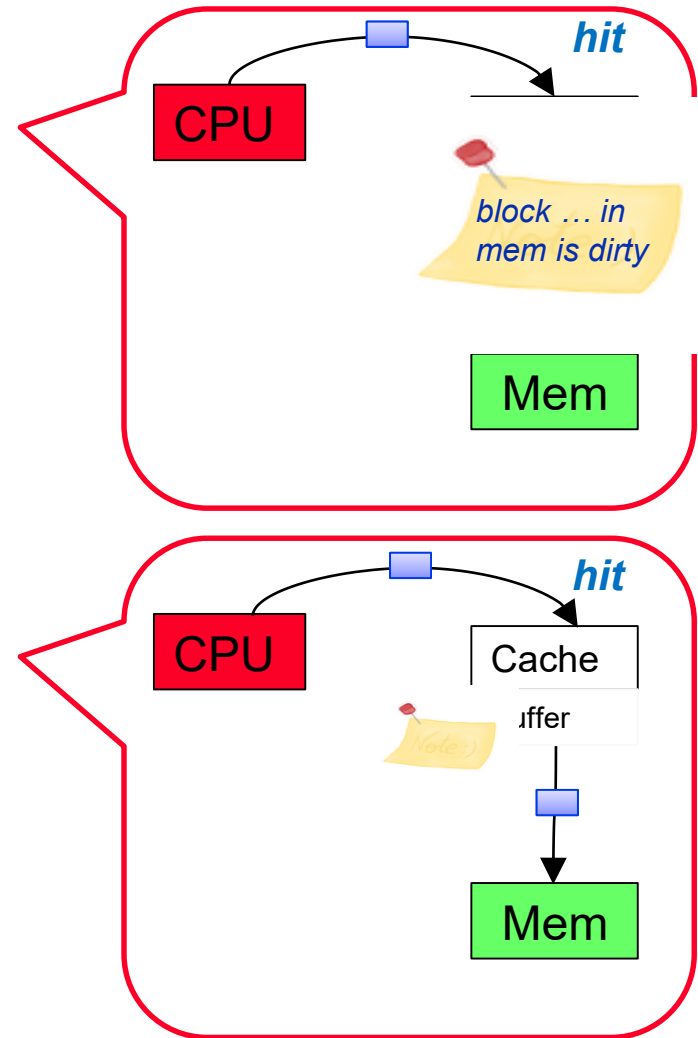
# Write-Through

- ❑ On data-write hit, could just update the block in cache
  - | But then cache and memory would be inconsistent
- ❑ Write through: also update memory
- ❑ But makes writes take longer
  - | e.g., if base CPI = **1**, **10%** of instructions are stores, write to memory takes **100** cycles
    - Effective CPI = **1** + **10%** × **100** = **11**
- ❑ Solution: write buffer
  - | Holds data waiting to be written to memory
  - | CPU continues immediately
    - Only stalls on write if write buffer is



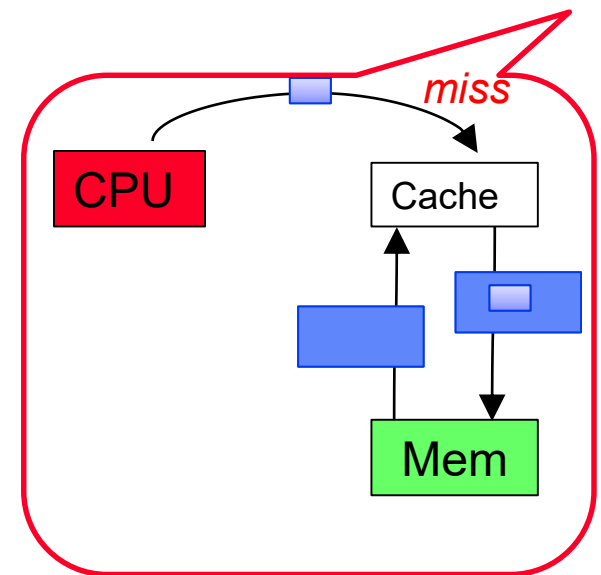
# Write-Back

- ❑ Alternative: On data-write hit, just update the block in cache
  - | Keep track of whether each block is dirty
- ❑ When a dirty block is replaced
  - | Write it back to memory
  - | Can use a write buffer to allow replacing block to be read first



# Write Allocation

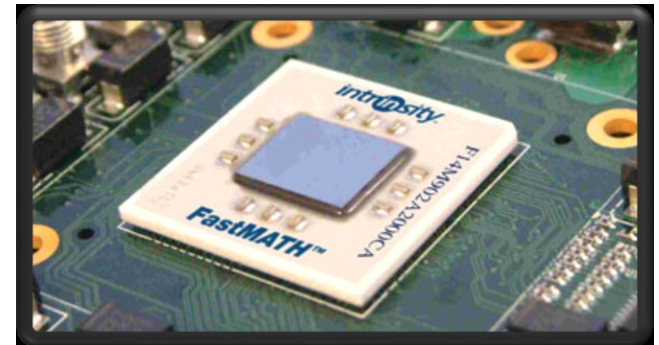
- ❑ What should happen on a write miss?
- ❑ Alternatives for write-through
  - | Allocate on miss: fetch the block
  - | Write around: don't fetch the block
    - Since programs often write a whole block before reading it (e.g., initialization)
- ❑ For write-back
  - | Usually fetch the block



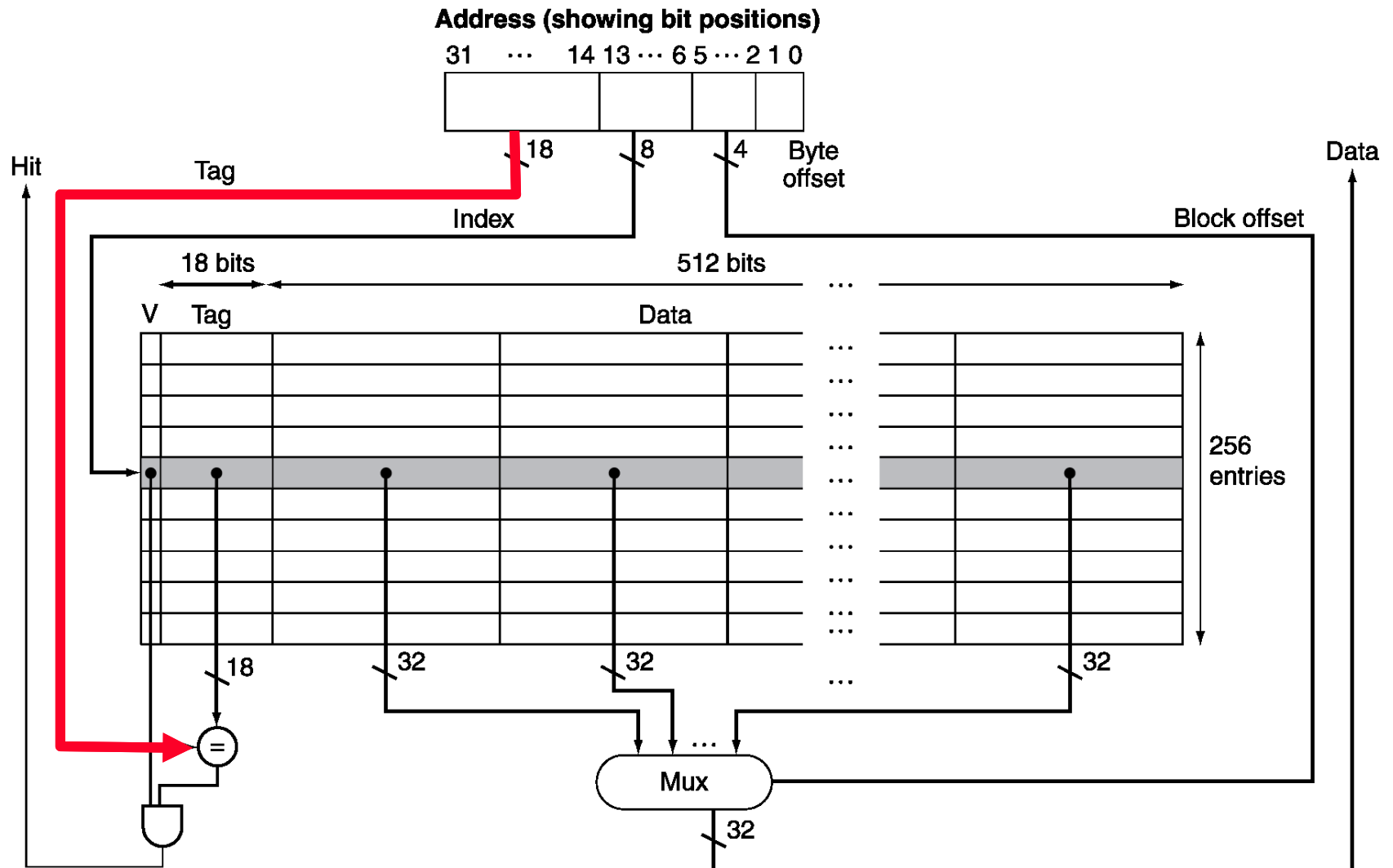
## Example: Intrinsic FastMATH

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- ❑ Embedded MIPS processor
  - | 12-stage pipeline
  - | Instruction and data access on each cycle
- ❑ Split cache: separate I-cache and D-cache
  - | Each 16KB:  $256 \text{ blocks} \times 16 \text{ words/block}$
  - | D-cache: write-through or write-back
- ❑ SPEC2000 miss rates
  - | I-cache: 0.4%
  - | D-cache: 11.4%
  - | Weighted average: 3.2%



# Example: Intrinsity FastMATH



## Example: Asus K43SJ

### ❑ Notebook: Asus K43SJ

| Intel(R) Core(TM) i5-2410M CPU @ 2.30GHz

```
Intel SNB 2295 MHz
L1 Cache: 32K 76495 MB/s
L2 Cache: 256K 34770 MB/s
L3 Cache: 3072K 26077 MB/s
Memory : 8170M 16047 MB/s
IMC : Intel(R) Core(TM) i5-24
Settings: RAM : 0 MHz (DDR3- 0)
```

=  $1/5.37297 \sim 0.18\text{ns}$

| Cache miss: Access time =  $1/0.07375 \sim 13.56\text{ns}$   
(75 times bigger)

```
tiennd@tiennd:~$ sudo hdparm -tT /dev/sda2

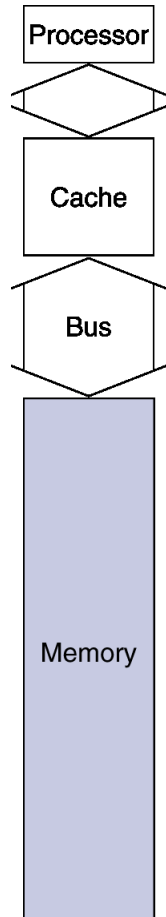
/dev/sda2:
Timing cached reads: 10740 MB in 2.00 seconds = 5372.97 MB/sec
Timing buffered disk reads: 222 MB in 3.01 seconds = 73.75 MB/sec
tiennd@tiennd:~$
```



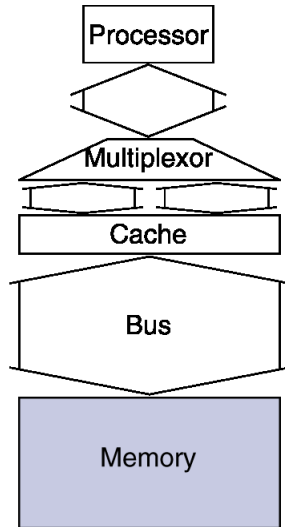
# Main Memory Supporting Caches

- ❑ Use DRAMs for main memory
  - | Fixed width (e.g., 1 word)
  - | Connected by fixed-width clocked bus
    - Bus clock is typically slower than CPU clock
- ❑ Example cache block read
  - | 1 bus cycle for address transfer
  - | 15 bus cycles per DRAM access
  - | 1 bus cycle per data transfer
- ❑ For 4-word block, 1-word-wide DRAM
  - | Miss penalty =  $1 + 4 \times 15 + 4 \times 1 = 65$  bus cycles
  - | Bandwidth = 16 bytes / 65 cycles = 0.25 B/cycle

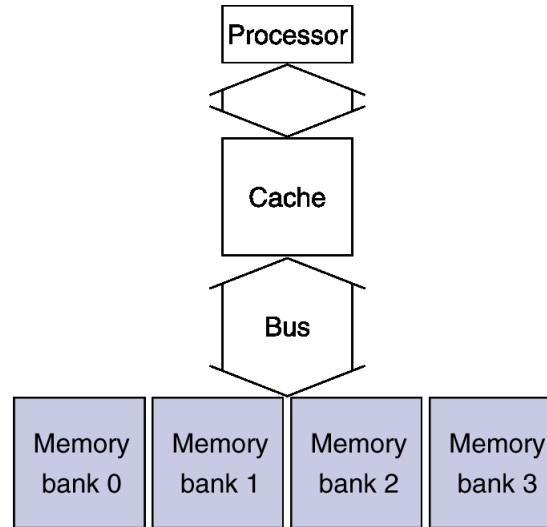
# Increasing Memory Bandwidth



a. One-word-wide memory organization



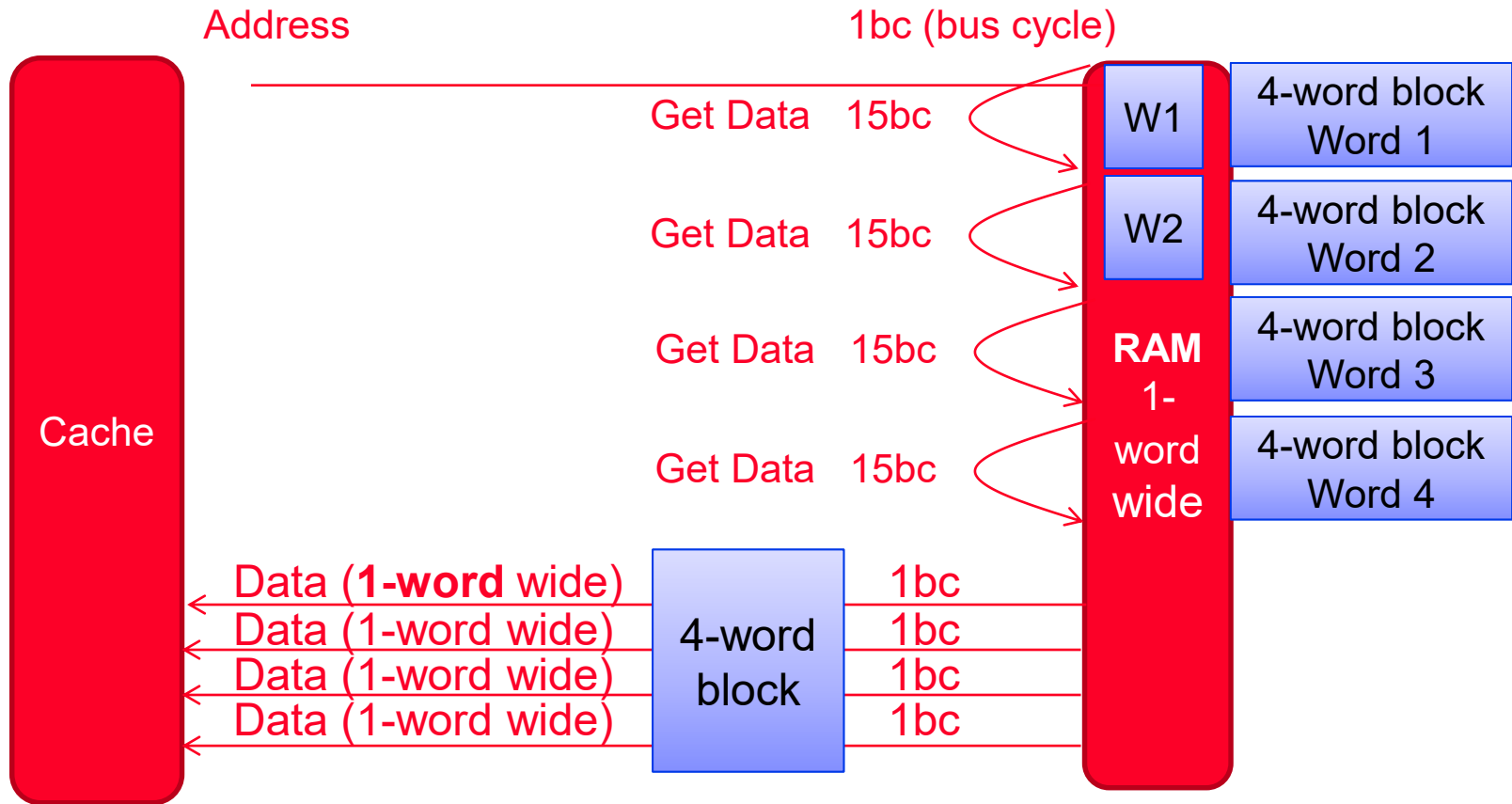
b. Wider memory organization



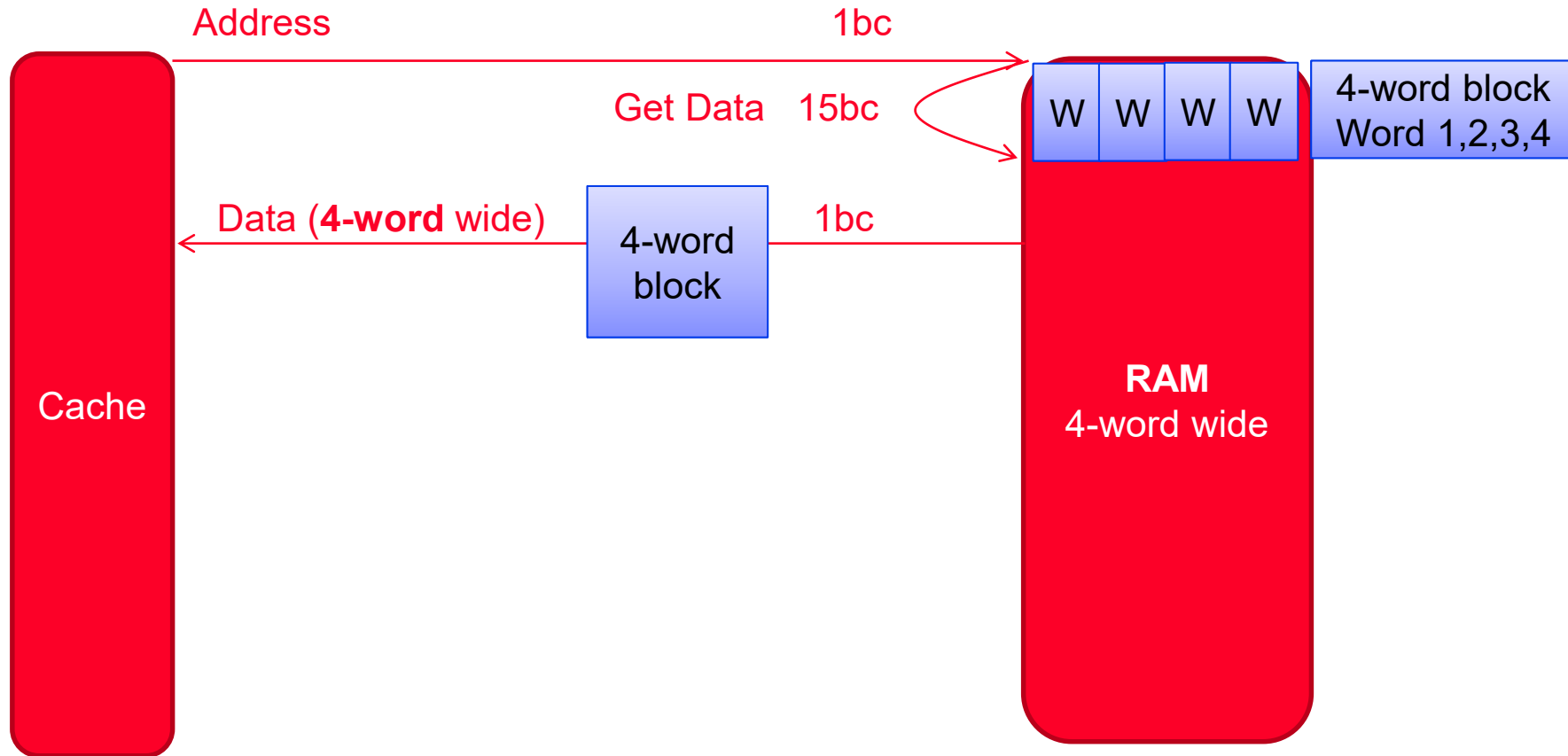
c. Interleaved memory organization

- **4-word wide memory**
  - Miss penalty =  $1 + 1 \times 15 + 1 \times 1 = 17$  bus cycles
  - Bandwidth =  $16 \text{ bytes} / 17 \text{ cycles} = 0.94 \text{ B/cycle}$
- **4-bank interleaved memory**
  - Miss penalty =  $1 + 1 \times 15 + 4 \times 1 = 20$  bus cycles
  - Bandwidth =  $16 \text{ bytes} / 20 \text{ cycles} = 0.8 \text{ B/cycle}$

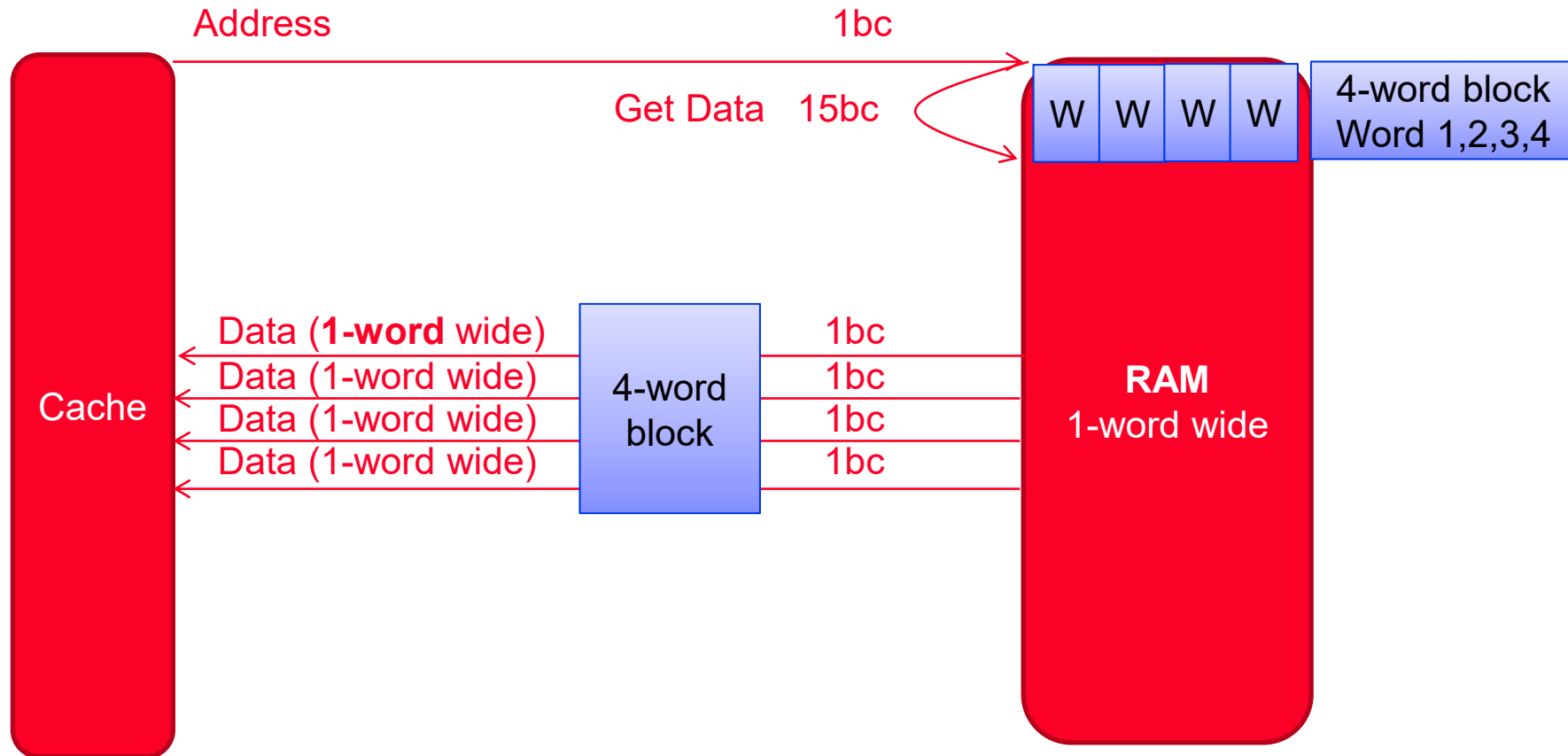
# 4-word block, 1-word wide memory (a)



# 4-word block, 4-word wide memory (b)

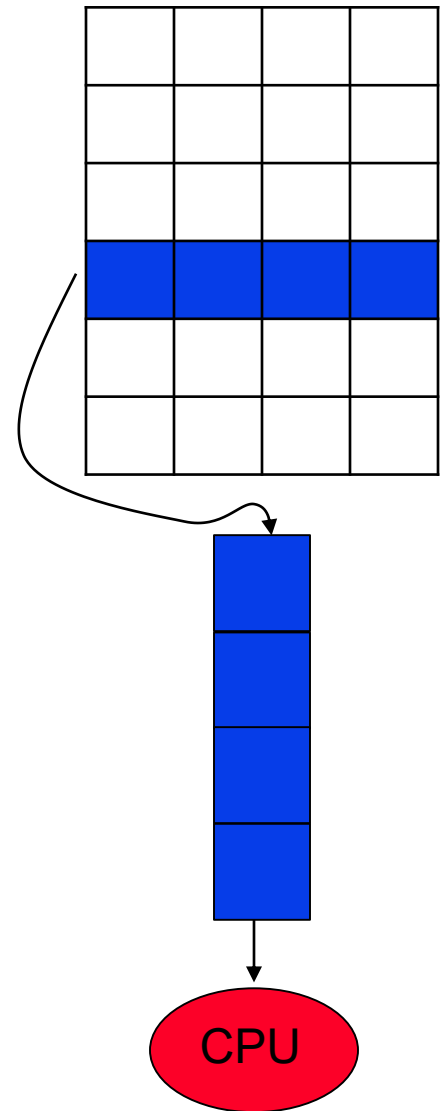


# 4-word block, 4 bank 1-word memory (c)



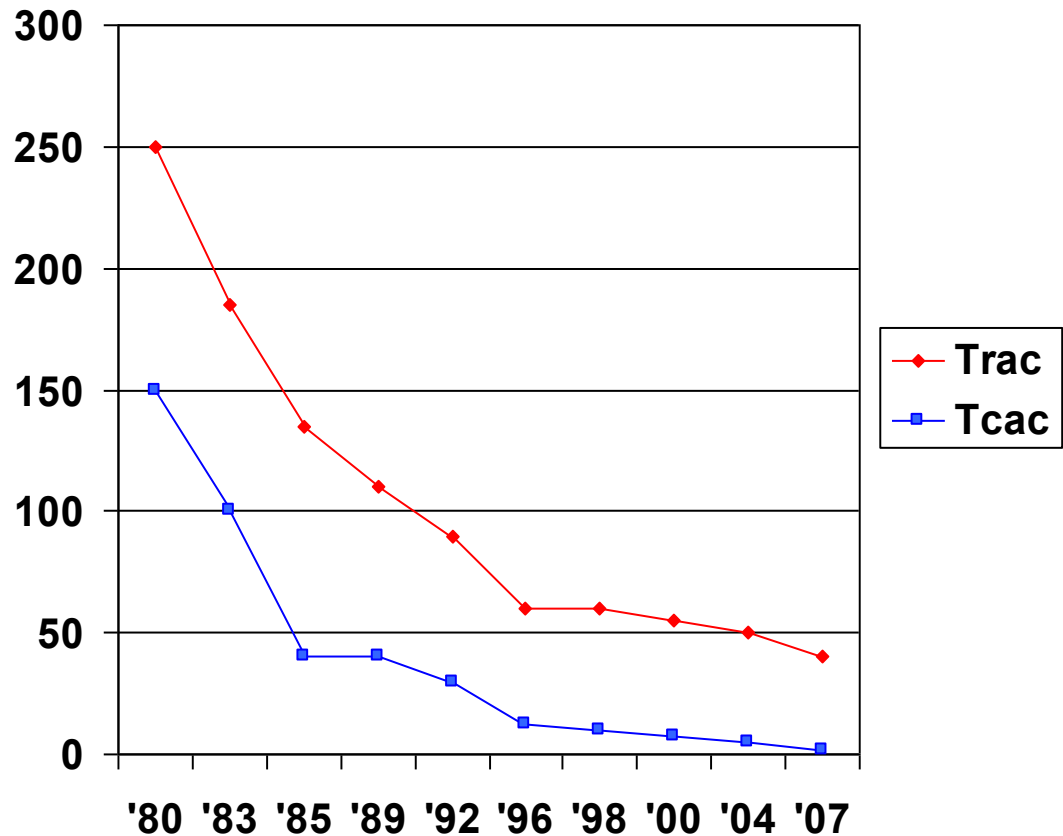
# Advanced DRAM Organization

- ❑ Bits in a DRAM are organized as a rectangular array
  - | DRAM accesses an entire row
  - | Burst mode: supply successive words from a row with reduced latency
- ❑ Double data rate (DDR) DRAM
  - | Transfer on rising and falling clock edges
- ❑ Quad data rate (QDR) DRAM
  - | Separate DDR inputs and outputs



# DRAM Generations

Year	Capacity	\$/GB
1980	64Kbit	\$1500000
1983	256Kbit	\$500000
1985	1Mbit	\$200000
1989	4Mbit	\$50000
1992	16Mbit	\$15000
1996	64Mbit	\$10000
1998	128Mbit	\$4000
2000	256Mbit	\$1000
2004	512Mbit	\$250
2007	1Gbit	\$50



# Measuring Cache Performance

- ❑ Components of CPU time
  - | Program execution cycles
    - Includes cache **hit** time
  - | Memory stall cycles
    - Mainly from cache **misses**
- ❑ With simplifying assumptions:


$$\begin{aligned} & \text{Memory stall cycles} \\ &= \frac{\text{Memory accesses}}{\text{Program}} \times \text{Miss rate} \times \text{Miss penalty} \\ &= \frac{\text{Instructions}}{\text{Program}} \times \frac{\text{Misses}}{\text{Instruction}} \times \text{Miss penalty} \end{aligned}$$



# Cache Performance Example

## □ Given

- | I-cache miss rate = 2%
- | D-cache miss rate = 4%
- | Miss penalty = 100 cycles
- | Base CPI (ideal cache) = 2
- | Load & stores are 36% of instructions



Tỷ lệ miss với cache dữ liệu	4%	
Số chu kì truy cập bộ nhớ	100	
Số chu kì/lệnh (hit 100%)	2	
Tỷ lệ lệnh truy cập bộ nhớ	36%	
Số chu kì đợi lệnh t.bình	2	
Số chu kì đợi dữ liệu t.bình	1.44	
CPI thực tế có trễ bộ nhớ	5.44	

## □ Miss cycles per instruction

- | I-cache:  $0.02 \times 100 \times 1 = 2$
- | D-cache:  $0.04 \times 100 \times 0.36 = 1.44$

## □ Actual CPI = $2 + 2 + 1.44 = 5.44$

- | Ideal CPU is  $5.44/2 = 2.72$  times faster

# Average Access Time

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- ❑ Hit time is also important for performance
- ❑ Average memory access time (AMAT)
  - |  $AMAT = \text{Hit time} + \text{Miss rate} \times \text{Miss penalty}$
- ❑ Example
  - | CPU with 1ns clock, hit time = 1 cycle, miss penalty = 20 cycles, l-cache miss rate = 5%
  - |  $AMAT = (1 + 5\% \times 20) \times 1 = 2\text{ns}$ 
    - 2 cycles per instruction

# Performance Summary

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- ❑ When CPU performance increased
  - | Miss penalty becomes more significant
- ❑ Decreasing base CPI
  - | Greater proportion of time spent on memory stalls
- ❑ Increasing clock rate
  - | Memory stalls account for more CPU cycles
- ❑ Can't neglect cache behavior when evaluating system performance

# Associative Caches

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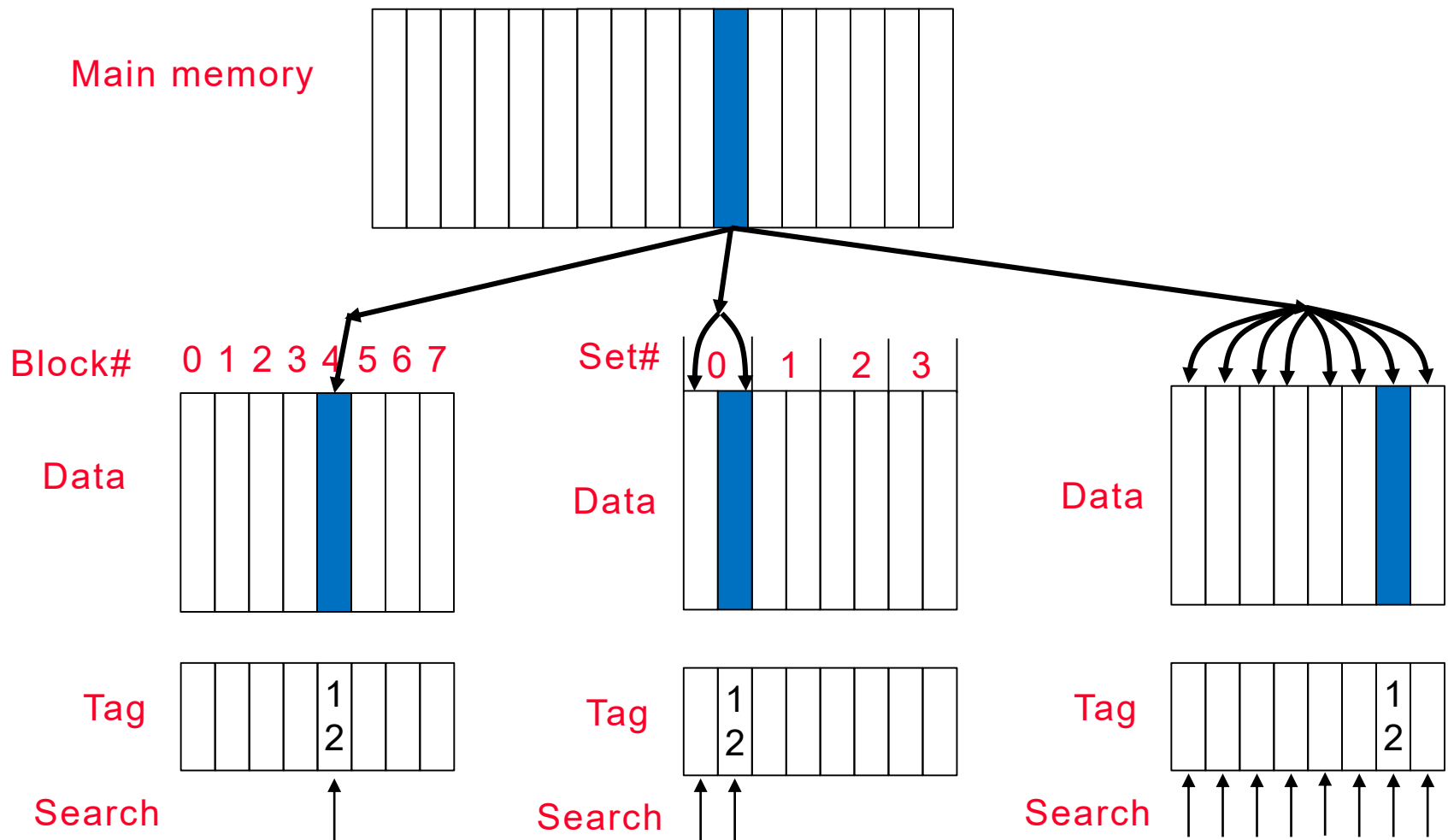
## ❑ Fully associative

- | Allow a given block to go in any cache entry
- | Requires all entries to be searched at once
- | Comparator per entry (expensive)

## ❑ $n$ -way set associative

- | Each set contains  $n$  entries
- | Block number determines which set
  - (Block number) modulo (#Sets in cache)
- | Search all entries in a given set at once
- |  $n$  comparators (less expensive)

# Associative Cache Example



# Spectrum of Associativity

❑ For a cache with 8 entries

**One-way set associative  
(direct mapped)**

Block	Tag	Data
0		
1		
2		
3		
4		
5		
6		
7		

**Two-way set associative**

Set	Tag	Data	Tag	Data
0				
1				
2				
3				

**Four-way set associative**

Set	Tag	Data	Tag	Data	Tag	Data	Tag	Data
0								
1								

**Eight-way set associative (fully associative)**

Tag	Data	Tag	Data	Tag	Data	Tag	Data	Tag	Data	Tag	Data	Tag	Data	Tag	Data

# Associativity Example

- ❑ Compare 4-block caches
  - | Direct mapped, 2-way set associative, fully associative
  - | Block access sequence: 0, 8, 0, 6, 8
- ❑ Direct mapped

Access sequence	Block address	Cache index	Hit/miss	Cache content after access			
				0	1	2	3
1	0	0	miss	Mem[0]			
2	8	0	miss	Mem[8]			
3	0	0	miss	Mem[0]			
4	6	2	miss	Mem[0]		Mem[6]	
5	8	0	miss	Mem[8]		Mem[6]	

 %4

# Associativity Example

## ❑ 2-way set associative

Access sequence	Block address	Cache index	Hit/miss	Cache content after access			
				Set 0		Set 1	
1	0	0	miss	Mem[0]			
2	8	0	miss	Mem[0]	Mem[8]		
3	0	0	hit	Mem[0]	Mem[8]		
4	6	0	miss	Mem[0]	Mem[6]		
5	8	0	miss	Mem[8]	Mem[6]		

$\%2$

## ■ Fully associative

Access sequence	Block address		Hit/miss	Cache content after access			
1	0		miss	Mem[0]			
2	8		miss	Mem[0]	Mem[8]		
3	0		hit	Mem[0]	Mem[8]		
4	6		miss	Mem[0]	Mem[8]	Mem[6]	
5	8		hit	Mem[0]	Mem[8]	Mem[6]	

$\%1$



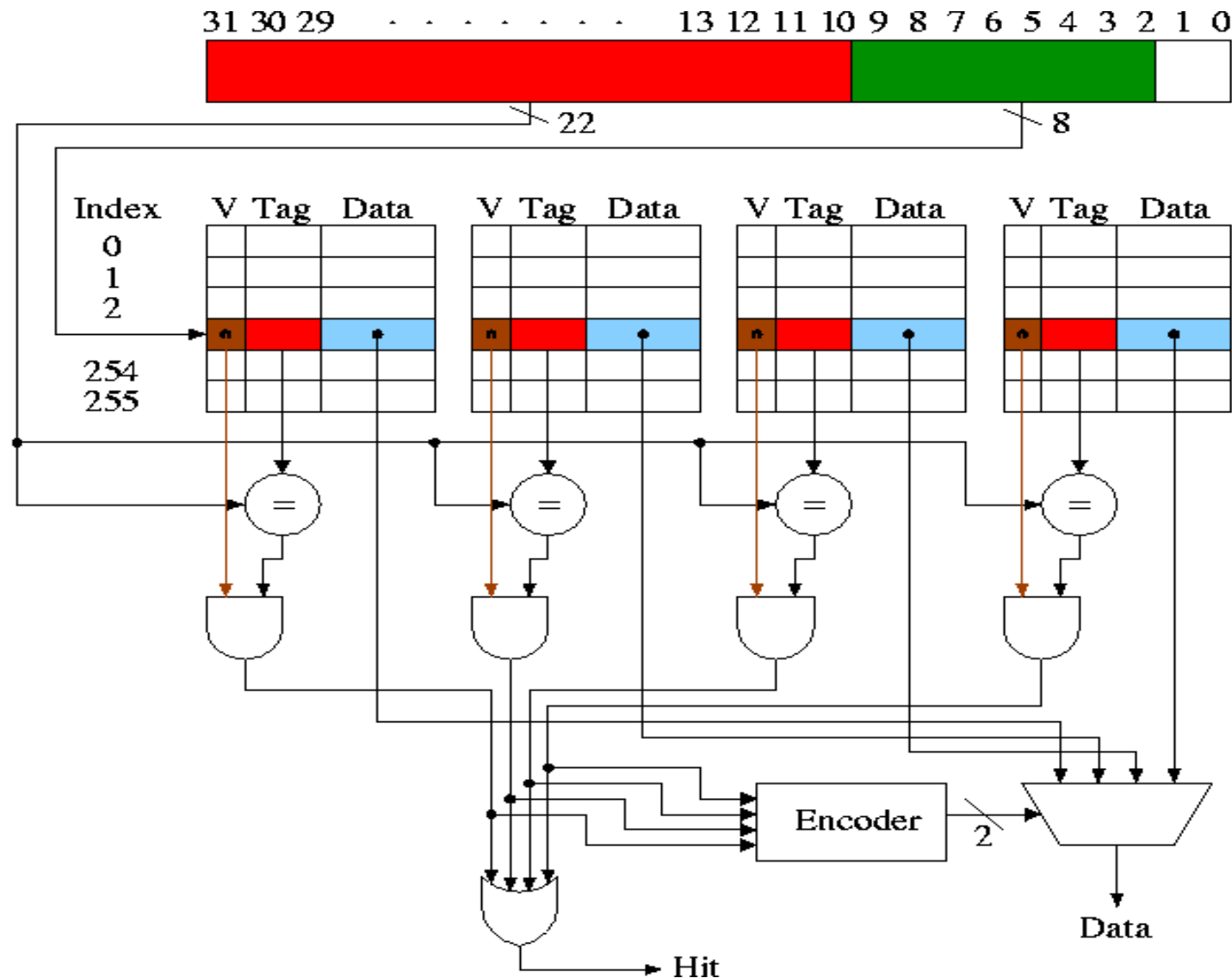
# How Much Associativity

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- ❑ Increased associativity decreases miss rate
  - | But with diminishing returns
- ❑ Simulation of a system with 64KB D-cache, 16-word blocks, SPEC2000
  - | 1-way: 10.3%
  - | 2-way: 8.6%
  - | 4-way: 8.3%
  - | 8-way: 8.1%

[di'miniʃɪp] (adj) hạ bớt, giảm bớt

# Set Associative Cache Organization



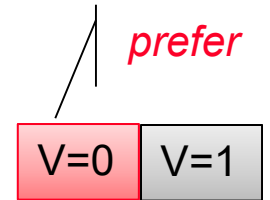
# Replacement Policy

---

- ❑ Direct mapped: no choice

- ❑ Set associative

- | Prefer non-valid entry, if there is one
- | Otherwise, choose among entries in the set



- ❑ Least-recently used (LRU)

- | Choose the one unused for the longest time
  - Simple for 2-way, manageable for 4-way, too hard beyond that

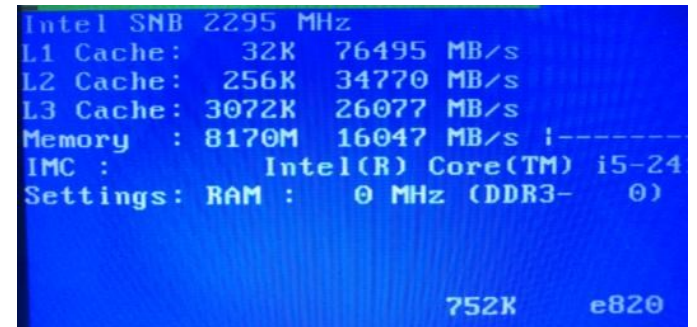
- ❑ Random

- | Gives approximately the same performance as LRU for high associativity

# Multilevel Caches

---

- ❑ Primary cache attached to CPU
  - | Small, but fast
- ❑ Level-2 cache services misses from primary cache
  - | Larger, slower, but still faster than main memory
- ❑ Main memory services L-2 cache misses
- ❑ Some high-end systems include L-3 cache



A screenshot of a system information window with a blue background and white text. It displays various hardware specifications including CPU speed, cache sizes, and memory details.

Component	Value
Intel SNB	2295 MHz
L1 Cache	32K 76495 MB/s
L2 Cache	256K 34770 MB/s
L3 Cache	3072K 26077 MB/s
Memory	8170M 16047 MB/s
IMC	Intel(R) Core(TM) i5-24
Settings: RAM	0 MHz (DDR3- 0)

752K e820

# Multilevel Cache Example

---

## □ Given

- | CPU base CPI = **1**, clock rate = **4GHz**
- | Miss rate/instruction = **2%**
- | Main memory access time = **100ns**

## □ With just primary cache

- | Miss penalty = **100ns/0.25ns** = 400 cycles
- | Effective CPI = **1** + **0.02** × 400 = 9

## Example (cont.)

---

- ❑ Now add L-2 cache
  - | Access time = 5ns
  - | Global miss rate to main memory = 0.5%
- ❑ Primary miss with L-2 hit (*Miss L1, hit L2*)
  - | Penalty = 5ns/0.25ns = 20 cycles
- ❑ Primary miss with L-2 miss (*Miss L1 & L2*)
  - | Extra penalty = 400 cycles
- ❑  $\text{CPI} = 1 + 0.02 \times 20 + 0.005 \times 400 = 3.4$
- ❑ Performance ratio =  $9/3.4 = 2.6$

# Multilevel Cache Considerations

## ❑ Primary cache

- | Focus on minimal hit time

## ❑ L-2 cache

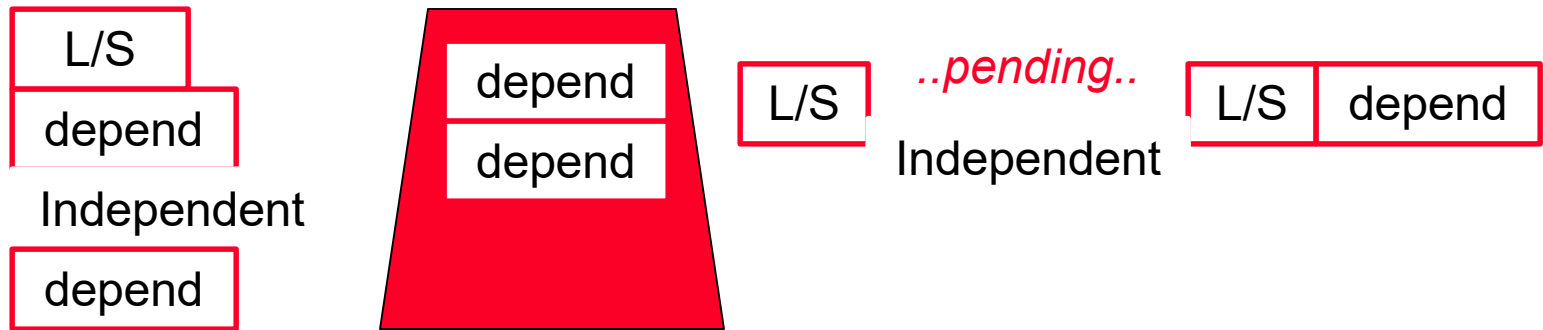
- | Focus on low miss rate to avoid main memory access
- | Hit time has less overall impact

## ❑ Results

- | L-1 cache usually smaller than a single cache
- | L-1 block size smaller than L-2 block size

# Interactions with Advanced CPUs

- ❑ Out-of-order CPUs can execute instructions during cache miss
  - | Pending store stays in load/store unit
  - | Dependent instructions wait in reservation stations
    - Independent instructions continue

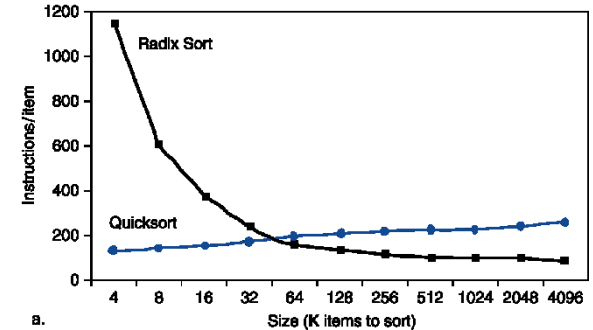


- ❑ Effect of miss depends on program data flow
  - | Much harder to analyse
  - | Use system simulation

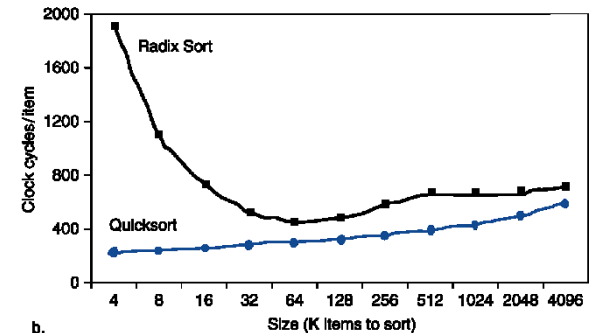


# Interactions with Software

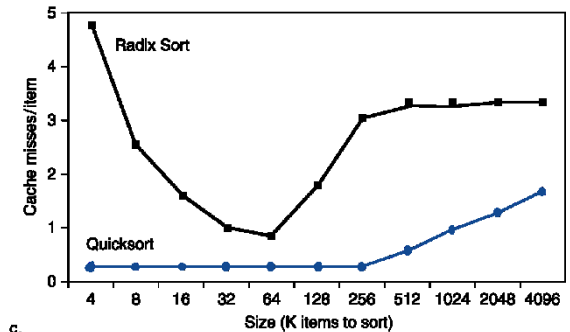
- ❑ Misses depend on memory access patterns
  - | Algorithm behavior
  - | Compiler optimization for memory access



a.



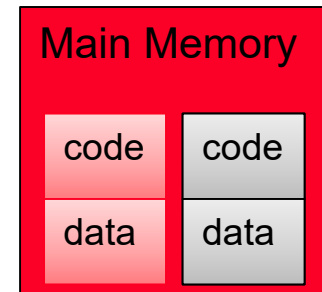
b.



c.

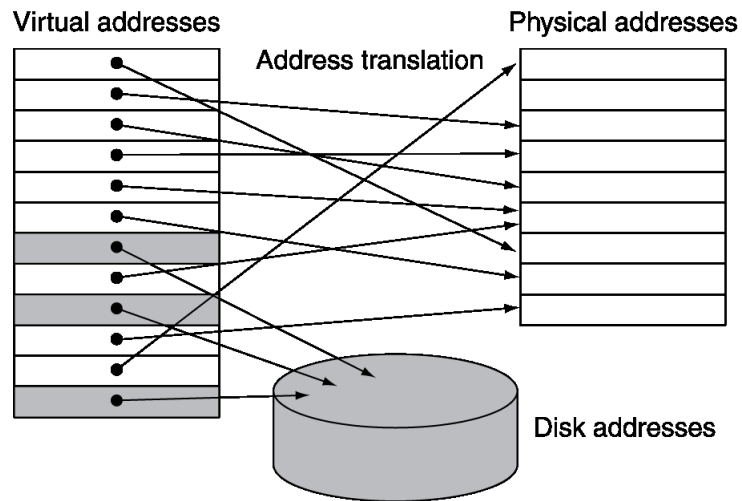
## Virtual Memory

- ❑ Use main memory as a “cache” for secondary (disk) storage
  - | Managed jointly by **CPU hardware** and the **operating system** (OS)
  
- ❑ Programs share main memory
  - | Each gets a private virtual address space holding its frequently used code and data
  - | Protected from other programs
  
- ❑ CPU and OS translate virtual addresses to physical addresses
  - | VM “block” is called a page
  - | VM translation “miss” is called a **page fault**

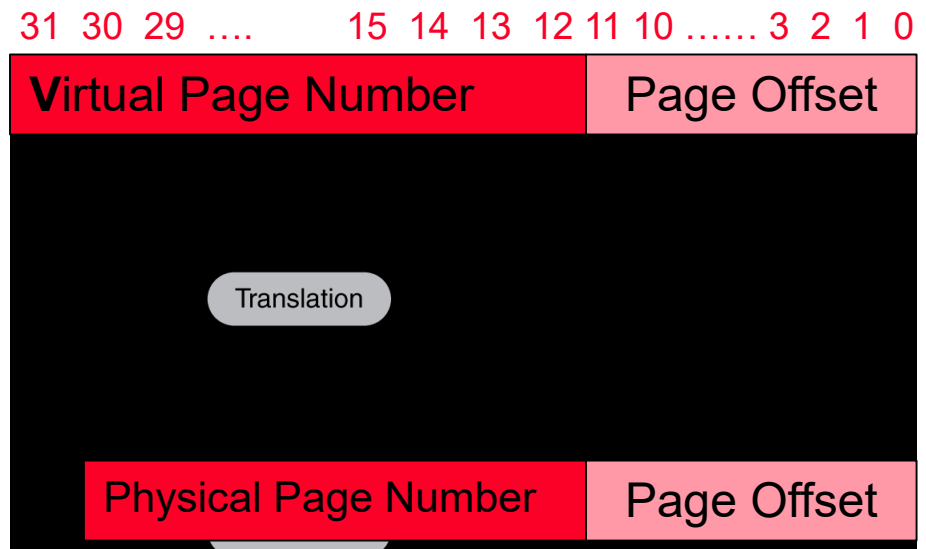


# Address Translation

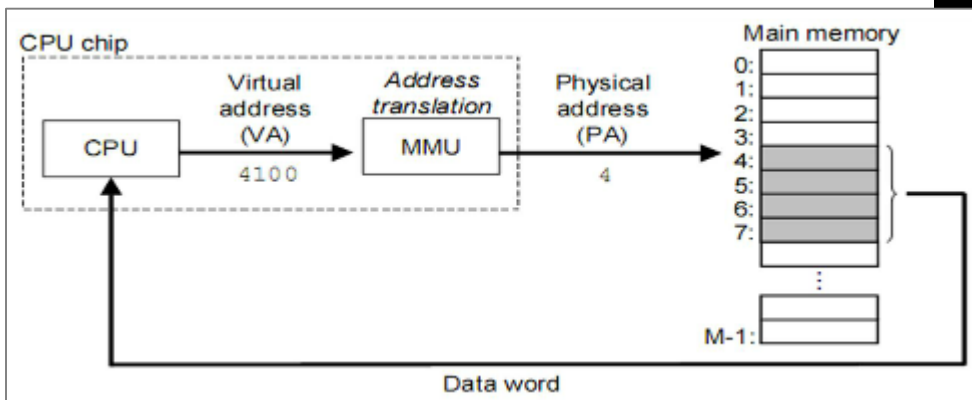
- ❑ Fixed-size pages (e.g., 4K)



Virtual Address



Physical Address



# Page Fault Penalty

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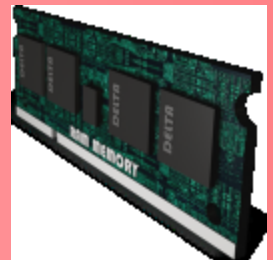
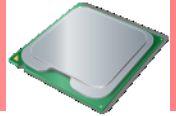
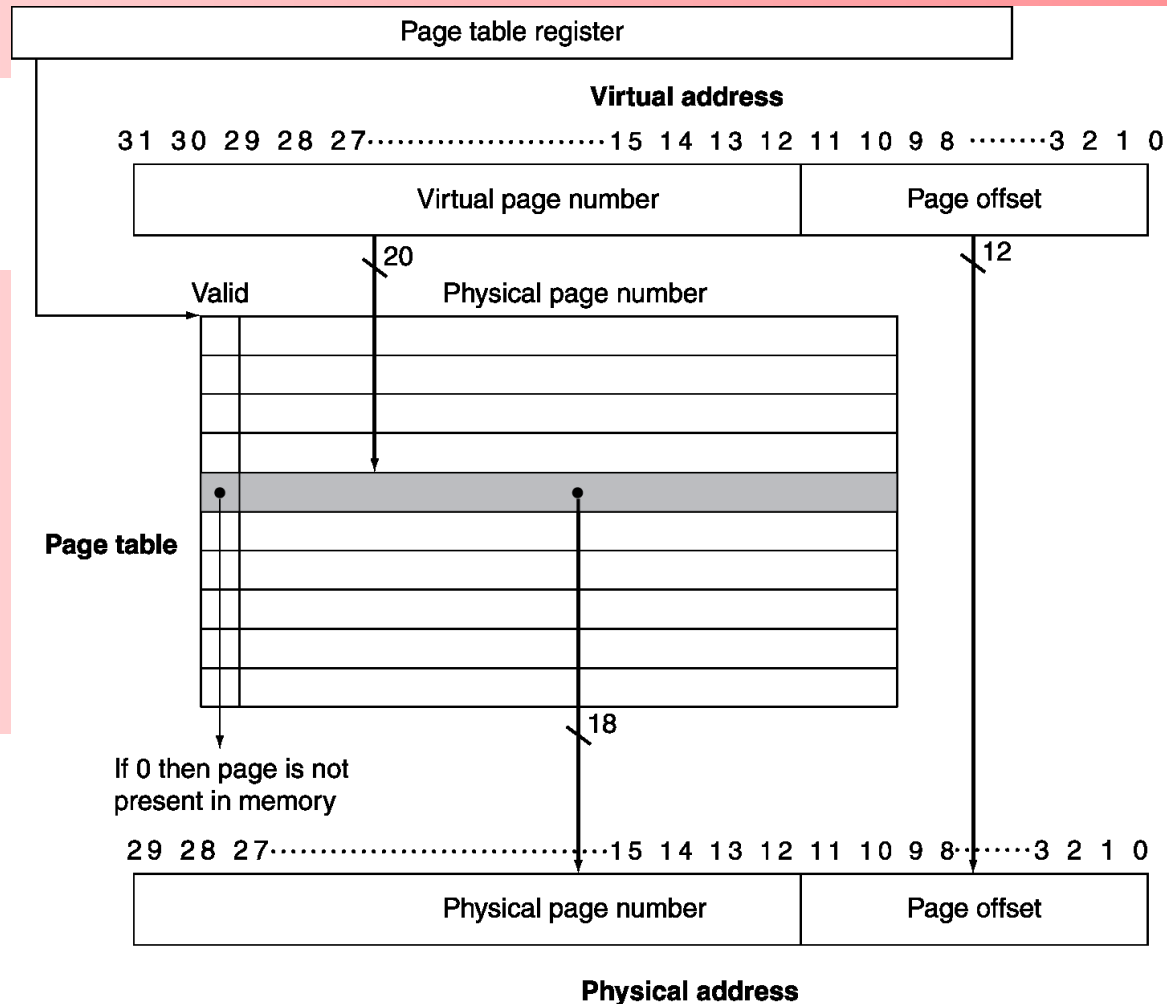
- ❑ On page fault, the page must be fetched from disk
  - | Takes millions of clock cycles
  - | Handled by OS code
- ❑ Try to minimize page fault rate
  - | Fully associative placement
  - | Smart replacement algorithms

# Page Tables

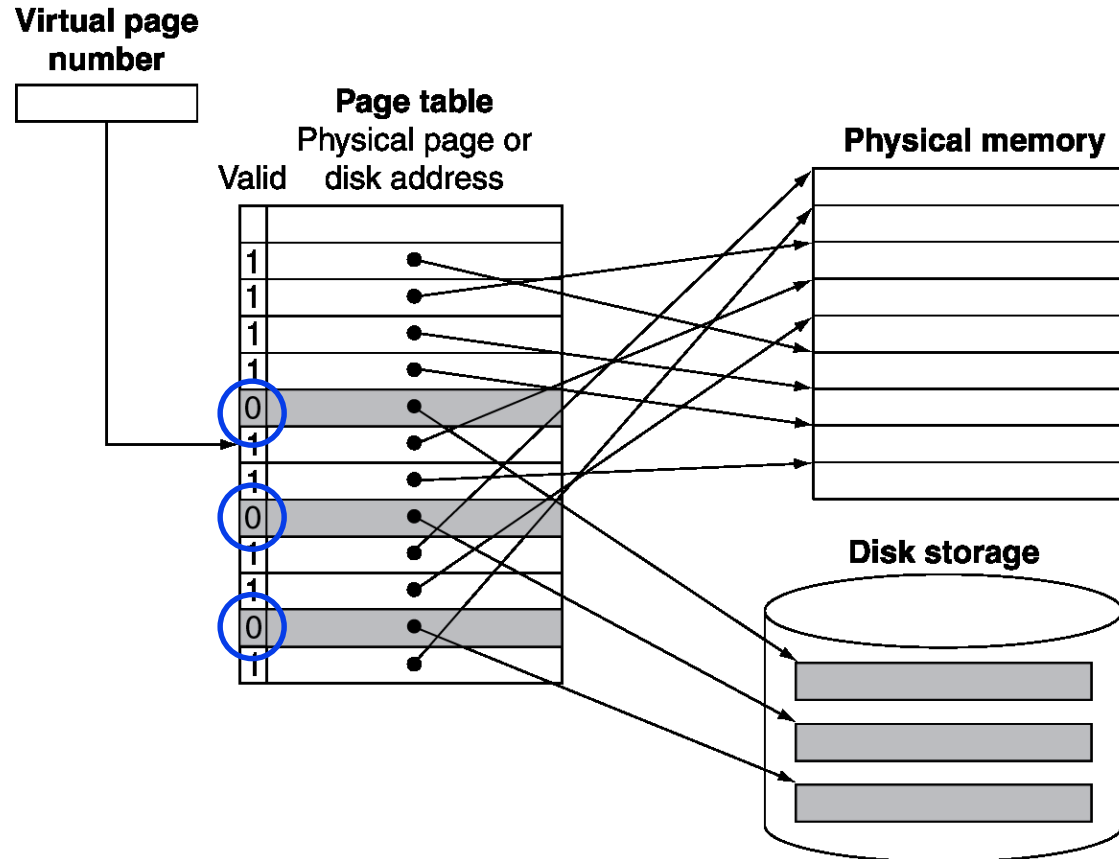
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- ❑ Stores placement information
  - | Array of **P**age **T**able **E**ntries, indexed by virtual page number
  - | Page table register *in CPU* (CR3) points to page table in *physical memory*
- ❑ If page is present in memory
  - | PTE stores the physical page number
  - | Plus other status bits (referenced, dirty, ...)
- ❑ If page is not present
  - | PTE can refer to location in swap space on disk

# Translation Using a Page Table



# Mapping Pages to Storage



# Replacement and Writes

---

- ❑ To reduce page fault rate, prefer least-recently used (LRU) replacement
  - | **Reference bit** (aka use bit) in PTE set to 1 on access to page
  - | Periodically cleared to 0 by OS
  - | A page with reference bit = 0 has not been used recently
- ❑ Disk writes take millions of cycles
  - | Block at once, not individual locations
  - | Write through is impractical
  - | Use write-back
  - | **Dirty bit** in PTE set when page is written

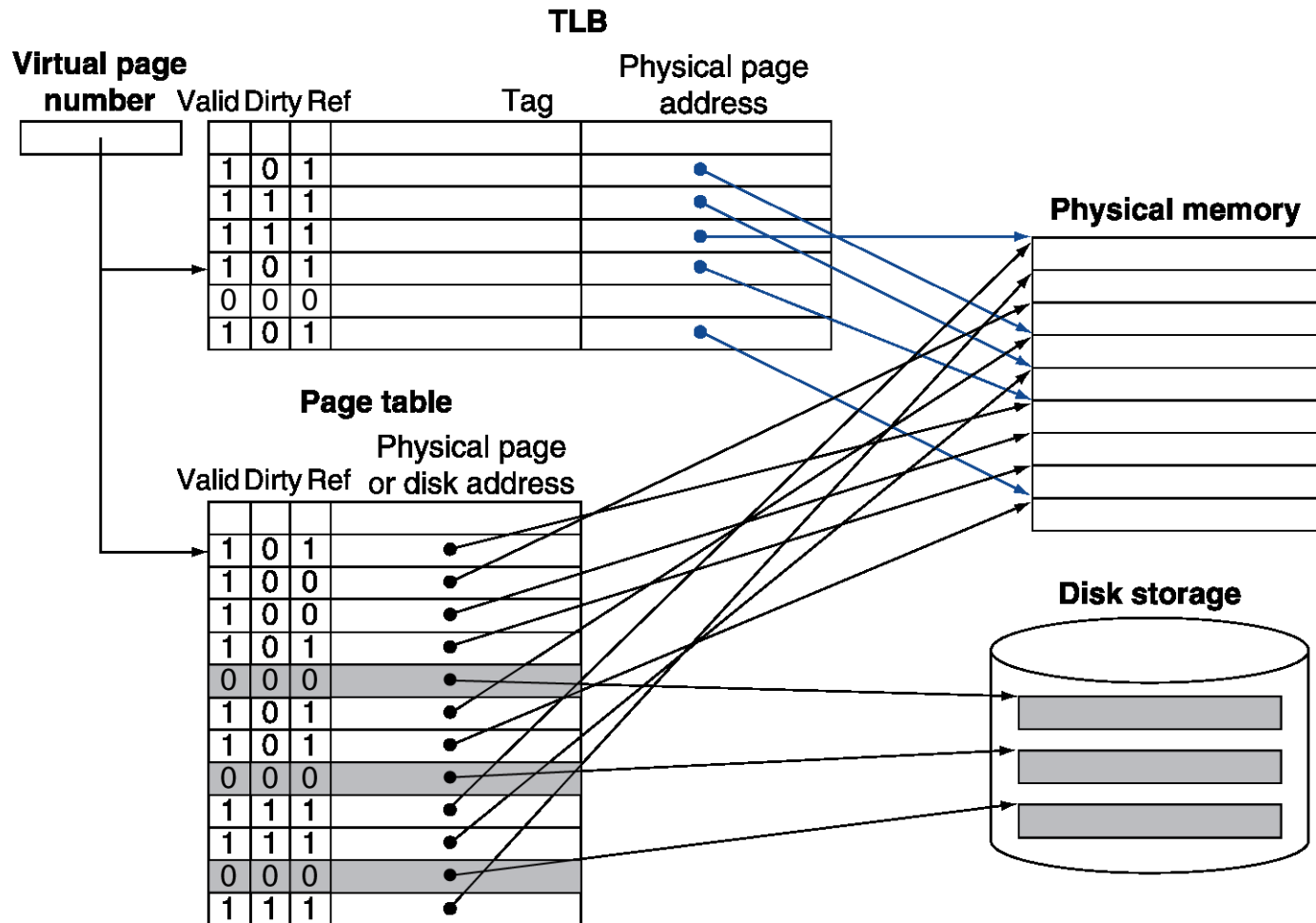


## Fast Translation Using a TLB

---

- ❑ Address translation would appear to require extra memory references
  - | One to access the PTE
  - | Then the actual memory access
- ❑ But access to page tables has good locality
  - | So use a fast cache of PTEs **within the CPU**
  - | Called a Translation Look-aside Buffer (TLB)
  - | Typical: 16–512 PTEs, 0.5–1 cycle for hit, 10–100 cycles for miss, 0.01%–1% miss rate
  - | Misses could be handled by hardware or software

# Fast Translation Using a TLB



# TLB Misses

---

- ❑ If page is in memory
  - | Load the PTE from memory and retry
  - | Could be handled in hardware
    - Can get complex for more complicated page table structures
  - | Or in software
    - Raise a special exception, with optimized handler
- ❑ If page is not in memory (page fault)
  - | OS handles fetching the page and updating the page table
  - | Then restart the faulting instruction

# TLB Miss Handler

---

- ❑ TLB miss indicates
  - | Page present, but PTE not in TLB
  - | Page not present
- ❑ Must recognize TLB miss before destination register overwritten
  - | Raise exception
- ❑ Handler copies PTE from memory to TLB
  - | Then restarts instruction
  - | If page not present, page fault will occur

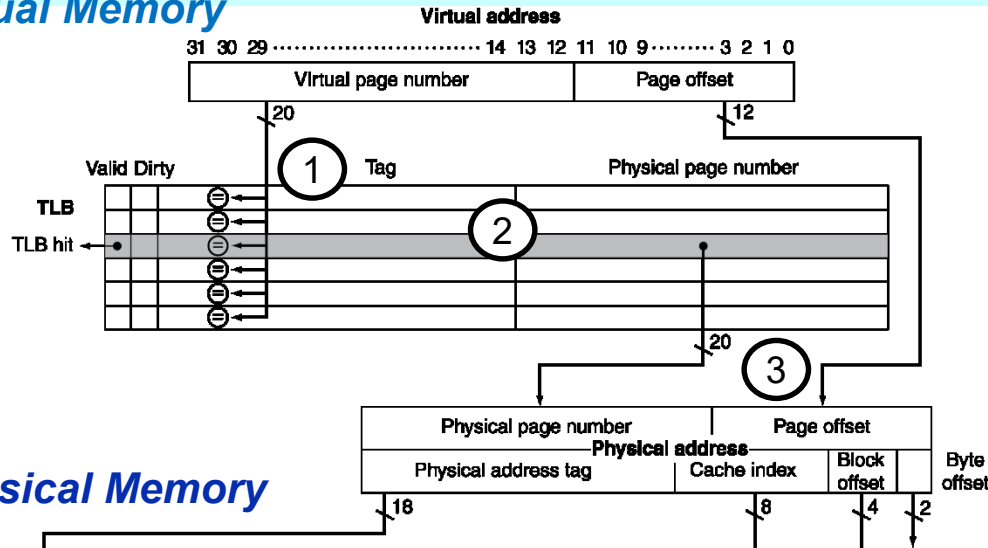
## Page Fault Handler

---

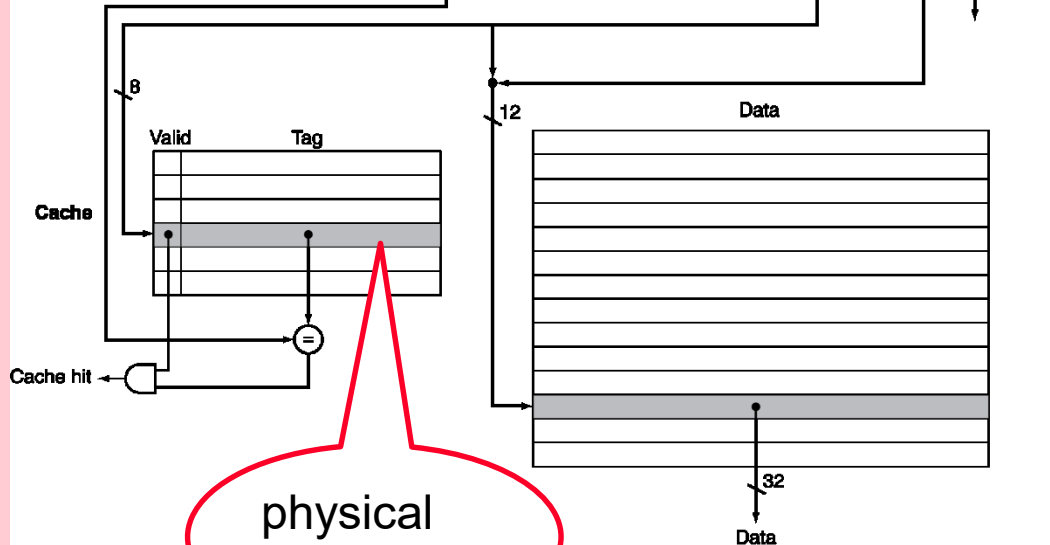
- ❑ Use faulting virtual address to find PTE
- ❑ Locate page on disk
- ❑ Choose page to replace
  - | If dirty, write to disk first (*reread write back*)
- ❑ Read page into memory and update page table
- ❑ Make process runnable again
  - | Restart from faulting instruction

# TLB and Cache Interaction

## Virtual Memory



## Physical Memory



❑ If cache tag uses physical address

| Need to translate before cache lookup

❑ Alternative: use virtual address tag

| Complications due to aliasing

- Different virtual addresses for shared physical address

physical  
or virtual?

# Memory Protection

---

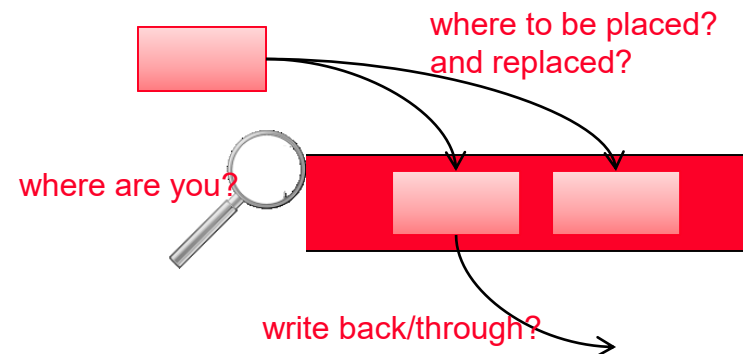
- ❑ Different tasks can share parts of their virtual address spaces
  - | But need to protect against errant access
  - | Requires OS assistance
- ❑ Hardware support for OS protection
  - | Privileged supervisor mode (aka kernel mode)
  - | Privileged instructions
  - | Page tables and other state information only accessible in supervisor mode
  - | System call exception (e.g., syscall in MIPS)

errant /'erənt/ sai lầm

# The Memory Hierarchy

## The BIG Picture

- ❑ Common principles apply at all levels of the memory hierarchy
  - | Based on notions of caching
- ❑ At each level in the hierarchy
  - | Block placement
  - | Finding a block
  - | Replacement on a miss
  - | Write policy





# Block Placement

---

- ❑ Determined by associativity
  - | Direct mapped (1-way associative)
    - One choice for placement
  - | n-way set associative
    - n choices within a set
  - | Fully associative
    - Any location
- ❑ Higher associativity reduces miss rate
  - | Increases complexity, cost, and access time

## Finding a Block

---

Associativity	Location method	Tag comparisons
Direct mapped	Index	1
n-way set associative	Set index, then search entries within the set	n
Fully associative	Search all entries	#entries
	Full lookup table	0

### ❑ Hardware caches

- | Reduce comparisons to reduce cost

### ❑ Virtual memory

- | Full table lookup makes full associativity feasible
- | Benefit in reduced miss rate

# Replacement

---

- ❑ Choice of entry to replace on a miss
  - | Least recently used (LRU)
    - Complex and costly hardware for high associativity
  - | Random
    - Close to LRU, easier to implement
- ❑ Virtual memory
  - | LRU approximation with hardware support

# Write Policy

---

## ❑ Write-through

- | Update both upper and lower levels
- | Simplifies replacement, but may require write buffer

## ❑ Write-back

- | Update upper level only
- | Update lower level when block is replaced
- | Need to keep more state

## ❑ Virtual memory

- | Only write-back is feasible, given disk write latency

# Sources of Misses

---

## ❑ Compulsory misses (aka cold start misses)

- | First access to a block



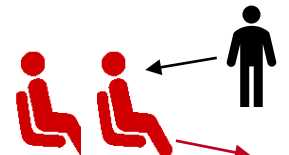
## ❑ Capacity misses

- | Due to finite cache size
- | A replaced block is later accessed again

compulsory /kəm'pʌlsəri/:  
bắt buộc

## ❑ Conflict misses (aka collision misses)

- | In a non-fully associative cache
- | Due to competition for entries in a set
- | Would not occur in a fully associative cache of the same total size



# Cache Design Trade-offs

---

Design change	Effect on miss rate	Possible Negative performance effect
Increase cache size	Decrease capacity misses	May increase access time
Increase associativity	Decrease conflict misses	May increase access time
Increase block size	Decrease compulsory misses	Increases miss penalty. For very large block size, may increase miss rate due to pollution.

## Virtual Machines

- ❑ Host computer emulates guest operating system and machine resources
  - | Improved isolation of multiple guests
  - | Avoids security and reliability problems
  - | Aids sharing of resources
- ❑ Virtualization has some performance impact
  - | Feasible with modern high-performance computers
- ❑ Examples
  - | IBM VM/370 (1970s technology!)
  - | VMWare
  - | Microsoft Virtual PC (Hyper-V)



# Virtual Machine Monitor

---

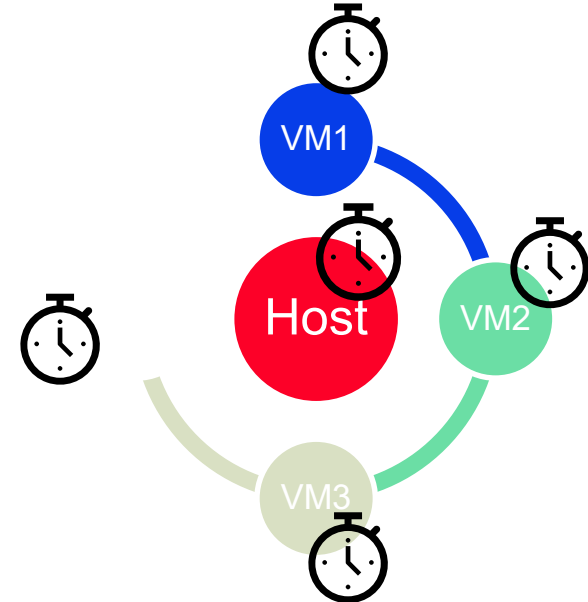
- ❑ Maps virtual resources to physical resources
  - | Memory, I/O devices, CPUs
- ❑ Guest code runs on native machine in user mode
  - | Traps to VMM on privileged instructions and access to protected resources
- ❑ Guest OS may be different from host OS
- ❑ VMM handles real I/O devices
  - | Emulates generic virtual I/O devices for guest



## Example: Timer Virtualization

---

- ❑ In native machine, on timer interrupt
  - | OS suspends current process, handles interrupt, selects and resumes next process
- ❑ With Virtual Machine Monitor
  - | VMM suspends current VM, handles interrupt, selects and resumes next VM
- ❑ If a VM requires timer interrupts
  - | VMM emulates a virtual timer
  - | Emulates interrupt for VM when physical timer interrupt occurs



# Instruction Set Support

---

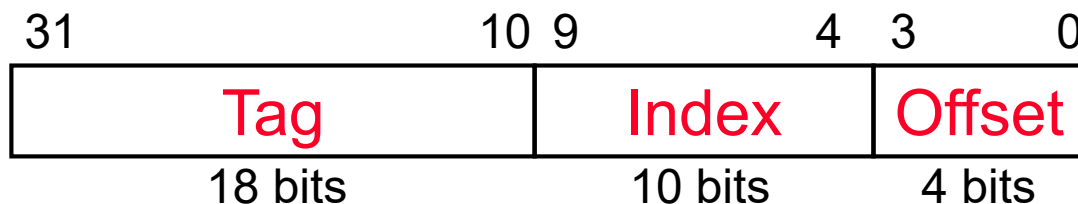
- ❑ User and System modes
- ❑ Privileged instructions only available in system mode
  - | Trap to system if executed in user mode
- ❑ All physical resources only accessible using privileged instructions
  - | Including page tables, interrupt controls, I/O registers
- ❑ Renaissance of virtualization support
  - | Current ISAs (e.g., x86) adapting

**IBM 370, June 30, 1970**

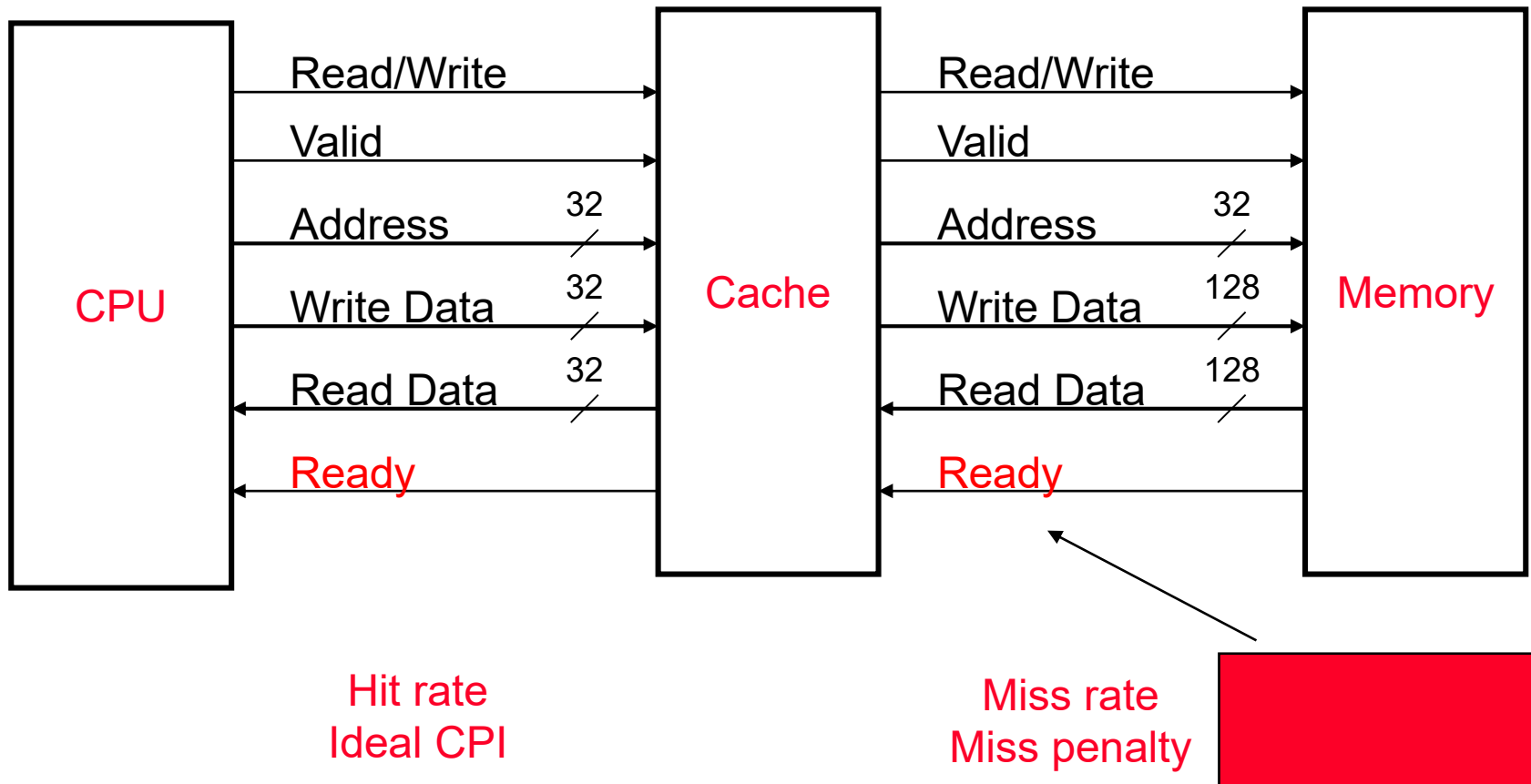


## Cache Control

- ❑ Example cache characteristics
  - | Direct-mapped, write-back, write allocate
  - | Block size: 4 words (16 bytes)
  - | Cache size: 16 KB (1024 blocks)
  - | 32-bit byte addresses
  - | Valid bit and dirty bit per block
  - | Blocking cache
    - CPU waits until access is complete

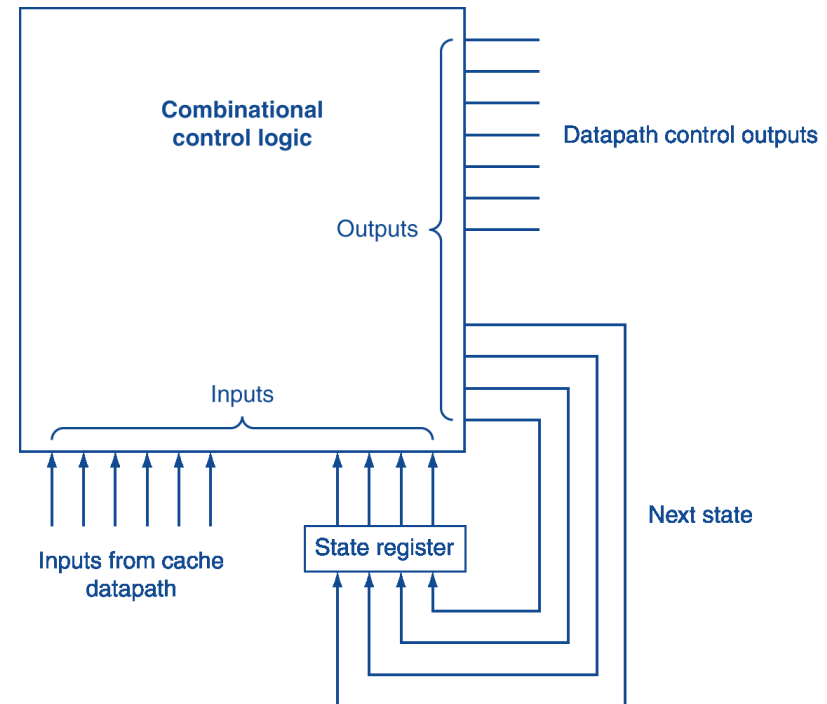


# Interface Signals

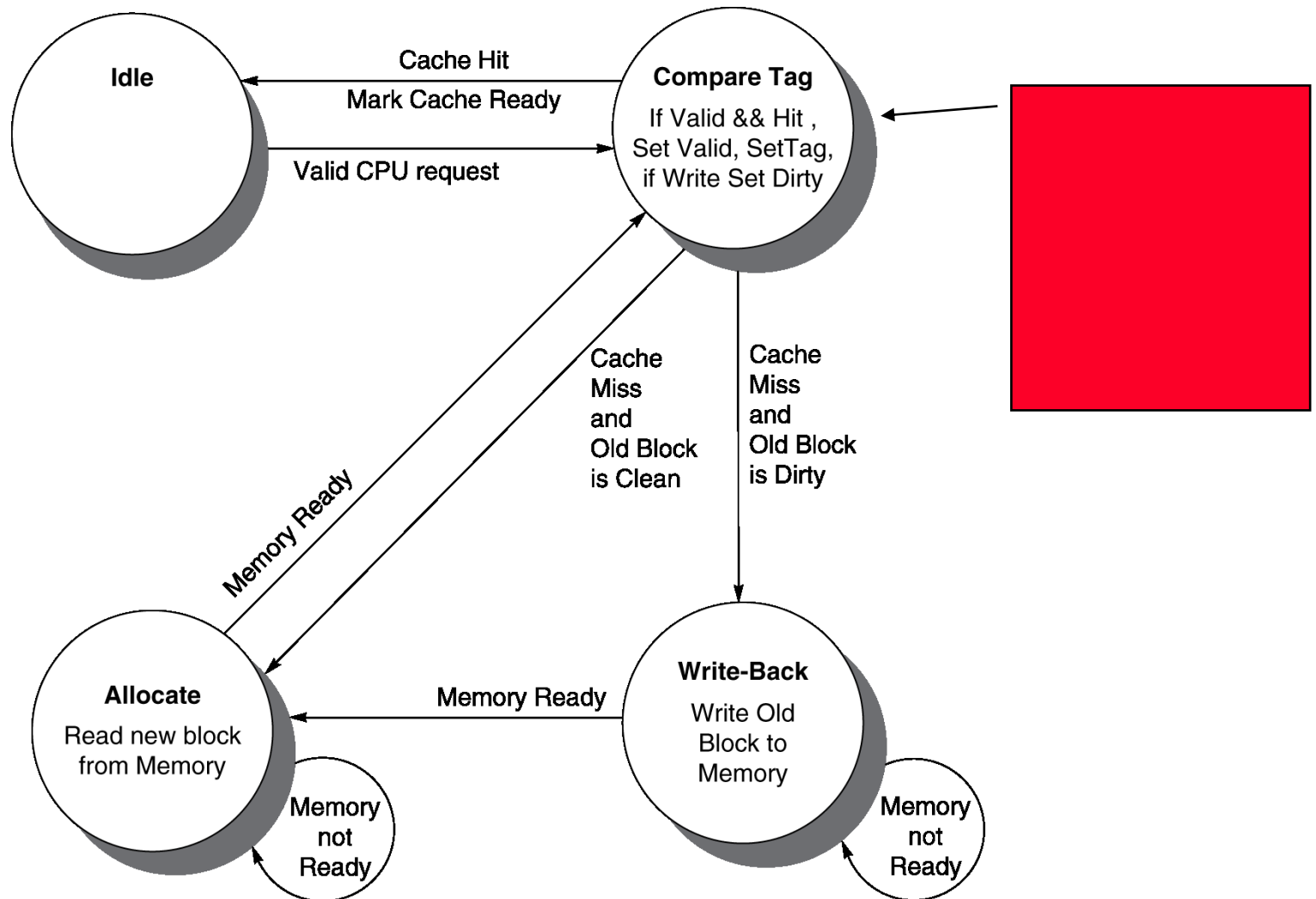


# Finite State Machines

- ❑ Use an FSM to sequence control steps
- ❑ Set of states, transition on each clock edge
  - | State values are binary encoded
  - | Current state stored in a register
  - | Next state  
=  $f_n$  (current state, current inputs)
- ❑ Control output signals  
=  $f_o$  (current state)



# Cache Controller FSM



## Cache Coherence Problem

- ❑ Suppose two CPU cores share a physical address space
  - | Write-through caches

Time step	Event	CPU A's cache	CPU B's cache	Memory
0				0
1	CPU A reads X	0		0
2	CPU B reads X	0	0	0
3	CPU A writes 1 to X	1	0	1

# Coherence Defined

---

❑ Informally: Reads return most recently written value

❑ Formally:

- | P writes X; P reads X (no intervening writes)  
⇒ read returns written value
- |  $P_1$  writes X;  $P_2$  reads X (sufficiently later)  
⇒ read returns written value
  - c.f. CPU B reading X after step 3 in example
- |  $P_1$  writes X,  $P_2$  writes X  
⇒ all processors see writes in the same order
  - End up with the same final value for X



# Cache Coherence Protocols

---

- ❑ Operations performed by caches in multiprocessors to ensure coherence
  - | Migration of data to local caches
    - Reduces bandwidth for shared memory
  - | Replication of read-shared data
    - Reduces contention for access
- ❑ Snooping protocols
  - | Each cache monitors bus reads/writes
- ❑ Directory-based protocols
  - | Caches and memory record sharing status of blocks in a directory

# Invalidating Snooping Protocols

- ❑ Cache gets exclusive access to a block when it is to be written
  - | Broadcasts an invalidate message on the bus
  - | Subsequent read in another cache misses
    - Owning cache supplies updated value

CPU activity	Bus activity	CPU A's cache	CPU B's cache	Memory
				0
CPU A reads X	Cache miss for X	0		0
CPU B reads X	Cache miss for X	0	0	0
CPU A writes 1 to X	Invalidate for X	1		0
CPU B read X	Cache miss for X	1	1	1

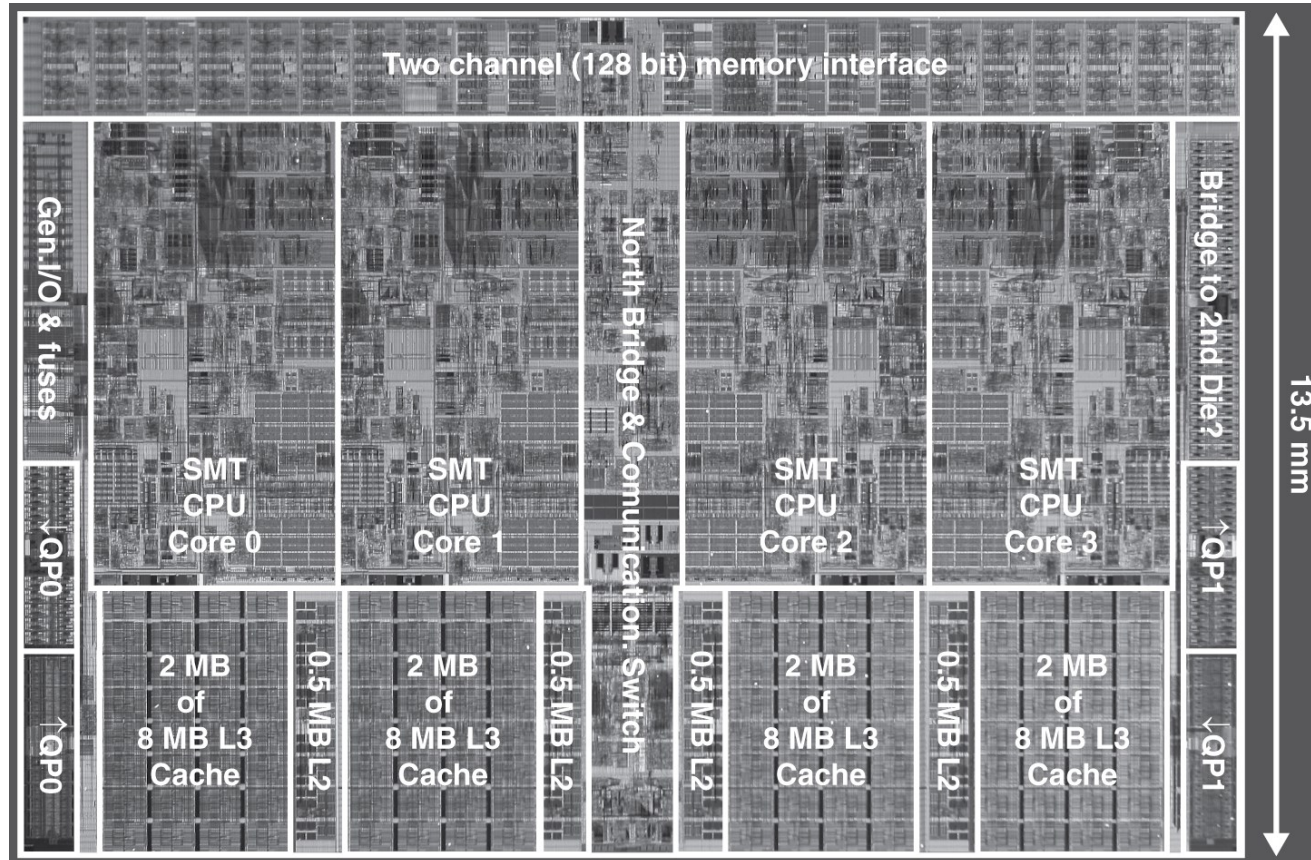
# Memory Consistency

---

- ❑ When are writes seen by other processors
  - | “Seen” means a read returns the written value
  - | Can’t be instantaneously
- ❑ Assumptions
  - | A write completes only when all processors have seen it
  - | A processor does not reorder writes with other accesses
- ❑ Consequence
  - | P writes X then writes Y  
⇒ all processors that see new Y also see new X
  - | Processors can reorder reads, but not writes

# Multilevel On-Chip Caches

## Intel Nehalem 4-core processor



Per core: 32KB L1 I-cache, 32KB L1 D-cache, 512KB L2 cache

## 2-Level TLB Organization

---

	Intel Nehalem	AMD Opteron X4
Virtual addr	48 bits	48 bits
Physical addr	44 bits	48 bits
Page size	4KB, 2/4MB	4KB, 2/4MB
L1 TLB (per core)	L1 I-TLB: 128 entries for small pages, 7 per thread (2×) for large pages L1 D-TLB: 64 entries for small pages, 32 for large pages Both 4-way, LRU replacement	L1 I-TLB: 48 entries L1 D-TLB: 48 entries Both fully associative, LRU replacement
L2 TLB (per core)	Single L2 TLB: 512 entries 4-way, LRU replacement	L2 I-TLB: 512 entries L2 D-TLB: 512 entries Both 4-way, round-robin LRU
TLB misses	Handled in hardware	Handled in hardware

## 3-Level Cache Organization

	Intel Nehalem	AMD Opteron X4
L1 caches (per core)	L1 I-cache: 32KB, 64-byte blocks, 4-way, approx LRU replacement, hit time n/a L1 D-cache: 32KB, 64-byte blocks, 8-way, approx LRU replacement, write-back/allocate, hit time n/a	L1 I-cache: 32KB, 64-byte blocks, 2-way, LRU replacement, hit time 3 cycles L1 D-cache: 32KB, 64-byte blocks, 2-way, LRU replacement, write-back/allocate, hit time 9 cycles
L2 unified cache (per core)	256KB, 64-byte blocks, 8-way, approx LRU replacement, write-back/allocate, hit time n/a	512KB, 64-byte blocks, 16-way, approx LRU replacement, write-back/allocate, hit time n/a
L3 unified cache (shared)	8MB, 64-byte blocks, 16-way, replacement n/a, write-back/allocate, hit time n/a	2MB, 64-byte blocks, 32-way, replace block shared by fewest cores, write-back/allocate, hit time 32 cycles

n/a: data not available

# Miss Penalty Reduction

---

- ❑ Return requested word first
  - | Then back-fill rest of block
- ❑ Non-blocking miss processing
  - | Hit under miss: allow hits to proceed
  - | Mis under miss: allow multiple outstanding misses
- ❑ Hardware prefetch: instructions and data
- ❑ Opteron X4: bank interleaved L1 D-cache
  - | Two concurrent accesses per cycle

# Pitfalls

---

- ❑ Byte vs. word addressing
  - | Example: 32-byte direct-mapped cache, 4-byte blocks
    - Byte 36 maps to block 1
    - Word 36 maps to block 4
- ❑ Ignoring memory system effects when writing or generating code
  - | Example: iterating over rows vs. columns of arrays
  - | Large strides result in poor locality



# Pitfalls

---

- ❑ In multiprocessor with shared L2 or L3 cache
  - | Less associativity than cores results in conflict misses
  - | More cores  $\Rightarrow$  need to increase associativity
- ❑ Using AMAT to evaluate performance of out-of-order processors
  - | Ignores effect of non-blocked accesses
  - | Instead, evaluate performance by simulation

# Pitfalls

---

- ❑ Extending address range using segments
  - | E.g., Intel 80286
  - | But a segment is not always big enough
  - | Makes address arithmetic complicated
- ❑ Implementing a VMM on an ISA not designed for virtualization
  - | E.g., non-privileged instructions accessing hardware resources
  - | Either extend ISA, or require guest OS not to use problematic instructions

## Concluding Remarks

---

- ❑ Fast memories are small, large memories are slow
  - | We really want fast, large memories ☹
  - | Caching gives this illusion ☺
- ❑ Principle of locality
  - | Programs use a small part of their memory space frequently
- ❑ Memory hierarchy
  - | L1 cache ↔ L2 cache ↔ ... ↔ DRAM memory  
↔ disk
- ❑ Memory system design is critical for multiprocessors