Weekly report

Maire AIMAR-BEURTON and LE Van Linh

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Abstract

This document contains the summary about the morphometry and deep learning studied. Besides, it also contains the algorithms to apply for image processing such as segmentation or detection the dominant points.

Part I

Morphometry

Chapter 1

Segmentation

1.1 Canny algorithm

In 1986, **John F.Canny** had proposed a method to determine the edge in image. This is a technique to detect the useful structure of the object in digital image. Until now, the Canny algorithm[1] is used widely for the segmentation in computer vision. The process of Canny algorithm can be described in 4 steps as follows:

1. Smoothing the image to reduce the noises by using Gaussian filter

2. Finding the intensity and direction gradient of each pixel in image

3. Eliminating the weak edge by using the edge thinning technique.

4. Applying double threshold to determine the potential edges

1.1.1 Gaussian filter

To smooth the image, a Gaussian filter is applied to convolve with the image. This step will help to reduce the effects of the noises on the edge detector. Normally, the equation of a Gaussian kernel with size $(2k + 1)$ x $(2k + 1)$ is computed as:

$$H_{ij} = \frac{1}{2\pi\sigma^2}exp(-\frac{(i - (k + 1))^2 + (j - (k + 1))^2}{2\sigma^2}); 1 \leq i, j \leq (2k + 1) \qquad (1.1)$$

where k is the size of kernel, and it should be a odd number.
For example, a 3x3 Gaussian filter with $\sigma = 1$ as followed:

$$G = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix} \qquad (1.2)$$

The selection of the size of the Gaussian kernel is important, it will affect the performance of the detector. If the size of the kernel is large, the detector can be sensitive to noise; otherwise, if the kernel's size is small, the detector can be destroy many strong edge. In the practice, this step is combined into Sobel convolution with a 3x3 kernel, which used to finding the intensity and direction gradients at each pixels of image.

1.1.2 Sobel convolution

The points belong to the edge in an image can stay in any direction, so the Canny algorithm uses four filters to detect the edges (vertical, horizontal and two diagonal edges) in the image. And the Sobel operator is used to detect the edges. This operator returns a value for the first derivative in horizontal direction (G_x) and the vertical direction (G_y). From these values, the gradient and direction of edge at each pixel are determined:

$$G = \sqrt{G_x{}^2 + G_y{}^2} \tag{1.3}$$

$$\phi = atan2(G_y, G_x) \tag{1.4}$$

In this case, the kernel of Sobel convolution is 3x3, and it is also combined the Gaussian filter to smooth the image. The kernels are used to convolute the horizontal direction and vertical direction as follows:

$$G_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}, G_y = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix} \tag{1.5}$$

The edge direction angle is rounded to one of four angles which were presented for four directions: vertical, horizontal, and two diagonals $0^o, 45^o, 90^o$ and 135°.

1.1.3 Non-maximum suppression

Non-maximum suppression is applied to thin the edge in an image. Thus, this operation is used to suppress all the gradient values to 0 except the local maximal. At every pixel, it suppress the gradient value of the center pixels if its magnitude is smaller than the magnitude of one out of two neighbors in the gradient direction. In details:

- If the gradient direction angle is **0** degree, the point will be considered to be on the edge if the gradient magnitude is greater than the magnitude at pixels in the **east** and **west** directions.

- If the gradient direction angle is **45** degree, the point will be considered to be on the edge if the gradient magnitude is greater than the magnitude at pixels in the **north east** and **south west** directions.

- If the gradient direction angle is **90** degree, the point will be considered to be on the edge if the gradient magnitude is greater than the magnitude at pixels in the **north** and **south** directions.

- If the gradient direction angle is **135(-45)** degree, the point will be considered to be on the edge if the gradient magnitude is greater than the magnitude at pixels in the **north east** and **south west** directions.

1.1.4 Double threshold

After applying the non-maximum suppression, the edges pixels are presented. However, there are still some edge pixels effected by noise. Double threshold will filter out the edge pixels with the weak gradient value and preserve the edge with the hight gradient value.

- A pixel called strong pixel (hence, it belong to the edge), if the edge pixel's gradient value is higher than the high threshold value.

- A pixel will be suppressed, if the edge pixel's gradient value is smaller than the low threshold value.

- A pixel called weak pixel (can be belong to the edge or not), if the edge pixel's gradient value is larger than low threshold value and smaller than high threshold value. A weak pixel can be belong to the edge if it connected with a strong pixel in 8-connected; else, it will be suppressed.

Thus, the accuracy of algorithm is depended on two parameters: the kernel of Gaussian filter and thresholds value. As said before, if we choose incorrect the kernel size of Gaussian filter, we can not reduce the noise or we can remove the real edge. Besides, the values of double threshold is also important to filter out the edge pixels. In practice, 1:3 is the good ratio between lower threshold and upper threshold in Canny.

1.1.5 Summary

1.2 Suzuki algorithm

Chapter 2

Dominant points

In shape analysis, extracting features from the curves is an important step because in another way, we can re-construct the shape from the features. The term dominant points, also called as siginficant points, points of interest, corner points or landmarks is assigned to the points which have the high effect on boundary of object; their dectection is a very important aspect in contours methods because these concentrate the information of a curve on the shape.

Dominant points can be used to produce a presentation of a shape contour for futher processing. The representation ... In the content of this chapter, we will discuss about the methods to determine the dominant in digital image.

There are many approaches developed for detecting dominant points and the methods can be classified into three groups follows:

- Dectermine the dominant points using some significat measure other than curvature

- Evaluate the curvature by transforming the contour to the Gaussian scale space.

- Search for dominant points by estimating directly the curvature in the original image space.

2.1   Method 1

2.2   Method 2

2.3   Method 3

Chapter 3

Software

3.1 The software architecture

The architecture of program is followed 3-tier model. There-tier architecture is an architecture that each tier is designed, developed and maintained as independent. The advantage of this architecture is intended to allow any upgraded or replaced independent between the tiers. When user want to change the requirements or technology of a tier, it will non-affect to other tiers.

The architecture of three-tiers includes:

- **Data tier**: includes the classes which were designed for the data structure of program. It also provides the persistence mechanism to access the data.

- **Logic tier**: controls the functionality of application by performing detailed processing.

- **Presentation tier**: displays information related to user. It is a layer which received the require from user to program or return the result from program to user.

3.2 The classes architecture

Part II

Deep learning

Chapter 4

Machine Learning

Machine learning is a norm refer to teach the computer the abilities which are only done by the humans. A machine learning algorithm is an algorithm that is able to learn from data. Most of machine learning algorithms can be divided into two categories: supervised learning and unsupervised learning algorithms.

A machine learning algorithm is built based on the tasked for a machine learning system. We have many kinds of task can be solved with machine learning. Some of common machine learning tasks include the following:

- *Classification*: In this type of task, the computer is asked to indicate a category in k category which the input belongs to. To solve this task, the learning algorithm uses a function $y = f(x)$, the model assigns the input described by vector x to a category identified by score y.

- *Classification without input*: A challenge of classification is missing the input vectors. In this case, to solve the classification task, the learning algorithm only has to define a single function mapping from a vector input to a category output. When some of inputs are missing, instead of providing a single classification function, the learning algorithm must learn a set of functions. Each function corresponds to classifying x with different subset of its inputs missing.

- *Regression*: the computer program is asked to predict a numerical value given some input.

- *Transcription*: machine learning system is asked to observe a relatively unstructured representation of some kind of data and transcribe it into discrete, textual form.

- *Translation*: The input already contains the sequence of symbols in some languages, the computer program must convert it into the sequence of symbols of other languages.

- *Structure output*: involve any task where the output is a vector with important relationships between the different elements.

- *Anomaly detection*

- *Synthesis and sampling*: The program is asked to generate the new example that are similar with the training data.

- *Imputation of missing value*: The algorithm mus provide a prediction of the values of the missing entries in a new example.

- *Denoising*

- *Density estimation or probability mass function estimation*

4.1 Supervised learning algorithms

4.2 Unsupervised learning algorithms

4.3 Stochastic Gradient Descent

Chapter 5

Classification

Classification is a most of important task in machine learning. In classification, a function is constructed to determine the category of the input. Generally, the model of classification as following:

The process of classification includes two steps:

1. **Training**: Use the **training set** to learn what every object of a class looks like. This duration is called training a classifier or learning a model. The training set is a set with the objects which have labeled with specific category.

2. **Evaluation**: To evaluate the quality of the classifier. We use a new set **(test set)** of the objects and try to ask the classifier predict the category of the object in the test set.

In the content of this chapter, we will discuss about the classification techniques, especially, linear classification which technique has used more in neural network and deep learning.

5.1 Nearest Neighbour Classifier

The first approach to Classifier, we will develop Nearest Neighbour Classifier. This classifier do not have any relation with deep learning or convolutional networks, but it will help us to have an overview about classification problem.

The idea of Nearest Neightbour Classifier is comparing each image in test data set with all image in training data set and predict the label of closet training image. And one of simplest methods to compare two images is comparing each pixels of two images and sum of all the differences. Assum that we have two vector I_1, I_2 presented for two images, the equation to compare two images is following (called **L1 distance**):

$$d_1(I_1, I, 2) = \sum_p |I_1{}^p - I_2{}^p| \tag{5.1}$$

Actually, we have many ways to compute the distances between two image. Instead of using L1 distance, we can use **L2 distance**, which has indicated by square root of euclidean distance between two vectors. The form of L2 distance as:

$$d_2(I_1, I, 2) = \sqrt{\sum_p (I_1{}^p - I_2{}^p)^2} \tag{5.2}$$

For example, this is a way to compute distace between two images (fig. 5.1):

test image					training image					pixel-wise absolute value differences			
56	32	10	18		10	20	24	17		46	12	14	1
90	23	128	133	−	8	10	89	100	=	82	13	39	33
24	26	178	200		12	16	178	170		12	10	0	30
2	0	255	220		4	32	233	112		2	32	22	108

→ 456

Figure 5.1: An example used **L1 distance** to compare two images

5.2 K-Nearest Neighbour Classifier

In the case of Nearest Neighbour Classifier, we just determine only one closest image in the training data with the test image when we wish to make a prediction. It means that we need some images in training data set that closest with the test image. In this case, we can use the **k-Nearest Neighbour Classifier**. The idea of this method is finding top **k** closest images instead of singel closest image (hence, when k = 1, we recover the Nearest Neighbour Classifier).

In practice, what is the best value of k that we should to use? Besides that, we have many choices for compute the distance between two images different with L1 distance, L2 distance. The method called **hyperparameters** is vary for this work. This method comes in the design of many Machine Learning algorithsm, and it is used to choose the setting values. We should try out many different values and see what works best. This is the idea, but we must be done vary carefully. Another noticed that, we do not try to evaluate on test data set with each k. After having the k, we evaluate on the test set only a single time, at the end of procedure.

The idea is spitting the training data set in two subsets: the first subset is used to training, the other subset is used to validate (called **validation set**). The validation set is used as the test set to indicate the value of k. At the end of procedure, we could determine values of k work best. We would then use this value and evaluate once on the actual test set.

In summary, split the training set into training set and validation set. use validation ton tune all hyperparameters. At the end run a single time on the test set and evaluate the result.

5.3 Linear Classification

The (k-)Nearest Neighbour Classifier had introduced about the problem of Image classification, which is predicting the label to an image from a fixed set of labels. But with the these methods, we must spend more time with large datasets an the cost for classifying is expensive. Another classification methods is known as **linear classification** which is the core of neural networks. The linear classification has two main components:

- **Score function**: which used to map the raw data to score of a category.

- **Loss function**: that quantifies the agreement between predict score and the truth category of the data.

The simplest function of a linear mapping is:

$$y = f(x_i, W, b) = W x_i + b \tag{5.3}$$

Where:

- x_i is the raw data, *example: an image.*

- W: a matrix parameter, called **weight** matrix

- b: vector, called **bias** vector

- y: score when consider the data x_i belongs to a category.

In equation above, the input image x_i is fixed but we can control the setting of parameters **W and b**. Our goal is setting the parameters that the computing score match with the truth labels of image.
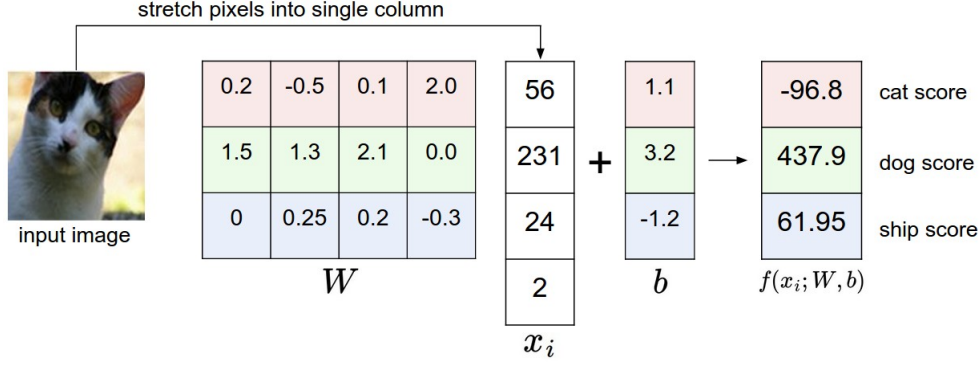

Figure 5.2: An example of mapping an image to a class scores

In training process, it is a little cumbersome to keep two sets of parameters (W,b) separately. A commonly trick is used to combine two sets of parameters into a single matrix that holds both of them by extending a vector x_i with one additional dimension and keep the constant defaut 1. Now, the new score function will be:

$$y = f(x_i, W, b) = W x_i \tag{5.4}$$

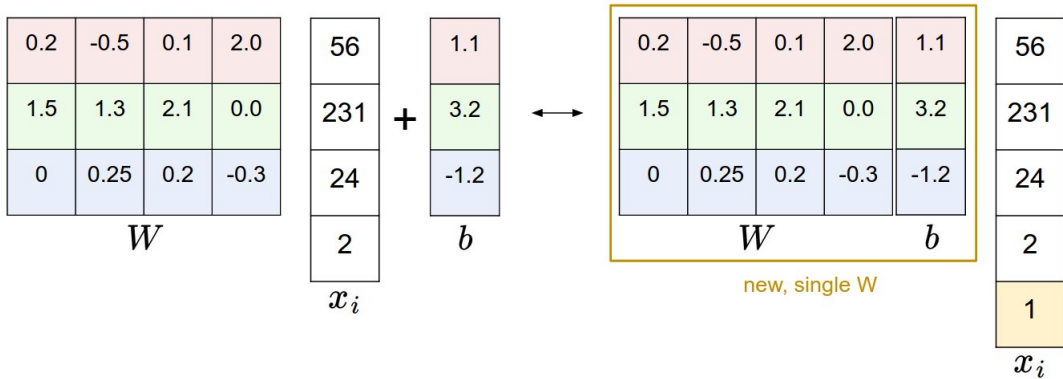Visualation of new score function:

Figure 5.3: An example of bias trick

As described, we defined a score functions from a pixels value of an image to class scores with set of parameters **W**. Moreover, we need to control over parameters W such that the class scores are consistent with the ground truth labels in the training data. But not all cases are perfect, the class scores just near with the score of truth labels. So, we are going to measure the wrong with a **loss function**. Intuitively, the loss will be high if we are doing a poor classifier, ant it will be low if we are doing well. Multicalss Support Vector Machine (SVM) and Softmax function are two commonly methods for this purpose.

5.3.1 Multiclass Support Vector Machine loss

5.3.2 Softmax classifer

Chapter 6

Deep Network

Chapter 7

Convolutional Neural Network

Convolutional Neural Networks (CNNs) are similar with the original of Neural Networks. Neural Networks receive an input and pass it through a series of hidden layer. Each hidden layer is made from a set of neurons, where each neuron is full connected with all neurons of previous layer. Actually, the neural networks do not scale well to full images...

7.1   Architecture

A CNN is made from the layers. The common layers in CNN are convolutional, nonlinear, pooling and full connected layers. CNN takes image as an input, pass it through the series of layers and get an ouput. Each layer has a difference function to transform the input to another layer.
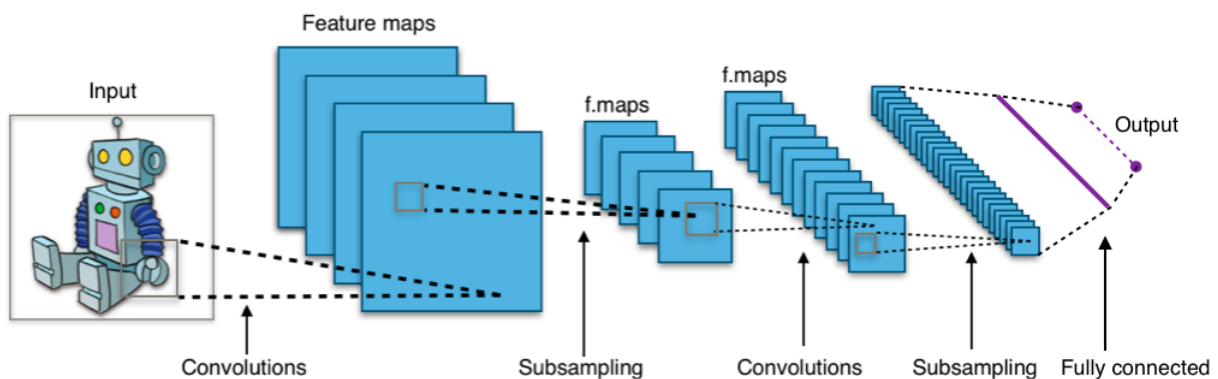

Figure 7.1: An architecture of convolutional neural network

7.1.1   Convolutional layer

7.1.2   Pooling layer

7.1.3   Full connected layer

7.2   Testing

Part III

Conclusion

Chapter 8

Discussion

Chapter 9

Conclusion

Bibliography

[1] John Canny. A computational approach to edge detection. *IEEE Transactions on pattern analysis and machine intelligence*, (6):679–698, 1986.