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# A path choice approach to activity modeling with a pedestrian case study

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# Presentation outline

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- **Motivation:** Why pedestrian activities?
- **Detection:** Where are pedestrians?
- **Modeling** pedestrian behavior:
  - Activity-episode sequences and activity patterns
  - Activity network
  - Activity paths
  - Choice set generation
  - Activity path choice model for WiFi traces
- **Conclusion**
- **Future work**



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# MOTIVATION



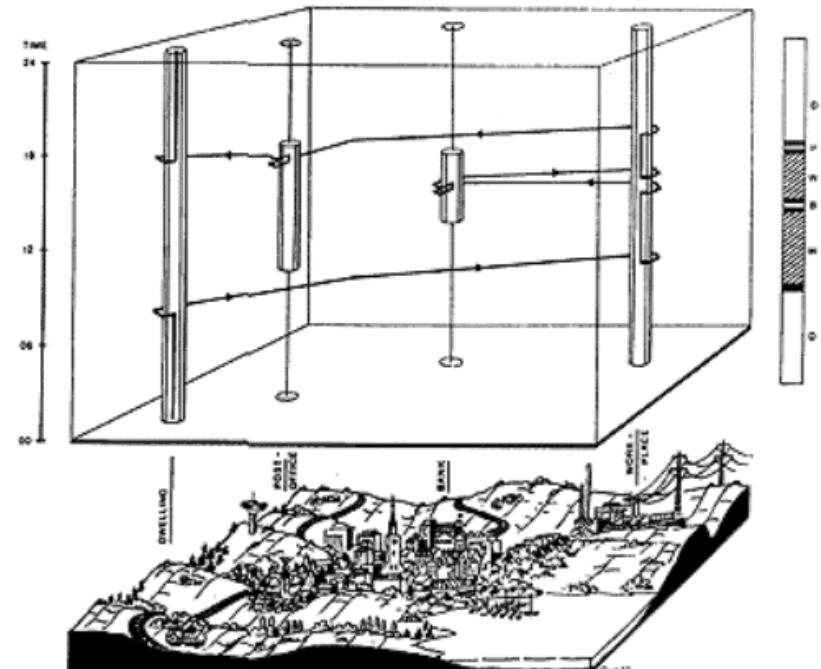
# Activity modeling for pedestrian infrastructure

## Goal

- Adapt traditional activity modeling framework for pedestrian activities

## Challenges

- Detect pedestrians
- Model activity patterns
- Forecast scenarios



Carlstein, T. (1978)

# 3 examples

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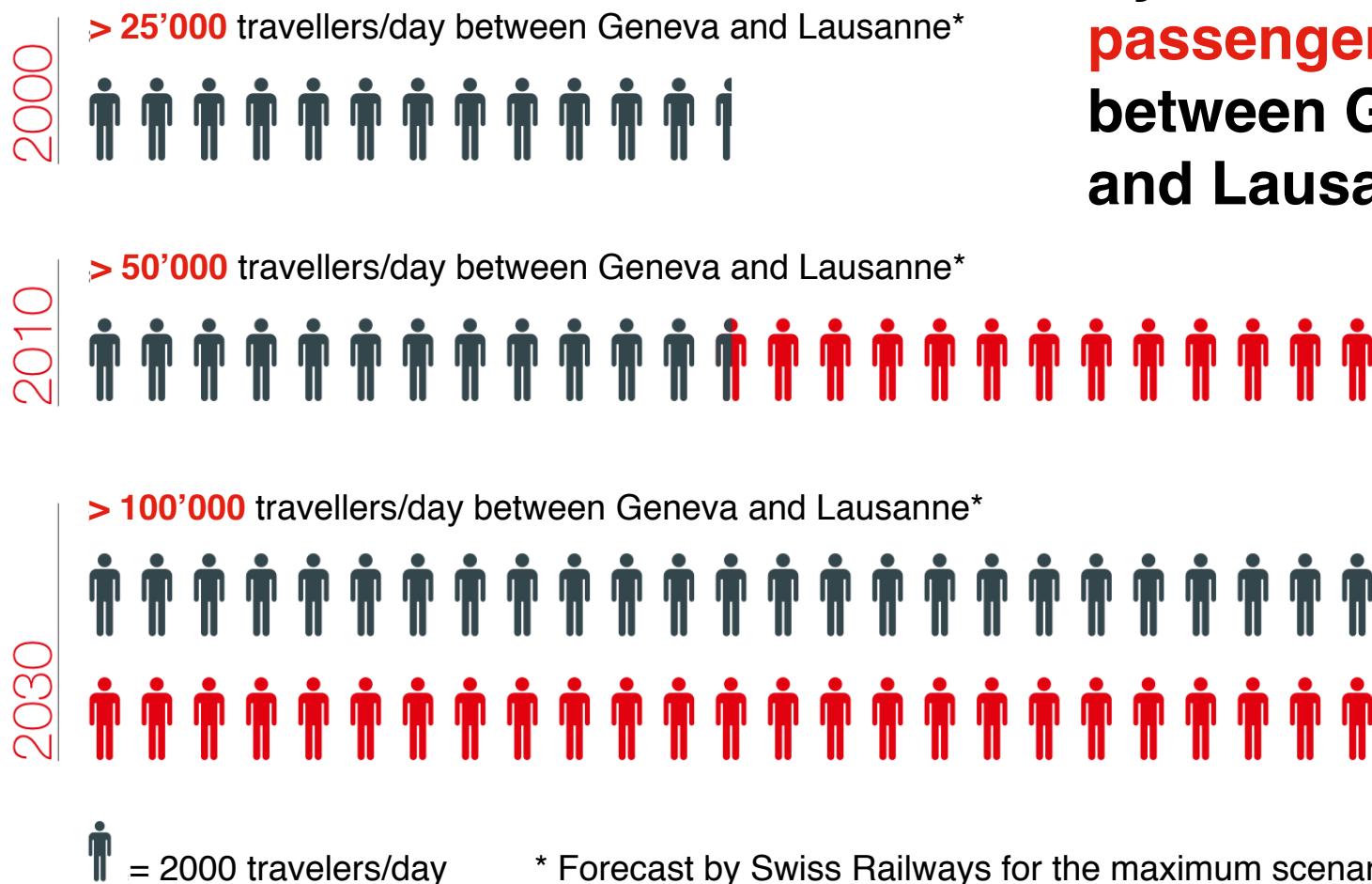
- **Multimodal transport hubs:**  
Lausanne railway station
- **Mass gathering:**  
Paléo music festival
- **Campus:**  
EPFL new “Quartier Nord”

# Walking is the key for efficient multimodal transport systems



Crowd in a railway station in Mumbai, India  
Photo: National Geographic

# Lake Geneva region: Léman 2030



**By 2030, 100'000 passengers per day between Geneva and Lausanne**

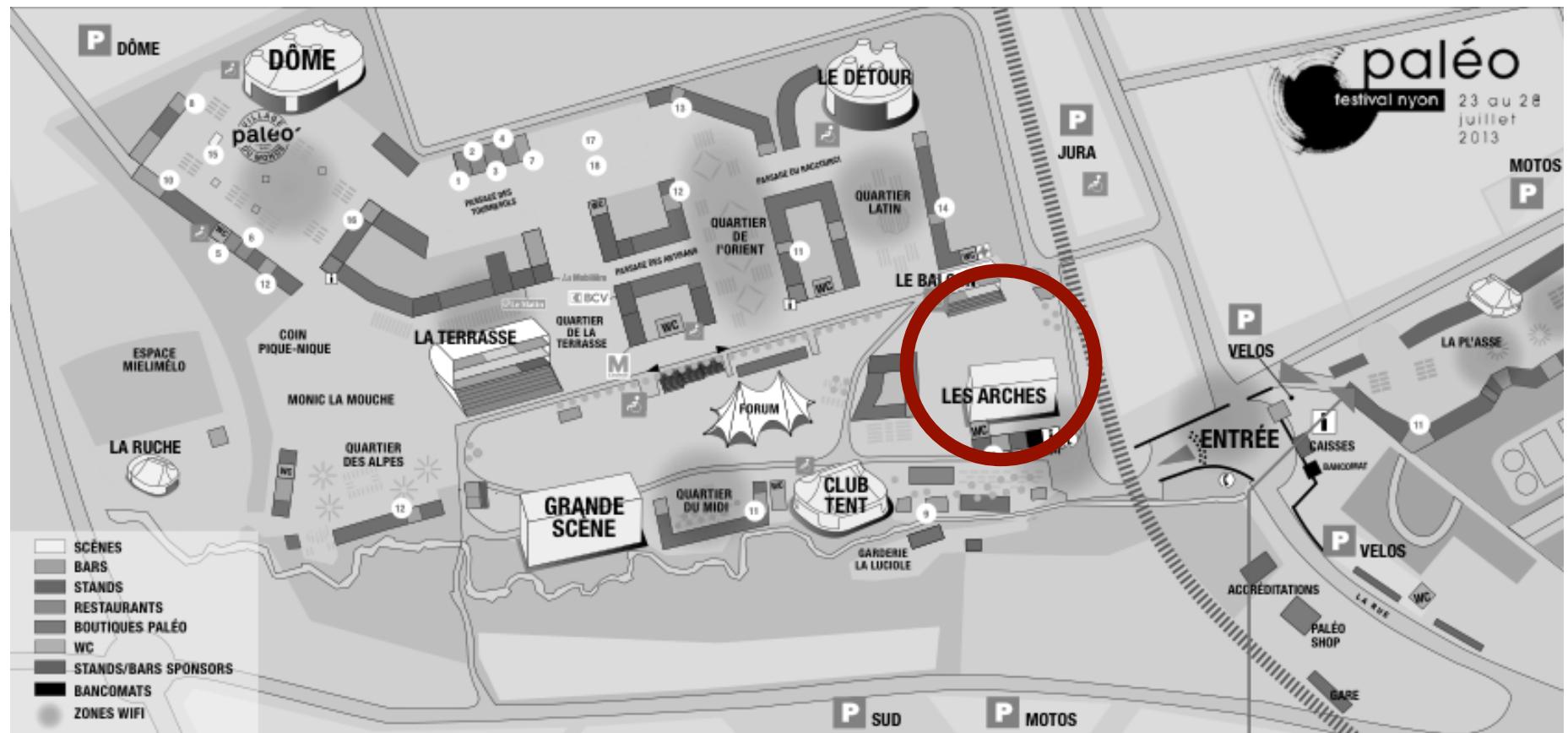
# Mass gathering



# Paléo 2012



# Paléo 2013



# Campus



# EPFL

## Quartier Nord



TRANSP-OR



# Campus



# DETECTION



# Data input

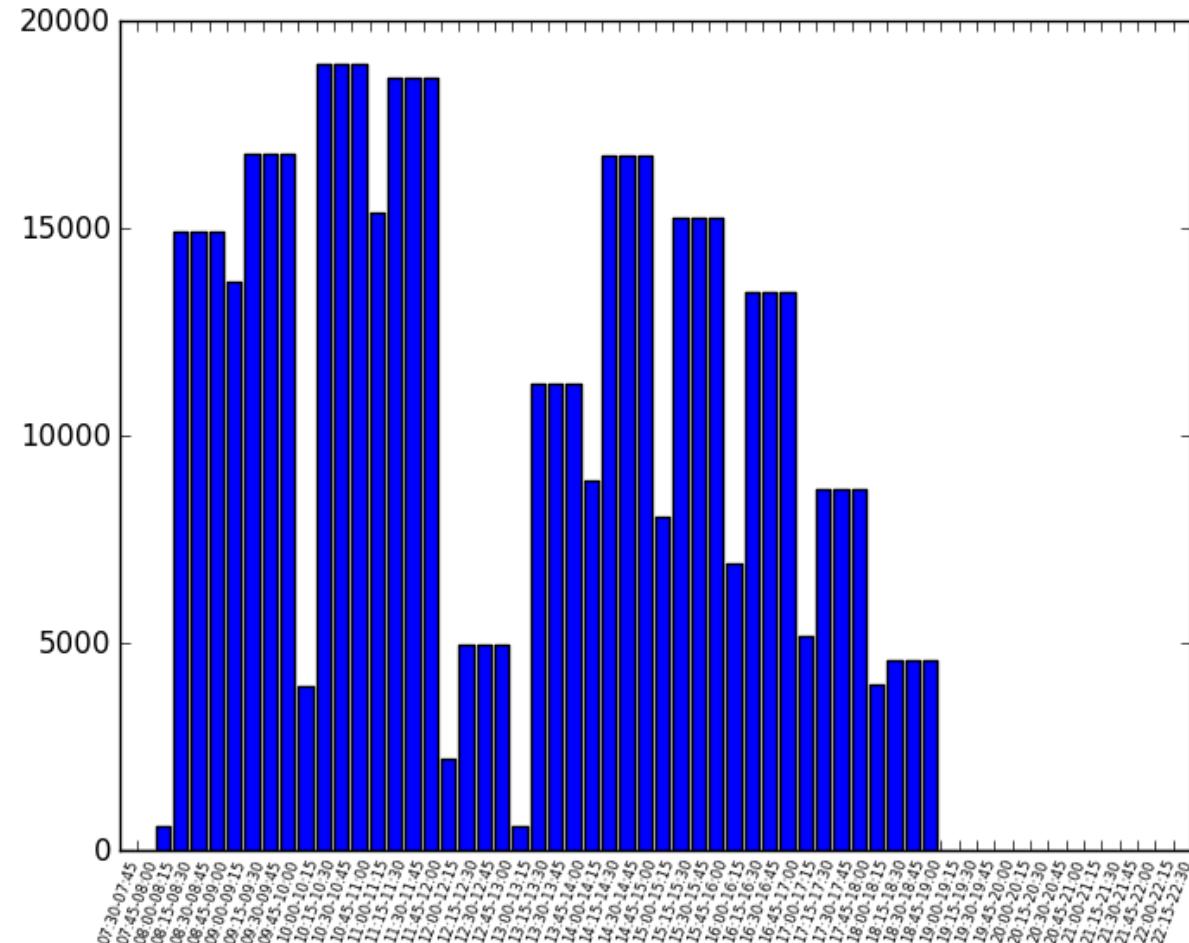
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- Localization data with full coverage of the facility
- Semantically-enriched routing graph for pedestrians
- Potential attractivity measure

# Data requirement: Potential attractivity

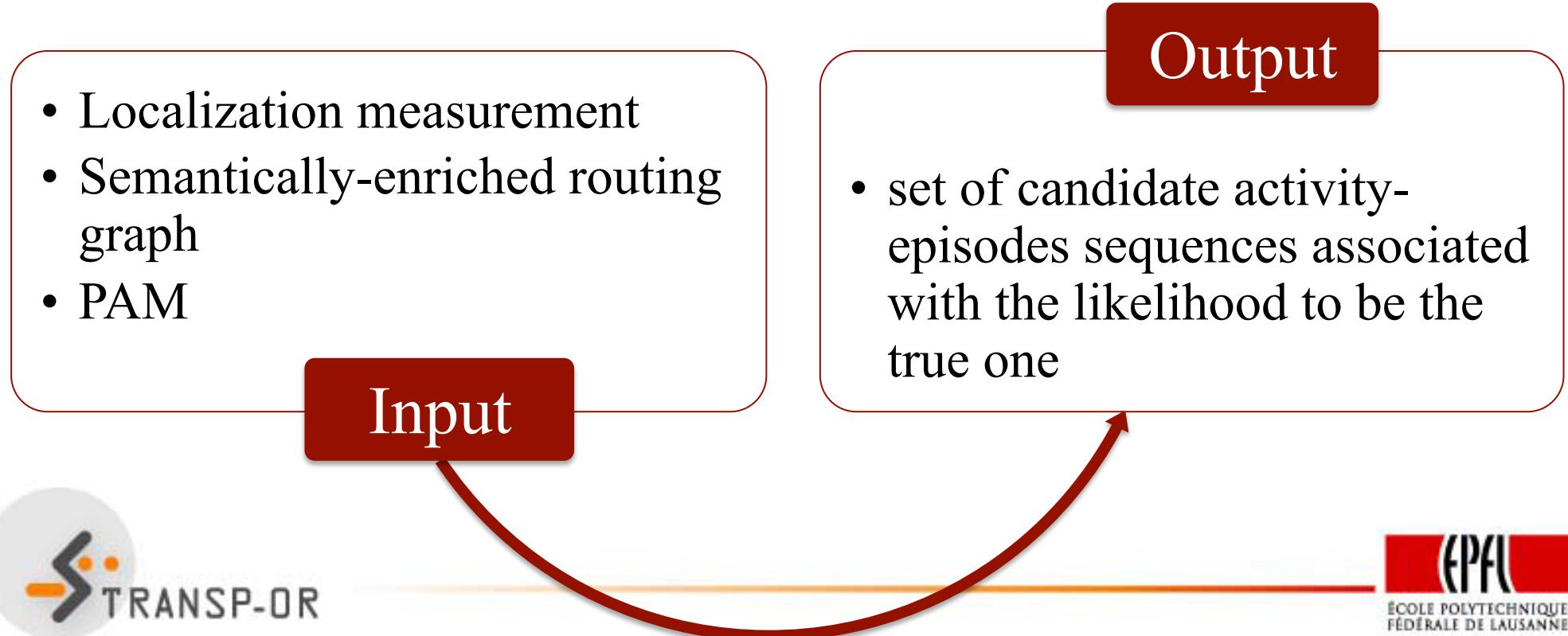
- Potential attractivity measure (PAM) depends on
  - Destination attractivity  $att(x, t)$ 
    - Classroom, platform, scene, ...
  - Time-constraints  $\delta_{x,i}(t)$ 
    - Class schedules, train schedules, opening hours, ...
- Examples:
  - 1500 passengers on platform 4 arriving at 16h04
  - 32 students in a classroom from 8h15 to 10h
  - 400 seats in a restaurant open from 11h to 14h30

# Data requirement: Potential attractivity



# Methodology

- Goal: extract the possible activity-episodes performed by pedestrians from digital traces from communication networks



# Probabilistic measurement model

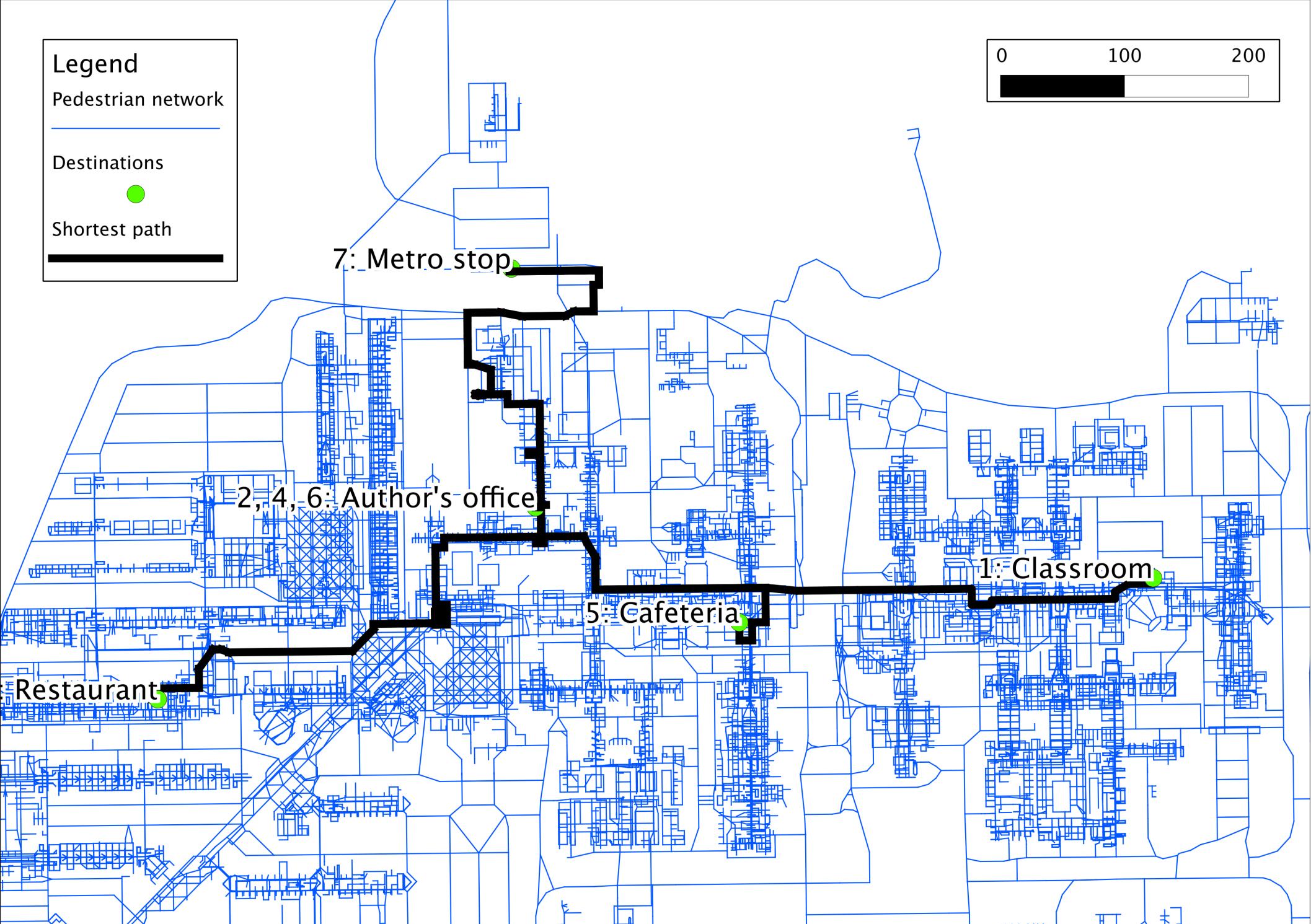
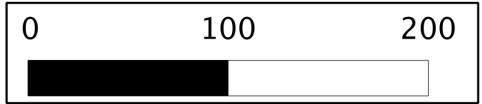
$$P(a_{1:m} | \hat{s}_{1:n}) \propto P(\hat{s}_{1:n} | a_{1:m}) \cdot P(a_{1:m})$$

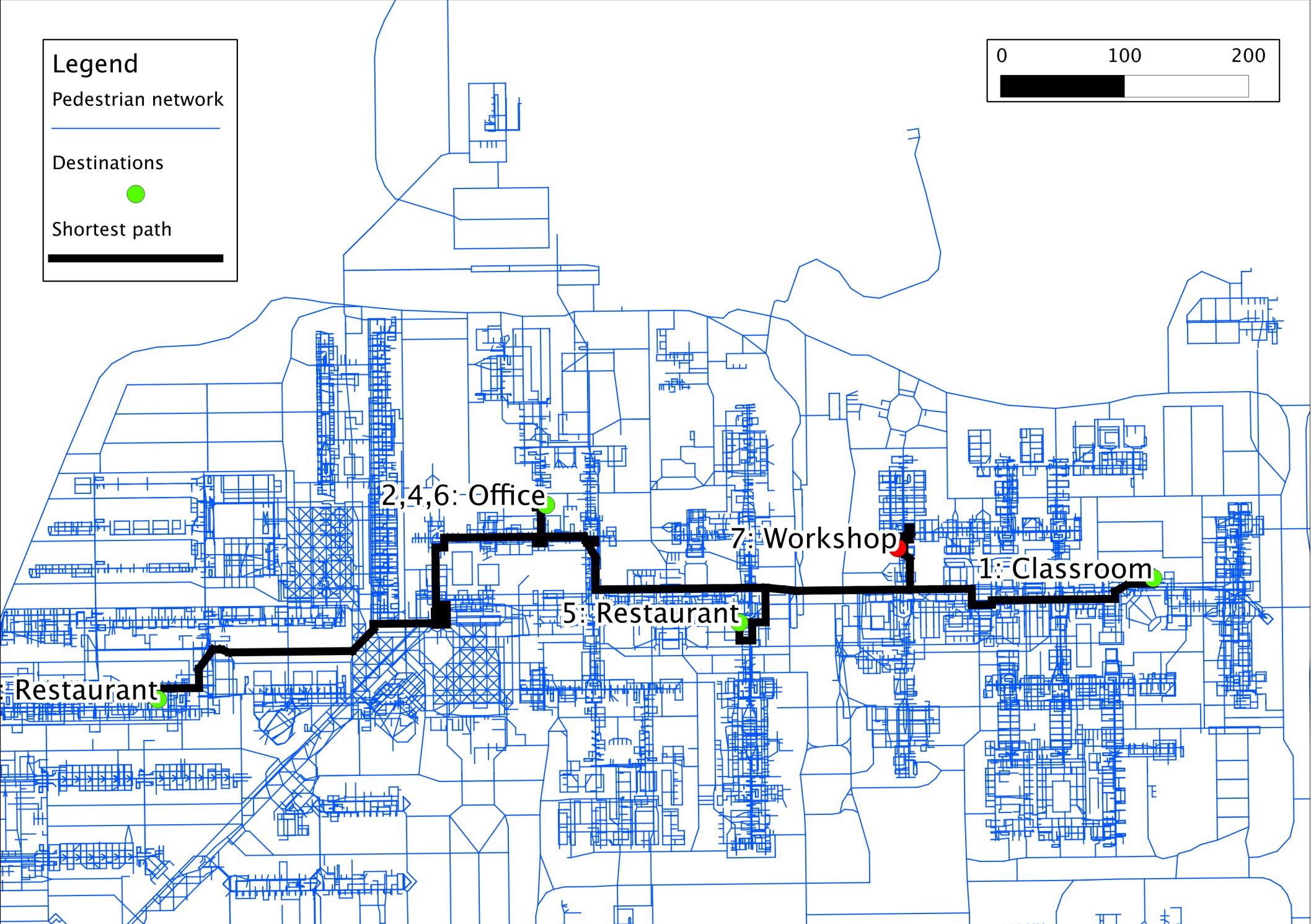
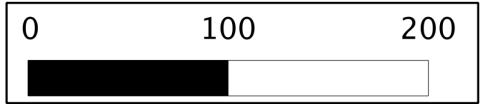
Measurement likelihood

Prior

Activity probability



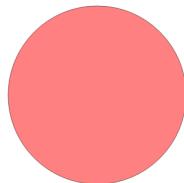




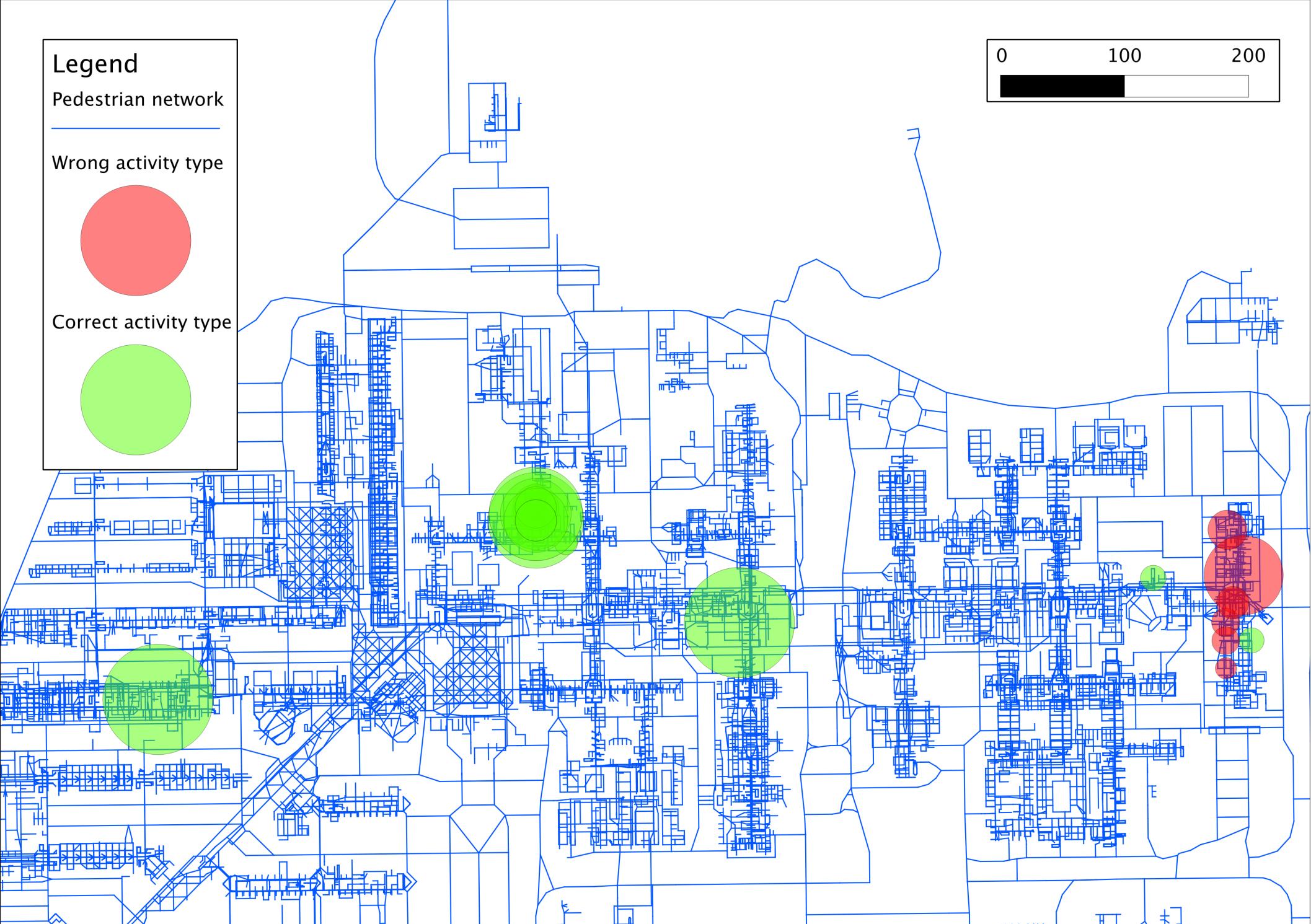
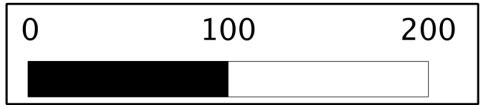
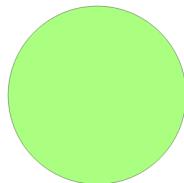
## Legend

Pedestrian network

Wrong activity type



Correct activity type



# More on detection

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- Technical report:  
A. Danalet, B. Farooq and M. Bierlaire. A Bayesian Approach to Detect Pedestrian Destination-Sequences from WiFi Signatures, 2013.

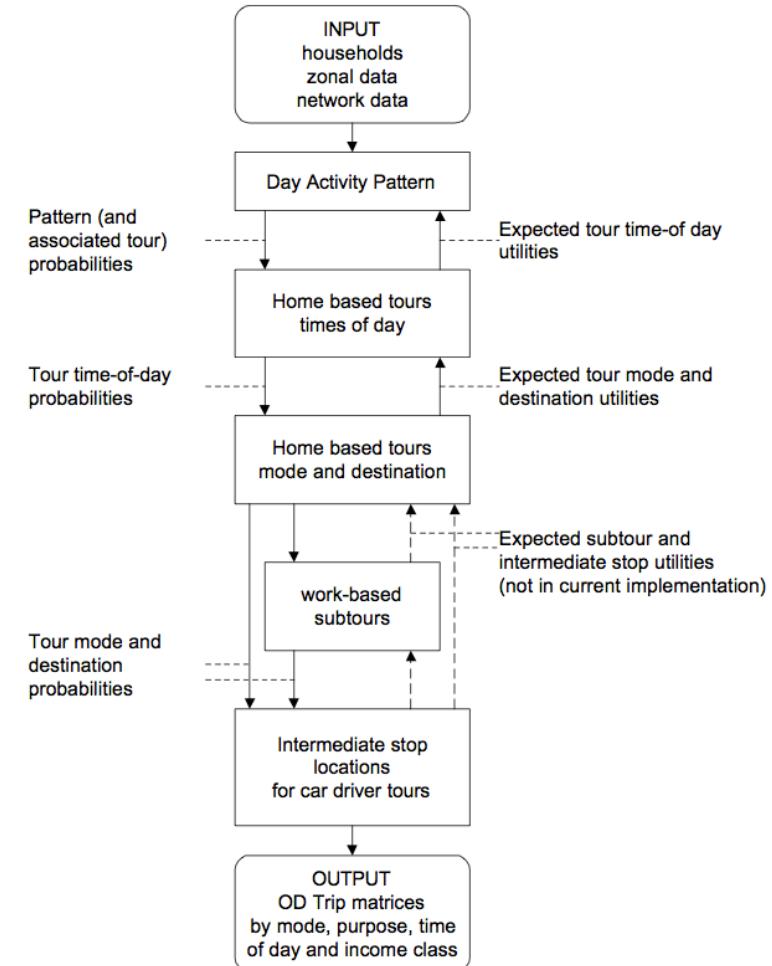
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# A PATH CHOICE APPROACH TO ACTIVITY MODELING



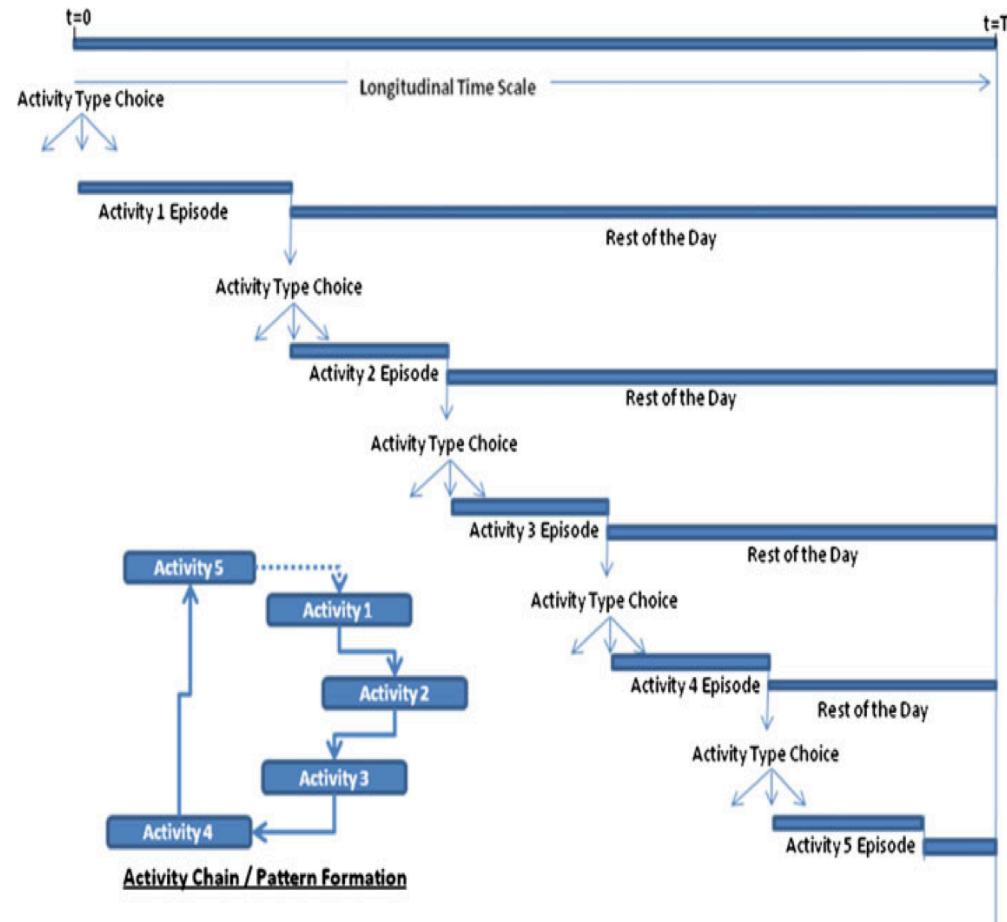
# Activity travel pattern

- System of choice models (Bowman, 1998)
  - Activity pattern choice model
  - Tour choice model
    - primary destination
    - mode choice
    - time of day
    - number of stops in the tour
  - Trip choice model
    - idem, for secondary destinations



# Dynamic discrete continuous models

- Continuous time
- Composite activity integrating all activities in the rest of the day
- Maximization of utility between the current specific activity and the composite future activity
- Activity pattern built sequentially



Habib, K. M. N. (2011)

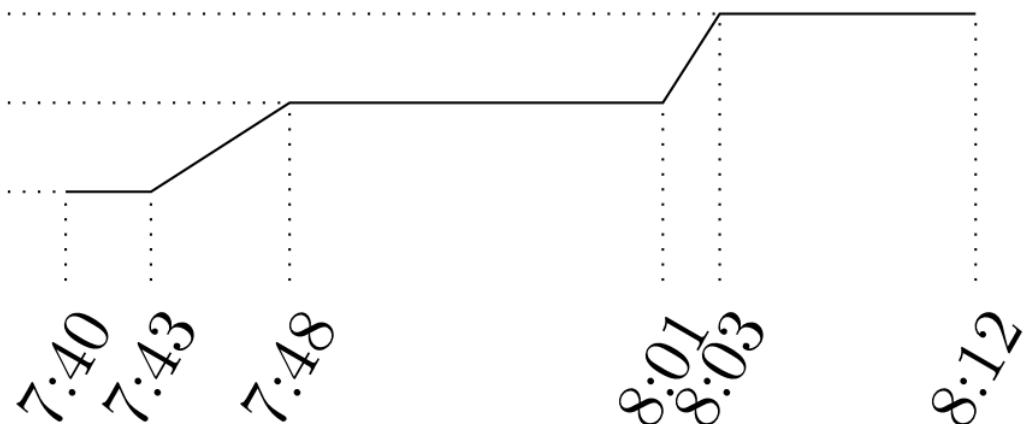
# Activity-episode sequences and activity patterns

## Activity types

Waiting for the train

Having a coffee

Buying a ticket



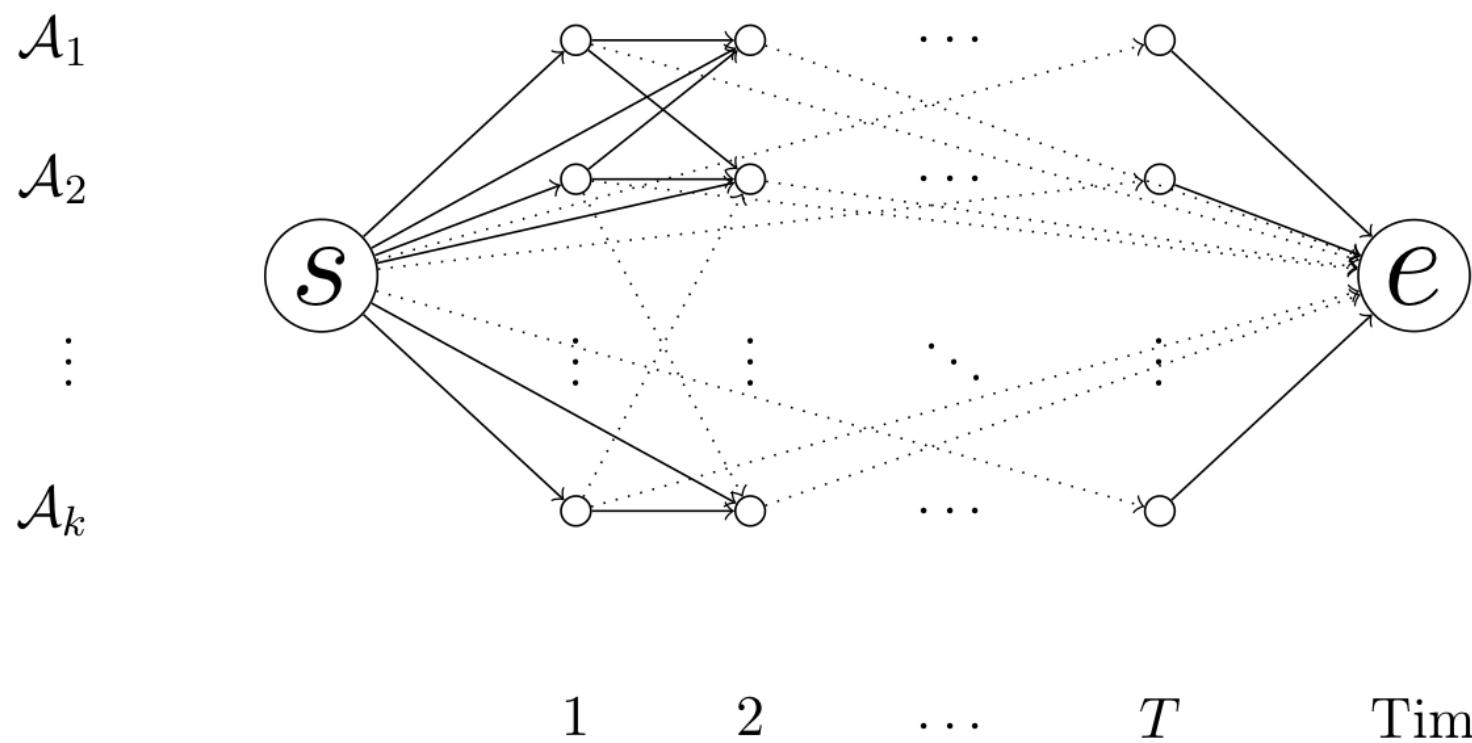
# Activity-episode sequences and activity patterns

- Activity episode  $a_n = (x, t^-, t^+)$ 
  - Start and end times are continuous random variables
  - Activity-episode sequences  $(a_1, \dots, a_{M_n}) = a_{1:M_n}$
- Activity types  $\mathcal{A}_1, \mathcal{A}_2, \dots, \mathcal{A}_K$
- Activity  $A_n = (A(a_n), t^-, t^+)$ 
  - Activity pattern  $(A_1, \dots, A_{M_n}) = A_{1:M_n}$
  - Set of all activity patterns corresponding to an observation  $\mathcal{L}_i$
- All activity patterns are associated to a measurement likelihood
- Activity patterns are the behavior we observe

# Activity network

Activity types

Activity network



# Activity network

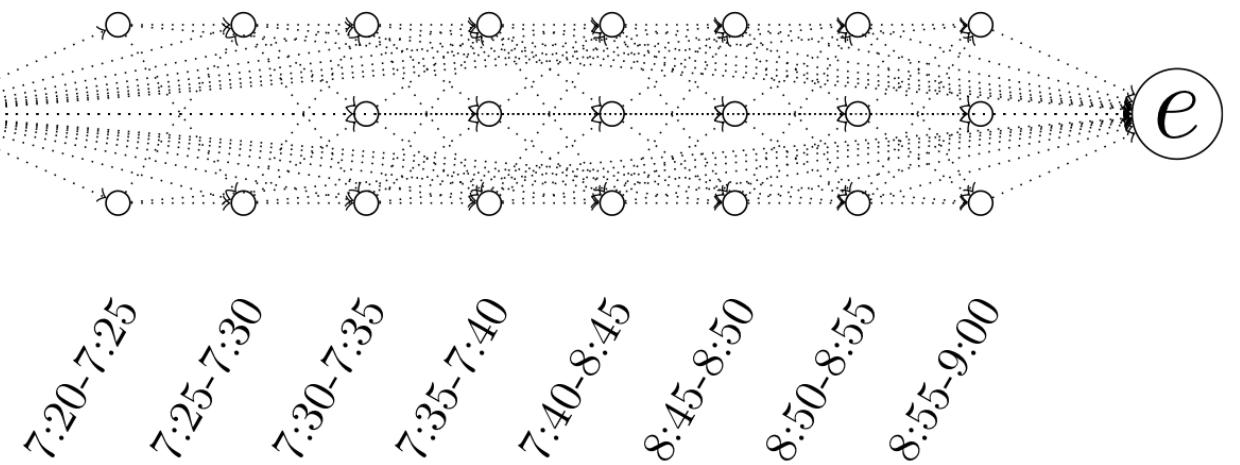
Activity types

Waiting for the train

Having a coffee

Buying a ticket

Activity network



# Activity network

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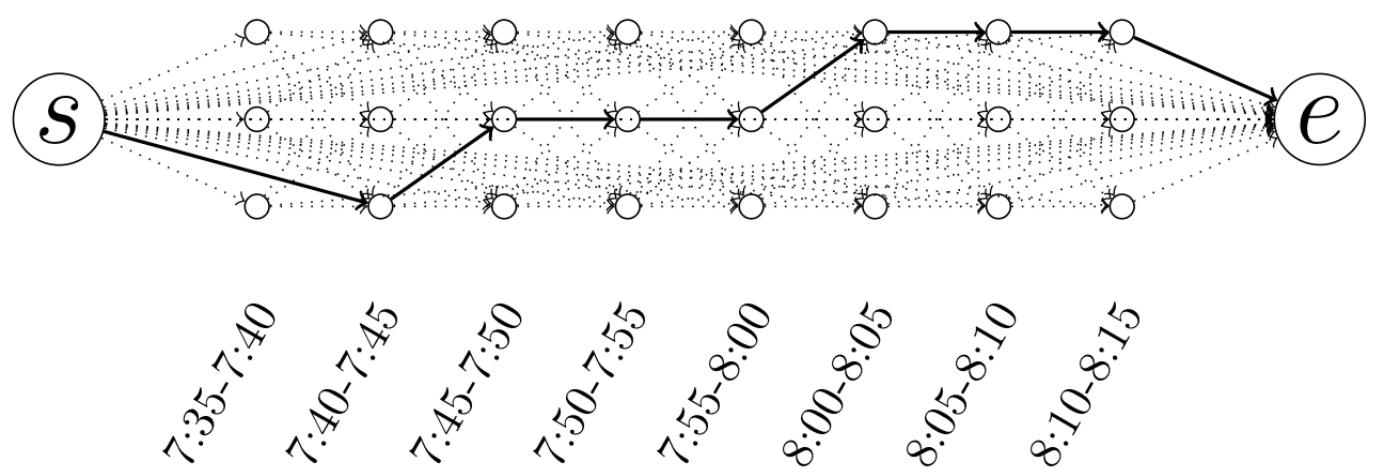
- Contains all possible activity patterns
  - Universal choice set
- Discretization of time  $\tau \in 1, 2, \dots, T$
- Nodes  $\mathcal{A}_{k,\tau}$ 
  - represent the performance by an individual of an activity type  $k$  for a unit of time  $\tau$
  - Beginning and end of the observed activity pattern:  $s, e$
  - Max number of nodes:  $KT + 2$
- Edges
  - Max number of edges:  $2KT + K^2T$

# Activity paths

Waiting for the train

Having a coffee

Buying a ticket



# Activity paths $\mathcal{A}_{1:T}$

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- Representation of  $A_{1:M_n}$  in an activity network
- All activity paths are associated to a measurement likelihood
- Activity of the time unit in the activity network = longest activity in the activity pattern for this time interval

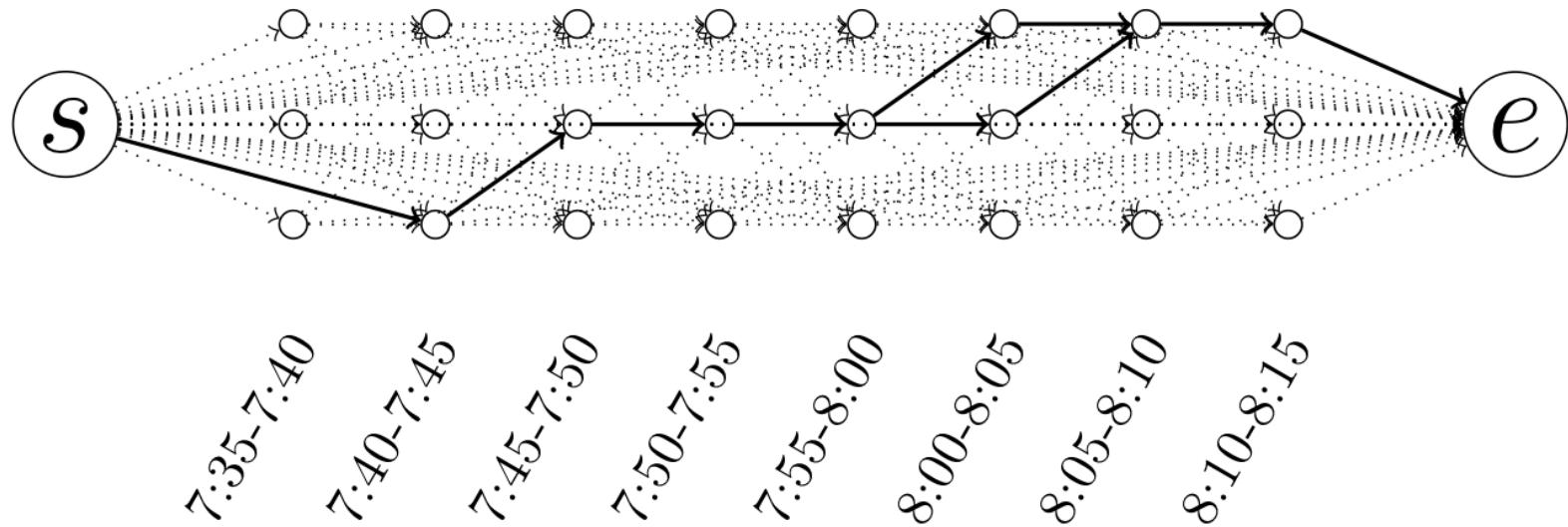
# Activity paths

- Time is a random variable. If support is larger than a time unit, one activity pattern can be represented by several activity paths

Waiting for the train

Having a coffee

Buying a ticket



# Choice set generation

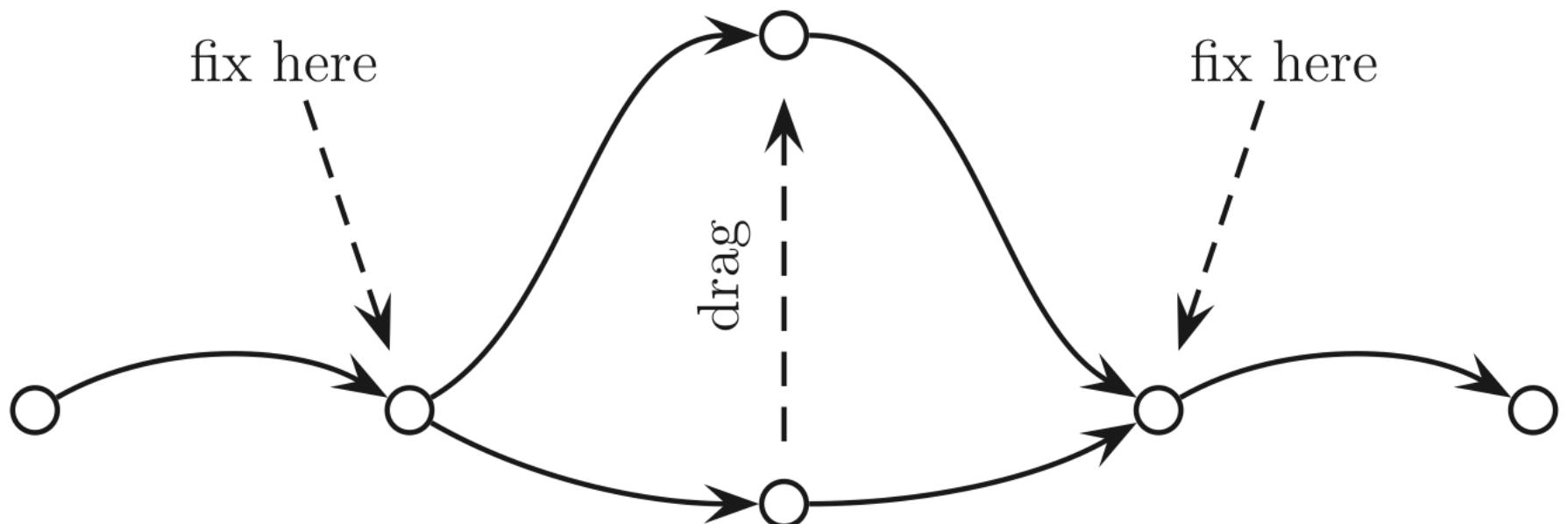
- In route choice context, universal choice set is big
- Decision maker doesn't consider all of them
- Consideration choice set not available or too small
- Consideration choice set modeling
  - Latent class choice model
  - Repeated shortest path search
  - Branch-and-bound
- Sampling of alternatives from the universal choice set
  - Frejinger, Bierlaire and Ben-Akiva (2009)
  - Fosgerau, Frejinger and Karlstrom (2013)

# Choice set generation: Metropolis-Hastings algorithm

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- Flötteröd and Bierlaire (2013)
- Paths are sampled according to an arbitrary distribution, avoiding complete enumeration
- Sampling probabilities do not need to be defined by link, but can be defined directly for the whole path
- Chen (2013) in Ch.5: weight function is composed of the length and frequency of observation
- Frejinger and Bierlaire (2010): « sample should include attractive alternatives »

# Choice set generation: Metropolis-Hastings algorithm



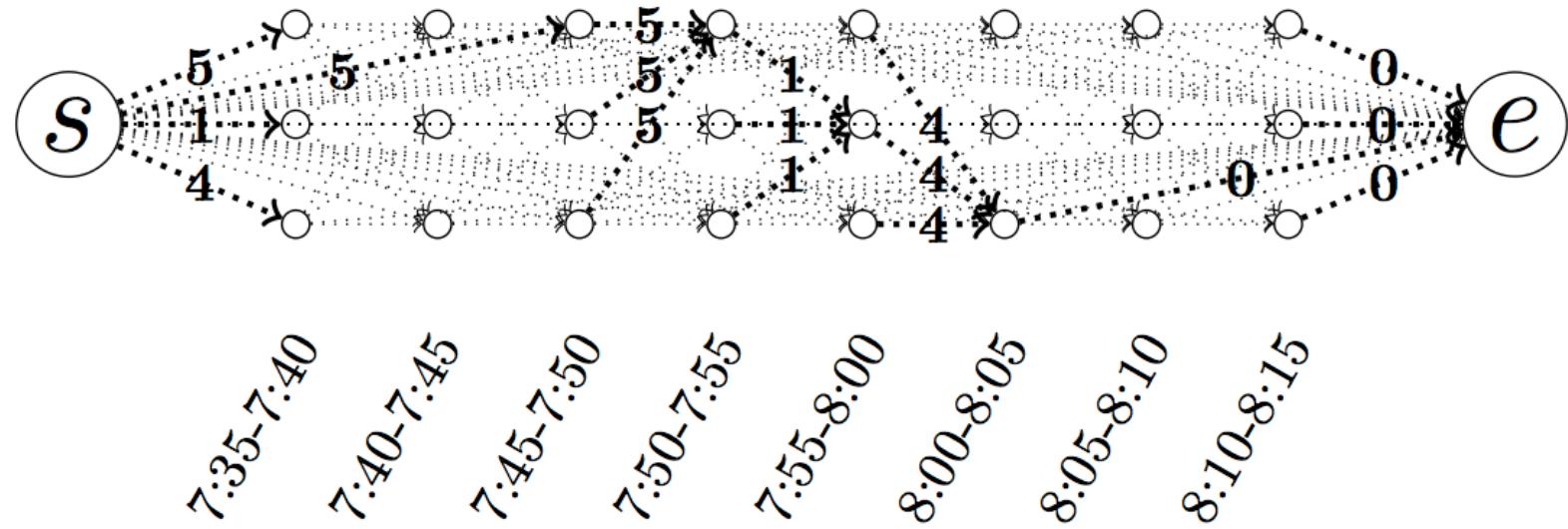
# Choice set generation in the activity network

- We propose to use potential attractivity measure

Waiting for the train

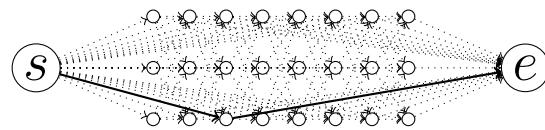
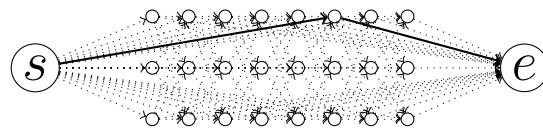
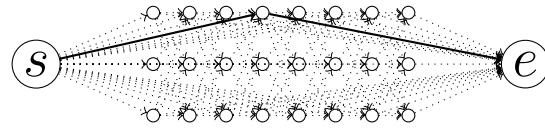
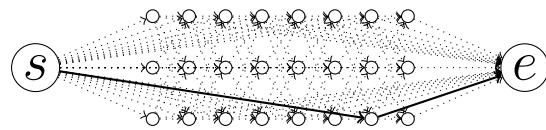
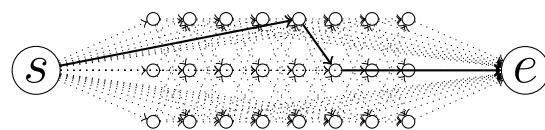
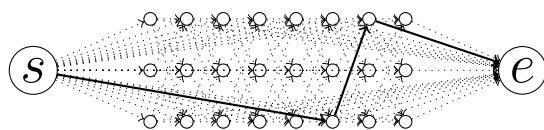
Having a coffee

Buying a ticket



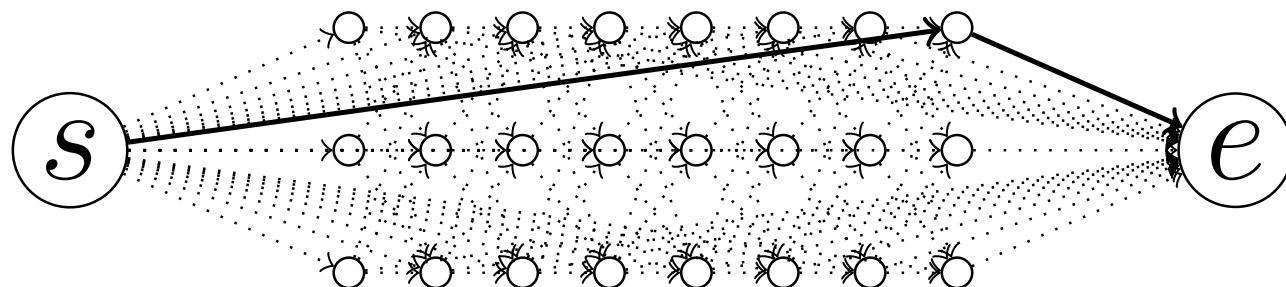
# Choice set generation in the activity network

- Based only on potential attractivity measure:  
too short (based on shortest path)



# Choice set generation in the activity network

- Force it to end on the platform: same problem
- Most likely output is



# Choice set generation in the activity network

- Attractivity is link additive
- With the Metropolis-Hastings algorithm, possibility to define non-link-additive cost
- Penalty for path length different from the observed ones

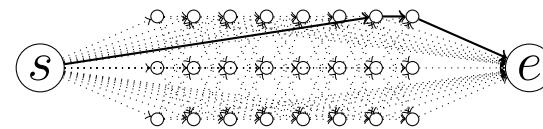
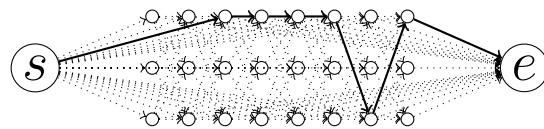
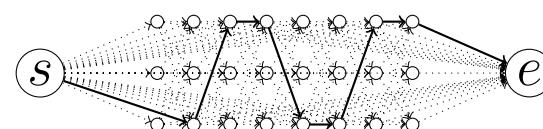
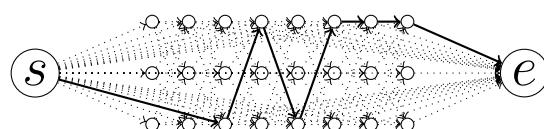
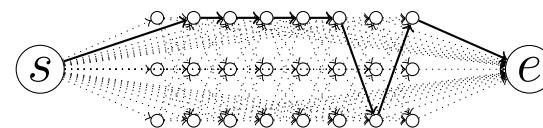
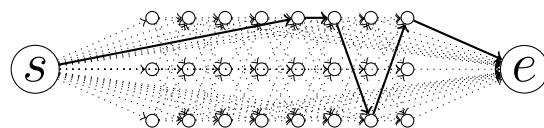
$$\delta_{\Gamma}(\Gamma) = \prod_{k=1}^K \left( \frac{1}{N} \sum_{\mathcal{A}_{1:T} \in N} \mathcal{I}(|\mathcal{A}_{1:T,k}| = |\Gamma_k|) \right)$$



# Choice set generation in the activity network

- With target weight defined as

$$\delta(\Gamma) = -\mu_v \cdot \sum_{v \in \Gamma} \delta_v(v) - \delta_\Gamma(\Gamma)$$



# Activity path choice model for WiFi traces

- Inspired by Bierlaire and Frejinger (2008) and Chen (2013): each individual  $n$  generates  $J$  network-free signals  $\hat{s}_{1:J}$

$$P(\hat{s}_{1:T}) = \sum_{\mathcal{A}_{1:T} \in \mathcal{U}} P(\hat{s}_{1:T} | \mathcal{A}_{1:T}) \cdot P(\mathcal{A}_{1:T} | \mathcal{U}; \beta)$$


  
 Measurement likelihood      Choice model



# Activity path choice model for WiFi traces: route choice model

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- To be operationalized, the model must correct
  - for the sampling of alternatives
  - for the correlation structure of a route choice

# Activity path choice model for WiFi traces: sampling of alternatives

- Frejinger et al. (2009): a sampling correction term must be added

$$\ln q(\mathcal{C}_n | \Gamma) = \ln \frac{k_{\Gamma_n}}{q(\Gamma)}$$

Nb of occurrences  
Sampling probability

- Sampling probability requires full enumeration

$$q(\Gamma) = \frac{b(\Gamma)}{\sum_{\Gamma' \in \mathcal{U}} b(\Gamma')}$$

but cancels out in logit

# Activity path choice model for WiFi traces: sampling of alternatives

$$\begin{aligned} P(\Gamma | \mathcal{C}_n) &= \frac{e^{\mu V_{\Gamma n} + \ln \frac{k_{\Gamma n}}{q(\Gamma)}}}{\sum_{\Gamma' \in \mathcal{C}_n} e^{\mu V_{\Gamma n} + \ln \frac{k_{\Gamma' n}}{q(\Gamma')}}} \\ &= \frac{\sum_{\Gamma' \in \mathcal{U}} b(\Gamma') \cdot e^{\mu V_{\Gamma n} + \frac{k_{\Gamma n}}{b(\Gamma)}}}{\sum_{\Gamma' \in \mathcal{U}} b(\Gamma') \cdot \sum_{\Gamma' \in \mathcal{C}_n} e^{\mu V_{\Gamma n} + \frac{k_{\Gamma' n}}{b(\Gamma')}}} \\ &= \frac{e^{\mu V_{\Gamma n} + \frac{k_{\Gamma n}}{b(\Gamma)}}}{\sum_{\Gamma' \in \mathcal{C}_n} e^{\mu V_{\Gamma n} + \frac{k_{\Gamma' n}}{b(\Gamma')}}} \end{aligned}$$

# Activity path choice model for WiFi traces: path size

- Ben-Akiva and Bierlaire (1999): path size logit
- Path size attribute  $PS_p$  corrects the utility for the correlation related to overlapping segments

$$PS_{\Gamma} = \sum_{a \in \Gamma} \frac{1}{M_a} \frac{L_a}{L_{\Gamma}}$$

← Arcs and  
path length

- When using universal choice set, full enumeration

$$M_a = \sum_{\Gamma' \in \mathcal{U}} \delta_{a\Gamma'} \leftarrow \begin{array}{l} \text{link-path} \\ \text{incidence variable} \end{array}$$

- Frejinger et al. (2009): use a large set of paths

# Activity path choice model for WiFi traces: activity path size

- Due to the structure of the activity network, the activity path size is:

$$APS_{\Gamma} = \frac{1}{K^{\tau-1}}$$

- The deterministic part of the utility function

$$V_{\Gamma n} = \beta x + \ln \frac{k_{\Gamma n}}{b(\Gamma)} + \beta_{PS} \ln APS_{\Gamma}$$

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# CONCLUSION

# Conclusion

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- Discretization of time: loosing information but
  - Easier to specify
  - Integration of measurement error in the model
- Modeling framework
  - allows to define choice attributes related to the whole activity pattern (e.g., number of episodes, number of times in the shopping mall or restaurant, etc.)
  - does not need an *a priori* definition of primary activity
  - does not need the definition of *home*

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# FUTURE WORK



# Future work

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- Implementation of the model on campus data
- Currently: activity = location category
  - If the share of activities per location category does not change over time: prediction still all right
  - If they change? Stated preference survey about activities per location category?
- Once activity/location category chosen: destination choice conditional on it

$$P(a_{1:M_n}) = P(\mathcal{A}_{1:T}) \cdot P(x|\mathcal{A}_{1:T})$$



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# THANK YOU



# References

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