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# 1 Theoretical study

## 2 Numerical study

Omegas – normally distributed

### 2.1 $r_{\infty}(K)$ – simulated vs predicted

#### 2.1.1 Euler method

**Design and initiation** My implementation of the Euler method is object-oriented. This may not be the computationally most efficient way, but I'm still somewhat of a beginner with code, so I appreciate the clarity that object-oriented programming affords.

The first type of object is simply an Oscillator with three variables:  $\omega$ ,  $\theta_{t-1}$  and  $\theta_t$ . A  $\Delta t = 1$  is enough in the Euler method. An Oscillator gets initiated with its natural frequency and the current-period  $\theta$ . The last-period  $\theta$  is initiated as zero, since the first part of making an 'Euler step' forwards is to hand over  $\theta_t$  to  $\theta_{t-1}$ .

The other object type is the OscPopulation . It consists of a list of Oscillators and a construction mode, namely the distribution according to which the  $\omega$ s are distributed. When an OscPopulation is initiated, for each Oscillator a natural frequency and initial phase are drawn from the respective type of random distribution. An Oscillator object is then initiated with those values and assigned to a place in the list within the OscPopulation object.

#### Running the simulation

#### 2.1.2 Numerical integration

The strategy to integrate the consistency equation is to loop through different values of r and check which ones make the right-hand side approximately equal to one. In a loop around this one, we cycle through the different values for K to get the values of the desired  $r_{\infty}(K)$  relationship.

**2.2** 
$$r(t)$$
 for  $K = [1, 2]$ 

Omegas – uniformly distributed

- 2.3  $r_{\infty}(K)$
- 2.4 r(t) for different initial conditions  $\theta_0$
- 2.5 r(t) for different initial conditions  $\omega_0$