

$$P(\text{open} | X_1) = \frac{P(X_1 | \text{open}) P(\text{open})}{P(X_1)}$$

$$= \frac{P(X_1 | \text{open}) P(\text{open})}{P(X_1 | \text{open}) P(\text{open}) + P(X_1 | \sim \text{open}) P(\sim \text{open})}$$

$$P(X_1 | \text{open}) = 0.6$$

$$P(X_1 | \sim \text{open}) = 0.3$$

$$P(\text{open}) = P(\sim \text{open}) = \frac{1}{2}$$

$$P(\text{open} | X_1, X_2) = \frac{P(X_2 | \text{open}, X_1) P(\text{open} | X_1)}{P(X_2 | \text{open}, X_1) P(\text{open} | X_1) + P(X_2 | \sim \text{open}, X_1) P(\sim \text{open} | X_1)}$$

