

## K-means

1. Compute the new position of the cluster centres after 1 step of k-means. Data:  $\langle 1, 1 \rangle$ ,  $\langle 0, 2 \rangle$ ,  $\langle -1, 2 \rangle$ ,  $\langle 5, 6 \rangle$ ,  $\langle 7, 5 \rangle$ . Cluster centres:  $\langle -1, -1 \rangle$ ,  $\langle 4, 6 \rangle$ .

Points assigned to cluster  $\langle -1, -1 \rangle$ :  $\langle 1, 1 \rangle$ ,  $\langle 0, 2 \rangle$ ,  $\langle -1, 2 \rangle$

Points assigned to cluster  $\langle 4, 6 \rangle$ :  $\langle 5, 6 \rangle$ ,  $\langle 7, 5 \rangle$

New cluster centres:  $\langle (1+0-1)/3, (1+2+2)/3 \rangle = \langle 0, 1.66 \rangle$  and  
 $\langle (5+7)/2, (6+5)/2 \rangle = \langle 6, 5.5 \rangle$

2. Same as (1), with the single cluster centre:  $\langle 1, -1 \rangle$

New cluster centre:  $\langle 2.4, 3.2 \rangle$ .

3. Same as (1), with data:  $\langle 1, 3 \rangle$ ,  $\langle 2, 2 \rangle$ ,  $\langle 3, -1 \rangle$ ,  $\langle 4, 2 \rangle$ ,  $\langle 5, -3 \rangle$ ,  $\langle 5, 4 \rangle$ ,  $\langle 4, 5 \rangle$ ,  $\langle 3, -6 \rangle$ ,  $\langle 2, 5 \rangle$ ; and centres:  $\langle 0, 1 \rangle$ ,  $\langle 0, -1 \rangle$ .

Points assigned to cluster  $\langle 0, 1 \rangle$  =  $\langle 1, 3 \rangle$ ,  $\langle 2, 2 \rangle$ ,  $\langle 4, 2 \rangle$ ,  $\langle 5, 4 \rangle$ ,  $\langle 4, 5 \rangle$ ,  $\langle 2, 5 \rangle$

Points assigned to cluster  $\langle 0, -1 \rangle$  =  $\langle 3, -1 \rangle$ ,  $\langle 5, -3 \rangle$ ,  $\langle 3, -6 \rangle$

New cluster centres:  $\langle 3, 3.5 \rangle$ ,  $\langle 3.66, -3.33 \rangle$