## CS 61A Fall 2015

# Structure and Interpretation of Computer Programs

FINAL

### INSTRUCTIONS

- You have 3 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written  $8.5" \times 11"$  crib sheet of your own creation and the official CS 61A study guides.
- Mark your answers on the exam itself. We will not grade answers written on scratch paper.

Last name	
First name	
Student ID number	
BearFacts email (_@berkeley.edu)	
TA	
Room	
Seat	
Name of the person to your left	
Name of the person to your right	
All the work on this exam is my own. (please sign)	

#### 1. (10 points) From the Other Side

For each of the expressions in the table below, write the output displayed by the interactive Python interpreter when the expression is evaluated. The output may have multiple lines. If an exception is raised, write "Exception". If evaluation would run forever, write "Forever". If an iterator or generator value would be displayed, write "Iterator" (instead of something like <str\_iterator object at 0x...>).

The first three rows have been provided as examples.

Assume that you have started python3 and executed the following statements (which do not cause errors):

```
class Adele:
    times = '1000'
    def __init__(self, you):
        self.call = you
    def __str__(self):
        return self.times
class Hello(Adele):
    def __next__(self):
        return next(self.call)
never = iter('scheme2Bhome')
def any(more):
    next(never)
    print(outside)
    yield next(never)
    print(next(never))
    yield more(more)
outside = Hello(any(any))
```

Expression	Interactive Output
'a'	'a'
iter('a')	Iterator
print('a') + 1	a Exception
next(never)	S
next(outside)	
next(next(outside))	
list(never)[:3]	
next(next(outside))	

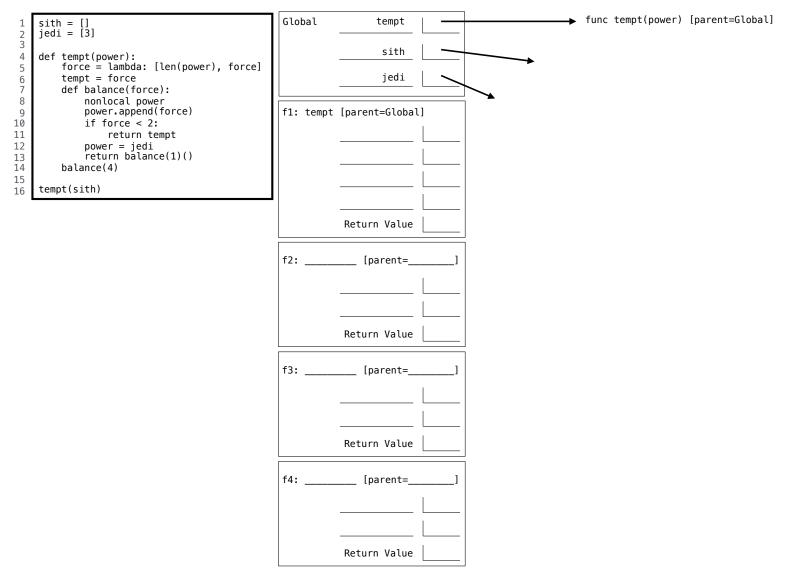
Name: \_\_\_\_\_\_\_ 3

#### 2. (16 points) Endor

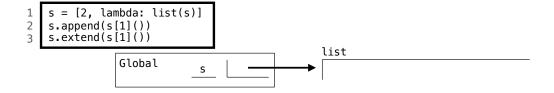
(a) (8 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames.

A complete answer will:

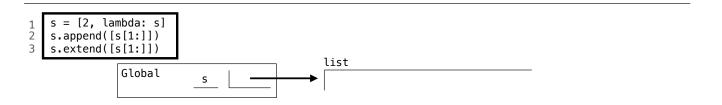
- Add all missing names and parent annotations to all frames.
- Add all missing values created or referenced during execution.
- Show the return value for each local frame.



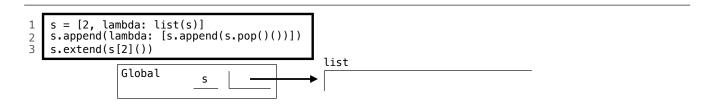
(b) (8 pt) Fill in the value for s in the global frame that results from executing each block of code below. You do not need to draw any local lambda frames. You must use box-and-pointer diagrams for full credit. The list methods append, extend, and pop are demonstrated on the midterm 2 study guide, page 2, right column. Hint: You may want to write your answer on scratch paper first in order to avoid messy diagrams.



func  $\lambda()$  line 1> [parent=Global]



func  $\lambda()$  line 1> [parent=Global]



Name: 5

5. (10 points) Forest Pat	3. (	10 points	Forest	Path
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**Definition.** A path through a Tree is a list of adjacent node values that starts with the root value and ends with a leaf value. For example, the paths of Tree(1, [Tree(2), Tree(3, [Tree(4), Tree(5)])]) are

```
[1, 2]
[1, 3, 4]
[1, 3, 5]
```

The Tree class is defined on the midterm 2 study guide. The one function defined below is used in the questions below to convert true and false values into the numbers 1 and 0, respectively.

```
def one(b):
    if b:
        return 1
    else:
        return 0
```

(a) (3 pt) Implement bigpath, which takes a Tree instance t and an integer n. It returns the number of paths in t whose sum is at least n. Assume that all node values of t are integers.

(b) (2 pt) Circle the  $\Theta$  expression that describes the number of paths in a tree with n nodes in which every non-leaf node has at least 2 branches.

 $\Theta(1)$   $\Theta(\log n)$   $\Theta(n)$   $\Theta(n^2)$   $\Theta(2^n)$ 

**Definition.** A path through a Tree is a list of adjacent node values that starts with the root value and ends with a leaf value. For example, the paths of Tree(1, [Tree(2), Tree(3, [Tree(4), Tree(5)])]) are

```
[1, 2]
[1, 3, 4]
[1, 3, 5]
```

(c) (3 pt) Implement allpath which takes a Tree instance t, a one-argument predicate f, a two-argument reducing function g, and a starting value s. It returns the number of paths p in t for which f(reduce(g, p, s)) returns a true value. The reduce function is on the final study guide. You do not need to call it, though.

```
def allpath(t, f, g, s):
      """Return the number of paths p in t for which f(reduce(g, p, s)) is true.
      >>> t = Tree(1, [Tree(2), Tree(3, [Tree(4), Tree(5)])])
      >>> even = lambda x: x % 2 == 0
      >>> allpath(t, even, max, 0) # Path maxes are 2, 4, and 5; 2 & 4 are even
      >>> allpath(t, even, pow, 2)  # E.g., pow(pow(2, 1), 2) is even
      >>> allpath(t, even, pow, 1) # Raising 1 to any power is odd
      .....
      if t.is_leaf():
         return one(_____)
      return sum([____])
(d) (2 pt) Re-implement bigpath (part a) using allpath (part c). Assume allpath is defined correctly.
  from operator import add, mul
  def bigpath(t, n):
      """Return the number of paths in t that have a sum larger or equal to n.
      >>> t = Tree(1, [Tree(2), Tree(3, [Tree(4), Tree(5)])])
      >>> bigpath(t, 3)
      >>> bigpath(t, 6)
      >>> bigpath(t, 9)
      1
      .....
      return allpath(t, _____, , _____, , _____)
```

Name: 7

#### 4. (8 points) Cucumber

Cucumber is a card game. Cards are positive integers (no suits). Players are numbered from 0 up to players (0, 1, 2, 3 in a 4-player game). In each Round, the players each play one card, starting with the starter and in ascending order (player 0 follows player 3 in a 4-player game). If the card played is as high or higher than the highest card played so far, that player takes control. The winner is the last player who took control after every player has played once. Implement Round so that play\_round behaves as described in the doctests below. Part of your score on this question will be assigned based on *composition* (don't repeat yourself).

```
def play_round(starter, cards):
   """Play a round and return all winners so far. Cards is a list of pairs.
   Each (who, card) pair in cards indicates who plays and what card they play.
   >>> play_round(3, [(3, 4), (0, 8), (1, 8), (2, 5)])
   >>> play_round(1, [(3, 5), (1, 4), (2, 5), (0, 8), (3, 7), (0, 6), (1, 7)])
   It's not your turn, player 3
   It's not your turn, player 0
   The round is over, player 1
   [1, 3]
   >>> play_round(3, [(3, 7), (2, 5), (0, 9)]) # Round is never completed
   It's not your turn, player 2
   [1, 3]
   r = Round(starter)
   for who, card in cards:
      try:
         r.play(who, card)
      except AssertionError as e:
         print(e)
   return Round.winners
class Round:
   players, winners = 4, []
   def __init__(self, starter):
      self.starter, self.player, self.highest = starter, starter, -1
   def play(self, who, card):
      assert _____, 'The round is over, player '+str(who)
      assert _____, "It's not your turn, player "+str(who)
      self.player = _____
      if card >= self.highest:
          ______ , _____ , _____ = _____ , ______ , _______
      if _____:
         self.winners.append(self.control)
   def complete(self):
      return _____
```

#### 5. (14 points) Grouper

(a) (4 pt) Implement group, which takes a one-argument function f and a list s. It returns a list of groups. Each group is a list that contains all the elements x in s that return equal values for f(x). The elements in a group appear in the same order that they appeared in s. The groups are ordered by the order in which their first elements appeared in s.

(b) (4 pt) Implement group\_link, which takes a one-argument function f and a Link instance s. It returns a linked list of groups. Each group is a Link instance containing all the elements x in s that return equal values for f(x). The order of groups and elements is the same as for group. The Link class appears on your midterm 2 study guide. The filter\_link function appears in the appendix on the last page of this exam.

Name: 9

**Definition.** The multi-grouping by function f of list s is formed by the following iterative process with k starting at 0 and increasing by 1 each iteration.

- Group together all elements that yield equal values when applying f repeatedly, k times.
- If all elements are in a single group, the process is complete. Otherwise, place each new group in a (possibly nested) list and repeat.

For example, if f is lambda x: max(x-3, 0) and s is [2, 4, 3, 4, 2], then

return 3 \* x + 1

- In the k=0 iteration, the 2's are grouped, the 4's are grouped, and the 3 is alone: [[2, 2], [3], [4, 4]]
- In the k=1 iteration, f(2)==f(3), and so the 2's group and 3's group are grouped: [[[2, 2], [3]], [[4, 4]]]
- In the k=2 iteration, f(f(2))==f(f(3))==f(f(4)). All elements are in a single group, so we're done.
- (c) (4 pt) Implement multigroup, which returns the multi-grouping by f of a list s. Assume that the process terminates and that group (part a) is implemented correctly.

```
def multigroup(f, s):
      """Return a multi-grouping by f of the elements in s.
      >>> multigroup(lambda x: max(x-3, 0), [2, 4, 3, 4, 2])
      [[[2, 2], [3]], [[4, 4]]]
      >>> multigroup(abs, [5])
      >>> multigroup(abs, [5, 5])
      [5, 5]
      >>> multigroup(abs, [5, 5, -5])
      [[5, 5], [-5]]
      >>> multigroup(lambda x: x // 10, [123, 145, 126, 149])
      [[[123], [126]], [[145], [149]]]
      >>> multigroup(lambda x: x[1:], ['tin', 'man', 'can'])
      [[['tin']], [['man'], ['can']]]
      >>> multigroup(lambda x: max(x-1, 0), [2, 4, 3, 4, 2])
      [[[[2, 2]]], [[[3]]], [[[[4, 4]]]]
      def using(g, s):
          if len(s) == 1:
              return _____
          else:
              grouped = group(g, s)
              return using(lambda x: _____, grouped)
      return using(lambda x: _____, s)
(d) (2 pt) How many square brackets are in the return value of multigroup(hail, [3, 20, 128])? Assume
  that multigroup is implemented correctly.
   def hail(x):
      if x == 1:
          return 1
      elif x % 2 == 0:
          return x // 2
      else:
```

#### 6. (10 points) Pair Emphasis

(a) (6 pt) Implement parens by crossing out whole lines below. It takes a Scheme value and returns the number of parentheses required to write the value in standard Scheme notation.

```
; Return the number of parentheses in s.
  (parens 3)
                         -> 0
                         -> 2
  (parens (list 3 3))
 (parens '(3 . 3))
 (parens '(3 . (3)))
                        -> 2
                               because (3.(3)) simplifies to (3.3)
 (parens '((3)))
                         -> 4
  (parens '(()))
; (parens '((3)((3)))) \rightarrow 8
(define (parens s)
    (f s 0))
    (f s 2))
    (f s #f))
    (f s #t))
(define (f s t)
    (cond ((pair? s) (+
           1
            2
            t
            (if t 1 0)
            (f (car s) 0)
            (f (cdr s) 0)
            (f (car s)
                       2)
            (f (cdr s)
            (f (car s) #t)
            (f (cdr s) #f)
            (f (car s) t)
            (f (cdr s) t)
          ))
           ((null? s)
           0
           1
            2
            (if t 1 0)
          (else 0)))
```

(b) (2 pt) Write a quote expression that evaluates to the Scheme list (1 (2) 3) that has as many parentheses as possible in the expression. For example, a well-formed (but incorrect) answer is (quote (1 (2) 3)).

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(c) (2 pt) How many total calls to scheme\_eval would be required to evaluate (parens 3) in your Scheme interpeter (Project 4)? Assume that parens is implemented correctly. Assume you are not using the tail-recursive scheme\_optimized\_eval.

Name:	11
7. (12 points) Highly Exclusive	
(a) (4 pt) Complete the definition of no-fib, the stream of all positive in These are all positive integers excluding 1, 2, 3, 5, 8, 13, The stream	
(define (p prev curr n)	
(if	
	))
(define no-fib (p 3 5 4))	
(b) (4 pt) A Hamming number is a positive integer that has no prime far Hamming numbers are pow(2, i) * pow(3, j) * pow(5, k) for so The first 20 Hamming numbers are 1, 2, 3, 4, 5, 6, 8, 9, 10, 12, 15, 16 Complete the SQL statements below so that the final statement general as its rows the Hamming numbers less than 100 in increasing order.	ome non-negative integers i, j, and k. , 18, 20, 24, 25, 27, 30, 32, and 36.
create table t as select 2 as k union select 3 us	nion select 5;
with ham(n) as (	
select	union
select from	where
) select n from ham order by n;	
(c) (4 pt) Select all positive integers that have at least 3 proper multiple proper multiple $m$ of $n$ is an integer larger than $n$ such that $n$ evenly	
The resulting table should have two columns. Each row contains a multiples) and the number of its proper multiples up to X. For example up to 20: 6, 9, 12, 15, and 18. Therefore, 3 5 is a row. There are five 2 9, 3 5, 4 4, and 5 3. Your statement must work correctly even if as 30) to receive full credit.	le, the integer 3 has 5 proper multiples rows in the table when X is 20: 1 19,
<pre>create table X as select 20 as X; with ints(n) as (select 1 union select n+1 from</pre>	ints, X where n < X)
select from	
where	
*****	
group by having _	

8. (0 points) Draw! (Optional) In 2050, what will a CS 61A teaching assistant (GSI/UGSI) look like?

```
Appendix. This is not a question.

def filter_link(f, s):
    """Return a Link with the elements of s for which f returns a true value."""
    if s is Link.empty:
        return s
    else:
        filtered = filter_link(f, s.rest)
        if f(s.first):
            return Link(s.first, filtered)
        else:
            return filtered
```