

CS 6290

Privacy-enhancing Technologies

Department of Computer Science

Slides credit in part from E. Ben-Sasson, D. Dziembowski, I. Eyal, R. Geambasu, and F. Greenspan, A. Judmayer, A. Juels, A. Miller, J. Poon, V. Shmatikov, D. Song, and F. Zhang

Lecture 1 – Introduction

Prof. Cong WANG

CS Department
City University of Hong Kong

When people talk about privacy...



“If you've done
nothing wrong...”

“Get over it”



“No one cares”

2010



1999

2009



Privacy
is King.

That's iPhone.

The future is private.



(Facebook's F8 developer conference in 2019)

Rising privacy concerns

Target data theft affected 70 million customers

⌚ 10 January 2014

Nearly one billion people in China had their personal data leaked, and it's been online for more than a year

By [Yong Xiong](#), [Hannah Ritchie](#) and [Nectar Gan](#), CNN
6 minute read · Updated 11:31 PM EDT, Tue July 5, 2022

Meta Paid More Than \$300 Million for Personal Data

Processing

It comes after Irish officials also fined Meta, saying the Facebook and Instagram owner stored some user passwords without proper safeguards

By [Mauro Orru](#) [Follow](#)
Oct. 24, 2024 6:30 am ET

Major data breaches

Entity	Year	Records	Organization type	Method	Sources
Yahoo	2013	3,000,000,000	web	hacked	[640] [641]
National Public Data	2024	2,900,000,000+ (claimed), including names, email addresses, phone numbers, Social Security numbers, and mailing addresses	data broker	hacked	[471]
Verifications.io (total leaks)	2019	2,000,000,000	online marketing	poor security	[620]
First American Corporation	2019	885,000,000	financial	poor security	[343]
Verifications.io (first leak)	2019	809,000,000	online marketing	poor security	[619]
Collection No. 1	2019	773,000,000	various	compilation of multiple data breaches	[256]
Ticketmaster	2024	560,000,000	ticket distribution	hacked third party service	[579] [580]
Facebook	2019	540,000,000	social network	poor security	[333] [334]
Marriott International	2018	500,000,000	hotel/casino	hacked	[444]
Yahoo	2014	500,000,000	web	hacked	[642] [643] [644] [645] [646]
Friend Finder Network	2016	412,214,295	web	poor security / hacked	[347] [348]
Myspace	2016	360,000,000+, including usernames, passwords email addresses	social network	poor security/account recovery	[467] [468] [469]

https://en.wikipedia.org/wiki/List_of_data_breaches

Reasons?

Big data and machine learning technologies **push away** from privacy principles.

E.g., Foundational Fair Information Practices (FIPs):

- Collection limitation
 - Data quality
 - Purpose specification
 - Use limitation
 - Security
 - Openness/notice
 - Individual participation
 - Accountability
- 
- ```
graph LR; A1[• Collection limitation] --> B1[• Security]; A2[• Data quality] --> B2[• Openness/notice]; A3[• Purpose specification] --> B3[• Individual participation]; A4[• Use limitation] --> B4[• Accountability];
```

# Privacy-enhancing technologies to answer:

- How can we guarantee that the collected user data are not misused and privacy policies not violated?
- How can we protect user privacy while simultaneously allowing effective data sharing and utilization?
- When the servers are not fully trusted, how can we still provide desirable services to users and respect their privacy?

# Teaching team

- Instructor:
  - Prof. Cong WANG
  - Tel(O): +852 3442 2010
  - Email: [congwang@cityu.edu.hk](mailto:congwang@cityu.edu.hk)
- Teaching assistant:
  - Dr. Yufei CHEN
  - Email: [yufeichen8@cityu.edu.hk](mailto:yufeichen8@cityu.edu.hk)

# Teaching materials

- Weekly lecture notes, tutorials, reading materials
  - usually provided before class
- No required textbook; several recommended books:
  - **Bitcoin and Cryptocurrency Technologies: A Comprehensive Introduction**, by Arvind Narayanan, Joseph Bonneau, Edward Felten, Andrew Miller, and Steven Goldfeder
  - **Introduction to Modern Cryptography**, by Jonathan Katz and Yehuda Lindell
  - **The Algorithmic Foundations of Differential Privacy**, by Cynthia Dwork and Aaron Roth
  - **A Pragmatic Introduction to Secure Multi-Party Computation**, by David Evans, Vladimir Kolesnikov, and Mike Rosulek

# Teaching pattern

- Lecture and Tutorials (3 hours per week)
  - Information sessions
  - Discussions on commonly asked question
  - Discussions based on lecture materials/assigned readings

# Assessment

- **60% Continuous Assessment:**
  - 30% assignments
    - 3 programming-based assignments to be submitted in total
    - Per assignment: implementation code + experiment report
  - 30 % group project + oral presentation
    - 3 students per group
    - System projects, theoretical projects, or survey projects
- **40% Final Examination**
- Plagiarism will not be tolerated

# Announcements and Q&A

- You have to check Canvas and emails!
  - Announcements, material, assignments, etc.
- Ask questions:
  - Use canvas->discussions
    - Serve like a public bulletin so everyone can see the discussions
    - TA and I will check the discussions
  - Email to me or TA
    - Use CityU mailbox, i.e., [congwang@cityu.edu.hk](mailto:congwang@cityu.edu.hk)
    - Do **NOT** use Canvas->mailbox (inbox)!
      - Mails could get lost...

# Tentative course overview

- An introduction to four advanced topics and their respective privacy-enhancing technologies, including:
  - **Part I: Cryptocurrency and blockchain systems**
    - Bitcoin and how it works, smart contracts, dApps, and DeFi
  - **Part II: Confidential computing technologies**
    - Focus on zero-knowledge proof (ZKP), secure multi-party computation (MPC), and secure hardware
  - **Part III: Data privacy**
    - Data attacks, k-anonymization, differential privacy
  - **Part IV: Privacy in the wild**
    - Online tracking and countermeasures, private machine learning, and other trending technologies

# Tentative course overview

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# The rise of cryptocurrencies

Bitcoin Price (USD) – Source : coinbase.com



- Bitcoin sparked research into multiple challenging areas and applications
  - More than 2000+ cryptocurrency startups

# Bitcoin use today

# Online sites

1.

## Get Bitcoin

There are several ways to get Bitcoins, but the easiest is to exchange them for currency at your bank or a Bitcoin exchange. You can also buy Bitcoins from friends, accept them as payment for goods or services, or generate new Bitcoins through a process called "mining."

[Sign Up at Coinbase.com](#)



2.

## Shop Overstock.com

You can now pay for all your favorite products on Overstock.com using Bitcoins! As the first major retailer to accept Bitcoins, Overstock.com is expanding the possibilities of Bitcoin purchases by offering thousands of products to the Bitcoin community.

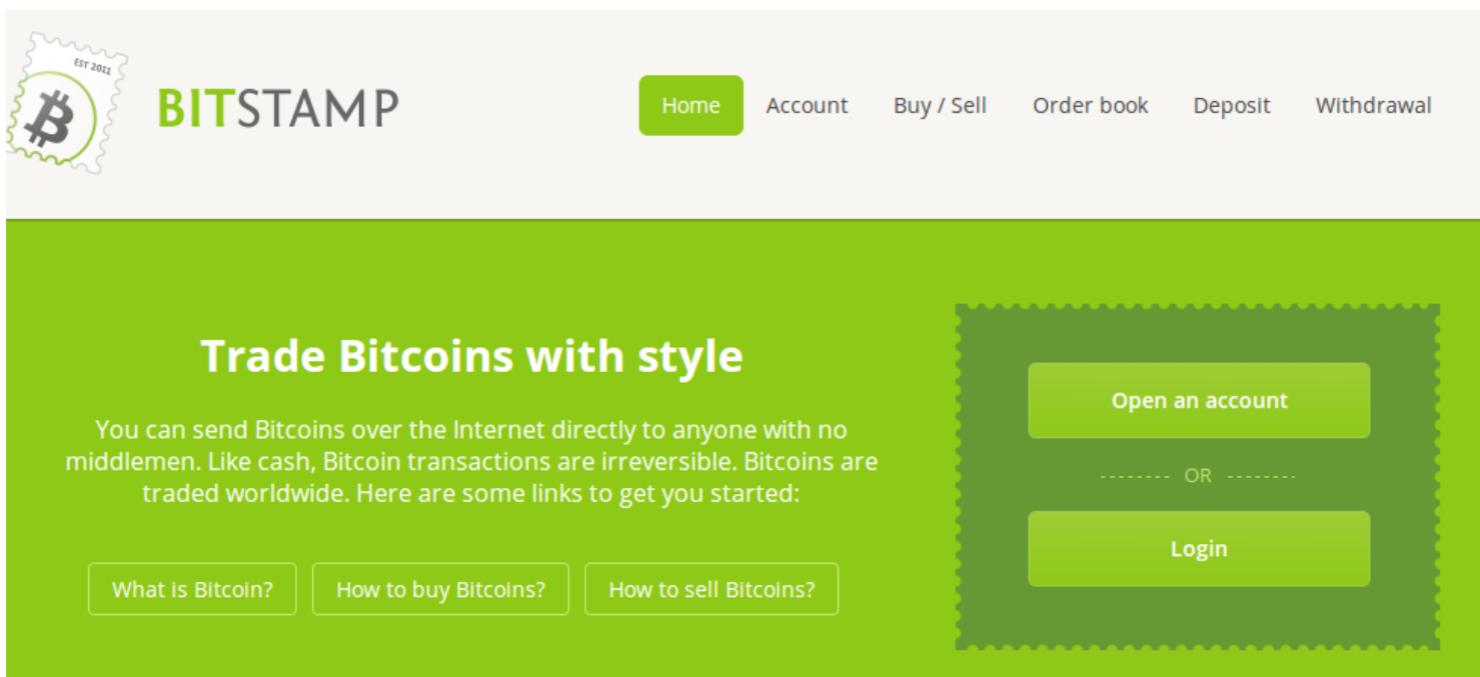


# ATMs



Sell your Bitcoins!

# Bitcoin exchanges



Tyler Moore and Nicolas Christin. Beware the middleman: Empirical analysis of Bitcoin-exchange risk. *Financial Cryptography*, 2013.

# Bitcoins has its dark sides



The image is a composite of two screenshots. On the left, the Silk Road anonymous market website is shown. It features a logo with a camel and the text 'Silk Road anonymous market'. Below the logo is a sidebar with a 'Shop by Category' section. The categories listed are: Drugs (2,399), Cannabis (341), Dissociatives (65), Ecstasy (209), Opioids (156), Other (144), Precursors (12), Prescription (526), Psychedelics (427), and Stimulants (273). Other categories include Apparel (114), Art (7), Books (743), Collectibles (12), Computer equipment (19), Custom Orders (26), Digital goods (310), Drug paraphernalia (89), Electronics (20), Erotica (319), Fireworks (2), Food (3), Forgeries (58), Hardware (2), Home & Garden (7), Jewelry (48), Lab Supplies (5), Lotteries & games (29), and Medical (5). On the right, a red Cryptolocker 2.0 message box is displayed. The box has a large shield icon in the center. The text inside the box reads: 'Your personal files are encrypted', 'Your files will be lost without payment on: 11/24/2013 3:16:34 PM', 'To retrieve the private key, you need to pay 0.5 bitcoins.', 'Click proceed to payment to obtain private key.', and 'Any attempt to remove or damage this software will lead to immediate private key destruction by server.' A yellow oval highlights the text 'To retrieve the private key, you need to pay 0.5 bitcoins.' Below the message box, there are links for 'See files', '<< Back', and 'Proceed to payment >>'. At the bottom, there is a note: 'Why bother with newcomers to the SR Crystal scene with high prices and international customs hoopla..... Best price on SR, and operates with your safety in mind.' and '-----Δ•This listing is for 1g of Crystal•Δ-----'.

**Tor + Bitcoin = End-to-end anonymity for commercial transactions**

# Bitcoins has its dark sides

Bitcoin has stimulated

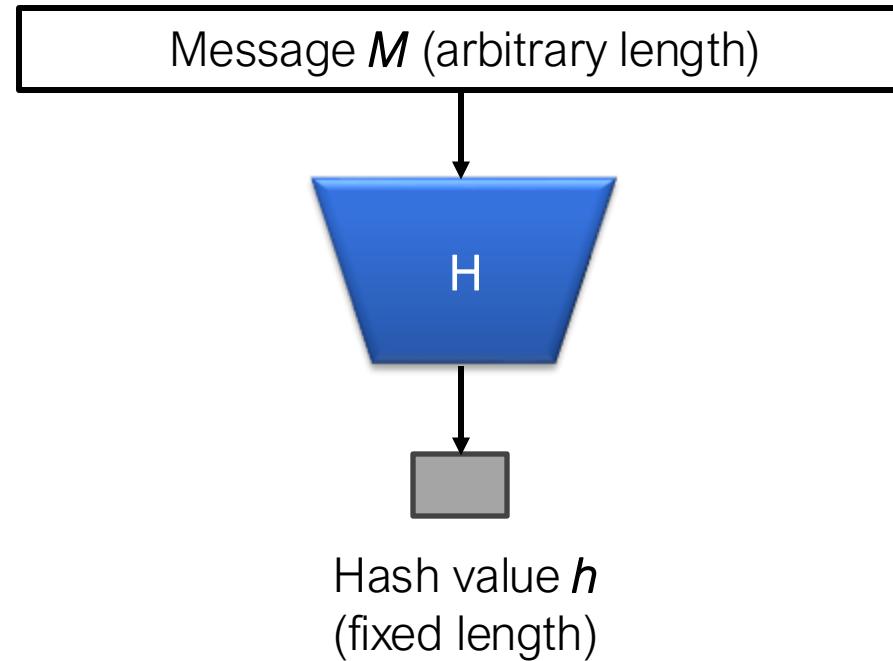
- Money laundering
- Theft of Bitcoin wallets
- Illicit marketplaces (Silk Road)
- Rogue mining
  - E.g., ZeroAccess botnet
- Ransomware



# How bitcoin works?

# Background: Hash function

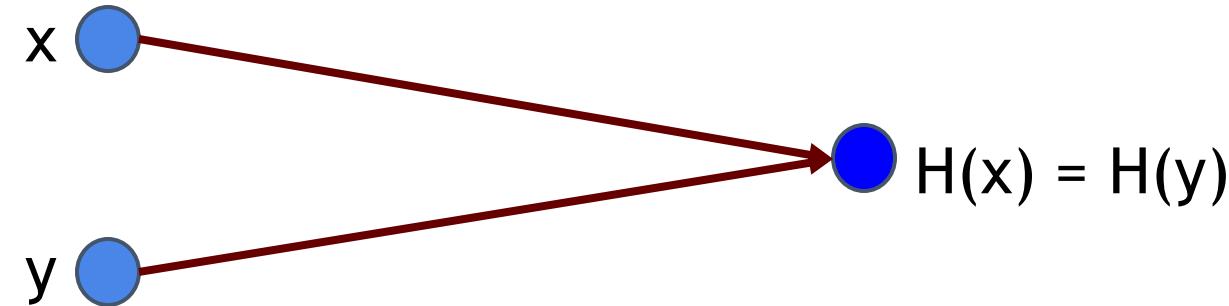
- Map data of arbitrary size to data of a fixed size
  - E.g., takes any string as input and generates fixed-size output  
**(we'll use 256 bits)**
  - Efficiently computable
- Security properties:
  - Collision-resistant
  - Hiding
  - Puzzle-friendly



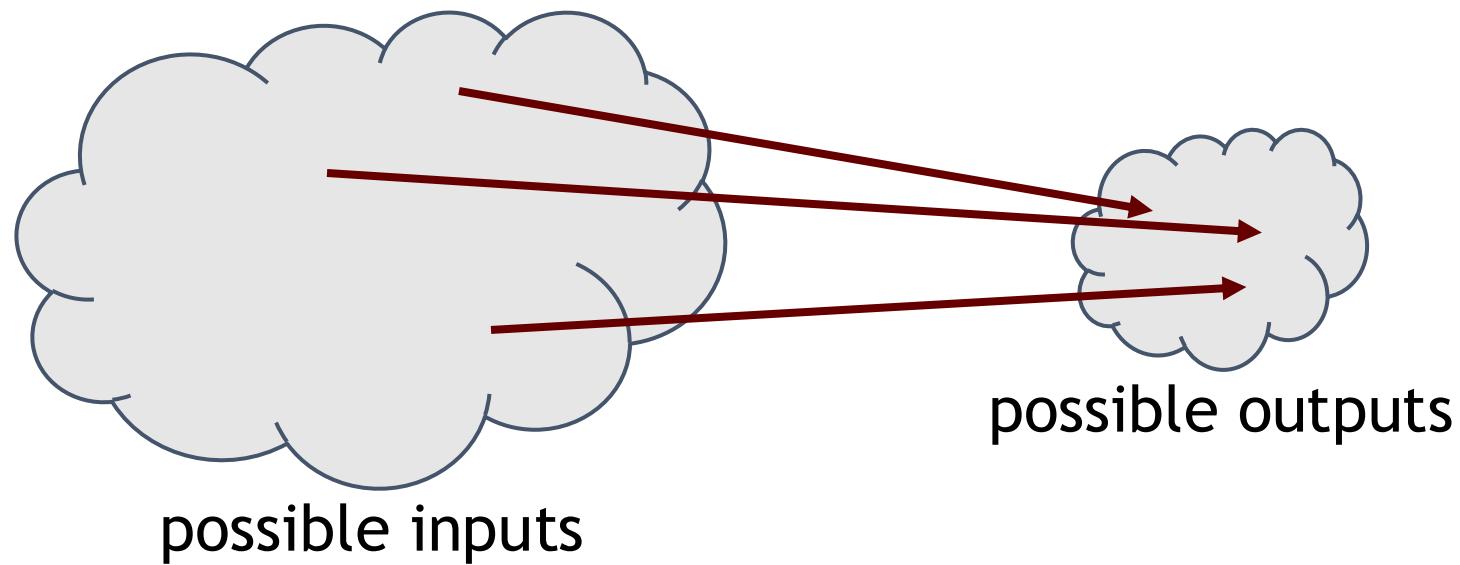
# Property 1: Collision-resistant

- Difficult to find  $x$  and  $y$  such that

$$x \neq y \text{ and } H(x) = H(y)$$



# Collisions do exist ...



## ... but can anyone find them?

# How to find a collision

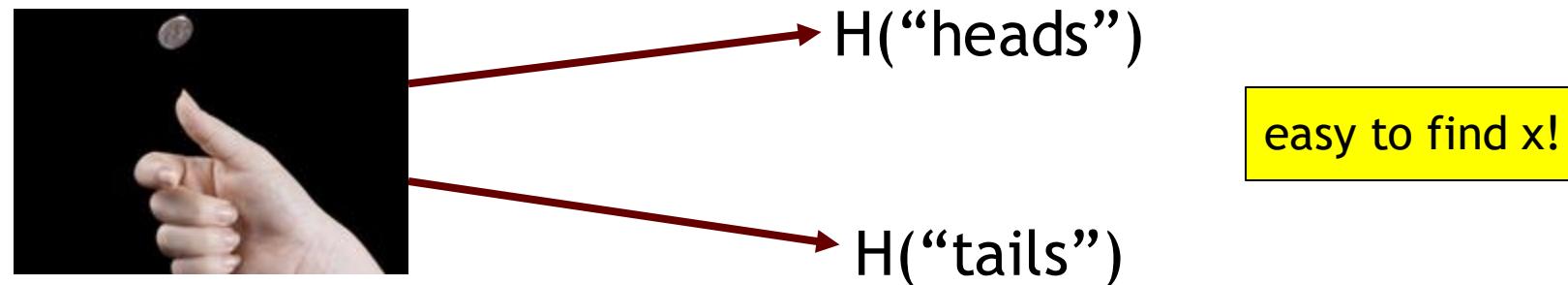
- A cryptographic hash is expected to have a collision resistance strength of  $n/2$  bits (lower due to birthday paradox)
    - If you can randomly generate a sequence  $2^{130}$  inputs 99.97% chance that two of them will collide
  - This works no matter what  $H$  is ...
  - But it takes too long to matter
- Is there a faster way to find collisions?
- For some possible  $H$ 's, yes.
- For others, we don't know of one.
- No  $H$  has been proven collision-free.

# Application: Hash as message digest

- If we know  $H(x) = H(y)$ ,  
it's safe to assume that  $x = y$ .
- To recognize a file that we saw before, just remember its hash.
- Useful because the hash is small for network transmission.

# Property 2: Hiding

- We want something like this:  
**Given  $H(x)$ , it is infeasible to find  $x$ .**



# Hiding property

- If  $r$  is sampled uniformly at random from a high-entropy domain, then given an outcome  $H(r \mid \mid x)$ , it is infeasible to find  $x$ .

Note:  $r$  is a secret and is **NOT given** here.

No particular value is chosen with more than negligible probability.

# Commitment API

- $(com, key) := \text{commit}(msg)$
- $match := \text{verify}(com, key, msg)$
- Security properties:
  - Hiding: Given  $com$ , infeasible to find  $msg$ .
  - Binding: Infeasible to find  $msg \neq msg'$  such that  $\text{verify}(\text{commit}(msg), msg') == \text{true}$

# Concrete construction sample

- $\text{commit}(\text{msg}) := (\text{H}(\text{key} \mid \text{msg}), \text{H}(\text{key}))$   
where  $\text{key}$  is a random 256-bit value
- $\text{verify}(\text{com}, \text{key}, \text{msg}) := (\text{H}(\text{key} \mid \text{msg}) == \text{com})$
- Security properties:
  - Hiding: Given  $\text{H}(\text{key} \mid \text{msg})$ , infeasible to find  $\text{msg}$ .
  - Binding: Infeasible to find  $\text{msg} \neq \text{msg}'$  such that
$$\text{H}(\text{key} \mid \text{msg}) == \text{H}(\text{key} \mid \text{msg}')$$

# Property 3: Puzzle-friendly

Puzzle-friendly:

- For **every possible** output value  $y$ ,  
if  $k$  is chosen uniformly at random and **public** to all,  
then it is **infeasible** to find  $\underline{x}$  such that  $H(k \mid \underline{x}) = y$ .

# Application: Search puzzle

- Given a “puzzle ID”  $k$ ,  
and a target set  $Y$ :

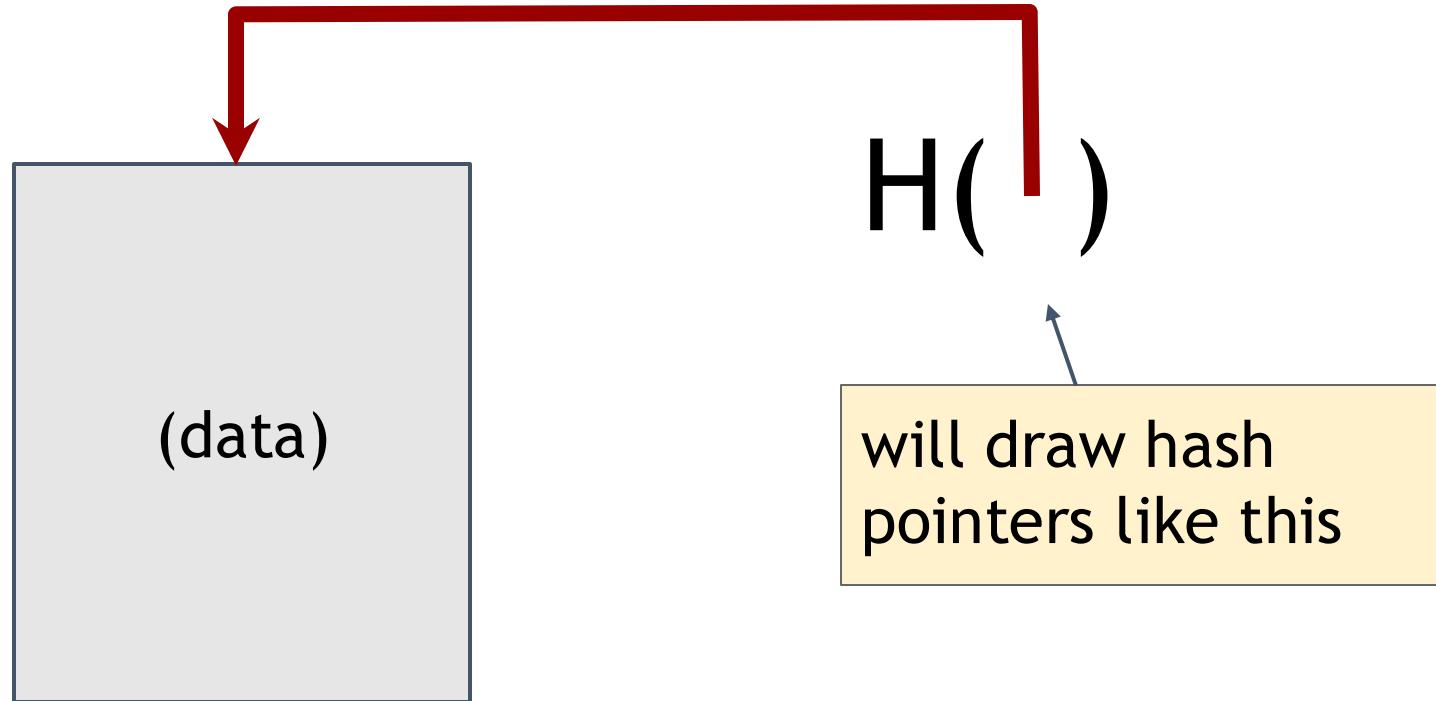
Try to find a “solution”  $x$  such that

$$H(k | x) \in Y.$$

- Puzzle-friendly property implies that no solving strategy is much better than trying random values of  $x$ .

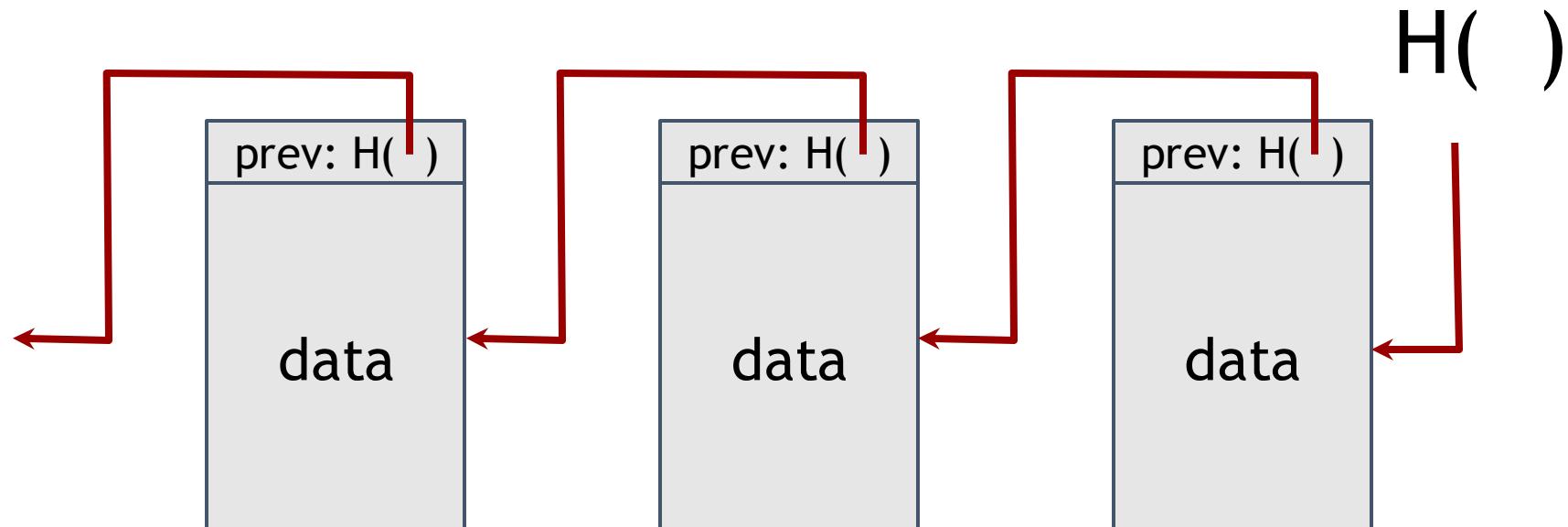
# Hash pointers

- Hash pointer is:
  - pointer to where some info is stored, and
  - (cryptographic) hash of the info
- If we have a hash pointer, we can
  - ask to get the info back, and
  - verify that it hasn't changed



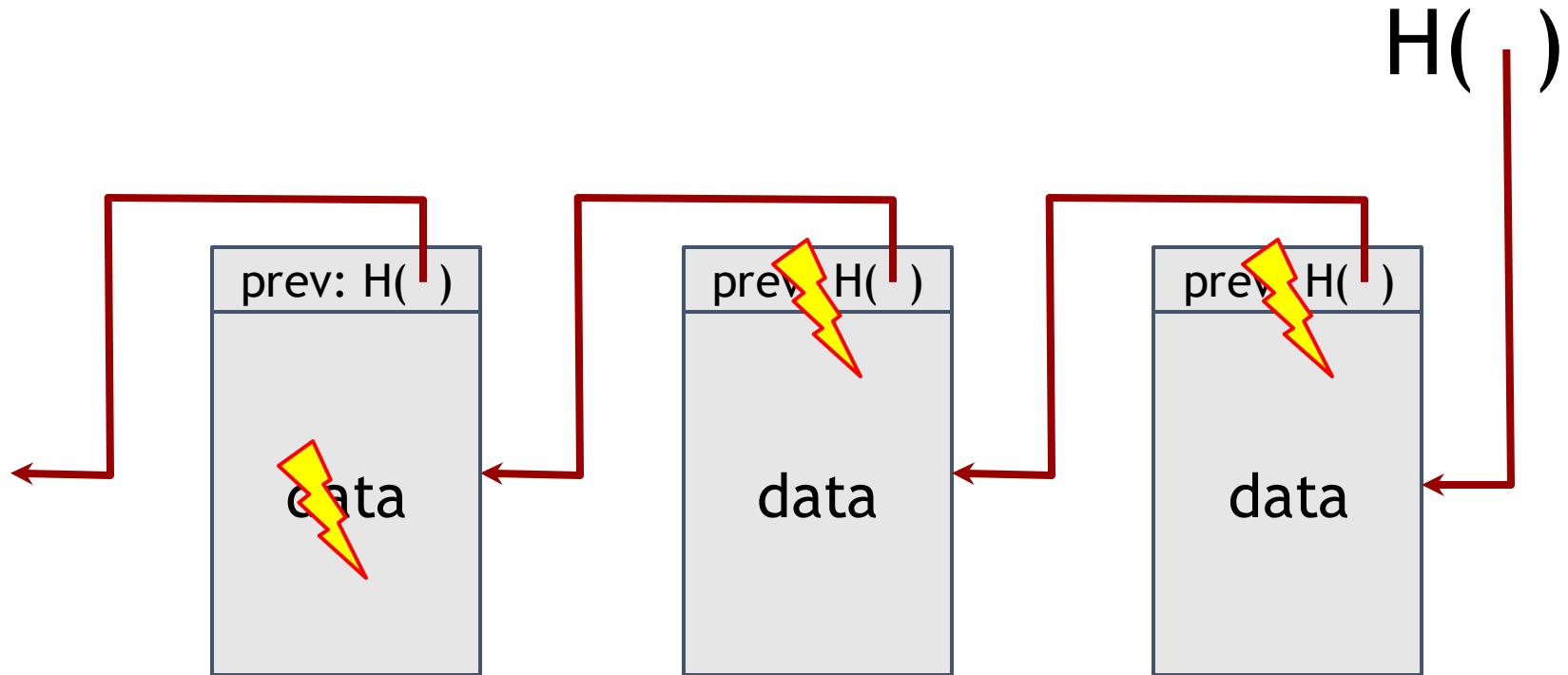
# “Blockchain”

- key idea: build data structures with hash pointers
- linked list with hash pointers = “block chain”



use case: tamper-evident log

# Detecting tampering



use case: tamper-evident log

# Background: Digital signatures

- What we want from signatures:
  - Only you can sign, but anyone can verify
  - Signature is tied to a particular document

$(sk, pk) := \text{generateKeys}(\text{keysize})$

sk: secret signing key

pk: public verification key

$\text{sig} := \text{sign}(sk, \text{message})$

$\text{isValid} := \text{verify}(pk, \text{message}, \text{sig})$

API for digital signatures

# Requirements for signatures

- “valid signatures verify”
  - $\text{verify}(\text{pk}, \text{message}, \text{sign}(\text{sk}, \text{message})) == \text{true}$
- “can’t forge signatures”
  - adversary who:
    - knows pk
    - gets to see signatures on messages of his choice
  - can’t produce a verifiable signature on another message

## Useful trick: public key == an identity

if you see sig such that  $\text{verify}(\text{pk}, \text{msg}, \text{sig}) == \text{true}$ ,  
think of it as

$\text{pk}$  says, “[ $\text{msg}$ ].

to “speak for”  $\text{pk}$ , you must know matching secret key  $\text{sk}$



GoofyCoin

Goofy can create new coins

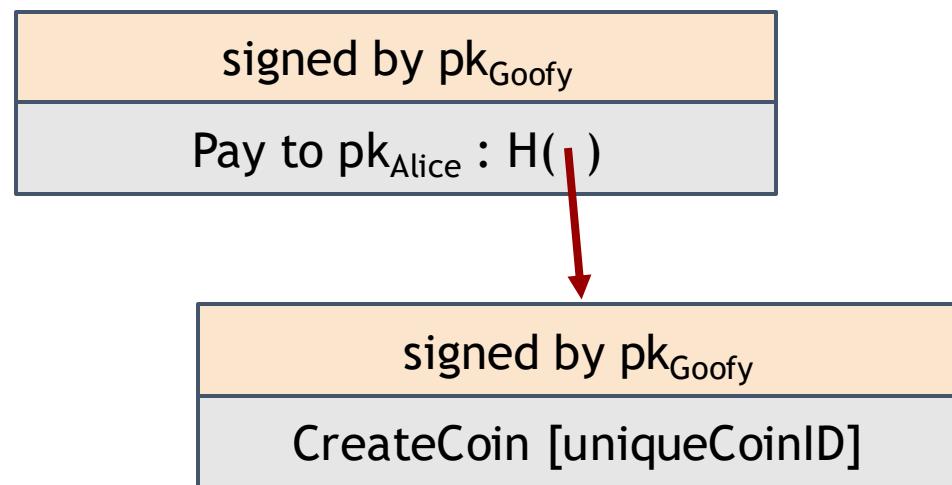
signed by  $pk_{Goofy}$

CreateCoin [uniqueCoinID]

New coins belong to me.



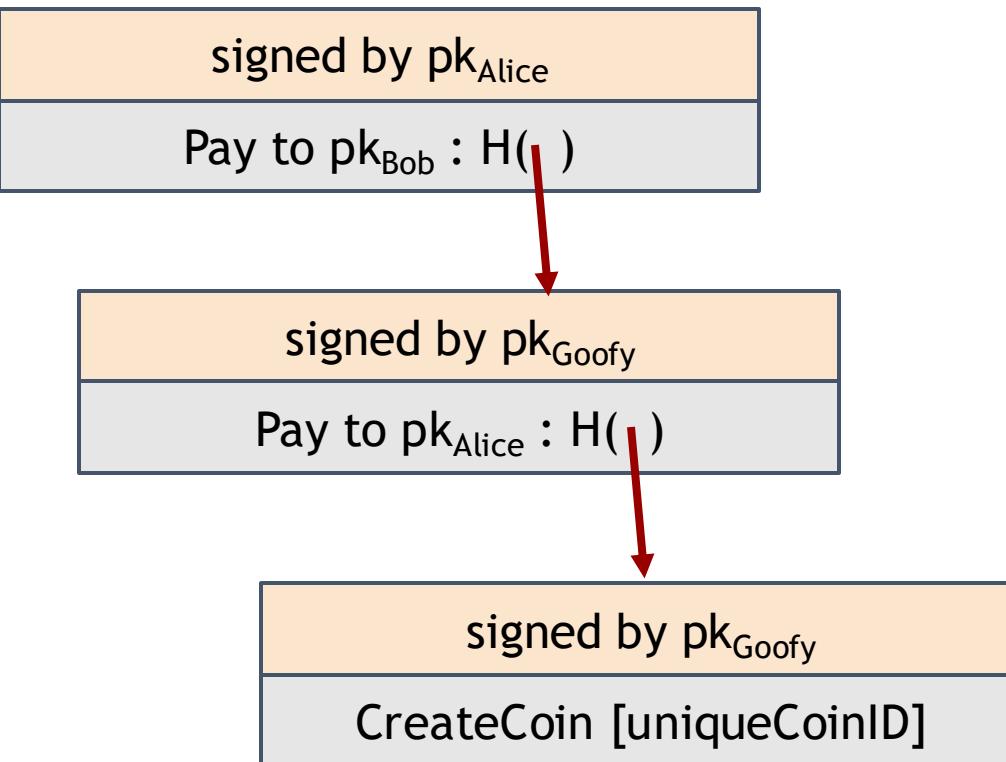
A coin's owner can spend it.



Alice owns it now.



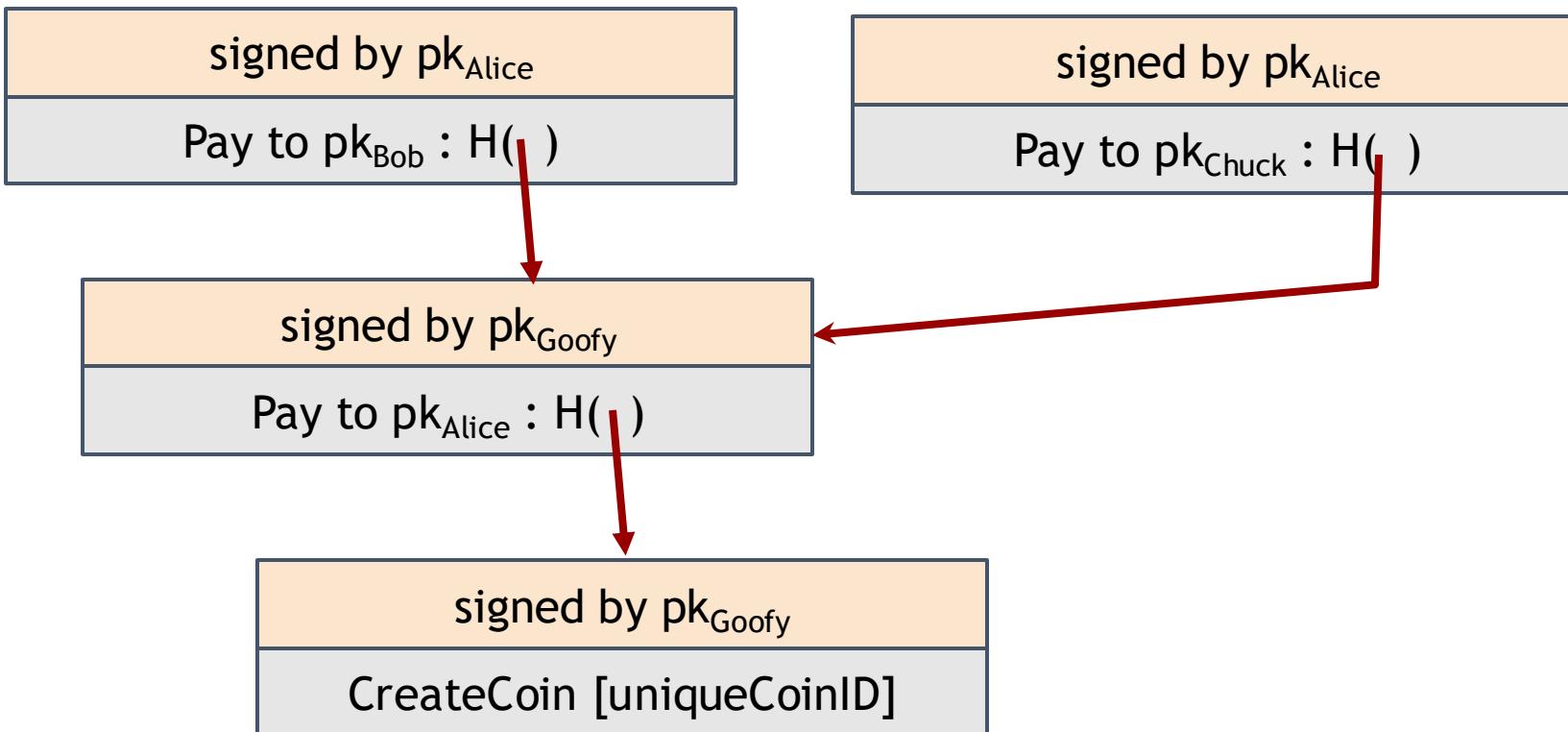
The recipient can pass on the coin again.



Bob owns it now.



# double-spending attack



double-spending attack

the main design challenge in digital currency

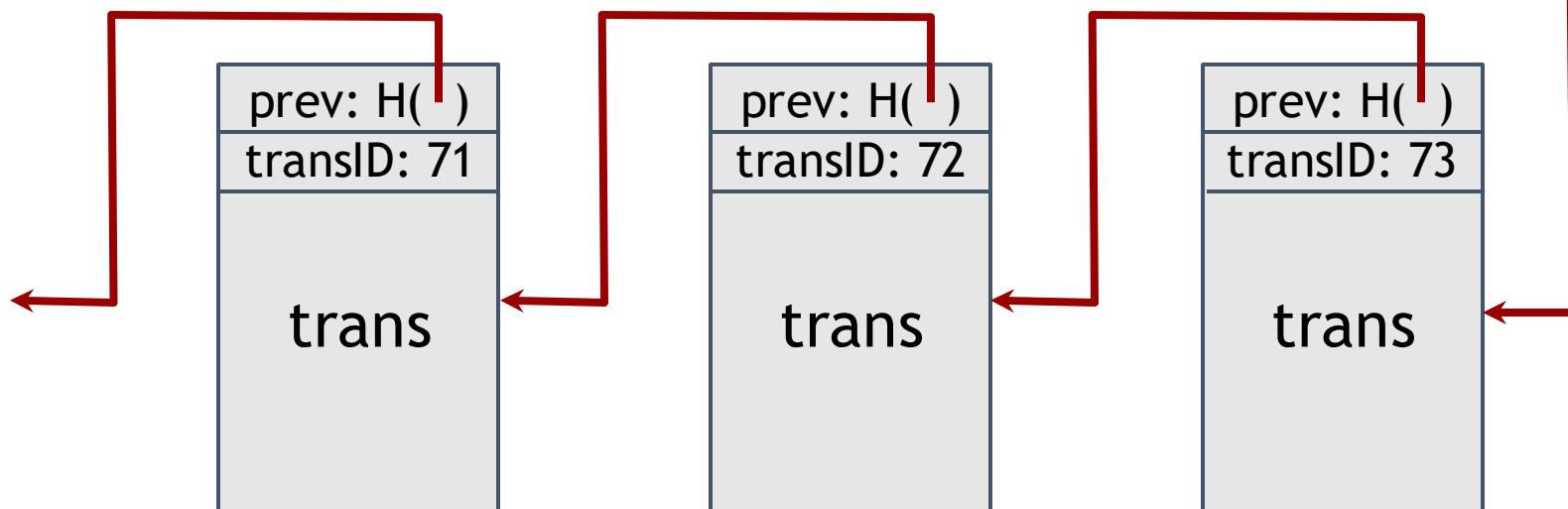


ScroogeCoin

Scrooge publishes a history of all transactions  
(a block chain, signed by Scrooge)



$H( )$



optimization: put multiple transactions in the same block

## CreateCoins transaction creates new coins

| transID: 73 type:CreateCoins |              |                  |
|------------------------------|--------------|------------------|
| coins created                |              |                  |
| <i>num</i>                   | <i>value</i> | <i>recipient</i> |
| 0                            | 3.2          | 0x...            |
| 1                            | 1.4          | 0x...            |
| 2                            | 7.1          | 0x...            |

Valid, because I said so.



PayCoins transaction consumes (and destroys) some coins,  
and creates new coins of the same total value

| transID: 73                              | type:PayCoins |           |  |  |
|------------------------------------------|---------------|-----------|--|--|
| consumed coinIDs:<br>68(1), 42(0), 72(3) |               |           |  |  |
| coins created                            |               |           |  |  |
| num                                      | value         | recipient |  |  |
| 0                                        | 3.2           | 0x...     |  |  |
| 1                                        | 1.4           | 0x...     |  |  |
| 2                                        | 7.1           | 0x...     |  |  |
| signatures                               |               |           |  |  |

Valid if:  
-- consumed coins valid,  
-- not already consumed,  
-- total value out = total value in, and  
-- signed by owners of all consumed coins

What are the problems with ScroogeCoin?

Can we use ScroogeCoin in real life?

# Can we use ScroogeCoin in real life?

“How to Time-Stamp a Digital Document”, Haber and Stornetta, 1991

Surety: Linked-timestamping service, 1995

Publishes hash of the tail on New York Times, Lost and Found section





Crucial question:

Can we descroogify the currency,  
and operate without any central,  
trusted party?

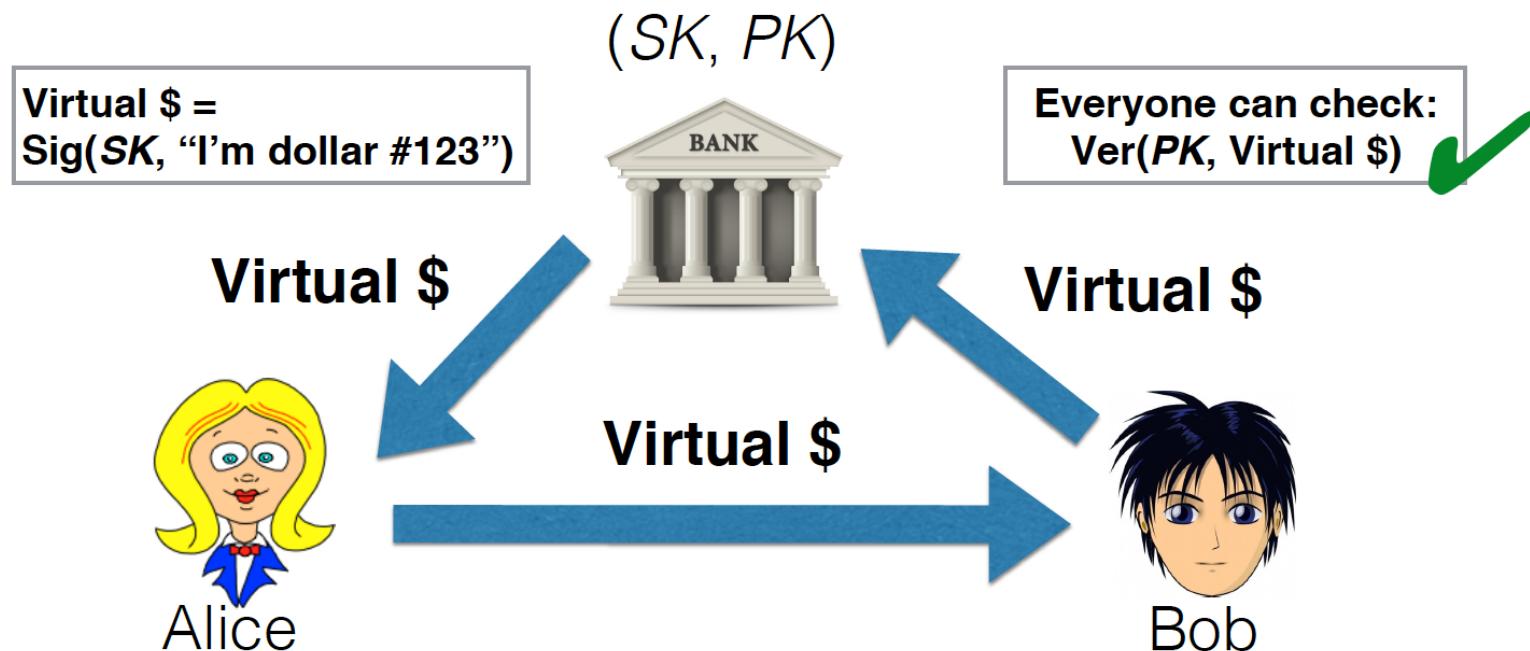
# Bitcoin: A Peer to Peer Electronic Cash System



# Historical backdrop

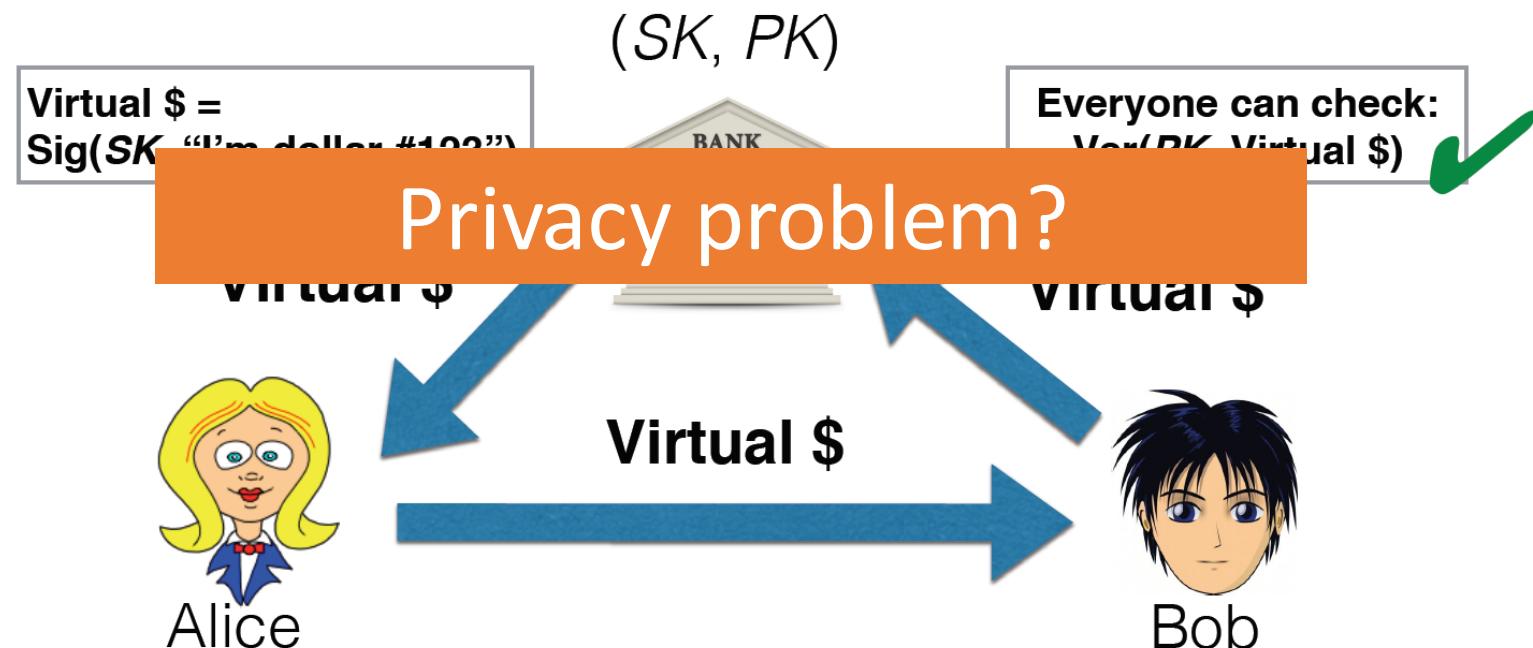
One of the earliest proposed uses of digital signatures (RSA) was to create virtual currency (in Ireland)

- Idea: A bank creates coins consisting of digital signatures
- Simplified version...



# E-cash

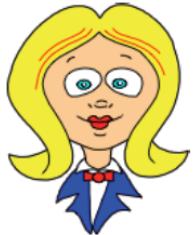
- Bank can also record spent serial numbers
- Bob can verify validity of coin online



# Blind digital signatures (Chaum, 1982)

- Ideas:
  - Alice chooses a serial number  $z$  for virtual \$
  - Bank digitally signs  $z$  without seeing it
- RSA setup:
  - Public key:  $(N, e)$ ; private key  $(N, d)$
  - Full-domain hash:  $H: \{0,1\}^* \rightarrow \mathbb{Z}_N$

# RSA blind signature



serial num.  $z \leftarrow \$$

$$c = H(z)$$

$$r \leftarrow \$ Z_N$$



$$t = r^e c$$

$$\begin{aligned}s' &= t^d \\ &= r c^d\end{aligned}$$

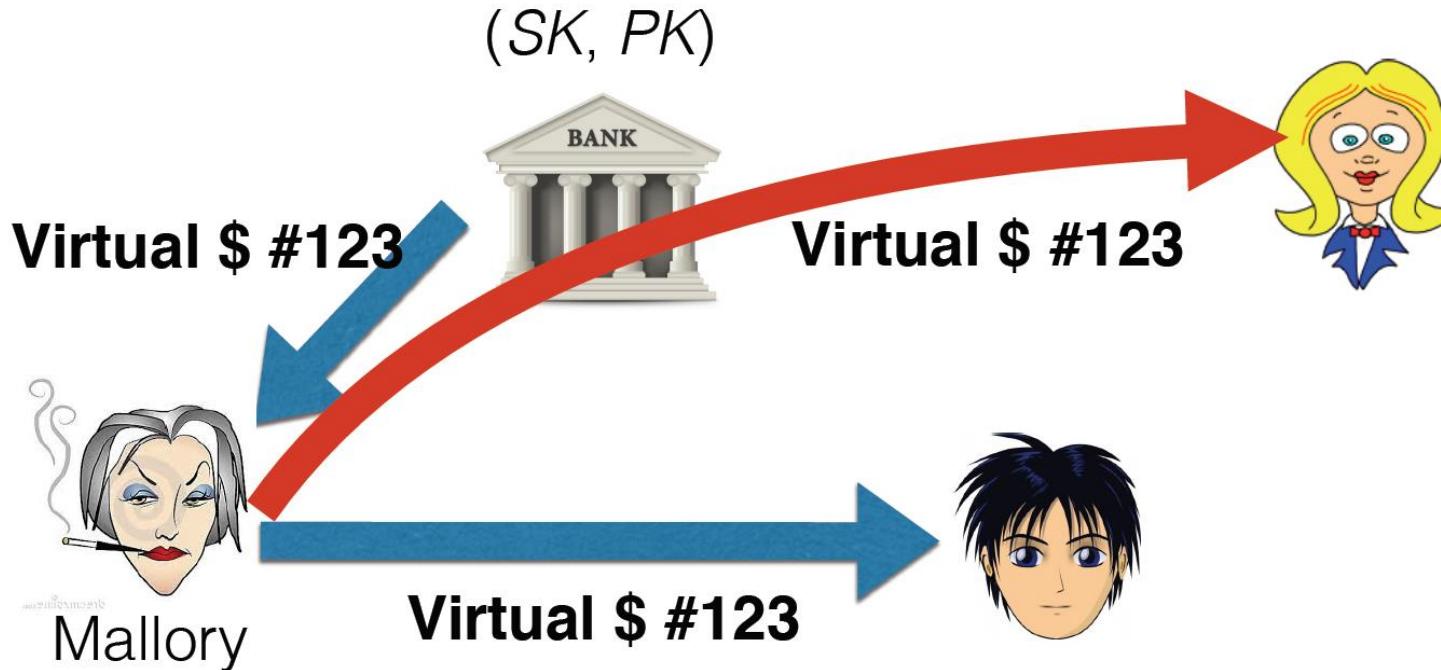
$$s'$$

$$\begin{aligned}s &= s' / r \\ &= c^d\end{aligned}$$

RSA public key  $(N, e)$ ; private key:  $(N, d)$   
Operations mod  $N$

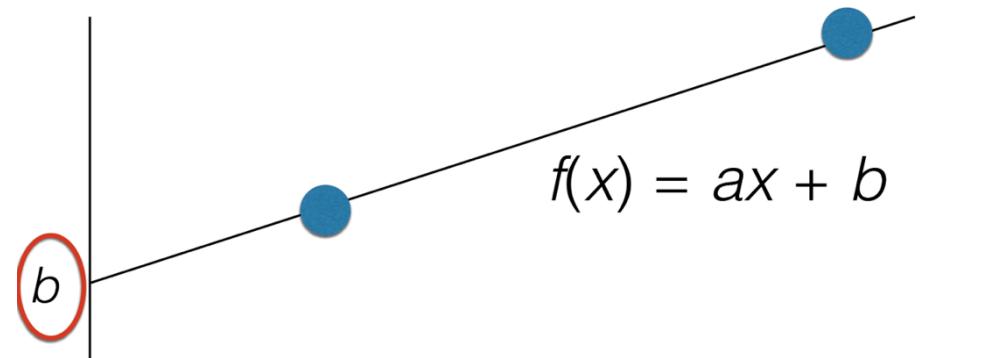
# What if we want to go offline?

- Suppose Mallory double-spends in **blinded** scheme?



# Conditional anonymity

- Intuition:
  - Identity encoded as value  $b$
  - Coin randomness encoded as value  $a$
  - Receiver challenges coin spender to reveal point  $f(x)$  when spending
  - Double-spending: two points uniquely specify a line



Despite promising, we still need  
a *trusted* third party.



The Times 03/Jan/2009 Chancellor on  
brink of second bailout for banks.



## Bitcoin: A Peer-to-Peer Electronic Cash System

Satoshi Nakamoto  
satoshin@gmx.com  
www.bitcoin.org

**Abstract.** A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending. We propose a solution to the double-spending problem using a peer-to-peer network. The network timestamps transactions by hashing them into an ongoing chain of

[bitcoin-0.1.0.rar](#)  
[bitcoin-0.1.0.tgz](#)

Paper published in 2008  
Source code in 2009

# Wait...But who is Nakamoto?

Bitcoin's face



And another ...



# Bitcoin design -- from basic principles



# Key property #1

## Bitcoin is pseudonymous

1. Each entity  $X$  has an (ECDSA) key pair  $(PK_X, SK_X)$
2. No association between  $X$  and real-world identity

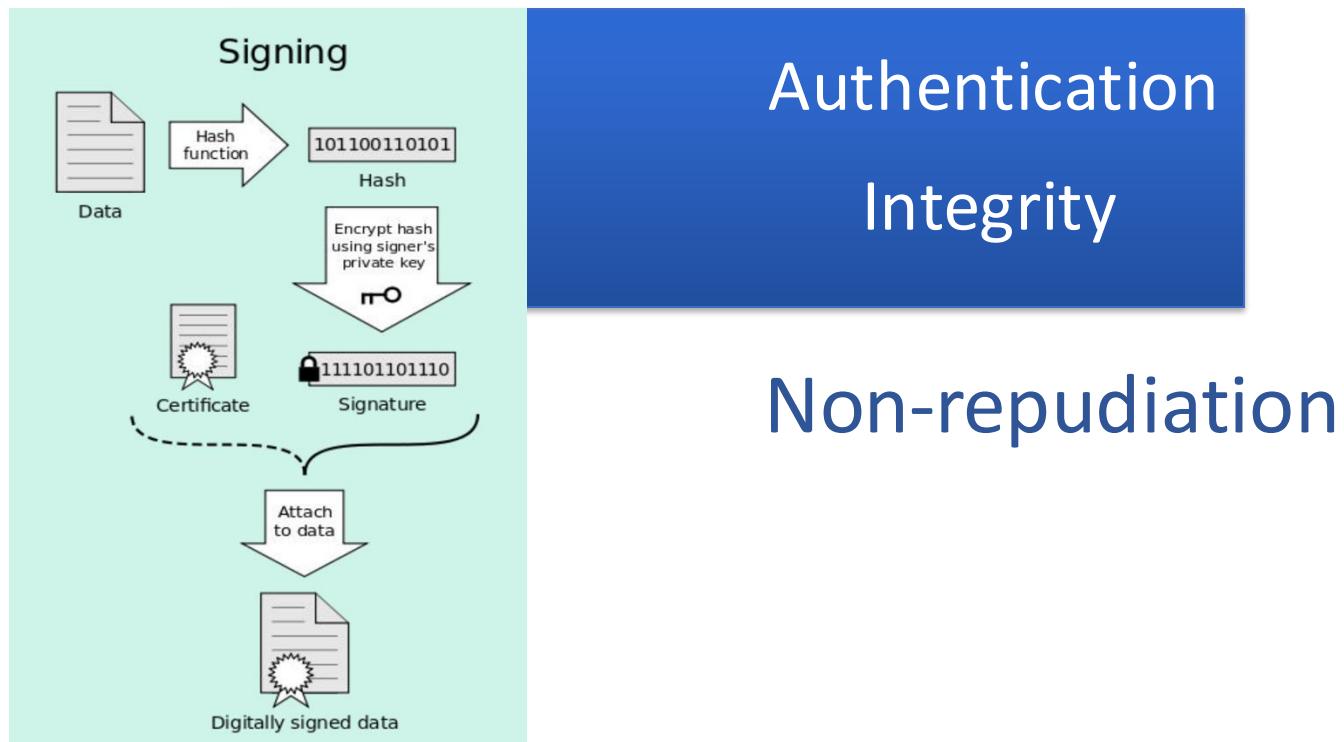


**PK:** hUK67H9fyg

**SK:** z4Pxc2kKn3

# Recall: digital signature

- First, create a message digest using a cryptographic hash
- Then, sign the message digest with your private key



# Digital signatures are used in bitcoin

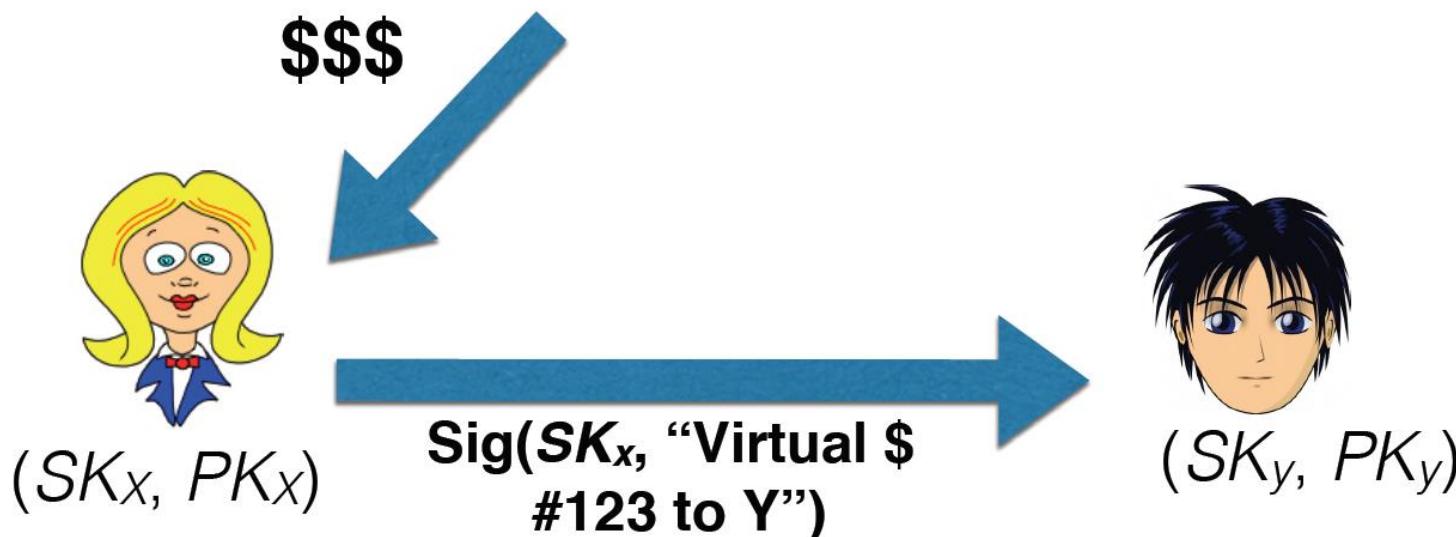
Bitcoin uses ECDSA

- “Elliptic-Curve Digital Signature Algorithm”
- Concretely, uses secp256k1 (slightly nonstandard) curve
  - Private key  $SK$  is 256 bits; (uncompressed) public key  $PK$  is 512 bits

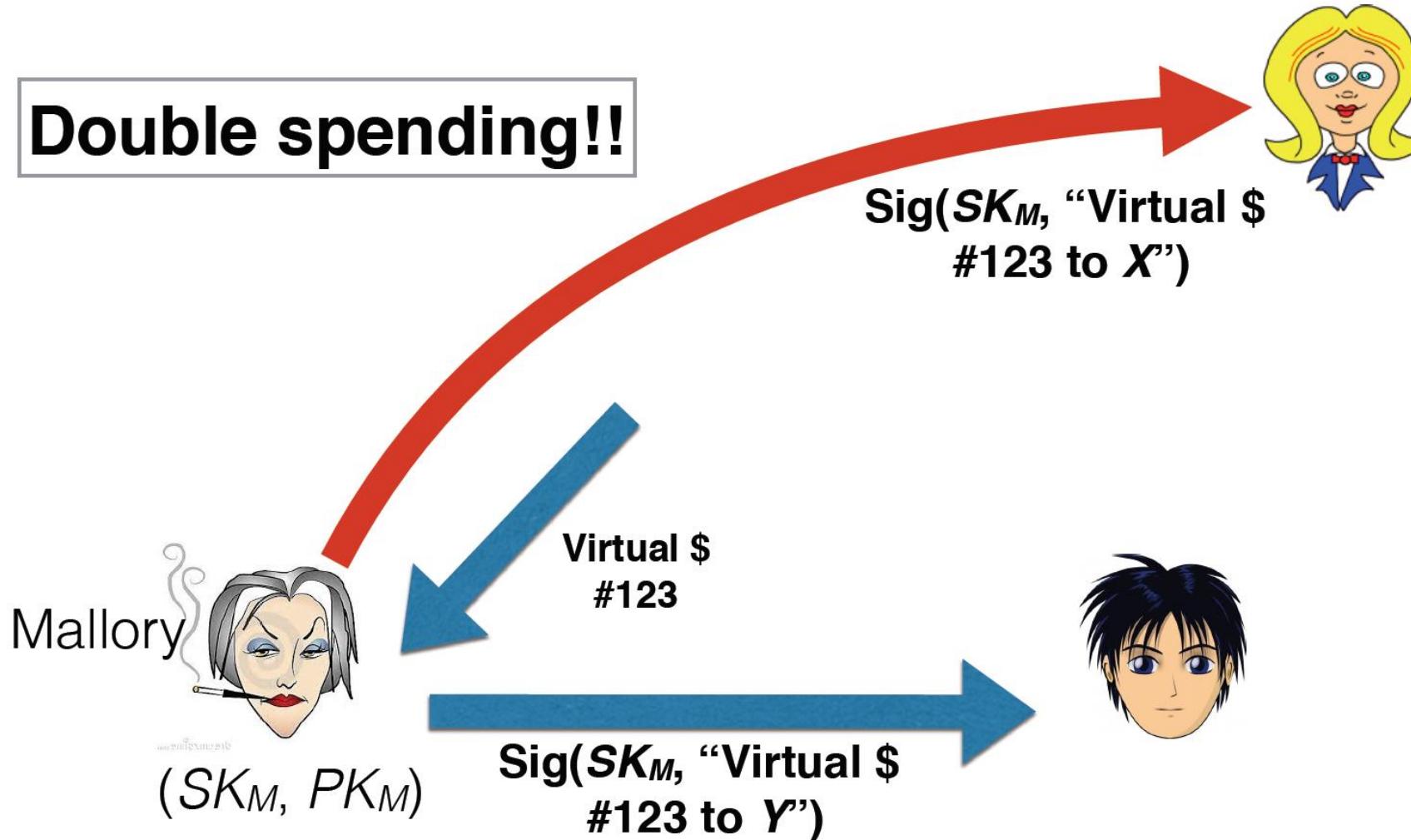


# Could build naïve system...

- Idea: Coins *and* transactions, i.e., flow of money, can be authenticated—neither is forgeable
- Thanks to public-key crypto, everyone can verify all coins and transactions (if public keys are distributed throughout system)



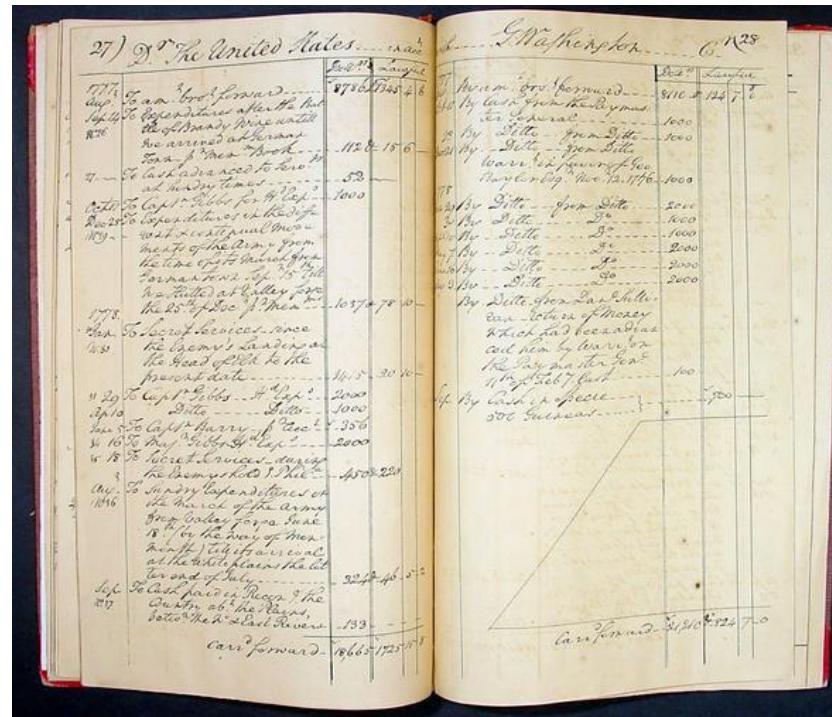
# But there is a problem



# The double spending problem

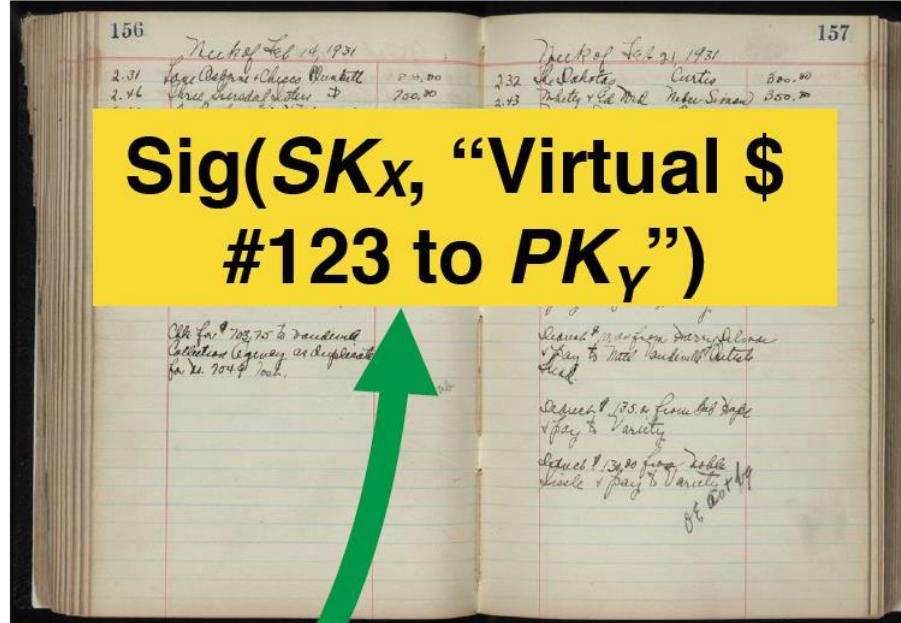
- Suppose Mallory gives the same dollar (dollar #123) to *both* Alice and Bob.
- The good news:
  - She can be caught after the fact.
  - Alice and Bob have (cryptographic) *proof* that Mallory cheated: Mallory's signatures!
- The bad news:
  - Either Alice or Bob is out a dollar.
  - Who's going to prosecute Mallory?
  - E.g., suppose Mallory is halfway around the world?

# What a bank will do to prevent double spending?



Maintain a ledger to record every transaction!

# Bitcoin entities emulate a *public* trusted bulletin-board (ledger)



$(SK_x, PK_x)$



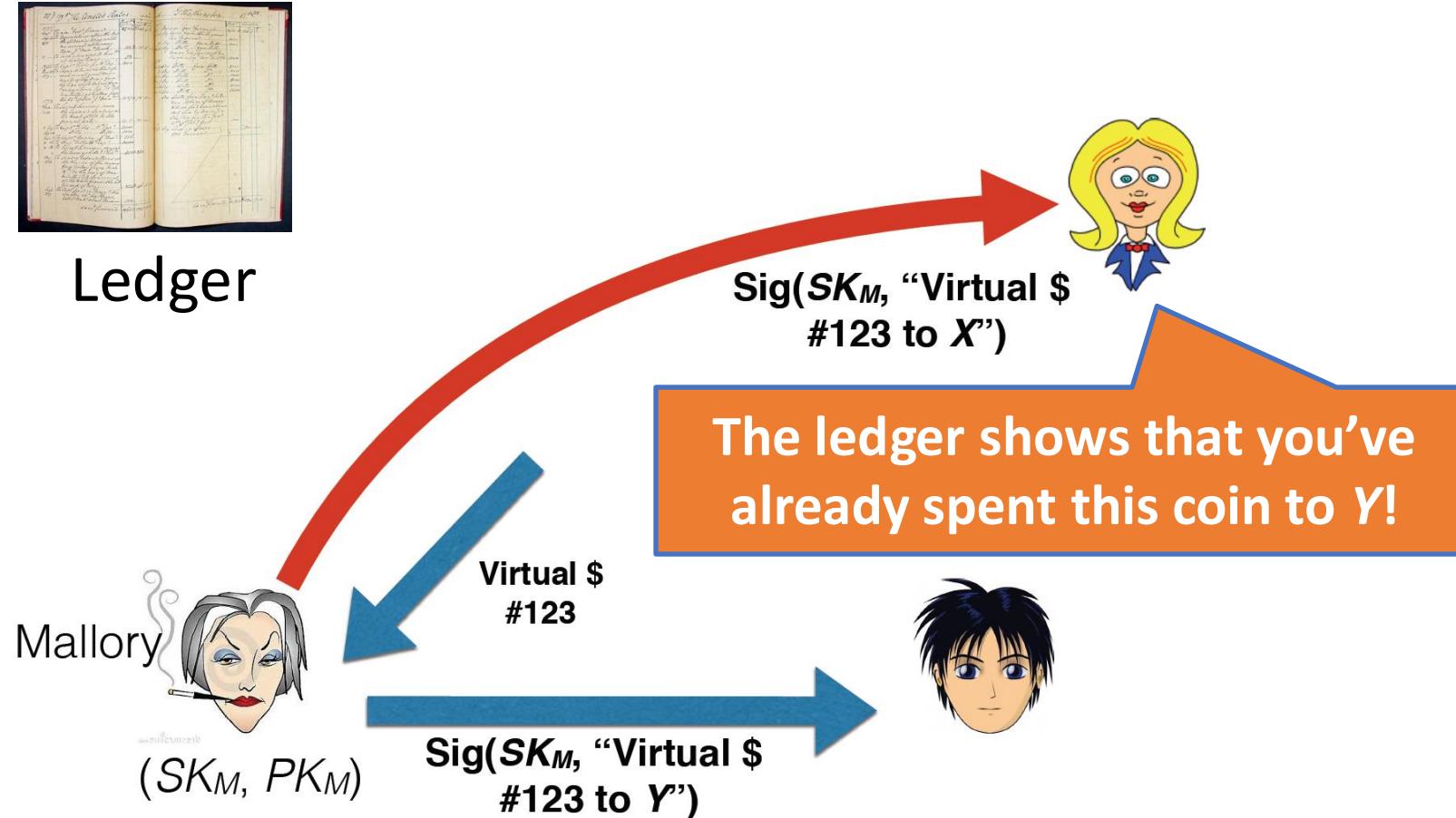
**$Sig(SK_x, “Virtual \$$   
 $\#123 \text{ to } PK_y”)$**



$(SK_y, PK_y)$

Bob checks  
Sig and  
ledger ✓

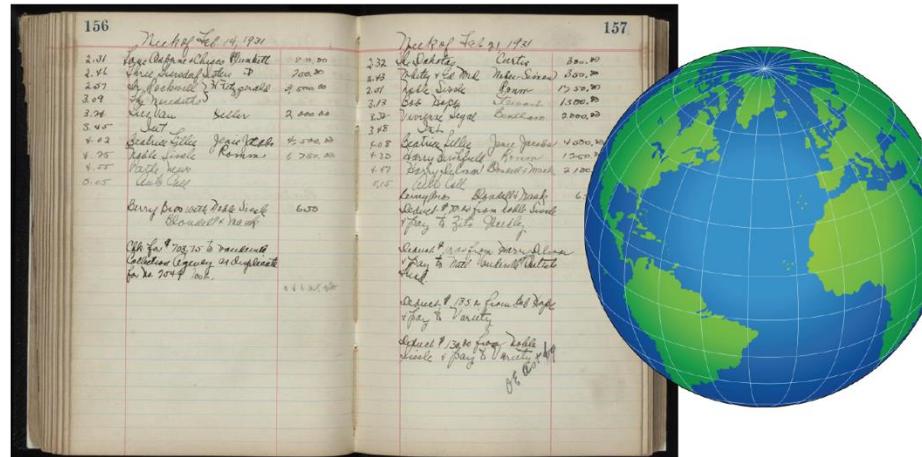
# The *public* ledger prevents double spending



# Key property #2

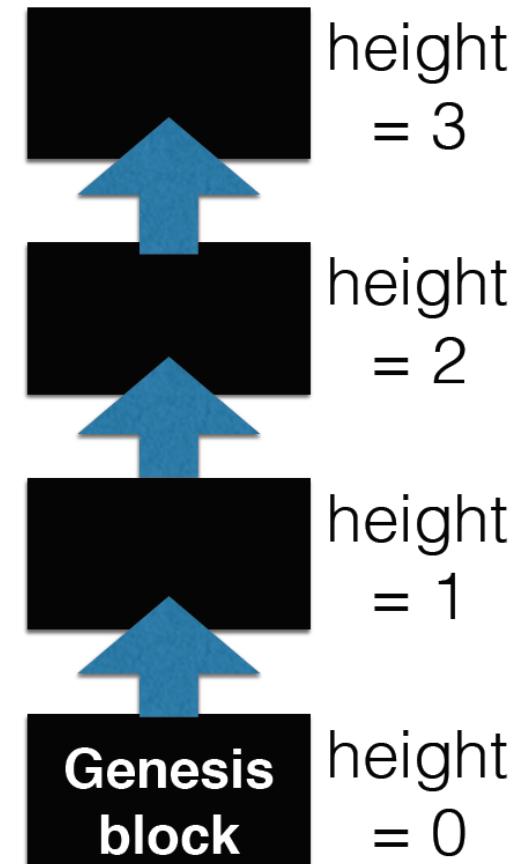
## Bitcoin is decentralized

1. Has a ledger, but with **no Bank!**
  2. The ledger is *agreed upon* and *distributed* among many entities
  3. The ledger is called **blockchain** in Bitcoin

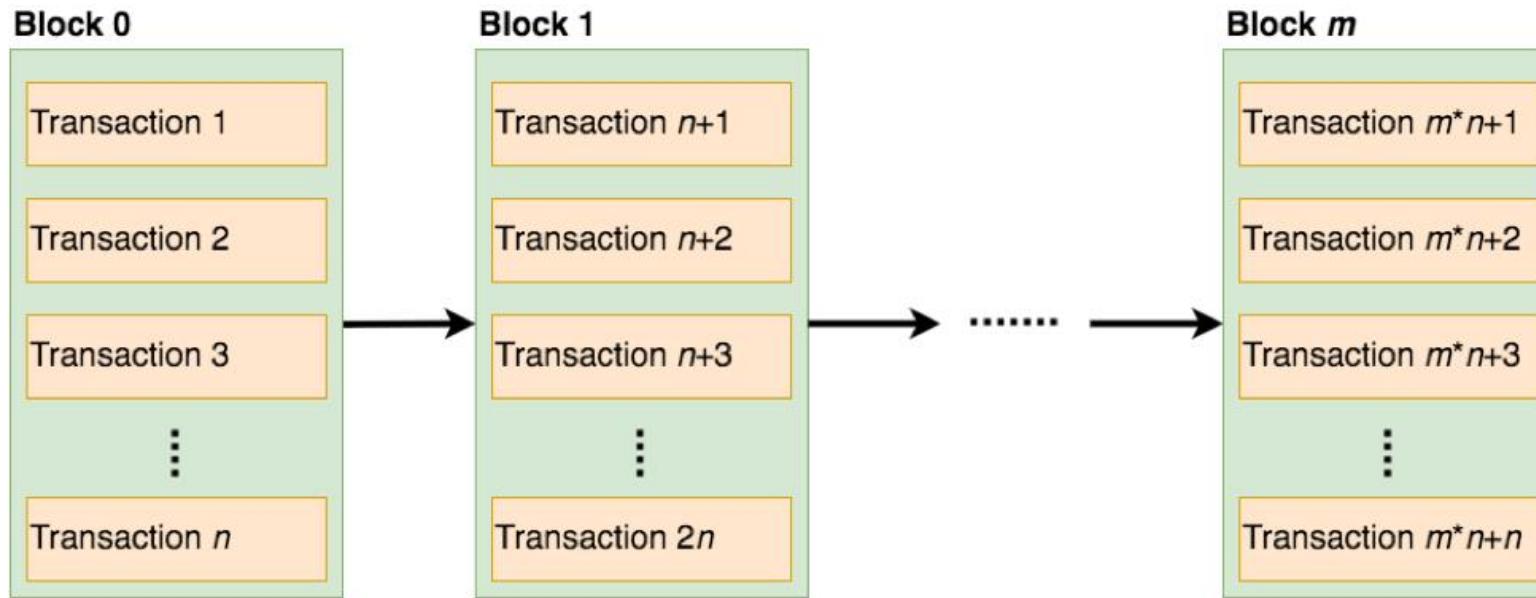


# Blockchain

- Record of *every* transaction in Bitcoin system
- Maintained as append-only data structure
- New block added every 10 minutes (on average)
- Each block contains a bundle of latest transactions.
  - E.g.,  $\text{SIG}_{\text{SKA}}$  [“Alice sends 0.4 BTC to Bob”]
  - (Actually, there’s a scripting language, but we’ll gloss over it...)



# Block of transactions



One block every 10 minutes

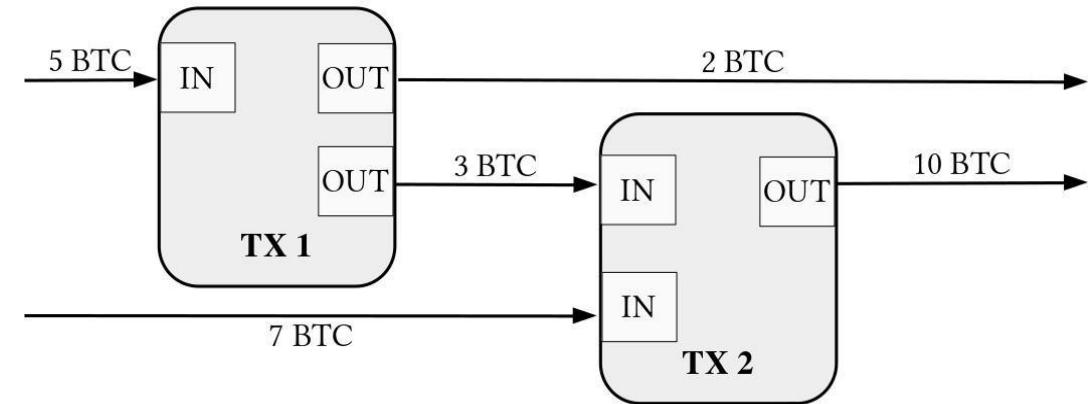
Around 2000 transactions per block

Q: what's the average transaction rate?  
(transactions/second)

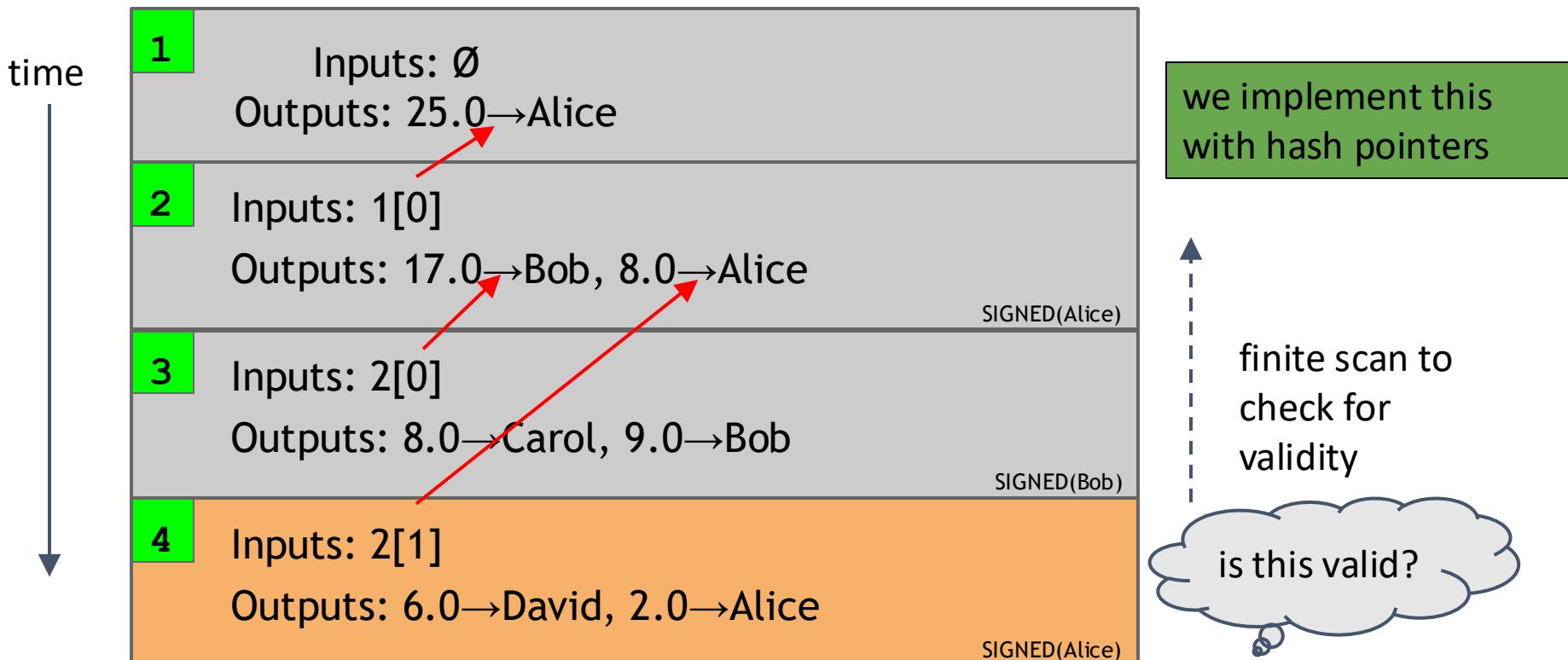
[https://ycharts.com/indicators/bitcoin\\_average\\_transactions\\_per\\_block](https://ycharts.com/indicators/bitcoin_average_transactions_per_block) Assessed on Jan. 5 2023.

# UTXO model

- Unspent transactions output (UTXO)
  - No explicit “account balances”
  - Structured in terms of transactions
- Your account balance is the combined value of all UTXOs you control
- Each transaction consumes at least one UTXO and creates at least one UTXO
- Each UTXO can only be consumed at most once and only in its entirety
- The sum of a transaction's inputs must be greater or equal to the sum of its outputs
  - The difference is the transaction fee

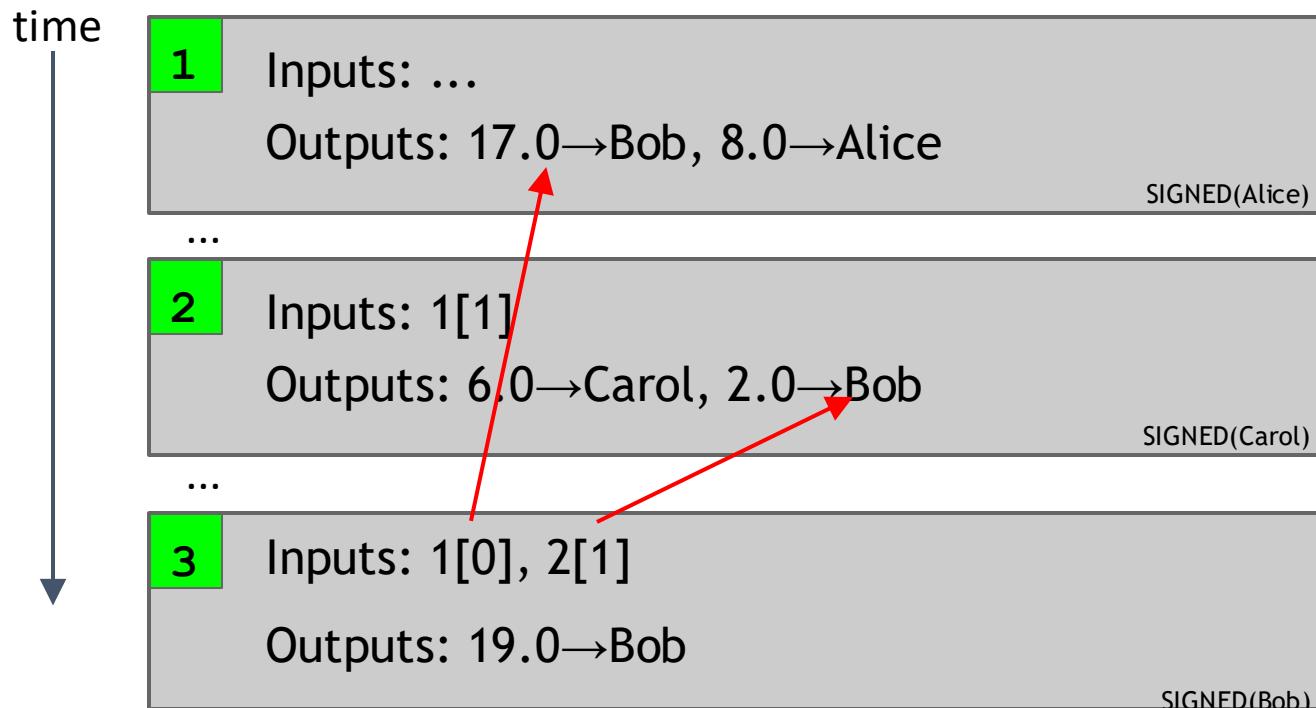


# Demo



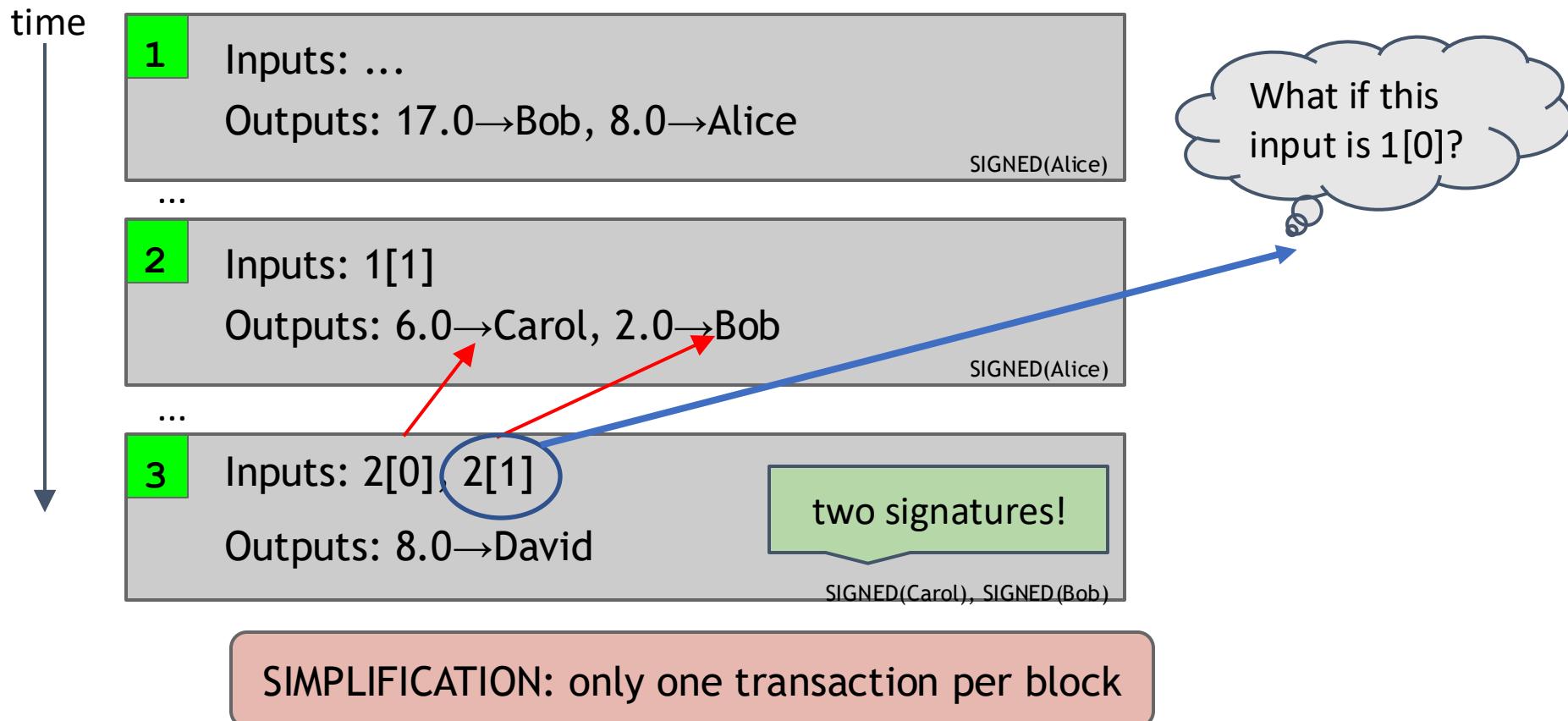
SIMPLIFICATION: only one transaction per block

# Merging value



SIMPLIFICATION: only one transaction per block

# Joint payments



# Key challenge in bitcoin

- **Distributed consensus:**

- All “correct” nodes decide on the **same** value

- This value must have been proposed by some **correct** node

- The protocol terminates

(more about this in the next class...)

# Bitcoin is a peer-to-peer system

When Alice wants to pay Bob:  
she broadcasts the transaction to all Bitcoin nodes



signed by Alice  
Pay to  $pk_{Bob}$  :  $H( )$

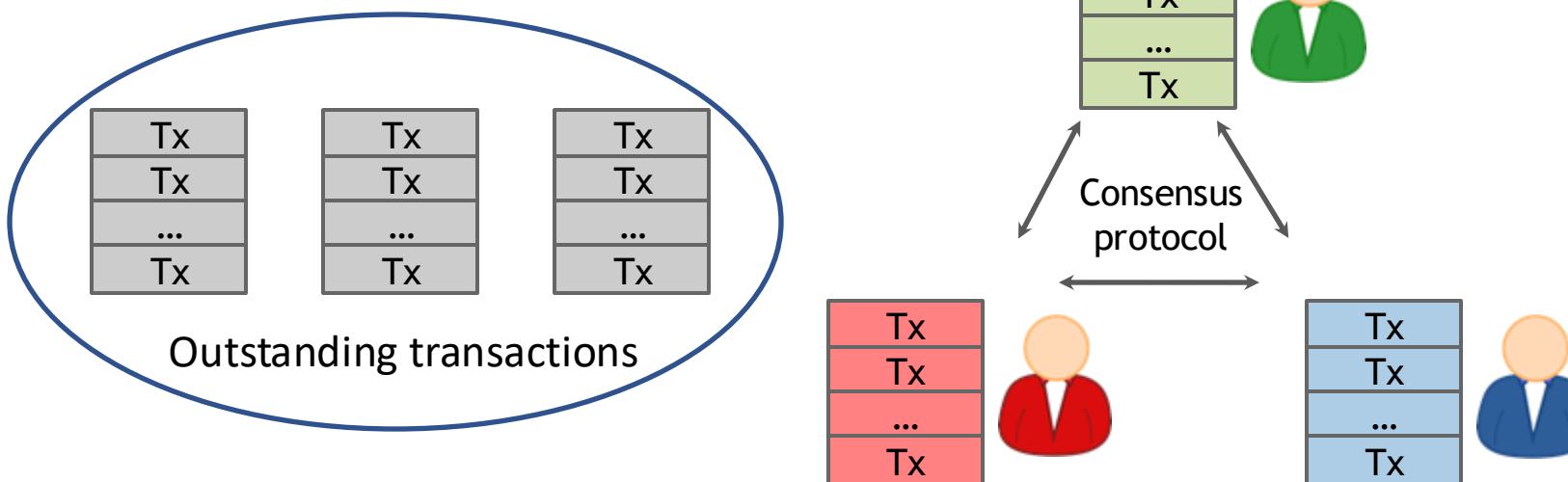


Note: Bob's computer is not in the picture

# How consensus could work in bitcoin

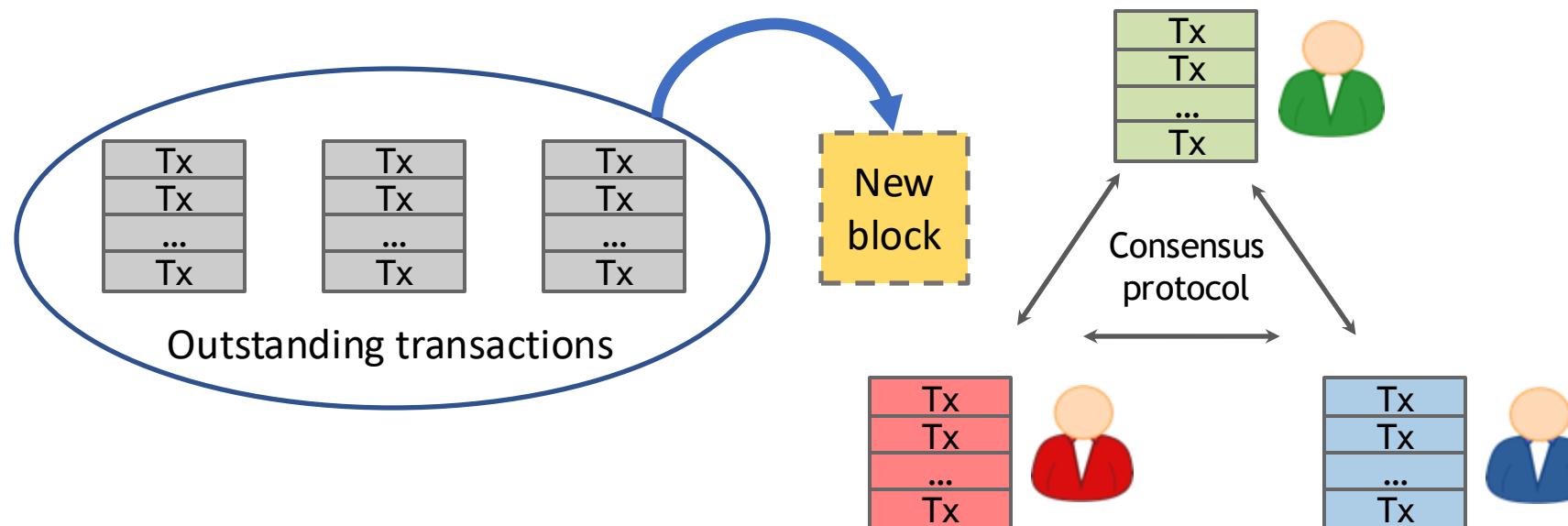
At any given time:

- All nodes have a sequence of blocks of transactions they've **reached consensus on**
- Each node has a set of outstanding transactions it's heard about



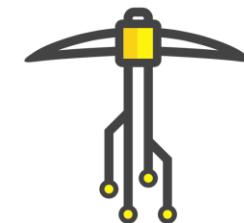
# How consensus could work in bitcoin

- Now, how does system decide which block to be extended?
- Ideal for P2P system: All clients in the world vote on the correct new block



# How consensus could work in bitcoin

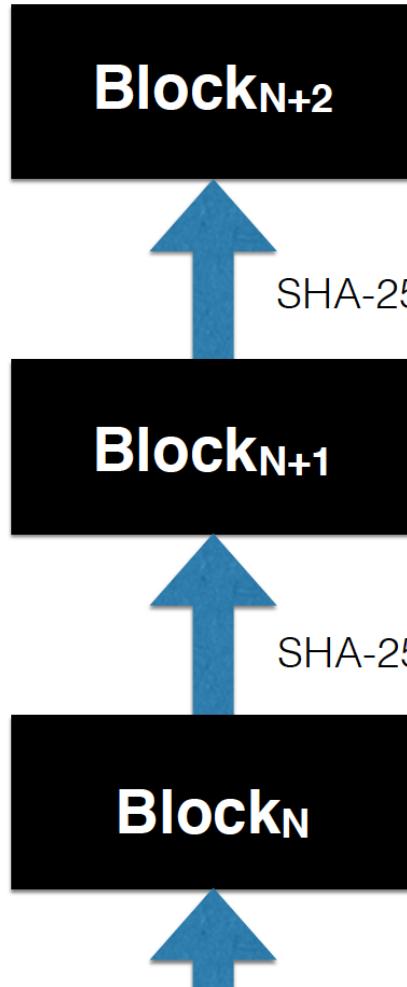
- But it's hard to ensure one vote per machine in a P2P system
  - E.g., there's the problem of "Sybil" attacks
    - one user creates multiple identities
- So "voting" (cleverly) in Bitcoin takes the form of hash power.
  - I.e., one vote per CPU (roughly speaking)



# “Mining” in bitcoin

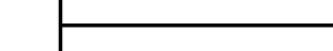
- All miners execute communal, computationally-intensive process called mining.
  - Together, mining community defines blockchain
- Intuition:
  - All miners collectively search for hard-to-compute “signature” on new block (solve a puzzle)
  - Attacker with little computing power unlikely to mine new valid block faster than honest ones
    - Security: assume less than 50% malicious

# Block mining



?

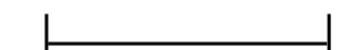
**Mining difficulty**



$\text{SHA-256}^2(\text{Block}_{N+1}, X_{N+1}, \text{ticket}_{N+1}) = 0x0000000000001d7a1\dots$

?

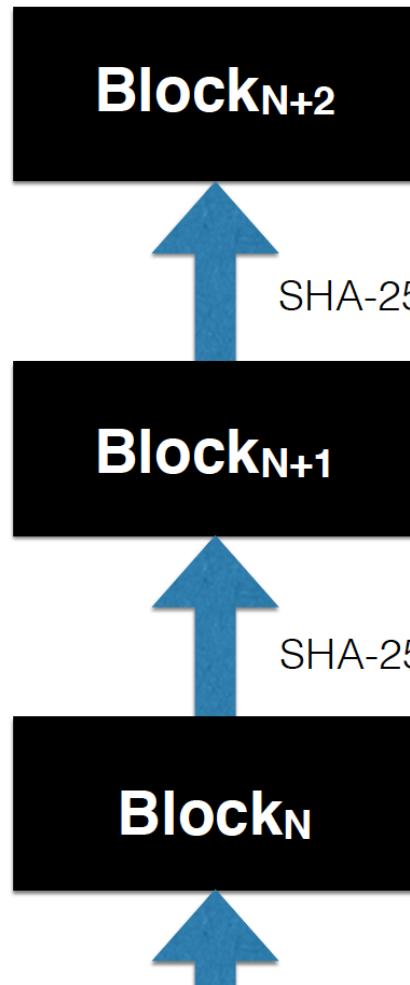
**Mining difficulty**



$\text{SHA-256}^2(\text{Block}_N, X_N, \text{ticket}_N) = 0x000000000000c67aa\dots$

Precise mining problem: Find a **ticket** that yields hash image with value less than target Z

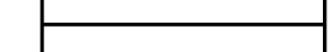
# Block mining



$\text{SHA-256}^2(\text{Block}_{N+1}, X_{N+1}, \text{ticket}_{N+1}) \stackrel{?}{\leq} Z$

**Mining difficulty**

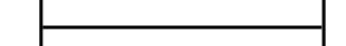
?



$\text{SHA-256}^2(\text{Block}_{N+1}, X_{N+1}, \text{ticket}_{N+1}) = 0x0000000000001d7a1...$

**Mining difficulty**

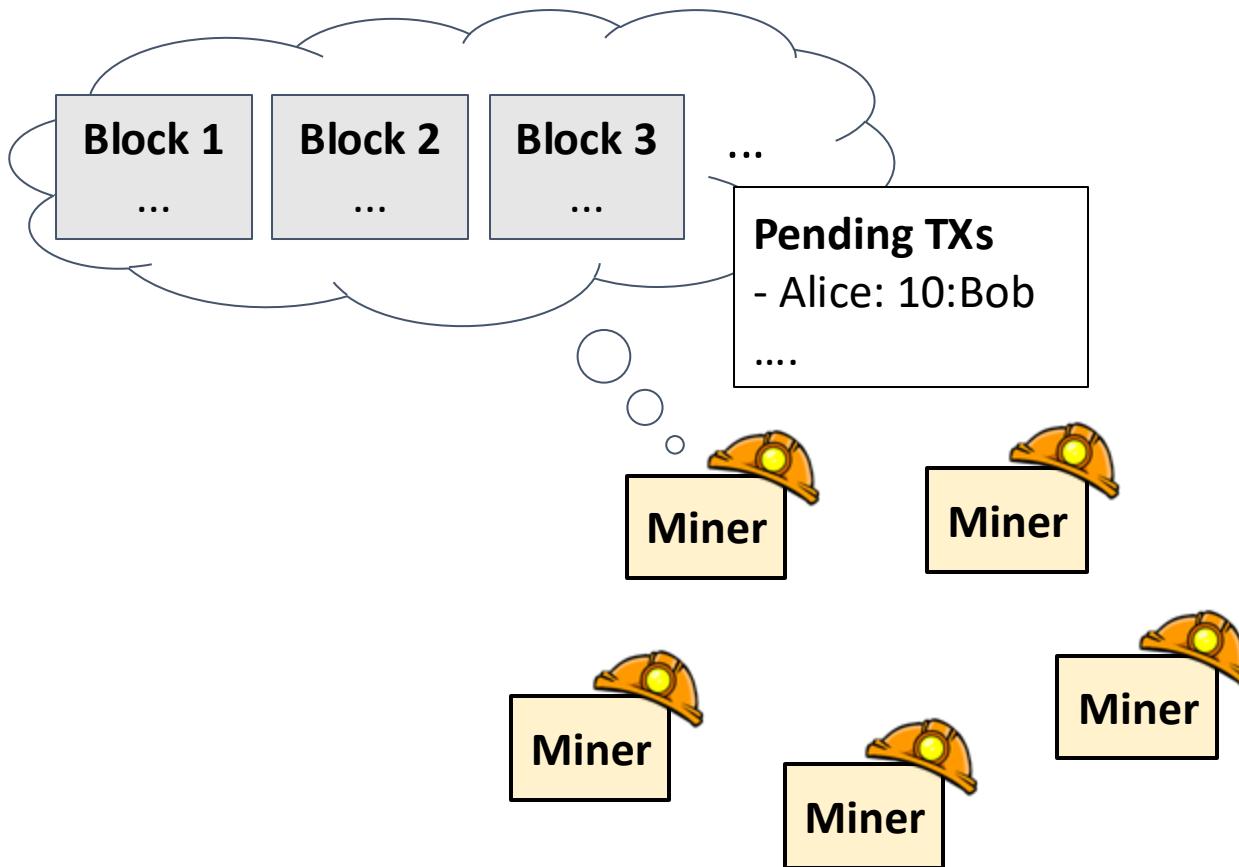
?



$\text{SHA-256}^2(\text{Block}_N, X_N, \text{ticket}_N) = 0x000000000000c67aa...$

$X_N = (\text{software version, hash (Merkle-tree root) of new transactions, and current time})$

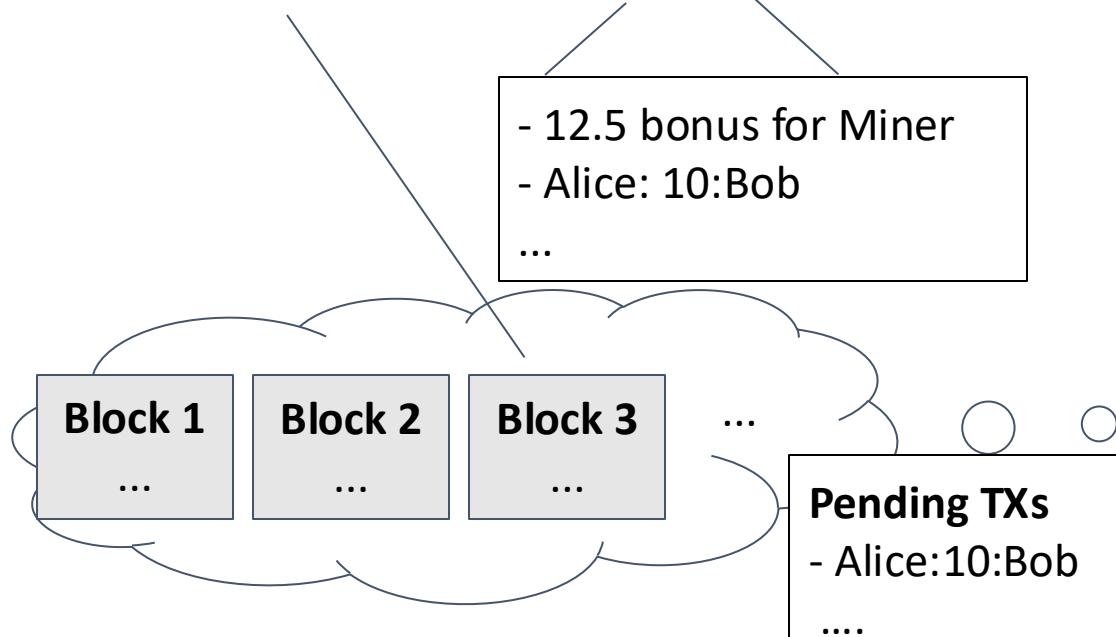
# Demo



# Miners commit new transactions by solving puzzles

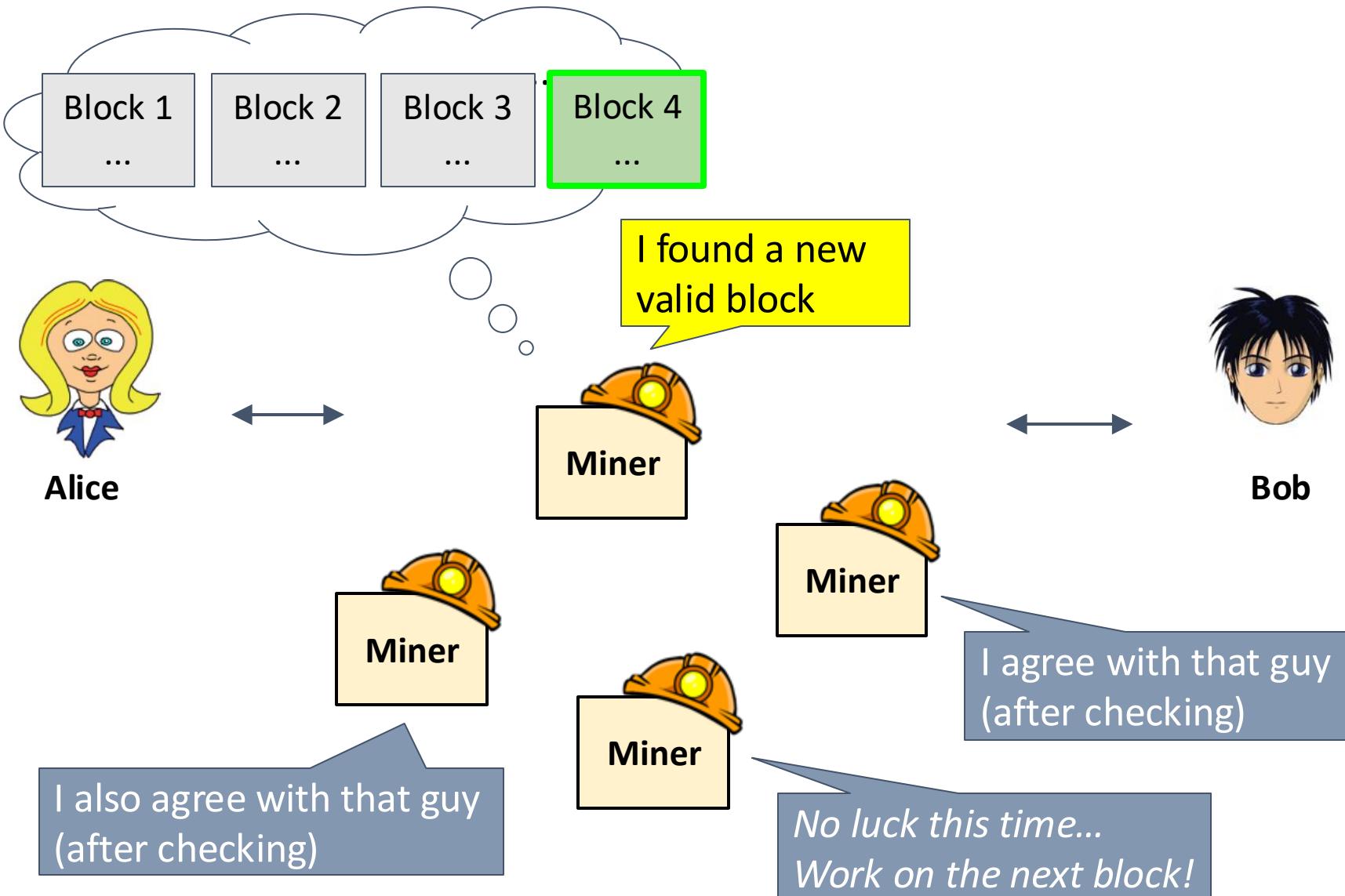
= 0x000\*\*\*...

Hash ( Block 3 | newTxns | 0xb9824 ) = 0x000c3f...



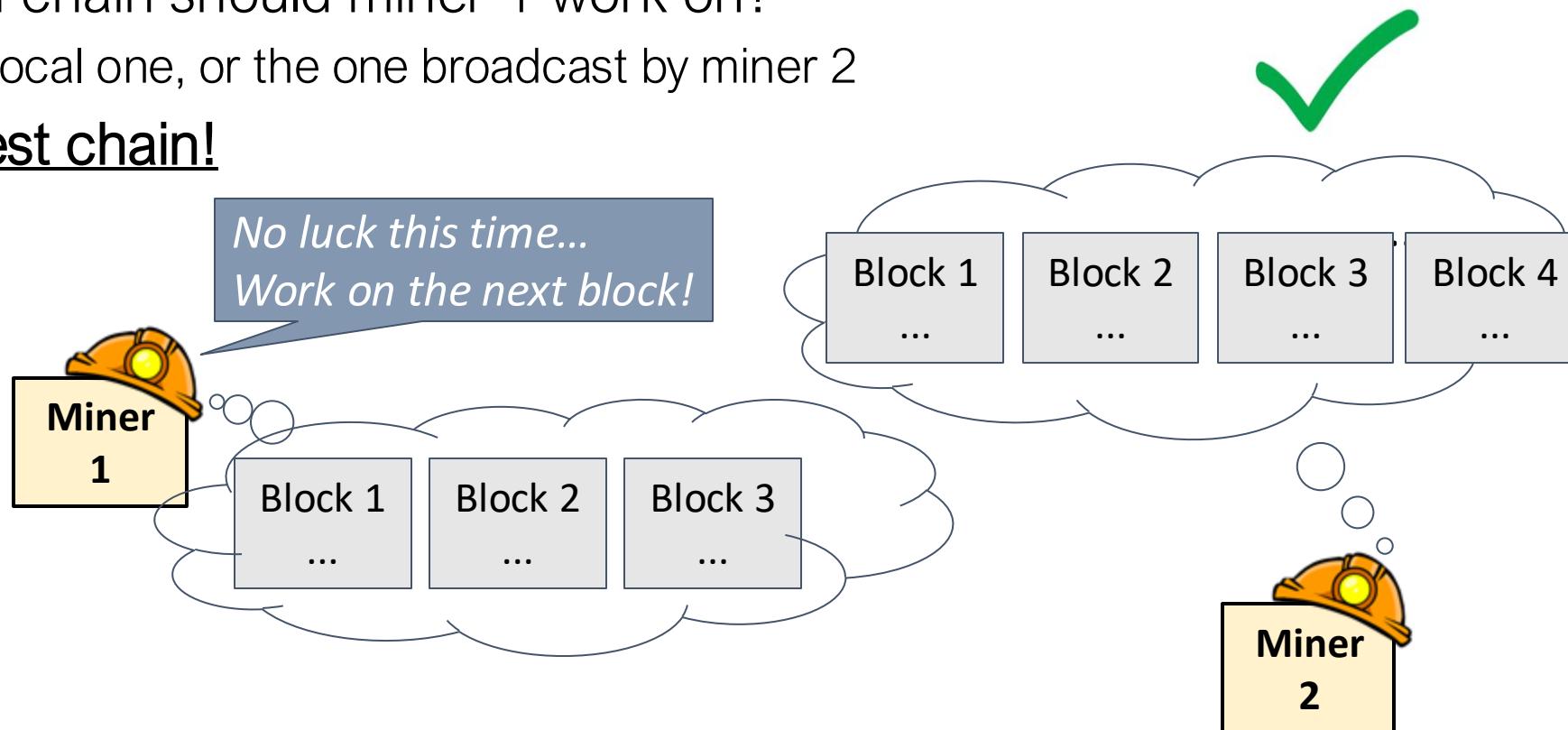
Each attempt has  $16^{-3}$  chance of success





# Longest chain rule

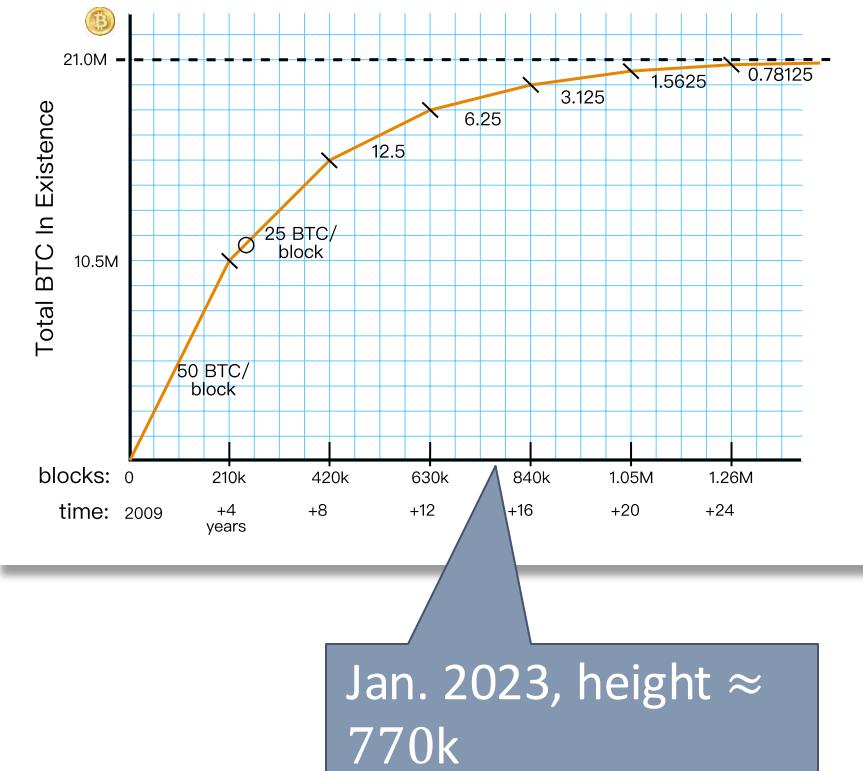
- One subtle question
  - Which chain should miner 1 work on?
    - His local one, or the one broadcast by miner 2
  - Longest chain!



# What's the incentive for miners to mine?



- Key idea: Bitcoin is a lottery
- Every miner tries tickets until a “winning” one is found
- The reward for the winner: Bitcoin!
  - Special transaction (*coinbase*) in block assigns BTC to winner
  - Originally, 50 BTC/block; today, 6.25 BTC/block
  - Winner also gets *transaction fees*
- 21 million BTC will be produced over the lifetime of the system



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TRANSACTION FEES ARE MEANT TO REPLACE BLOCK REWARDS



transaction fee = transaction value – spent value  
(transaction fee  $\geq 0$ )

Miner: I am more willing to include your transaction as I can earn more BTC from it!

# What's the incentive for miners to mine?



- In principle, Bitcoin is democratic
- *Anyone* can mine
- *Reward* is proportional to computational investment
- But...

# How long will it take to find a block?



- In the early days, with an PC (CPU mining).

```
while (1) {
 HDR[kNoncePos]++;
 IF (SHA256(SHA256(HDR)) < (65535 << 208) / DIFFICULTY)
 return;
}
```

**A typical PC can crank out about *one* bitcoin every  $4\frac{1}{2}$  years.**

-- WSJ Oct. 2017

<https://www.wsj.com/articles/hackers-latest-move-using-your-computer-to-mine-bitcoin-1509102002>. By Robert McMillan.

# GPU mining

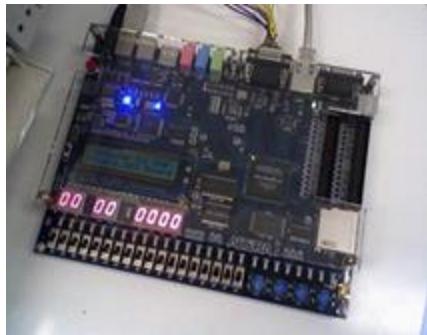


- GPUs designed for high-performance graphics
  - High parallelism
  - High throughput
- First used for Bitcoin ca. October 2010
- Implemented in OpenCL



Source:  
LeonardH,  
cryptocurren  
ciestalk.com

# FPGA mining



- Field Programmable Gate Area
- First used for Bitcoin ca. June 2011
- Implemented in Verilog



Bob Buskirk, [thinkcomputers.org](http://thinkcomputers.org)

# Bitcoin ASICs

## TerraMiner™ IV – 2TH/s Networked ASIC Miner

\$5,999

Shipping June 2014



**Pre-Order Terms:** This is a pre-order. 28nm ASIC bitcoin mining hardware products are shipped according to placement in the order queue, and delivery may take 3 months or more after order. All sales are final.



## 300 GH Bitcoin Mining Card The Monarch BPU 300 C

\$1,497.00

Qty: 1 **ADD TO CART**

Special purpose!

**THE LEOPARD**

**DETAILS :**

- 2.5 TH/s
- Dimensions: 15" x 13.3" x 13.7" (38cm x 34cm x 35cm)
- 28nm ASIC technology
- Silent Cooling
- In-built WiFi Connection (without Antenna)
- Less than 750 watt (0.3 per GH)
- 1 Year Guarantee
- \$ 5.800

**COMES WITH :**

1. Power Supply
2. Free Remote Power Outlet & Smartphone App
3. Free User Guide
4. Free Personal Assistance for Setup

**SHIPPING :**

- Worldwide, Express
- Included in the price
- Available: **100 Units: Shipping April (Week 3)**

# Professional mining centers

## Needs:

- cheap power
- good network
- cool climate





# Evolution of mining



CPU



GPU



FPGA



ASIC



gold pan



sluice box



placer mining



pit mining

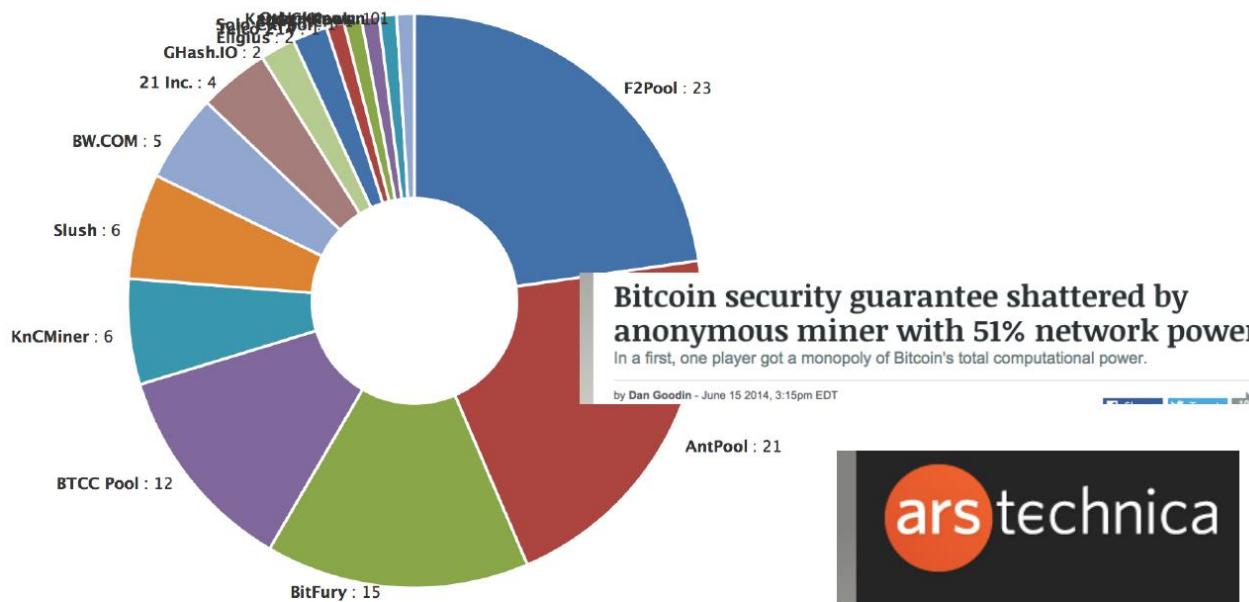
# Mining pools

## Hashrate Distribution

An estimation of hashrate distribution amongst the largest mining pools

The graph below shows the market share of the most popular bitcoin mining pools. It should only be used as a rough estimate and for various reasons will not be 100% accurate. **A large portion of Unknown blocks does not mean an attack on the network, it simply means we have been unable to determine the origin.**

24 hours - 48 hours - 4 Days

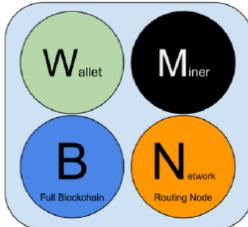


Researchers from Cornell University say that on multiple occasions, a single mining pool repeatedly contributed more than 51 percent of Bitcoin's total cryptographic hashing output for spans as long as 12 hours. The contributor was **GHash**, which bills itself as the "#1 Crypto & Bitcoin Mining Pool." During

# Mining blocks isn't enough

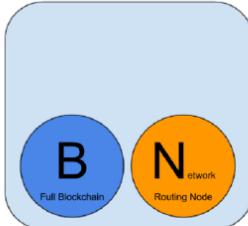
- What else is needed to make a working monetary system?

# Node types in bitcoin network



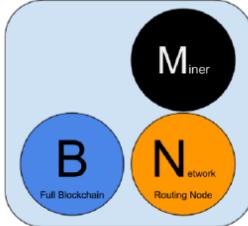
## Reference Client (Bitcoin Core)

Contains a Wallet, Miner, full Blockchain database, and Network routing node on the bitcoin P2P network.



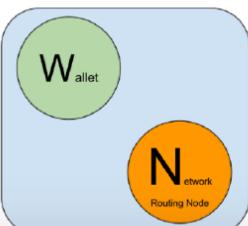
## Full Block Chain Node

Contains a full Blockchain database, and Network routing node on the bitcoin P2P network.



## Solo Miner

Contains a mining function with a full copy of the blockchain and a bitcoin P2P network routing node.



## Lightweight (SPV) wallet

Contains a Wallet and a Network node on the bitcoin P2P protocol, without a blockchain.

[Source: <http://chimera.labs.oreilly.com/books/1234000001802/ch06.html>]

# Routing functionality

- Transactions and blocks are broadcast to *entire network of nodes*
- Rebroadcast protocol
  - Each node transmits to 8 other (randomly selected) nodes
  - TCP on port 8333

# Storage

- Full nodes:
  - Store entire blockchain
  - Enforce consensus rules, ensuring blocks in blockchain adhere to
    - 6.25 BTC reward
    - Correct signatures on transactions
    - BTC not double-spent
    - Etc...

# Full node distribution

## GLOBAL BITCOIN NODES DISTRIBUTION

Reachable nodes as of Thu Jan 07 2021  
15:54:21 GMT+0800 (Hong Kong Standard Time).

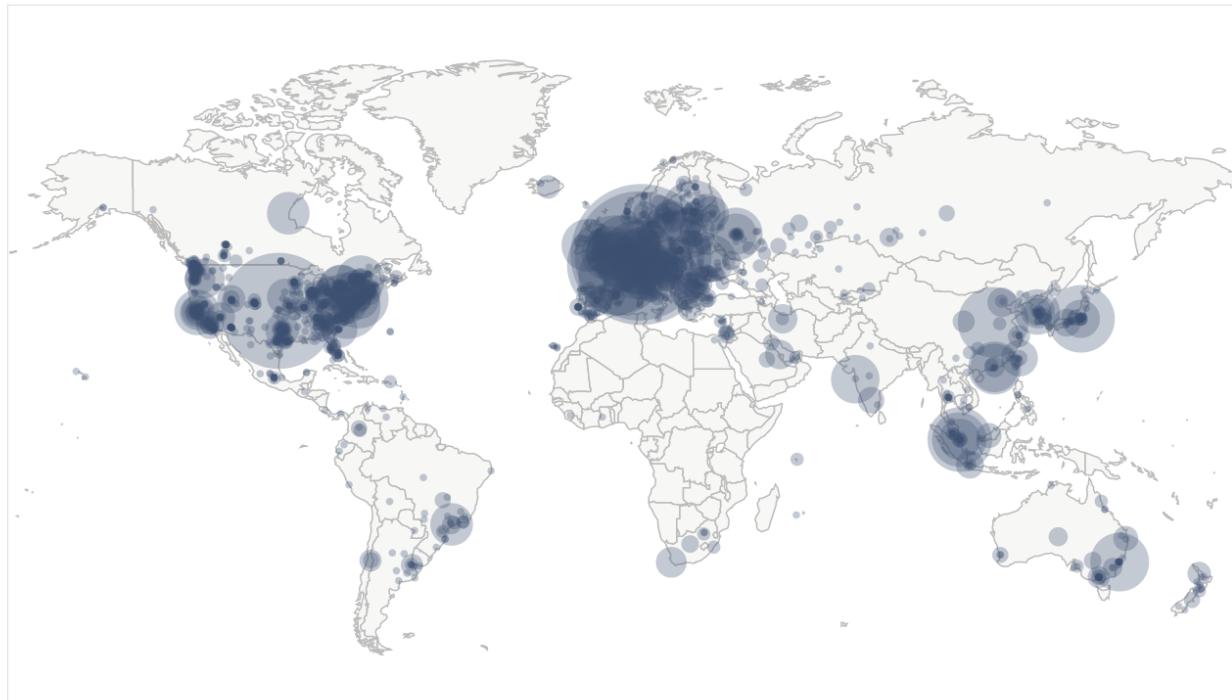
### 9812 NODES

[24-hour charts »](#)

Top 10 countries with their respective number of reachable nodes are as follow.

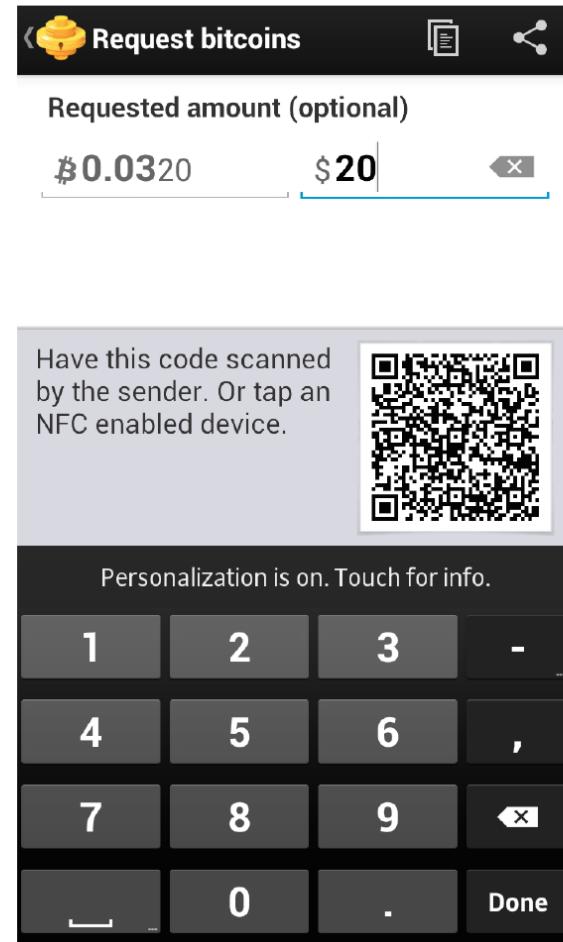
| RANK | COUNTRY            | NODES         |
|------|--------------------|---------------|
| 1    | United States      | 1956 (19.93%) |
| 2    | Germany            | 1794 (18.28%) |
| 3    | n/a                | 1232 (12.56%) |
| 4    | France             | 603 (6.15%)   |
| 5    | Netherlands        | 464 (4.73%)   |
| 6    | Canada             | 368 (3.75%)   |
| 7    | United Kingdom     | 342 (3.49%)   |
| 8    | Singapore          | 232 (2.36%)   |
| 9    | Russian Federation | 212 (2.16%)   |
| 10   | Japan              | 207 (2.11%)   |

[More \(98\) »](#)



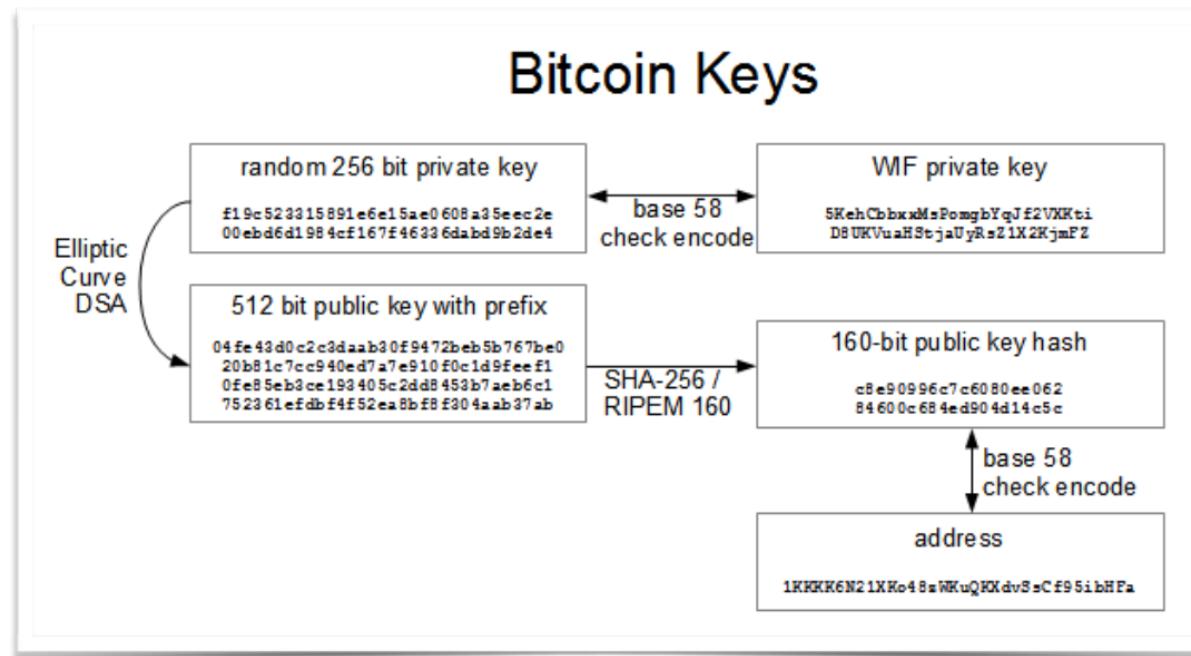
# Bitcoin wallets

- You don't need to mine or run full node to use Bitcoin
- Wallet are applications that permit easy management of a Bitcoins.
- What's going on under the hood?



# Bitcoin wallets: Under the hood

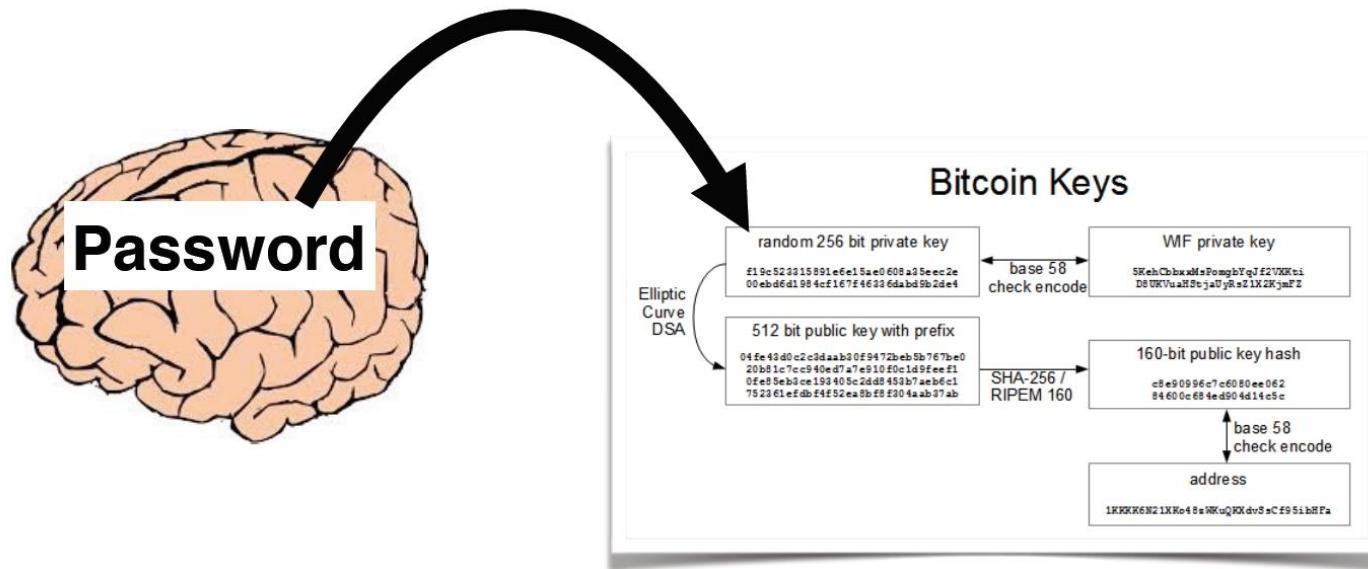
- Remember: identity associated with ECDSA digital signature key pair
  - *SK* used to sign / authorize transactions.
  - *PK* used to identify users and verify transactions.
- Bitcoin wallet stores, protects, and allows use of *SK* to make transactions.



Credit: Ken Shirriff

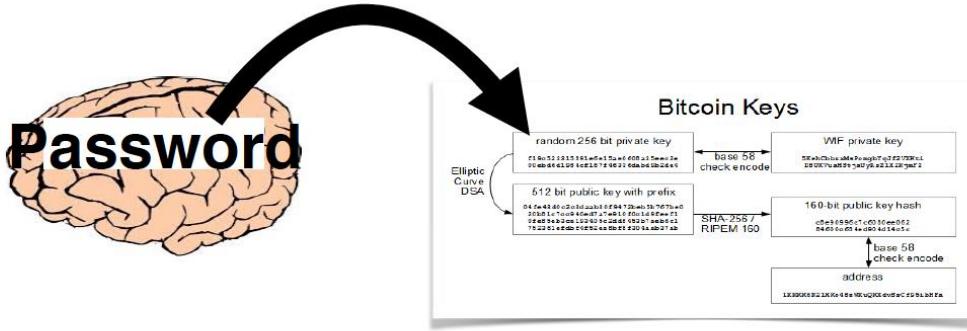
# Brain wallets

- You can generate *SK* from a password



- Your Bitcoin are then completely portable.

# Brain wallets



- Unfortunately, human brains are poor password stores...
  - Cracking brainwallets at one point rumored more profitable than mining...

 **Finders keepers? I found an address with 50 BTC via brain wallet!**

January 18, 2014, 04:58:04 PM

#1

I was playing around with the brain wallet and checking the addresses with blockchain. I found a wallet with a balance of 50 BTC! The coins were put in the wallet in 2011 and there hasn't been any activity since. I don't want to steal someones coins but if they are "lost" I don't want to have them just sitting there. It's a lot of money! I was thinking of sending a small amount into the wallet with a message letting the person know the situation. If nothing happens after a while I guess it's "Finders Keepers, Losers Weepers." What's the right thing to do in this situation?

# Related references

- Joseph Bonneau, Andrew Miller, Jeremy Clark, Arvind Narayanan , Joshua A. Kroll, and Edward W. Felten. “SoK: Research Perspectives and Challenges for Bitcoin and Cryptocurrencies”, in Proc. of IEEE S&P 2015.
- Arvind Narayanan, Joseph Bonneau, Edward Felten, Andrew Miller, Steven Goldfeder. “Bitcoin and Cryptocurrency Technologies”, in Princeton University Press, 2016 (first two chapters)
- Satoshi Nakamoto. “Bitcoin: A Peer-to-Peer Electronic Cash System”
- Bitcoin Wiki, online at [https://en.bitcoin.it/wiki/Main\\_Page](https://en.bitcoin.it/wiki/Main_Page)
- Maurice Herlihy. “Blockchains from a Distributed Computing Perspective ”, 2018

# Playground demo

- Start from hash:
  - <https://andersbrownworth.com/blockchain/hash>
- Till tokens:
  - <https://andersbrownworth.com/blockchain/tokens>