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Mon	$\mathtt{D}(\infty ext{-Cat})$	$\vec{\Sigma}$	$\vec{\Omega}$	\vec{P}	InfPreShf	$D(\infty\text{-Cat/C})$	$\vec{\sigma}$	$\vec{\omega}$	\vec{p}
ComMon	$\mathtt{D}(\infty ext{-Grpd})$	Σ	Ω	P	IntAct	D(∞-Grpd/G)	$\vec{\sigma}$	$\ddot{\omega}$	ÿ
IntGrp	$D(\infty\text{-Grpd}_0)$	Σ	Ω	P	IntActO	$D(\infty-Grpd_0/G_0)$	σ	ω	p

E. Dean Young

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We wish to acknowledge the collaborative efforts of E. Dean Young and Jiazhen Xia. Dean Young initially formulated the introduction with twelve goals, posting them on the Lean Zulip in August of 2023. Together the authors are pursuing these plans as a long term project.

1. Introduction

In this document I would like to develop a construction of the classifying space functor which can be applied indefinitely.

Segal ∞ -Spaces and their relationship with explore derivations and connections.

In this section, which makes use of the previous section concerning Haar integral, I intend to cover the ordinary versions of Poincare duality, Pontrjagin duality, and Fourier duality, as well as versions of these theorems using language enabled by the previous repositories. This won't culminate until far into the future, so for now I have jotted down some sketches.

2. Contents

Section	Description						
Unfinished							
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Unicode							
Introduction							
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Chapter 2:	Tensor Product of Abelian Groups						
⊗_(Ab)							
Chapt	er 3: Rings and Modules						
C:	hapter 4: ∞-Spaces						
Chapter 5	5: Tensor Product of ∞-Spaces						
⊗_(Spc)							
Chapter	6: ∞-Rings and ∞-Modules						
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Cnap	To. W-Derivations						

Chapter 17:	∞ -Connections

after this we develop chain complexes of these.

The table of contents below reflects the tentative long-term goals of the authors, with the main goal the pursuit of the Whitehead theorem for a point-set model involving Mathlib's predefined homotopy groups.

1. cup and cap product

Ideas for future applications:

- 1. https://arxiv.org/pdf/2206.13563.pdf
- 1. One of the basic things I wanted out of this was homotopy colimit preserving maps (E^{inf} -Alg A) $^{o} \longrightarrow \infty$ -Grpd

PART 1: PART I: ABELIAN GROUPS AND $\infty ext{-SPACES}$

Eight Structures						
2	Lax					
Unitial	Unitial Actional					
InternalMonoid	InternalMonoidAction	OperadicMonoid	OperadicMonoidAction			
InternalCommutative Monoid	InternalCommutativeMonoidAction	OperadicMonoid	OperadicMonoidAction			

Abelian Groups

Abelian groups are internal groups in internal groups.

Tensor Product of Abelian Groups

Rings and Modules

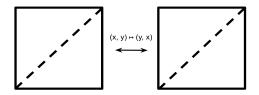
make sure to include Alg

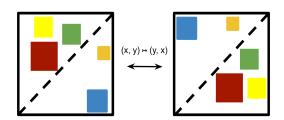
∞ -Spaces

The little squares operad is the square of the little lines operad:

$$OperadicGroup \bullet OperadicGroup : \infty\text{-}Cat_(A) \longrightarrow \infty\text{-}Cat_(A)$$

For example, ... is operadic groups in operadic groups in O^2 .





The commutative nature of composition in the little squares operad is interesting.

OperadicGroup²
$$\infty$$
_(∞ -Grpd)

Could ∞ -spaces be operadic groups in operadic groups?

Tensor Product of $\infty ext{-Spaces}$

$\infty ext{-Rings}$ and $\infty ext{-Modules}$

make sure to include ∞ -Alg...

$\infty ext{-Grpd} ightleftharpoons \infty ext{-Space}$

Set ⇄ AbelianGroup
∞ -Grpd $\rightleftharpoons \infty$ -Space
$Ring \rightleftharpoons \infty$ - $Ring$
$\operatorname{Mod}\nolimits R \rightleftarrows \infty\operatorname{-Mod}\nolimits R$

- 1. π_n of an ∞ -space arising from an ∞ -groupoid vs. H_n ...
- 2.
- 3.
- 4.

 $\mathtt{Ring} \ \rightleftarrows \ \infty\text{-}\mathtt{Ring}$

$\texttt{Mod} \ \mathtt{R} \ \rightleftarrows \ \infty\texttt{-Mod} \ \mathtt{R}$

PART 2: PART II: DERIVATIONS AND CONNECTIONS

	$(\infty$ -Alg R)/B $\rightleftharpoons \infty$ -Mod B
??? ⇄ ???	??? ⇌ ???

Lie Algebras

Lie Algebra Representations

Derivations

- 1. I would like to first construct the lie-algebra of derivations using the spectrum $\Omega^{\mbox{inf}}$.obj X. It seems related to coalgebra endomorphisms from $\Omega^{\mbox{inf}}$.obj X to itself.
- 2. Lie algebras and Der (A,A)

Connections

	1. I would like to first construct the lie-algebra representation of flat connections using the spectrum ω^{inf} .obj X).obj V.
	2.
	3. Lie algebra representations and
	4.
	5.
	6.
	7. Somehow connections are the dual of the free abelian group action
	Some goals:
	1.
	1. smooth (etale locally ???)
	2. analytic (etale locally ???)
$\mathbb{C}\mathrm{P}^1$, \mathbb{C}	$P^1 \cong \mathbb{C}(x)$
	3. Our $\mathbb R$ is ∂ .obj $\mathbb Z$ regarded as an object in $[\vec{\gamma},\infty_{-}(\infty\text{-Grpd})]$
	4. B.obj det : B.obj U(n) \longrightarrow B.obj U(1)
	5. Which E_{∞} Space have a Chern class?
	Cohomology with coefficients in $[-,B\mathbb{C}^X]$ plays a .
	1.
	2. d2 is wedge with (representable)

\mathtt{L}^∞ Algebras

 L^∞ Algebra Representations

∞ -Derivations

∞ -Connections

In this repository, I would like to think about the relationship between homotopy colimits, directed homotopy colimits, and homotopy colimits over based connected ∞ -groupoids and one object ∞ -groupoids, pariticularly as it concerns the six "fibrant replace and forget" functors.

I would also like to incorporate two notions of the formal addition of an interval object and directed interval object, as well as six theorems concerning monadicity that are related to it.

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