

$$T = h\nu \frac{\gamma(1 - \cos \varphi)}{1 + \gamma(1 - \cos \varphi)}$$

$$\varphi = \pi$$

$$\cos(\pi) = -1$$

$$= h\nu \frac{2\gamma}{1 + 2\gamma}$$

$$\gamma = \frac{h\nu}{m_e c}$$

$$= m_e c \frac{2\gamma^2}{1 + 2\gamma}$$

$$\Delta\nu = \frac{m_e c}{h} \frac{2\gamma^2}{1 + 2\gamma}$$

$$T = h \Delta\nu$$

$$\lambda_c = \frac{c}{\Delta\nu} ?$$

$$\frac{c}{\Delta\nu} = c \cdot \frac{h}{m_e c} \frac{1 + 2\gamma}{2\gamma^2}$$

$$= \frac{c}{\Delta\nu} \Delta\nu ?$$

$$\frac{h}{m} \frac{1 + \frac{h\nu}{mc}}{2 \left(\frac{h\nu}{mc}\right)^2} = \frac{h}{2m} \left(\frac{mc}{h\nu}\right)^2 \frac{mc + h\nu}{mc}$$

$$= \frac{mc^2}{2h\nu^2} \frac{mc + h\nu}{mc}$$

$$= \frac{c}{2h\nu^2} (mc + h\nu)$$

$$\frac{c}{\nu^2} \Delta\nu = \frac{c}{\nu^2} \frac{m_e c}{h} \frac{2\gamma^2}{1 + 2\gamma} = \frac{c}{\nu^2} \frac{mc}{h} \frac{2 \left(\frac{h\nu}{mc}\right)^2}{\frac{mc + 2h\nu}{mc}}$$

$$= \frac{c}{\cancel{\nu^2}} \frac{\cancel{mc}}{\cancel{h}} \frac{\cancel{mc}}{mc + 2h\nu} 2 \frac{\cancel{h^2 \nu^2}}{\cancel{m^2 c^2}}$$