Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

Preliminary

Statistical

Linear regression

Logit models

Time corie

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

05/08/2019

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with

Preliminary analysis

Statistical

Linear regression

Logit models

Time series

Section 1

Introduction to R(Studio)

R(Studio)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

- R is the actual programming language
- RStudio is an IDE (Integrated Development Environment) for R.
- R is case sensitive; e. g., Mean \neq mean
- R(Studio) may not work very well when files (or directory containing working files) have accented characters. If the locale language of your filesystem is not in English, then some errors may occur in those cases.

Basic calculations

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

- R can be used as a calculator
- Mathematical constants:
 - pi = 3.142
 - $\exp(1) = 2.718$
- Logarithms:
 - log(e) = 1
 - $\log 10(100) = 2$
 - log(16, base = 4) = 2

Display Information

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

- Getting help: in the console, put a question mark before the function name; RStudio will display the documentation:
- Set the display of decimal digits to 3, for a better output:

```
options(digits = 3)
```

Installing packages

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

One of the strengths of R is the increasing number of available packages (more than 14,000 of them): CRAN Packages

To install and use a package we have

- firstly to install it;
- then, to load it in the current session.

To install a package (e.g., tseries), we can use the install.packages("tseries") function.

To load it in the current session, use library(tseries)

To install a package, we can also use the Tools option in the RStudio window and follow Install Packages...

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with

Preliminary analysis

Statistical

Linear regression

Logit models

Time series

Section 2

Data Types and Data Structure

Data types

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

The data types used by R are

- numeric (double precision): 2.718, 1.4, ...
- integer: 1, −13, . . .
- complex: 2 − 3*i*, . . .
- logical: TRUE, FALSE. Also NA is considered logical
- character: "one plus two", "Hello world!"

Data Structure

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regressior models

Logit model

- Vector: basic data structure in R. Its components have the same data type.
- Matrix: think of linear algebra.
 - A matrix as a collection of vectors.
- Dataframe: similar to a matrix, except that it is not necessarily homogeneous.
 - A collection of vectors (of possible different types) with the same length.
- List: generic data structure containing other objects (vectors, other lists), not necessarily of the same length.

Assignment operator

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

In R, we assign a value, value, to an object x by means of \leftarrow :

x <- value

It is also possible to use =, but the equal sign has lower priority than <-.

Check the discussion at StackExchange.

Vectors

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

The easiest way to create a vector in R is to use the c() function:

$$v \leftarrow c(1, 3, 5, 7, 9)$$

V

Vectors: coercion

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

If we define a vector with components of different data types, the result will be coerced to the same data type

```
w \leftarrow c(1.56, "Hello World", 4, TRUE)
```

typeof(w)

```
## [1] "character"
```

Notice that

```
u <- c(1.56, 4, TRUE) typeof(u)
```

[1] "double"

Vectors by sequences

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

• Create a vector with the first 30 integer numbers:

$$(x < -1:30)$$

In reverse order:

$$(x < -30:1)$$

Vectors by sequences

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series

```
• Create a sequence of the first odd numbers, up to 11:
```

$$(y \leftarrow seq(1, 11, 2))$$

Repeat the character "Hello" 5 times:

```
## [1] "Hello" "Hello" "Hello" "Hello"
```

• Repeat the vector y, defined above, 2 times:

Length of a vector

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

analysis

Statistical Inference

Linear regression models

Logit models

Time series

```
The length of a vector (number of its components) is obtained with the function length()
```

```
x <- 1:30
length(x)
```

[1] 30

```
y <- seq(1, 11, 2)
length(y)
```

[1] 6

```
z <- rep("Hello", 5)
length(z)</pre>
```

[1] 5

Subsetting

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit model

Time series

```
Let y \leftarrow seq(1,11,2): 1, 3, 5, 7, 9, 11.
```

- Select the third component: y[3] = 5
- Exclude the fourth component: y[-4]: 1, 3, 5, 9, 11.
- Select the first four components: y[c(1:4)]: 1, 3, 5, 7
- Select the first, fifth and last element:

```
y[c(1, 5, length(y))]
```

```
## [1] 1 9 11
```

or

```
y[c(1, length(y) - 1, length(y))]
```

[1] 1 9 11

Subsetting

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

- Remove the first four components: y[-c(1:4)]: 9, 11.
- Select the second, fifth and sixth components: y[c(2, 5, 6)]: 3, 9, 11.
- Select components by using a vector of logic type:

```
s <- c(TRUE, TRUE, FALSE, FALSE, TRUE, FALSE)
y[c(s)]
```

```
## [1] 1 3 9
```

Vectorization

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regressior models

Logit models

Time series

Consider the vector

$$x < -1:100$$

Then,

- $x^2 = 1$, 4, 9, 16, 25, 36 ...
- 2*x+3 = 5, 7, 9, 11, 13, 15 ...
- sqrt(x) = 1, 1.414, 1.732, 2, 2.236, 2.449 ...

Vectorization

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Data Types and Data Structure

We can add up two vectors even when they have different lengths, provided that the length of one is an integer multiple of the other:

```
x < - seq(1,11,2)
y < -1:12
x + y
```

[1] 2 5 8 11 14 17 8 11 14 17 20 23 ##

```
Check for identity
```

```
all(x + y == rep(x,2) + y)
## [1] TRUE
identical(x + y, rep(x,2) + y)
## [1] TRUE
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Time series

Each of the following operators returns either TRUE or FALSE.

- == (equality)
- != (not equal to)
- > (greater than)
- (less than)
- >= (greater than or equal to)
- (less than or equal to)
- !x (not x)
- x | y (x OR y)
- x & y (x AND y)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regressior models

Logit models

Time series

Examples

Let $x \leftarrow c(1,2,3,4,5,6)$

- x > 4: FALSE, FALSE, FALSE, FALSE, TRUE, TRUE
- x == 4: FALSE, FALSE, FALSE, TRUE, FALSE, FALSE
- x != 3: TRUE, TRUE, FALSE, TRUE, TRUE, TRUE
- x == 4 | x != 3: TRUE, TRUE, FALSE, TRUE, TRUE, TRUE
- x == 4 & x != 3: FALSE, FALSE, FALSE, TRUE, FALSE, FALSE
- as.numeric(x == 4 | x != 3): 1, 1, 0, 1, 1, 1
- sum(as.numeric(x == 4 | x != 3)): 5

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Logical operators and subsetting

Subsetting will extract the values of the components that satisfy the given logical condition.

Let x < -c(1,2,3,4,5,6)

- x[x <= 0]: numeric(0) (empty set)</pre>
- $x[x \le 0 \mid x > 3]: 4, 5, 6$
- $x[x \le 0 \& x > 3]$: numeric(0) (empty set)
- $sum(x[x \le 0 \& x>3]): 0$

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Selection

```
y \leftarrow c(1, -2, 4, 6, 9, 2, 1)
```

- which (y <= 4): 1, 2, 3, 6, 7
 It selects which entries satisfy the condition. Indexing of vectors starts from 1.
- y[which(y <= 4)]: 1, -2, 4, 2, 1</p>
 It returns the values of the entries satisfying the condition.
- which(y == max(y)): 5 <= entry of the vector</pre>
- y[which(y == max(y))]: 9 <= maximum value

Matrices

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

A matrix A is specified by the number of its rows and columns, $m \times n$.

The **order** of rows and columns is **important**.

Matrix can be created by means of the matrix() function:

```
x <- 1:8
A <- matrix(x, nrow = 4, ncol = 2)
B <- matrix(x, nrow = 2, ncol = 4)
dim(A) # rows = 4; columns = 2</pre>
```

```
dim(B) # rows = 2; columns = 4
```

[1] 2 4

[1] 4 2

Matrices

```
Introduction
to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

В

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

```
## [,1] [,2]
## [1,] 1 5
## [2,] 2 6
## [3,] 3 7
## [4,] 4 8
```

Matrices: Subsetting

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introductio to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Timo corios

• Select the entry of the matrix A in the first row, second column:

A[1,2]

[1] 5

• Select the third column of the matrix B

B[,3]

[1] 5 6

Select the third row of the matrix A

A[3,]

[1] 3 7

Matrices: Subsetting

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Select the first and fouth column of the matrix B

```
## [,1] [,2]
## [1,] 1 7
## [2,] 2 8
```

Binding vectors: by columns

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

```
u <- 1:4
v = rev(u)
w <- rep(1,4)
C <- cbind(u,v,w)
rownames(C) <- c("1st", "2nd", "3rd", "4th")
C</pre>
```

Binding vectors: by rows

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

```
u <- 1:4
v = rev(u)
w <- rep(1,4)
D <- rbind(u,v,w)
colnames(D) <- c("1st", "2nd", "3rd", "4th")
D</pre>
```

```
## 1st 2nd 3rd 4th
## u 1 2 3 4
## v 4 3 2 1
## w 1 1 1 1
```

Matrix operations

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Timo sorio

- The sum of two compatible matrices is A + B
- The subtractino of two compatible matrices is A − B
- The product of two compatible matrices is A *** B
- The transpose of a matrix A is t(A)
- The inverse of a square matrix, A, if it exists, is solve(A)

Inverse matrix

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Timo sorios

```
x <- c(1,2,3,5, 4, 1, 2,2,1)
A <- matrix(x, nrow = 3, ncol = 3)
A1 <- solve(A)
A1 %*% A</pre>
```

The result is the identity matrix, up to round-off errors.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Time series

 We can use the function all.equal() to compare the results of solve(A) and A1 %*% A with the identity matrix:

```
all.equal(A1 %*% A, diag(3))
```

```
## [1] TRUE
```

 The function diag() can also be used to extract the diagonal elements of a matrix

```
diag(A)
```

```
## [1] 1 4 1
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regressior models

Logit models

Time series

$diag((1:5)^{(.5)})$

```
[,1] [,2] [,3] [,4] [,5]
##
   [1,]
            1 0.00 0.00
                            0 0.00
   [2,]
            0 1.41 0.00
                            0 0.00
##
   [3.]
           0 0.00 1.73
                            0 0.00
   [4,]
           0 0.00 0.00
                            2 0.00
##
   [5.]
            0 0.00 0.00
                            0 2.24
##
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Inference

regression models

Logit models

```
diag(log(1):log(5))

## [,1] [,2]
## [1,] 0 0
## [2,] 0 1
diag(log(1:5))
```

```
[,2] [,3] [,4] [,5]
##
        [,1]
   [1,]
             0.000
                    0.0 0.00 0.00
##
##
   [2,]
           0 0.693
                    0.0 0.00 0.00
   [3,]
            0.000
                    1.1 0.00 0.00
   [4,]
           0.000
                    0.0 1.39 0.00
##
  [5,]
           0.000
                    0.0 0.00 1.61
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

R has some built-in functions to deal with matrices. Consider ${\tt A}$

- rowSums(A) = 8, 8, 5
- colSums(A) = 6, 10, 5
- rowMeans(A) = 2.667, 2.667, 1.667

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model:

Time series

The operator **%*%**

The operator **%*%** works differently on vectors and matrices.

- On vectors it computes the dot product
- On matrices, the matrix multiplication (matrix multiplication is a form of ordered, vectorized dot product)

```
a <- c(1,2,3)
```

More matrices

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series

Vector can be coerced to work as matrices; in this case, columns matrices:

```
as.matrix(a)
        \lceil .1 \rceil
##
## [1,]
## [2,]
## [3,]
           3
t(as.matrix(b)) %*% as.matrix(a) # dot product
        [,1]
##
## [1,]
          32
```

More matrices

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

```
as.matrix(a) %*% t(as.matrix(b))
```

```
## [,1] [,2] [,3]
## [1,] 4 5 6
## [2,] 8 10 12
## [3,] 12 15 18
```

Dataframes

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo sorios

- Statistical analysis is done using datasets. A dataset contains a certain number of variables and observations.
- It is a good practice to have each variable set as a column vector and each observation as a row vector.
- A dataframe, in R, is the data structure of an observed dataset.
- A dataframe can be thought of as a matrix in which different columns may have different data types.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data

Working with a Dataframe

Preliminary analysis

Statistical

Linear regression

Logit models

Time series

Section 3

Working with a Dataframe

Preliminary analysis

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regressior models

Logit model

Time series

When loading a dataset for analysis, there are some aspects to consider.

- Understand the data: what the dataset is about; what are its variables; how many obervation the dataset contains.
- Oetermine whether there are missing observations; some functions will not work properly otherwise.
- Visualize some of its variables.

Import the dataset with RStudio

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Information about the dataset

- The dataset is taken from the UCI, Machine Learning Repository website.
- The dataset can be found here.
 - Clicking the link will download the file; we will load the dataset more conveniently later on, with a different set of tools.
- The dataset will be called **cleve** hereinafter in the presentation.
- The dataset format is csv (comma separated variables).

Import the dataset with RStudio

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

- Set the working directory to where you have downloaded the folder of the workshop.
- ② Open an R script and save it with a meaningful name.
- Write in the script
 cleve <- read.csv("cleve.csv", header = FALSE)
 and hit CTRL + Enter (Windows); CMD + Enter (Mac
 OSX) to execute.</pre>
- Try head(cleve) in the script and execute.

Working with the dataset

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regressior models

Logit models

Time series

Set the names of the variables:

- The documentation of the dataset is found here
- To work with only one variable from the dataset, e.g., age, we can extract it by means of \$.

```
age <- cleve$age
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with

Preliminary analysis

Statistical

Linear regression

Logit models

Time series

Section 4

Preliminary analysis

Properties of the dataset

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

The dataset is a dataframe

```
class(cleve)
```

```
## [1] "data.frame"
```

with

```
dim(cleve)
```

```
## [1] 303 14
```

```
nrow(cleve) = 303 observations and ncol(cleve) = 14 variables.
```

Properties of the dataset

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

The names of the variables can also be obtained by colnames(cleve).

The first six observations can be displayed by

head(cleve)

(Output omitted because it does not fit the slide.)

Slicing

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Display the first 3 observations of the first, third and seventh through ninth variables:

```
cleve[1:3,c(1,3,7:9)]
```

```
## age cp restcg thalac exang
## 1 63 1 2 150 0
## 2 67 4 2 108 1
## 3 67 4 2 129 1
```

or with (omitted for space)

Slicing

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introductior to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Examples

• Compute the number of individuals whose age is greater than, or equal to, 50 years:

```
length(cleve$age[cleve$age >= 50])
```

```
## [1] 216
```

2 Compute the number of individuals without a diagnosis of heart disease:

```
length(cleve$sex[cleve$diagnostic == 0])
```

```
## [1] 164
```

Remark The variable diagnostic is strictly positive if there is indication of a heart condition.

Slicing

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working witl a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Examples

Ompute the number of individuals with a diagnosis of heart disease and with fasting blood sugar > 120 mg/dl

```
## [1] 22
```

Compute the number of individuals with a diagnosis of heart disease or with fasting blood sugar > 120 mg/dl

```
## [1] 162
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Time series

```
Consider, e.g., the variable age. Compute:
```

• the mean (average)

mean(cleve\$age)

[1] 54.4

2 the median

median(cleve\$age)

[1] 56

the interquartile range

IQR(cleve\$age) # Q3 - Q1

[1] 13

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

4 the summary of the principal statistics

summary(cleve\$age)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 29.0 48.0 56.0 54.4 61.0 77.0
```

Remark The function summary() does not return neither the variance nor the standard deviation

Quantile distribution

```
quantile(cleve$age, c(.1, .25, .40, .60, .80))
```

```
## 10% 25% 40% 60% 80%
## 42 48 53 58 62
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit model:

Time series

It is possible to apply the summary() function to a full dataset, or to several variables of it

```
summary(cleve[,c(1,5,8)])
```

```
##
                       chol
                                    thalac
        age
                  Min .126
##
   Min.
          .29 0
                                Min.
                                       • 71
##
   1st Qu.:48.0
                  1st Qu.:211
                                1st Qu.:134
##
   Median:56.0
                  Median:241
                                Median: 153
##
   Mean :54.4
                  Mean : 247
                                Mean
                                       :150
##
   3rd Qu.:61.0
                  3rd Qu.:275
                                3rd Qu.:166
##
   Max. :77.0
                  Max
                         :564
                                Max
                                       :202
```

(Only three variables are selected for space.)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Timo carios

Variance and standard deviation

- The variance (resp., standard deviation) is computed by var() (resp., sd()).
- If the variable has NA (missing values), then var(), sd()
 return NA:

```
var(cleve$thal)
## [1] NA
sd(cleve$thal)
```

```
## [1] NA
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Variance

We can apply the function var() to a single variable or several of them; in the latter case, we obtain the variance-covariance matrix of the selected variables:

```
var(cleve[, c(1, 3, 5, 6)])
```

```
##
                         chol
                                 fbs
          age
                  ср
             0.9037 97.787
## age
       81.697
                             0.3816
                        3.595 -0.0137
## ср
        0.904 0.9218
## chol 97.787 3.5951 2680.849 0.1815
## fbs
        0.382 - 0.0137
                        0.181 0.1269
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time caries

Standard deviation

The standard deviation sd(), on the other hand, can only be applied to a single variable:

```
sd(cleve$age)
```

```
## [1] 9.04
```

sd(cleve\$chol)

[1] 51.8

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

Standard deviation of a set of variables

We have to vectorize the function sd() by means of apply():

```
apply(cleve[,11:13], 2, sd)
```

- The value 2 in the second parameter of the function apply() computes the standard deviation, sd, of each variable (column).
- The value 1 would compute the standard deviation of each row (observation).

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time cories

Standard deviation of a set of variables

```
apply(cleve[,11:13], 2, sd)
```

slope ca thal

0.616 NA NA

There are missing values in the dataset.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time corie

Count and remove NA's

Let's count them:

```
sum(is.na(cleve))
```

[1] 6

We can eliminate them (less than 2% of the observed values)

```
cleve <- na.omit(cleve)
sum(is.na(cleve))</pre>
```

[1] 0

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Standard deviation of a set of variables

```
apply(cleve[,11:13], 2, sd)
```

```
## slope ca thal
## 0.618 0.939 1.939
```

The variable slope has a slightly larger standard deviation now.

Contingency Tables

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series

Write a contingency table of gender and diagnosis of heart disease:

```
table(cleve$sex, cleve$diagnostic)
```

```
##
## 0 1 2 3 4
## 0 71 9 7 7 2
## 1 89 45 28 28 11
```

Using the with() function:

```
with(cleve, table(age, diagnostic))
```

(Same result; output omitted for space.)

Contingency Tables

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

```
Alternative to table
Using the xtabs() function:

xtabs(~ cleve$sex + cleve$diagnostic)

## cleve$diagnostic

## cleve$sex 0 1 2 3 4

## 0 71 9 7 7 2

## 1 89 45 28 28 11
```

Estimated Frequencies

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Redefine the variable diagnostic as dummy, with value 1 if some heart problem is observed:

```
cleve$diagnostic[cleve$diagnostic >0] <- 1</pre>
```

Table of estimated frequencies:

```
table(cleve$sex, cleve$diagnostic)/nrow(cleve)
```

```
## 0 0.2391 0.0842
## 1 0.2997 0.3771
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

and Data

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

```
barplot(table(cleve$diagnostic),
    main = "Diagnostic (observed)")
```



Lino AA Notarantonio (lino@tec.mx

Introduction to R(Studio

and Data
Structure

Working with a Dataframe

Preliminary analysis

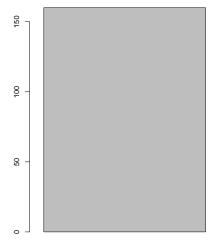
Statistica Inference

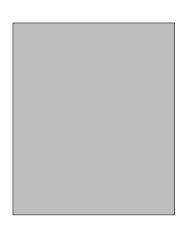
regression models

Logit models

Time series

Diagnostic (observed)





Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

Barplot with observed frequencies



Lino AA Notarantonio (lino@tec.mx

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

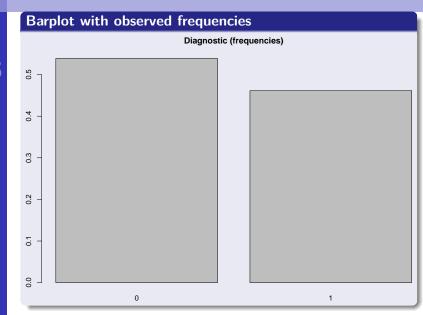
Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time serie



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time corie

Barplot with a contingency table

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

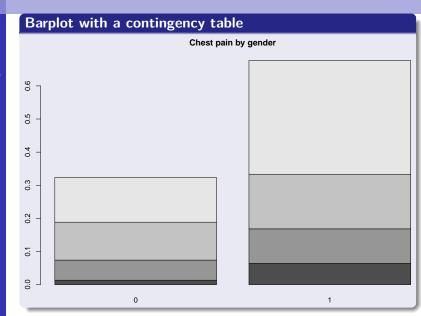
Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Time serie



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time carios

Grouped barplots

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

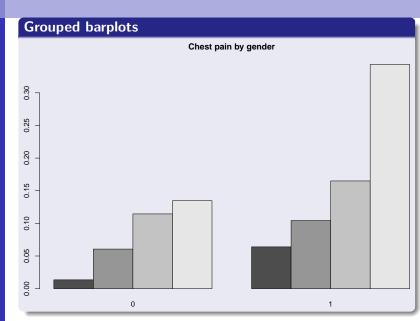
Preliminary analysis

Statistica Inference

regression models

Logit model:

Time series



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time corie

Grouped barplots with colors

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

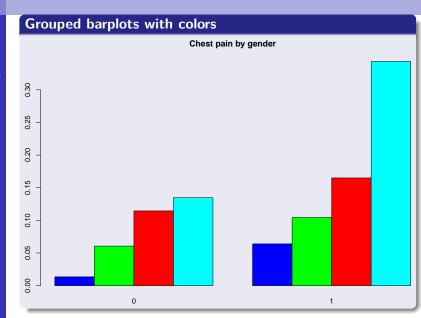
Working with a Dataframe

Preliminary analysis

Statistica Inference

regression models

Logit model:



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Variable "age"

boxplot(cleve\$age)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

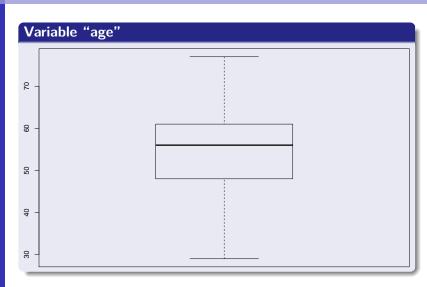
Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Timo carios



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with

Preliminary analysis

Statistica

Linear regression

Logit models

Time series

Age as a function of gender

boxplot(age ~ sex, data = cleve)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

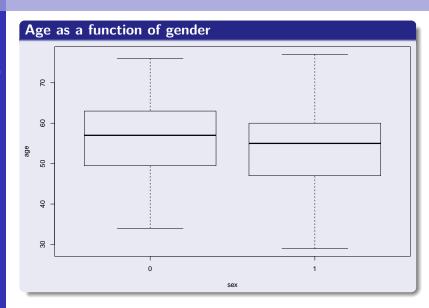
Preliminary analysis

Statistica Inference

Linear regressior models

Logit model

Timo sorio



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

Age as a function of gender, with positive diagnosis

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

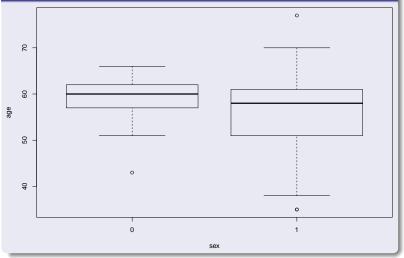
Statistica Inference

Linear regression models

Logit models

Timo sorio





Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Age as a function of gender

Justification

See, e.g., John M. Chalmers, William S. Cleveland, Beat Kleiner, Paul A. Tukey, "Graphical Methods for Data Analysis", Wadsworth International Group, Duxbury Press, 1983, pp. 60-63.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

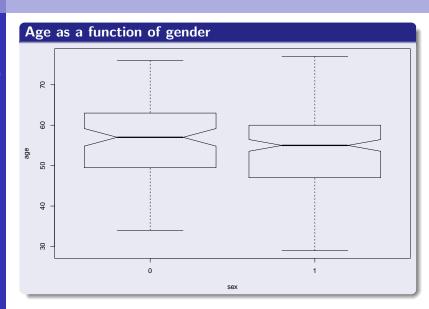
Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo caria



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with

Preliminary analysis

Statistica

Linear regression

Logit models

Time series

Age as a function of gender with positive diagnosis

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

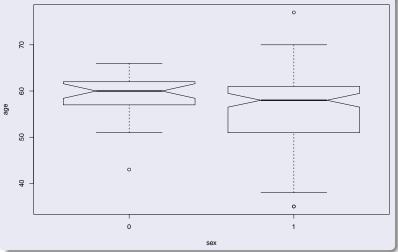
Statistica Inference

Linear regressior models

Logit models

Timo sorio





Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time cario

Two graphs side by side

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

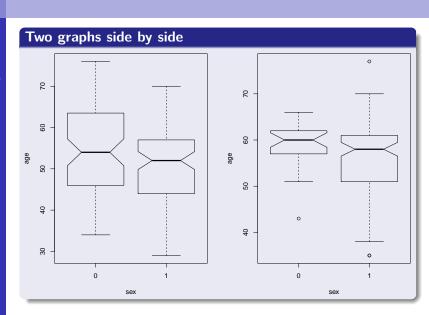
Preliminary analysis

Statistica Inference

Linear regression models

Logit models

-:....



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models



Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

Diagnostic

Preliminary analysis

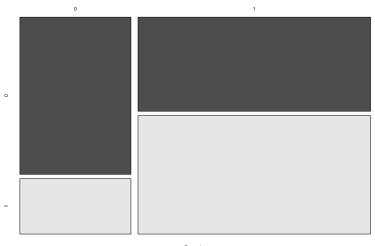
Statistica Inference

Linear regression models

Logit models

Time series





Gender

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time serie

The variable cp has four levels.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

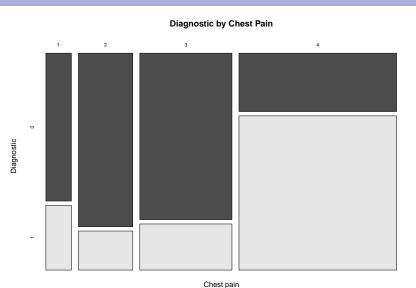
Working witl a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

The variable exang (exercise induced angina): 1 = yes; 0 = no

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

and Data
Structure

Working with a Dataframe

Diagnostic

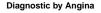
Preliminary analysis

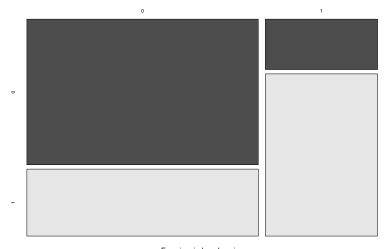
Inference

Linear regression models

Logit models

Time series





Exercise-induced angina

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica

Linear regression

Logit models

Timo carios

Consider the variable age.

plot(cleve\$age)

gives the scatterplot of the variable.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

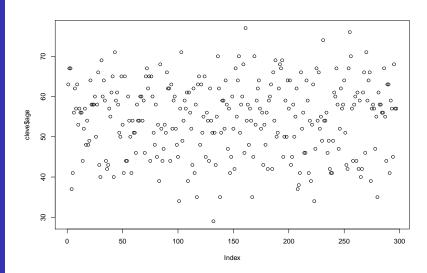
Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regressior models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical

Linear regression

Logit models

Time cories

```
plot(cleve$age, cleve$chol)
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

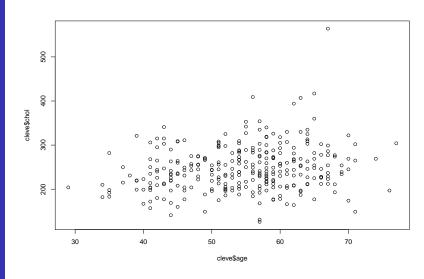
Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

With regression line:

```
plot(cleve$age, cleve$chol)
abline(lm(chol ~ age, data = cleve), col = "red")
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

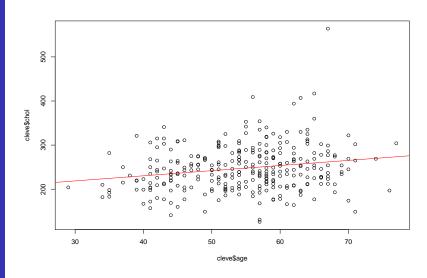
Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models



More Visualization

Introduction to R

Lino AA Notarantonio (lino@tec.mx

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

See the script visualization.R

Classification by K-means clustering

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Time series

See the script classification.R

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with

Preliminary analysis

Statistical Inference

Linear regression

Logit models

Time series

Section 5

Statistical Inference

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series

We want to determine whether there is a difference in age between individuals with no heart condition and those with an indication of a heart condition.

```
age.pos <- cleve$age[cleve$diagnostic == 1]
age.neg <- cleve$age[cleve$diagnostic == 0]</pre>
```

Formally

 H_0 : age.pos = age.neg

 H_1 : age.pos \neq age.neg

(significance level: $\alpha = .05$)

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

```
95% Confidence interval
```

```
t.test(age.pos, age.neg, mu = 0)
##
##
   Welch Two Sample t-test
##
## data: age.pos and age.neg
## t = 4, df = 295, p-value = 6e-05
## alternative hypothesis: true difference in means i
## 95 percent confidence interval:
## 2.12 6.11
## sample estimates:
## mean of x mean of y
       56.8
                 52.6
##
```

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

```
99% Confidence interval
```

```
t.test(age.pos, age.neg, mu = 0, conf.level = .99)
##
##
   Welch Two Sample t-test
##
## data: age.pos and age.neg
## t = 4, df = 295, p-value = 6e-05
## alternative hypothesis: true difference in means i
## 99 percent confidence interval:
## 1.49 6.74
## sample estimates:
## mean of x mean of y
       56.8 52.6
##
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression

Logit models

Timo carios

- The function t.test() uses by default the Welch t.test, with Welch-Satterthwaite correction for degrees of freedom.
- When the variances are equal, we can use

The test for equal variances is

```
var.test(age.pos, age.neg, mu = 0, ratio = 1)
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Timo carios

Power calculation

Having rejected the null hypothesis, we compute the power of the test under the alternative

$$H_1$$
: $age.pos - age.neg = 2.5$

A power calculation needs four parameters, α , sd, n (sample size), δ (true difference in mean). It must also specify whether the test is one sided or two sided.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series

Power calculation

```
power.t.test(n = nrow(cleve), sd =
  sqrt(var(age.pos)+var(age.neg)),
  sig.level = .05, delta = 2.5,
  alternative = "two.sided"
)
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Timo corios

Power calculation

```
##
##
        Two-sample t test power calculation
##
##
                  n = 297
##
             delta = 2.5
##
                 sd = 12.4
##
         sig.level = 0.05
##
             power = 0.689
       alternative = two.sided
##
##
## NOTE: n is number in *each* group
```

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series

Power calculation

Compute the sample size needed so that the power of the test is .90, when delta = 2.5; sd = 12.395, with $\alpha = .05$ in a two sided alternative:

```
##
##
        Two-sample t test power calculation
##
##
                  n = 518
##
             delta = 2.5
##
                 sd = 12.4
##
         sig.level = 0.05
             power = 0.9
##
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
```

Power curve

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression

Logit models

Time cories

```
curve(power.t.test(n=50,delta = x,
    sd = sqrt(var(age.pos)+var(age.neg)),
        type="two.sample",
        alternative="two.sided")$power,
        from=.1, to=10, xlab="delta",
        ylab="power")
```

Power curve

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

and Data
Structure

Working with a Dataframe

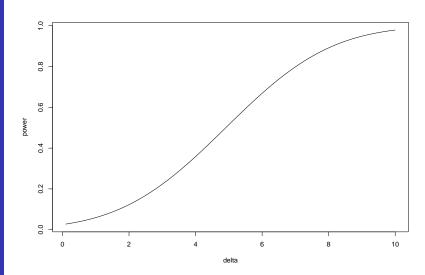
Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data

Working with

Preliminary analysis

Statistical

Linear regression models

Logit models

Time series

Section 6

Linear regression models

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

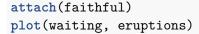
Preliminary analysis

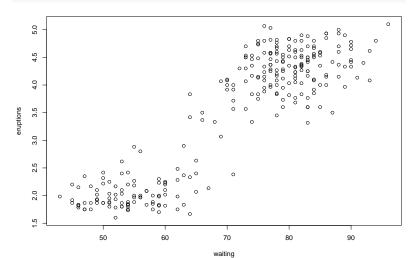
Statistica Inference

Linear regression models

Logit models

Time series





Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

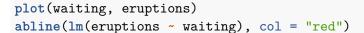
Preliminary analysis

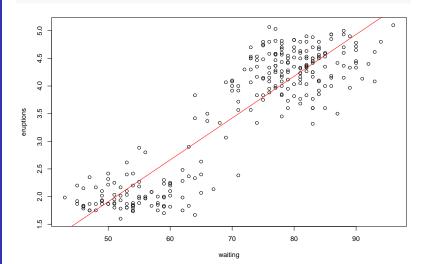
Statistica Inference

Linear regression models

Logit models

Time series





Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Let us consider the model

$$eruptions = \beta_0 + \beta_1 waiting + u$$

slrm <- lm(eruptions ~ waiting, data = faithful)</pre>

```
summary(slrm)
Introduction
          ##
Notarantonio
(lino@tec.mx)
           ## Call:
             lm(formula = eruptions ~ waiting, data = faithful)
          ##
           ## Residuals:
           ##
                  Min
                             10
                                 Median
                                               30
                                                       Max
           ## -1.2992 -0.3769
                                 0.0351 0.3491
                                                    1.1933
          ##
           ## Coefficients:
```

Linear regression models

to R Lino AA

Data Types

---## Signif. codes:

##

##

(Intercept) -1.87402 waiting

0.07563

0.001

0.00222 34.1

'**' 0.01

Estimate Std. Error t value Pr(>|t|)

0.16014 -11.7 <2e-16 *

<2e-16 *

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time cories

Estimation

```
Estimate eruptions, when waiting = 90.
```

```
eruptions.fit.coef <- coefficients(slrm)
c <- c(1,90)
eruptions.fit.coef %*% c
## [,1]
## [1,] 4.93</pre>
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Confidence interval

```
Find a 99% confidence interval for eruptions, when waiting = 90.
```

```
## fit lwr upr
## 1 4.93 4.8 5.07
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Prediction interval

Find a 99% confidence interval for a prediction of *eruptions*, when waiting = 90.

```
## fit lwr upr
## 1 4.93 3.64 6.23
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model:

Time series

Example 1

Consider the data **hsb2.csv**, which is in the Documentation of the workshop.

The description of the variables can be found here.

Estimate the standardized math score by race:

$$math = \beta_0 + \beta_1 race + u$$
.

The variable *race* is **categorical**.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time cories

Example 1

Model estimation

```
hsb2 <- read.csv("hsb2.csv")
m1 <- lm(math ~ factor(race), data = hsb2)
summary.m1 <- summary(m1)
typeof(summary.m1)</pre>
```

```
## [1] "list"
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Data Types

Linear regression models

Example 1

Model estimation: Extraction of the estimated coefficients

summary.m1\$coefficients

##	Estimate	Std.	Error	t value	Pr(> t)
## (Intercept)	47.417		1.82	26.018	1.72e-6	35
## factor(race)2	9.856		3.25	3.032	2.76e-0)3
## factor(race)3	-0.667		2.70	-0.247	8.05e-0)1
## factor(race)4	6.556		1.97	3.332	1.03e-0)3

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Data Types

Linear regression models

Example 1

Use of vectorization

```
summary.m1\$coefficients[2,]
```

Pr(>|t|) Estimate Std. Error t value ## 9.85606 0.00276 ## 3.25084

3.03185

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series

Example 2

Factor interaction

Estimate the standardized math score for gender, race.

R code

```
m2 <- lm(math ~ female*factor(race), data = hsb2)
summary.m2 <- summary(m2)</pre>
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Example 2

##

Estimated model

summary(m2)\$coefficients

female:factor(race)3

female:factor(race)4

## (Intercept)	49.23	2.49	19.760	3
## female	-3.96	3.68	-1.076	2
## factor(race)2	9.44	5.75	1.640	1
## factor(race)3	-3.95	4.21	-0.937	3
## factor(race)4	4.96	2.72	1.824	6
<pre>## female:factor(race)2</pre>	2.04	7.11	0.287	7

6.21

3.55

Estimate Std. Error t value P

5.59

3.97

1.111 2

0.893 3

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminar analysis

Statistica Inference

Linear regression models

Logit models

Time series

Example 3

Estimate the effect of the scores of reading skills, *read*; social studies, *socst*, y science, *science* on the score of mathematics, *math*.

Model

$$math = \beta_0 + \beta_1 read + \beta_2 socst + \beta_3 science + u$$
.

R code

m3 <- lm(math ~ read + socst + science, data = hsb2)
m3.estim <- summary(m3)

m3.estim\$coefficients

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

Example 3

Estimated model

##		Estimate	Std. Error	t	value	Pr(> t)
##	(Intercept)	11.887	2.7937		4.25	3.24e-05
##	read	0.313	0.0654		4.79	3.24e-06
##	socst	0.154	0.0548		2.82	5.37e-03
##	science	0.315	0.0599		5.25	3.96e-07

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model:

Time series

We randomly split the data and use one set to estimate the model and the rest to estimate the goodness of fit. To ensure reproducibility, we set the RNG seed to set.seed(13).

We shall validate firstly the second model, m2, with interaction of factors.

To validate other models, the only change needed is to change below the code where the actual model is specified,

linmodel.Train.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Example 2

```
set.seed(13)
TrainRows <- sample(1:nrow(hsb2),
      .8*nrow(hsb2), replace = FALSE)
Train <- hsb2[TrainRows,]</pre>
Valid <- hsb2[-TrainRows. ]
linmodel.Train <-
  lm(math ~ female*factor(race), data = Train)
mathPredic <-
  predict(linmodel.Train, Valid)
actual.predic <-
  data.frame(cbind(actual = Valid$math,
                    predicted = mathPredic))
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Timo carios

Example 2

Correlation matrix

```
corr.accuracy <- cor(actual.predic)
corr.accuracy</pre>
```

```
## actual predicted
## actual 1.000 0.278
```

predicted 0.278 1.000

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Accuracy: Min-Max

The Min-Max method compute the mean of the minimum over the mean of the maximum.

Values very close to 1 (Min-Max > .90) denotes excellent accuracy.

R code

[1] 0.863

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Accuracy: Mean Absolute Error (MAE)

If Ai are the actual (observed) values of the response and F_i are the forecast ones, then

$$MAE = \frac{1}{T} \sum_{i=1}^{I} |A_i - F_i|;$$

T is the sample size.

R code

mae

[1] 7.94

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Accuracy: Mean Absolute Percentage Error (MAPE)

The mean absolute percentage error (MAPE) is defined as

$$MAPE = \frac{1}{T} \sum_{i=1}^{I} \left| \frac{A_i - F_i}{A_i} \right|.$$

- Mape can be interpreted as the average percentage error.
- Sometimes, MAPE can be very large, enve though the forecast is reasonably good. If, e.g., $A_i \approx 10^{-3}$ and $|F_i A_i| \approx 10^{-1}$, entonces

$$\left|\frac{A_i - F_i}{A_i}\right| \approx 10^2$$

• If the forecast is exact, then MAPE = 0.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time cories

MAPE: R code

```
mape <- mean(
   abs((actual.predic$predicted -
     actual.predic$actual))/actual.predic$actual)
mape</pre>
```

[1] 0.159

On the average, the error is of about 16%.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Timo carios

The library lmtest permits to run tests to determine

- heteroskedasticity;
- serial autocorrelation;
- normality of errors, and
- correct specification of the model (RESET)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model:

Time series

We shall perform the diagnostics on the model in Example 3.

Heteroskedasticity

The underlying hypothesis test is

 H_0 : the model is homoskedastic

 H_1 : the model is heteroskedastic

Function bptest()

Apply the function **bptest()** to the fitted model.

library(lmtest)

bptest(m3)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Time series

Heteroskedasticity

```
bptest(m3)
##
## studentized Breusch-Pagan test
##
## data: m3
## BP = 9, df = 3, p-value = 0.03
```

Conclusion

There is evidence of heteroskedasticity.

We need to estimate errors robust to heteroskedasticity. To do that, we need the library sandwich.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Time series

Heteroskedasticity

Robust errors: HAC covariance matrix

The robust correction is supported by a paper of W.K. Newey & K.D. West, "A Simple, Positive Semi-Definite, Heteroskedasticity and Autocorrelation Consistent Covariance Matrix", 1987.

An implementation of the algorithm is NeweyWest() in the library sandwich:

```
library(sandwich)
```

```
NW <- NeweyWest(m3, lag =6, prewhite = FALSE)
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

ntroductio o R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Linear regression models

Logit models

Time series

Heteroskedasticity

Robust errors

##

The estimated robust errors are obtained using the function coeftest() of the library lmtest:

coeftest(m3, vcov = NW)

t test of coefficients:

t test of coefficients.

Estimate Std. Error t value Pr(>|t|)

(Intercept) 11.8865 2.2487 5.29 3.3e-07 *
read 0.3134 0.0632 4.96 1.6e-06 *
socst 0.1542 0.0490 3.15 0.0019 *

science 0.3145 0.0599 5.25 3.9e-07 *

Signif. codes: 0 '***' 0.001 '**' 0.01

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Serial autocorrelation

The purpose of the test is to determine whether there is any linear dependence among terms of the innovations.

We can apply the Durbin-Watson test, dwtest(), and the Breusch-Godfrey test, bgtest().

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit models

Time series

Serial autocorrelation

```
dwtest(m3)
##
## Durbin-Watson test
##
## data: m3
## DW = 2, p-value = 0.9
## alternative hypothesis: true autocorrelation is
```

Result

There is no evidence that $corr(u_t, u_{t-1}) \neq 0$.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Serial autocorrelation

```
bgtest(m3, order = 10)
##
## Breusch-Godfrey test for serial correlation of or
##
## data: m3
## LM test = 12, df = 10, p-value = 0.3
```

Result

There is no evidence of linear dependence among the first 10 terms of the innovations.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Time series

Normality

There are several normality test available.

- The Shapiro-Wilk test is available in the base library (loaded by default), but it cannot be applied to vectors with more than 5,000 observations.
- The Jarque-Bera test is available in the library tseries:

library(tseries)

 The normality of errors is less of a concern when the sample size is sufficiently large.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Normality: Shapiro-Wilk test

```
shapiro.test(m3$residuals)
##
## Shapiro-Wilk normality test
##
## data: m3$residuals
## W = 1, p-value = 0.5
```

Conclusion

There is no evidence of non-normality of errors.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Jarque-Bera test

```
jarque.bera.test(m3$residuals)
##
## Jarque Bera Test
```

##

data: m3\$residuals

X-squared = 3, df = 2, p-value = 0.2

Conclusion

There is no evidence of non-normality of errors.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

RESET

In this case the test is not very important, as there are only factors as regressors.

R code

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

```
resettest(m3, type = "fitted", power = 2:3)
##
##
    RESET test
##
## data: m3
## RESET = 0.8, df1 = 2, df2 = 194, p-value = 0.5
resettest(m3, type = "regressor", power = 2:3)
##
##
    RESET test
##
## data: m3
## RESET = 0.5, df1 = 6, df2 = 190, p-value = 0.8
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Timo carios

Plots

We can also apply plot() to a lm() object to obtain these tests.

It is an interactive plot and it is convenient to do it in the console.

plot(m3)

Plots: documentation

It can be found here (check "Details").

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model

Timo carios

Plots: Leverage and influential observations

The concepts of leverage and influential observations can be used as a proxy for finding whether a given observation is an outlier.

- Leverage is a measure of how far the independent variables of an observation are from those of other observations.
- An influential observation is one whose deletion will affect greatly the estimate.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Plots: Leverage and influential observations

- The leverage in a linear regression can be computed using the projection matrix (F. Hayashi, 2000, *Econometrics*, Princeton University Press, pp. 21-23).
- The Cook's distance defined in the next slide can be often used as a measure of observaions with high leverage;
 Cook's distance can also be used to detect highly influential observations.
- In R, the <u>residual-leverage</u> plot draws a red, dashed line identifying observations with Cook's distance greater than .5.
- In R, observations with leverage greater than 1 are omitted with a warning; check Residual-Leverage plot in "Details" here,

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Plots

Cook's distance

The Cook's distance is a tool that is used to check whether a single observation has a large influence on the estimate of the linear regression:

$$D_{i} = \frac{\sum_{j=1}^{T} \left(\widehat{y}_{j} - \widehat{y}_{j(i)}\right)^{2}}{(k+1)TSS}$$

where $\hat{y}_{j(i)}$ is the fitted response value when excluding i; TSS is the total sum of square (mean square error):

$$TSS = (1/T) \sum_{i=1}^{T} (y_i - \hat{y}_i)^2.$$

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with

Preliminary analysis

Statistical

Linear regression

Logit models

Time series

Section 7

Logit models

Logit model

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression

Logit models

Logit model

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

```
## probs.predicted2
## 0 1
## 0 0.323 0.215
## 1 0.148 0.313
```

Logit model

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

```
## probs.predicted3
## 0 1
## 0 0.374 0.165
## 1 0.226 0.236
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio)

Data Types and Data Structure

Working with

Preliminary analysis

Statistical

Linear regression

Logit models

Time series

Section 8

Libraries

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Needed libraries are forecast, tseries.

Download them,

install.packages("forecast", "tseries")

and then load then in your session

library(forecast)
library(tseries)

Time series

Introduction to R

Lino AA
Notarantonio

Introduction to R(Studio

Data Type and Data

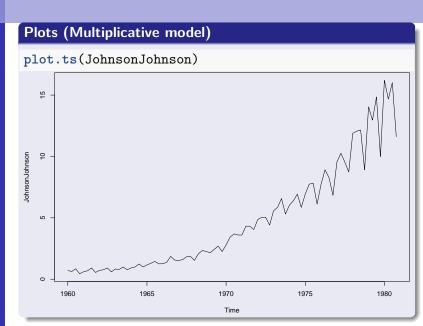
Working with

Preliminar

Statistica Inference

Linear regression models

Logit models



Time series

Introduction to R

Lino AA
Notarantonio

Introduction to R(Studio

Data Type and Data

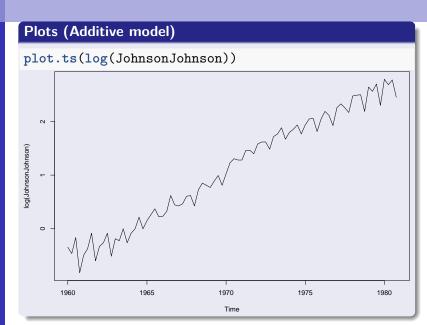
Working with

Preliminary analysis

Statistica Inference

Linear regression models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Let y_t be a stochastic process.

The idea of exponential smoothing is to compute the *one-step* ahead forecast, $\hat{y}_{T+1|T}$, as a weighted mean of the previous observed terms:

$$\widehat{y}_{T+1|T} = \alpha y_T + \alpha (1-\alpha) y_{T-1} + \cdots$$
$$= \alpha y_T + (1-\alpha) \widehat{y}_{T|T-1}, \qquad 0 \le \alpha < 1;$$

rearranging terms,

$$\widehat{y}_{t+1|t} = \alpha y_t + (1 - \alpha)\widehat{y}_{t|t-1},$$

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regressior models

Logit models

Time series

which gives

$$\begin{split} \widehat{y}_{t+1|t} &= \alpha y_t + (1 - \alpha) \widehat{y}_{t|t-1} = \widehat{y}_{t|t-1} + \alpha (y_t - \widehat{y}_{t|t-1}) \\ &= \widehat{y}_{t|t-1} + \alpha e_t, \end{split}$$

where $e_t = y_t - \hat{y}_{t|t-1}$ is the forecast error.

The value α is estimated optimizing the errors squared.

The work by Holt & Winters allowed the inclusion of seasonal, s_t , and trending, b_t , terms, beside the level term, ℓ_t .

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Holt-Winters Modeling (Additive model)

$$y_{t+h|t} = \ell_t + hb_t + s_{t-m+h_m^+}$$

$$\ell_t = \alpha(y_t - s_{t-m}) + (1 - \alpha)(\ell_{t-1} - b_{t-1})$$

$$b_t = \beta^*(\ell_t - \ell_{t-1}) + (1 - \beta^*)b_{t-1}$$

$$s_t = \gamma(y_t - \ell_{t-1} - b_{t-1}) + (1 - \gamma)s_{t-m}$$

where m denotes the seasonality period (per year) The symbol

$$h_m^+ = \lfloor (h-1) \mod(m) \rfloor + 1$$

makes sure that the estimation of the seasonality is the last year of the sample.

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminar analysis

Statistica Inference

Linear regression models

Logit models

Time series

Estimation

```
logJJ.forecast <- HoltWinters(
  log(JohnsonJohnson), beta = TRUE, gamma = TRUE)
logJJ.forecast</pre>
```

```
Introduction
to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Estimation

```
logJJ.forecast$coefficients[1]
```

```
## a
## 2.61
```

logJJ.forecast\$SSE # measure of estimate error

```
## [1] 0.661
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Plots

plot(logJJ.forecast)

The original series is plotted in black and the forecast is in red.

Introduction to R

Lino AA
Notarantonio

Introduction

Data Type and Data

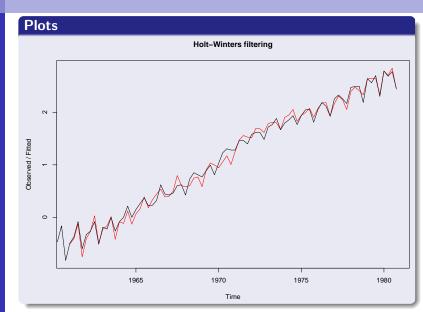
Working with

Preliminary analysis

Statistica Inference

Linear regression models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regressior models

Logit models

Time series

Estimate with an initial value

```
logJJ.forecast2 <- HoltWinters(
  log(JohnsonJohnson), beta = TRUE, gamma =
   TRUE, 1.start = .91) # arbitrary initial value
logJJ.forecast2</pre>
```

```
Introduction to R
```

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistical Inference

Linear regression models

Logit model

Time series

Estimate with an initial value

```
logJJ.forecast2$coefficients[1]
##
     а
## 2.68
logJJ.forecast$coefficients[1]
##
    а
## 2.61
logJJ.forecast$SSE # measure of estimate error
## [1] 0.661
logJJ.forecast2$SSE
## [1] 6.01
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Comparing plots

```
plot(logJJ.forecast2)
lines(logJJ.forecast$fitted[,1], col = "green")
```

The object is a matrix whose columns are, respectively, the fitted time series; its level part; its trend part and the seasonality. We select above the fitted part.

Introduction to R

Lino AA
Notarantonio

Introduction

Data Type and Data

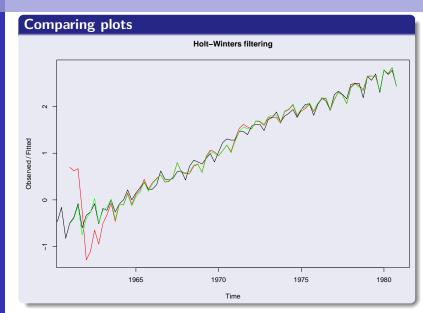
Working with a Dataframe

Preliminar analysis

Statistica Inference

Linear regressior models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica

Linear regressior models

Logit models

Time series

Forecast

Forecast can be performed using the library forecast

library(forecast)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Forecast

logJJ.forecast8095 <-</pre>

```
forecast.HoltWinters(logJJ.forecast, h=8)
```

- We use the first estimate, logJJ.forecast, as it is proven to be the better.
- The parameter h=8 will forecast the estimate eight periods in the future (two years).
- The forecast also plots a confidence interval (80%; 95% is the default).

Introduction to R

Lino AA
Notarantonio

Introduction to R(Studio

Data Type and Data

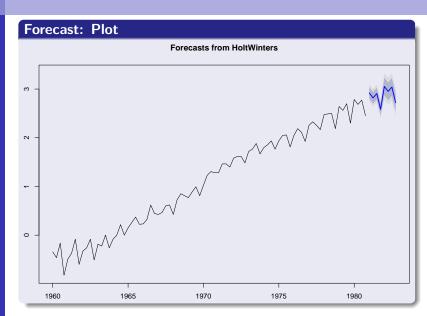
Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

Preliminar

Statistica Inference

Linear regression models

Logit models

Time series

Forecast: Plot

```
logJJ.forecast8599 <- forecast(
  logJJ.forecast, h=8, level = c(85,99))
plot(logJJ.forecast8599)</pre>
```

Introduction to R

Lino AA
Notarantonio

Introduction

Data Type and Data

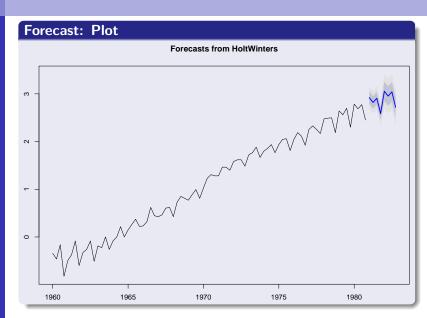
Working with

Preliminary analysis

Statistica Inference

Linear regressior models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Diagnostics

```
library(tseries)
ts8095.fitted <- as.ts(logJJ.forecast8095$fitted)
ts8095.fitted <- na.omit(ts8095.fitted)
ts8095.residuals <-
   as.ts(logJJ.forecast8095$residuals)
ts8095.residuals <-
   na.omit(as.ts(logJJ.forecast8095$residuals))</pre>
```

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

and Data Structure

Working with

Preliminary analysis

Statistica

Linear regression

Logit models

Time series

Diagnostics: ACF

acf(ts8095.residuals)

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Type and Data

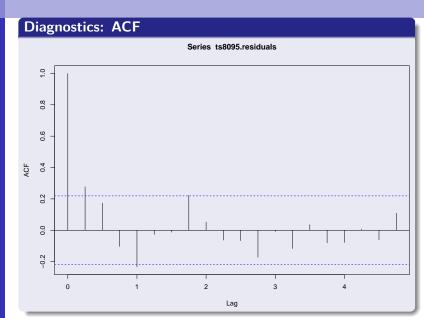
Working with a Dataframe

Preliminar analysis

Statistica Inference

Linear regressior models

Logit models



Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

Diagnostics: Ljung-Box Test

```
Box.test(ts8095.residuals, lag = 20)
##
## Box-Pierce test
##
## data: ts8095.residuals
## X-squared = 25, df = 20, p-value = 0.2
```

Conclusion

We do not reject the null hypothesis of no autocorrelation (for the first 20 lags).

Introduction to R

Lino AA Notarantonio (lino@tec.mx)

Introduction to R(Studio

Data Types and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit model:

Time series

Diagnostics: Augmented Dickey-Fuller Test

```
adf.test(ts8095.fitted)
##
## Augmented Dickey-Fuller Test
##
## data: ts8095.fitted
## Dickey-Fuller = -1, Lag order = 4, p-value = 0.8
## alternative hypothesis: stationary
```

Conclusion

There is evidence that the errors are not white noise.

Box-Jenkins approach

Introduction to R

Lino AA Notarantonio (lino@tec.mx

Introduction to R(Studio

Data Type and Data Structure

Working with a Dataframe

Preliminary analysis

Statistica Inference

Linear regression models

Logit models

Time series

See the script BoxJenkins.R