

IMMEDIATI

$$\int dx = x + c$$

$$\int k dx = kx + c$$

$$\int x dx = \frac{1}{2} x^2 + c$$

$$\int x^\alpha dx = \frac{1}{\alpha+1} x^{\alpha+1} + c$$

$$\int \frac{1}{x} dx = \ln|x| + c$$

$$\int \frac{1}{\sqrt{x}} dx = 2\sqrt{x} + c$$

$$\int e^x dx = e^x + c$$

$$\int a^x dx = \frac{a^x}{\ln a} + c$$

$$\int \sec x dx = -\cot x + c$$

$$\int \cot x dx = \ln|x| + c$$

$$\int \frac{1}{\cos^2 x} dx = \tan x + c$$

$$\int \frac{1}{\sin^2 x} dx = -\cot x + c$$

$$\int \frac{1}{x^2+1} dx = \arctg x + c$$

$$\int \frac{1}{\sqrt{1-x^2}} dx = \arcsin x + c$$

$$\int f'(x) \cdot [f(x)]^\alpha dx = \frac{1}{\alpha+1} [f(x)]^{\alpha+1} + c$$

$$\int \frac{f'(x)}{f(x)} dx = \ln|f(x)| + c$$

$$\int \frac{f'(x)}{\sqrt{f(x)}} dx = 2\sqrt{f(x)} + c$$

$$\int f'(x) e^{f(x)} dx = e^{f(x)} + c$$

$$\int f'(x) a^{f(x)} dx = \frac{a^{f(x)}}{\ln a} + c$$

$$\int f'(x) \sin[f(x)] dx = -\cos f(x) + c$$

$$\int f'(x) \cos[f(x)] dx = \sin f(x) + c$$

$$\int \frac{f'(x)}{\cos^2 f(x)} dx = \tan f(x) + c$$

$$\int \frac{f'(x)}{\sin^2 f(x)} dx = -\cot f(x) + c$$

$$\int \frac{f'(x)}{[f(x)]^2+1} dx = \arctg[f(x)] + c$$

$$\int \frac{f'(x)}{\sqrt{1-[f(x)]^2}} dx = \arcsin[f(x)] + c$$

PER SOSTITUZIONE

$$\int f(x) dx = \int f(g(t)) g'(t) dt$$

PER PARTI

$$\int f(x) \cdot g'(x) dx = f(x) \cdot g(x) - \int g(x) \cdot f'(x) dx$$

$$\int f(x) \cdot dg(x) = f(x) \cdot g(x) - \int g(x) df(x)$$

FUNZIONI FRATTE

$$\int \frac{N(x)}{D(x)} dx = \int \frac{D(x) \cdot Q(x) + R(x)}{D(x)} dx =$$

$$= \int Q(x) dx + \int \frac{R(x)}{D(x)} dx$$

N → numeratore

D → denominatore

Q → quoziente

R → resto

$$\frac{1}{\alpha+1} x^{\alpha+1}$$

$$\frac{1}{x^{1/2}}$$

$$x^{-1/2} \quad \frac{1}{-\frac{1}{2}+1} \quad 2\sqrt{x}$$

PROPRIETÀ

$$\int_a^b f(x) dx = - \int_b^a f(x) dx$$

$$\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx$$

$$\int_a^b [f(x) + g(x)] dx = \int_a^b f(x) dx + \int_a^b g(x) dx$$

CALCOLO

$$\int a dx = ax + c$$

$$\int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1} + c$$

$$\int x dx = \frac{x^2}{2} + c$$

$$\int \sin x dx = -\cos x + c$$

$$\begin{aligned} & \frac{1}{3} \int (1 - \sin^2 x) \cdot \cos x \\ & \frac{1}{3} \sin x + \frac{1}{3} \int (\sin^2 x)^2 (\cos x -) \\ & \frac{1}{3} \sin x + \frac{2}{3} \frac{1}{3} \sin^3 x \\ & \frac{1}{3} \left(\sin x + \frac{2}{3} \sin^3 x \right) \end{aligned}$$

$$\int (1 - \sin^2 x) \cdot \cos x$$

$$\frac{1}{3} \int \cos x + \frac{1}{3} \int \sin^2 x \cos x$$

$$\frac{1}{3} \sin x + \frac{1}{3} \int \sin^2 x \cos x$$