Labs

February 21, 2025

```
[1]: from notebookfuncs import *
        Chapter 2 Lab
[2]: print("Fit a model with ", 11, " variables")
    Fit a model with 11 variables
[3]: print?
    Signature: print(*args, sep=' ', end='\n', file=None, flush=False)
    Docstring:
    Prints the values to a stream, or to sys.stdout by default.
      string inserted between values, default a space.
      string appended after the last value, default a newline.
      a file-like object (stream); defaults to the current sys.stdout.
    flush
      whether to forcibly flush the stream.
               builtin_function_or_method
    Type:
[4]: 3 + 5
[4]: 8
[5]: "hello, " + " " + "world!"
[5]: 'hello, world!'
[6]: x = [3, 4, 5]
     X
[6]: [3, 4, 5]
```

```
[7]: y = [4, 9, 7]
      x + y
 [7]: [3, 4, 5, 4, 9, 7]
 [8]: import numpy as np
 [9]: x = np.array([3, 4, 5])
      y = np.array([4, 9, 7])
      x + y
[9]: array([7, 13, 12])
[10]: x = np.array([[1, 2], [3, 4]])
[10]: array([[1, 2],
             [3, 4]])
[11]: x.ndim
[11]: 2
[12]: x.dtype
[12]: dtype('int64')
[13]: x = np.array([[1, 2], [3.0, 4]])
      x.dtype
[13]: dtype('float64')
[14]: np.array([[1, 2], [3, 4]], float).dtype
[14]: dtype('float64')
[15]: x.shape
[15]: (2, 2)
[16]: x = np.array([1, 2, 3, 4])
      x.sum()
[16]: 10
[]:
[17]: x = np.array([1, 2, 3, 4])
      np.sum(x)
```

```
[17]: 10
[18]: x = np.array([1, 2, 3, 4, 5, 6])
      print("Beginning x:\n ", x)
      x_reshape = x_reshape(2, 3)
      print("reshaped x:\n", x_reshape)
     Beginning x:
       [1 2 3 4 5 6]
     reshaped x:
      [[1 2 3]
      [4 5 6]]
[19]: x_reshape[0, 0]
[19]: 1
[20]: x_reshape[1, 2]
[20]: 6
[21]: print("x before we modify x_reshape:\n", x)
      print("x reshape before we modify x reshape:\n", x reshape)
      x_reshape[0, 0] = 5
      print("x_reshape after we modify its top left element:\n", x_reshape)
      print("x after we modify top left element of x_reshape:\n", x)
     x before we modify x_reshape:
      [1 2 3 4 5 6]
     x_reshape before we modify x_reshape:
      [[1 2 3]
      [4 5 6]]
     x_reshape after we modify its top left element:
      [[5 2 3]
      [4 5 6]]
     x after we modify top left element of x_reshape:
      [5 2 3 4 5 6]
[22]: my_tuple = (1, 2, 3)
      # type error
      # my_tuple[0] = 10
[22]: (1, 2, 3)
[23]: x_reshape.shape, x_reshape.ndim, x_reshape.T
[23]: ((2, 3),
       2,
       array([[5, 4],
```

```
[2, 5],
[3, 6]]))
```

```
[24]: np.sqrt(x)
```

[24]: array([2.23606798, 1.41421356, 1.73205081, 2. , 2.23606798, 2.44948974])

```
[25]: x**2
```

[25]: array([25, 4, 9, 16, 25, 36])

```
[26]: x**0.5
```

[26]: array([2.23606798, 1.41421356, 1.73205081, 2. , 2.23606798, 2.44948974])

[27]: np.random.normal?

Docstring:

normal(loc=0.0, scale=1.0, size=None)

Draw random samples from a normal (Gaussian) distribution.

The probability density function of the normal distribution, first derived by De Moivre and 200 years later by both Gauss and Laplace independently [2]_, is often called the bell curve because of its characteristic shape (see the example below).

The normal distributions occurs often in nature. For example, it describes the commonly occurring distribution of samples influenced by a large number of tiny, random disturbances, each with its own unique distribution [2]_.

.. note::

New code should use the `~numpy.random.Generator.normal` method of a `~numpy.random.Generator` instance instead; please see the :ref:`random-quick-start`.

Parameters

loc : float or array_like of floats
 Mean ("centre") of the distribution.

scale : float or array_like of floats

Standard deviation (spread or "width") of the distribution. Must be non-negative.

size : int or tuple of ints, optional
Output shape. If the given shape is, e.g., ``(m, n, k)``, then

``m * n * k`` samples are drawn. If size is ``None`` (default),
a single value is returned if ``loc`` and ``scale`` are both scalars.
Otherwise, ``np.broadcast(loc, scale).size`` samples are drawn.

Returns

out : ndarray or scalar

Drawn samples from the parameterized normal distribution.

See Also

random.Generator.normal: which should be used for new code.

Notes

The probability density for the Gaussian distribution is

```
.. math:: p(x) = \frac{1}{\sqrt{2 \pi^2 }}

e^{-\frac{1}{x}} \{2 \pi^2 \}
```

where :math: `\mu` is the mean and :math: `\sigma` the standard deviation. The square of the standard deviation, :math: `\sigma^2`, is called the variance.

The function has its peak at the mean, and its "spread" increases with the standard deviation (the function reaches 0.607 times its maximum at :math: $x + \sigma$ and :math: $x - \sigma$. This implies that normal is more likely to return samples lying close to the mean, rather than those far away.

References

- .. [1] Wikipedia, "Normal distribution", https://en.wikipedia.org/wiki/Normal_distribution
- .. [2] P. R. Peebles Jr., "Central Limit Theorem" in "Probability,
 Random Variables and Random Signal Principles", 4th ed., 2001,
 pp. 51, 51, 125.

Examples

Draw samples from the distribution:

>>> mu, sigma = 0, 0.1 # mean and standard deviation >>> s = np.random.normal(mu, sigma, 1000)

Verify the mean and the variance:

```
>>> abs(mu - np.mean(s))
     0.0 # may vary
     >>> abs(sigma - np.std(s, ddof=1))
     0.1 # may vary
     Display the histogram of the samples, along with
     the probability density function:
     >>> import matplotlib.pyplot as plt
     >>> count, bins, ignored = plt.hist(s, 30, density=True)
     >>> plt.plot(bins, 1/(sigma * np.sqrt(2 * np.pi)) *
                      np.exp(-(bins - mu)**2 / (2 * sigma**2)),
                linewidth=2, color='r')
     >>> plt.show()
     Two-by-four array of samples from the normal distribution with
     mean 3 and standard deviation 2.5:
     >>> np.random.normal(3, 2.5, size=(2, 4))
     array([[-4.49401501, 4.00950034, -1.81814867, 7.29718677],
            [ 0.39924804, 4.68456316, 4.99394529, 4.84057254]]) # random
                builtin_function_or_method
     Type:
[28]: x = np.random.normal(size=50)
     x
[28]: array([ 0.08041773, -0.03026667, -0.75024594, 0.55309515, -0.05462602,
             -0.45598797, -1.31841838, 1.7935072, -1.51596114, -0.50126252,
            -1.30425185, -0.03340125, -1.35537998, 1.69153596, 1.42804145,
             0.07790256, 0.1058116, 1.10016254, 1.40118536, -0.17548991,
            -0.87869758, 0.69268256, 0.74976422, -1.1463767, 0.13973715,
             0.71530199, -1.27774347, 0.0999863, -0.9482597, 0.60169475,
            -0.11348222, -0.68666708, -1.29890979, 0.30813716, 1.75730809,
             0.43512618, -1.524111143, 0.71597162, -1.1332048, -1.3348259,
             0.6642063, -0.12842332, -0.08288676, -0.04559009, -1.76561078,
             0.19567015, -0.46276504, 1.44365583, -0.62148203, 0.46484459]
[29]: y = x + np.random.normal(loc=50, scale=1, size=50)
[29]: array([50.0979533, 49.26404285, 49.71799704, 49.41562921, 49.15535843,
            50.0941145 , 49.22353957, 51.91211385, 46.78992371, 49.35636789,
            47.89630029, 47.81683737, 50.34305891, 51.92732736, 52.42157283,
            49.59542562, 49.37032237, 51.34191185, 52.21067084, 49.4501618,
            49.25157637, 52.41226159, 49.73448335, 52.02641758, 48.32782489,
            50.86437636, 48.34873085, 49.79934532, 51.17431798, 50.12031479,
            50.35817915, 50.00245766, 46.69029529, 50.42398331, 50.94783997,
```

```
50.09013429, 47.71924593, 51.71021843, 49.15006387, 47.22155613,
             49.64516452, 48.90729793, 50.82616726, 50.31144179, 46.30683944,
             50.2992735 , 50.07729159, 52.25433213, 49.15060364, 49.82369515])
[30]: np.corrcoef(x, y)
[30]: array([[1.
                        , 0.70414113],
             [0.70414113, 1.
                                    ]])
[31]: print(np.random.normal(scale=5, size=2))
      print(np.random.normal(scale=5, size=2))
     [8.32626704 0.60313317]
     [ 2.64990968 -1.09541093]
[32]: rng = np.random.default_rng(1303)
      print(rng.normal(scale=5, size=2))
      rng = np.random.default_rng(1303)
      print(rng.normal(scale=5, size=2))
     [ 4.09482632 -1.07485605]
     [ 4.09482632 -1.07485605]
[33]: rng = np.random.default_rng(3)
      y = rng.standard_normal(10)
      np.mean(y), y.mean()
[33]: (-0.1126795190952861, -0.1126795190952861)
[34]: np.var(y), y.var(), np.mean((y - y.mean()) ** 2)
[34]: (2.7243406406465125, 2.7243406406465125, 2.7243406406465125)
[35]: np.sqrt(np.var(y)), np.std(y)
[35]: (1.6505576756498128, 1.6505576756498128)
[36]: np.var?
     Signature:
     np.var(
         a.
         axis=None,
         dtype=None,
         out=None,
         ddof=0,
         keepdims=<no value>,
         where=<no value>,
```

Call signature: np.var(*args, **kwargs)
Type: _ArrayFunctionDispatcher

String form: <function var at 0x7eba602e3ec0>

File: ~/ISLP/islpenv/lib/python3.12/site-packages/numpy/core/

→fromnumeric.py

Docstring:

Compute the variance along the specified axis.

Returns the variance of the array elements, a measure of the spread of a distribution. The variance is computed for the flattened array by default, otherwise over the specified axis.

Parameters

a : array_like

Array containing numbers whose variance is desired. If `a` is not an array, a conversion is attempted.

axis : None or int or tuple of ints, optional

Axis or axes along which the variance is computed. The default is to compute the variance of the flattened array.

.. versionadded:: 1.7.0

If this is a tuple of ints, a variance is performed over multiple axes, instead of a single axis or all the axes as before.

dtype : data-type, optional

Type to use in computing the variance. For arrays of integer type the default is `float64`; for arrays of float types it is the same as the array type.

out : ndarray, optional

Alternate output array in which to place the result. It must have the same shape as the expected output, but the type is cast if necessary.

ddof : int, optional

"Delta Degrees of Freedom": the divisor used in the calculation is ``N - ddof``, where ``N`` represents the number of elements. By default `ddof` is zero.

keepdims : bool, optional

If this is set to True, the axes which are reduced are left in the result as dimensions with size one. With this option, the result will broadcast correctly against the input array.

If the default value is passed, then `keepdims` will not be passed through to the `var` method of sub-classes of `ndarray`, however any non-default value will be. If the sub-class' method does not implement `keepdims` any exceptions will be raised.

```
where : array_like of bool, optional
    Elements to include in the variance. See `~numpy.ufunc.reduce` for
    details.
    .. versionadded:: 1.20.0
Returns
```

variance : ndarray, see dtype parameter above
 If ``out=None``, returns a new array containing the variance;
 otherwise, a reference to the output array is returned.

See Also

std, mean, nanmean, nanstd, nanvar
:ref:`ufuncs-output-type`

Notes

The variance is the average of the squared deviations from the mean, i.e., ``var = mean(x)``, where ``x = abs(a - a.mean())**2``.

The mean is typically calculated as ``x.sum() / N``, where ``N = len(x)``. If, however, `ddof` is specified, the divisor ``N - ddof`` is used instead. In standard statistical practice, ``ddof=1`` provides an unbiased estimator of the variance of a hypothetical infinite population. ``ddof=0`` provides a maximum likelihood estimate of the variance for normally distributed variables.

Note that for complex numbers, the absolute value is taken before squaring, so that the result is always real and nonnegative.

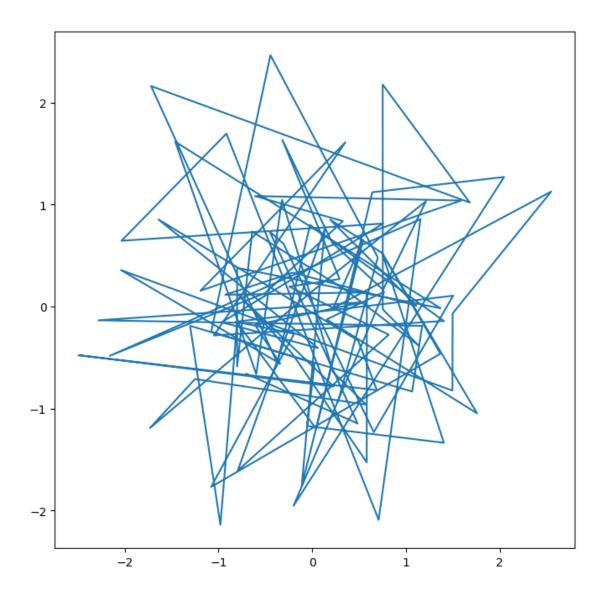
For floating-point input, the variance is computed using the same precision the input has. Depending on the input data, this can cause the results to be inaccurate, especially for `float32` (see example below). Specifying a higher-accuracy accumulator using the ``dtype`` keyword can alleviate this issue.

Examples

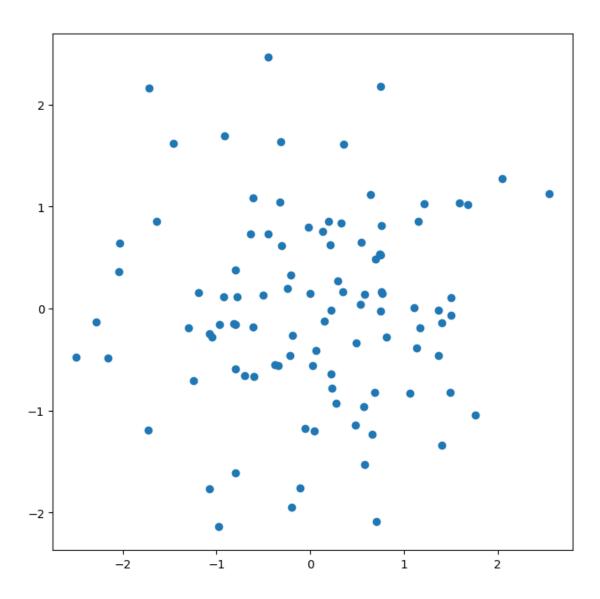
>>> a = np.array([[1, 2], [3, 4]]) >>> np.var(a) 1.25 >>> np.var(a, axis=0) array([1., 1.]) >>> np.var(a, axis=1) array([0.25, 0.25])

```
In single precision, var() can be inaccurate:
>>> a = np.zeros((2, 512*512), dtype=np.float32)
>>> a[0, :] = 1.0
>>> a[1, :] = 0.1
>>> np.var(a)
0.20250003
Computing the variance in float64 is more accurate:
>>> np.var(a, dtype=np.float64)
0.20249999932944759 # may vary
>>> ((1-0.55)**2 + (0.1-0.55)**2)/2
0.2025
Specifying a where argument:
>>> a = np.array([[14, 8, 11, 10], [7, 9, 10, 11], [10, 15, 5, 10]])
>>> np.var(a)
6.8333333333333 # may vary
>>> np.var(a, where=[[True], [True], [False]])
Class docstring:
Class to wrap functions with checks for __array_function__ overrides.
All arguments are required, and can only be passed by position.
Parameters
_____
dispatcher : function or None
    The dispatcher function that returns a single sequence-like object
   of all arguments relevant. It must have the same signature (except
   the default values) as the actual implementation.
    If ``None``, this is a ``like=`` dispatcher and the
    ``_ArrayFunctionDispatcher`` must be called with ``like`` as the
   first (additional and positional) argument.
implementation : function
   Function that implements the operation on NumPy arrays without
   overrides. Arguments passed calling the ``_ArrayFunctionDispatcher``
   will be forwarded to this (and the ``dispatcher``) as if using
    ``*args, **kwargs``.
Attributes
_____
_implementation : function
    The original implementation passed in.
```

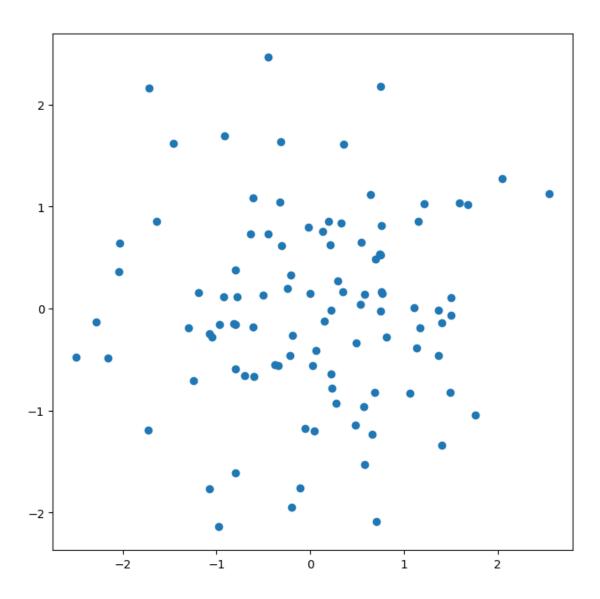
```
[37]: X = rng.standard_normal((10, 3))
      X
[37]: array([[ 0.22578661, -0.35263079, -0.28128742],
             [-0.66804635, -1.05515055, -0.39080098],
             [0.48194539, -0.23855361, 0.9577587],
             [-0.19980213, 0.02425957, 1.54582085],
             [0.54510552, -0.50522874, -0.18283897],
             [ 0.54052513, 1.93508803, -0.26962033],
             [-0.24355868, 1.0023136, -0.88645994],
             [-0.29172023, 0.88253897, 0.58035002],
             [0.0915167, 0.67010435, -2.82816231],
             [ 1.02130682, -0.95964476, -1.66861984]])
[38]: X.mean(axis=0)
[38]: array([ 0.15030588, 0.14030961, -0.34238602])
[39]: X.mean(axis=0)
[39]: array([ 0.15030588, 0.14030961, -0.34238602])
[40]: X.mean(0)
[40]: array([ 0.15030588, 0.14030961, -0.34238602])
[41]: X.mean(1)
[41]: array([-0.13604387, -0.70466596, 0.40038349, 0.45675943, -0.04765406,
             0.73533095, -0.04256834, 0.39038958, -0.68884708, -0.53565259])
[42]: X.mean()
[42]: -0.017256845138782704
[43]: ax.plot?
     Object `ax.plot` not found.
[44]: from matplotlib.pyplot import subplots
[45]: fig, ax = subplots(figsize=(8, 8))
      x = rng.standard_normal(100)
      y = rng.standard_normal(100)
      ax.plot(x, y);
```



```
[46]: fig, ax = subplots(figsize=(8, 8))
ax.plot(x, y, "o");
```



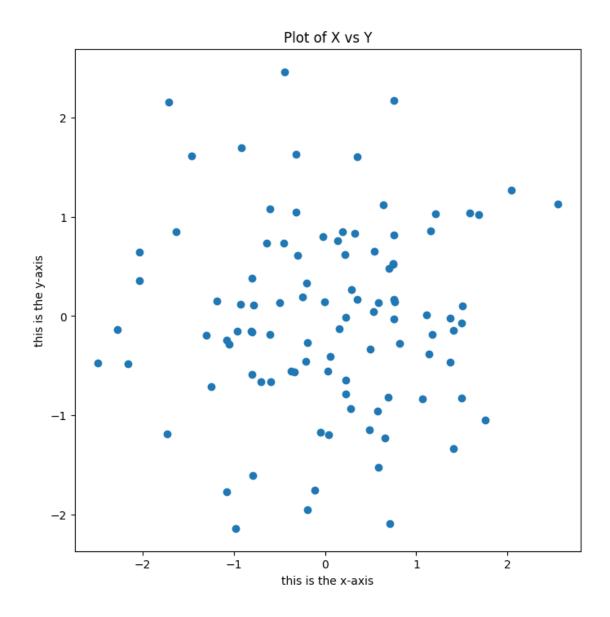
```
[47]: fig, ax = subplots(figsize=(8, 8))
ax.scatter(x, y, marker="o");
```

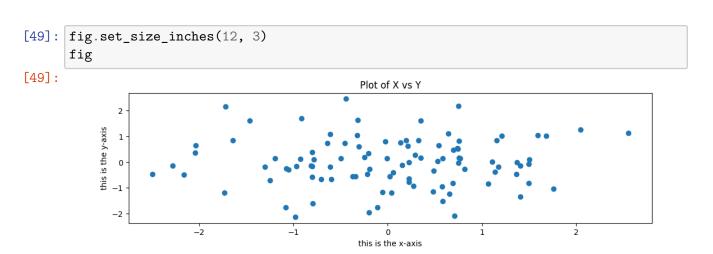


```
[48]: fig, ax = subplots(figsize=(8, 8))

ax.scatter(x, y, marker="o")
ax.set_xlabel("this is the x-axis")
ax.set_ylabel("this is the y-axis")
ax.set_title("Plot of X vs Y")
```

[48]: Text(0.5, 1.0, 'Plot of X vs Y')



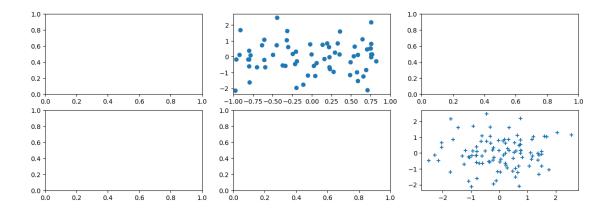


```
[50]: fig, axes = subplots(nrows=2, ncols=3, figsize=(15, 5))
                                                       0.8
                                                                                               0.8
                0.8
                                                       0.6
                                                                                               0.6
                0.6
                                                       0.4
                                                                                                0.4
                0.4
                                                       0.2
                                                                                                0.2
                0.2
                        0.2
                               0.4
                                      0.6
                                                                                    0.8
                                                        1.0
                1.0
                                                                                                1.0
                0.8
                                                                                               0.8
                0.6
                                                       0.6
                                                                                               0.6
                                                       0.4
                                                                                                0.4
                0.4
                0.2
                                                        0.2
                                                                                                0.2
               0.0 +
                                                        0.0
                                                                                               0.0
                        0.2
                                                                       0.4
                                                                                    0.8
                                                                                                        0.2
                                                                                                               0.4
                                                                                                                            0.8
                               0.4
                                            0.8
                                                                                                                     0.6
```

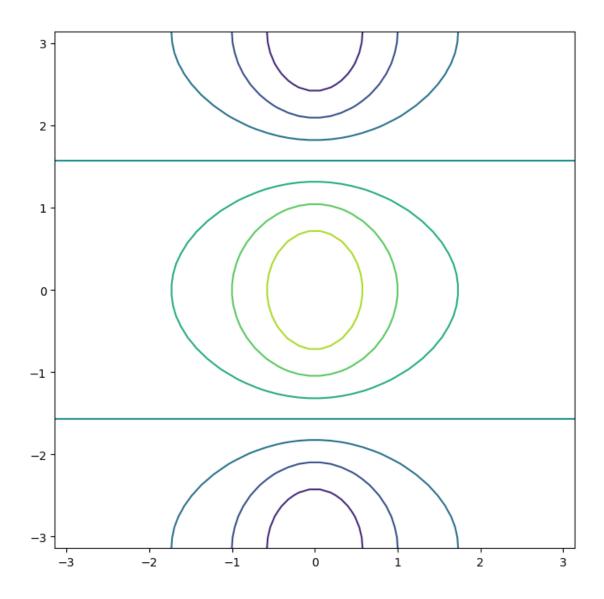
```
[51]: axes[0, 1].plot(x, y, "o")
        axes[1, 2].scatter(x, y, marker="+")
        fig
[51]:
              1.0
              0.8
                                                                                    0.8
              0.6
              0.4
                                                                                     0.4
              0.2
                                                                                     0.2
             0.0
                      0.2
                           0.4
                                 0.6
                                       0.8
                                                                                             0.2
                                                                                                        0.6
                                                                                                              0.8
                                                                                                                    1.0
                                             1.0
              1.0
                                                 1.0
              0.8
                                                 0.6
              0.6
              0.4
                                                                                     -1
              0.2
                                                 0.2
             0.0
                                                 0.0 +
```

```
[52]: fig.savefig("Figure.png", dpi=400)
    fig.savefig("Figure.pdf", dpi=200)

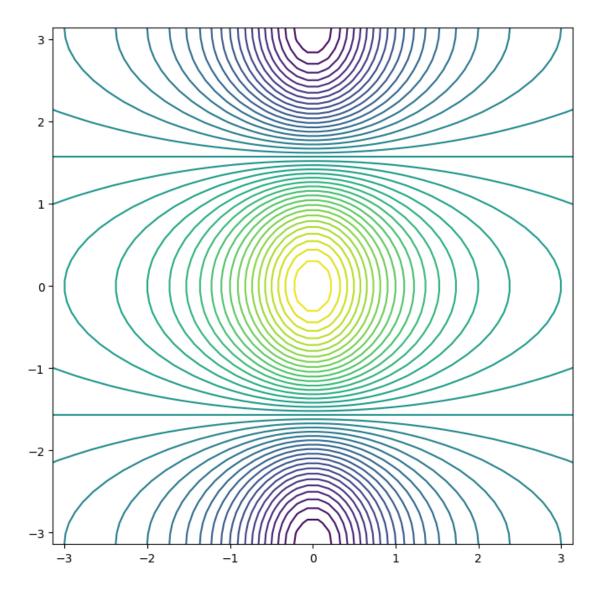
[53]: axes[0, 1].set_xlim([-1, 1])
    fig.savefig("Figure_updated.jpg")
    fig
```



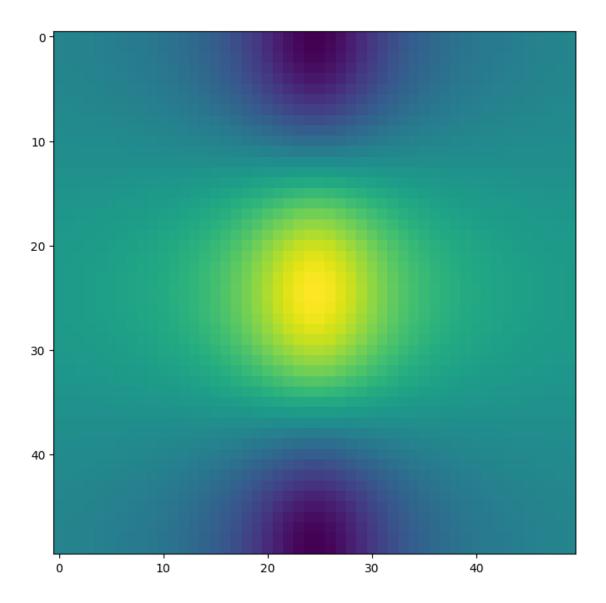
```
[54]: fig, ax = subplots(figsize=(8, 8))
      x = np.linspace(-np.pi, np.pi, 50)
      print(x)
      y = x
      f = np.multiply.outer(np.cos(y), 1 / (1 + x**2))
      ax.contour(x, y, f);
     [-3.14159265 -3.01336438 -2.88513611 -2.75690784 -2.62867957 -2.5004513
      -2.37222302 -2.24399475 -2.11576648 -1.98753821 -1.85930994 -1.73108167
      -1.60285339 -1.47462512 -1.34639685 -1.21816858 -1.08994031 -0.96171204
      -0.83348377 \ -0.70525549 \ -0.57702722 \ -0.44879895 \ -0.32057068 \ -0.19234241
      -0.06411414 0.06411414 0.19234241 0.32057068 0.44879895 0.57702722
       0.70525549  0.83348377  0.96171204  1.08994031  1.21816858  1.34639685
       1.47462512 1.60285339 1.73108167 1.85930994 1.98753821 2.11576648
       2.24399475 2.37222302 2.5004513
                                           2.62867957 2.75690784 2.88513611
       3.01336438 3.14159265]
```



```
[55]: fig, ax = subplots(figsize=(8, 8))
ax.contour(x, y, f, levels=45);
```



Executing <handle BaseAsyncIOLoop._handle_events(28, 1) created at /usr/lib/python3.12/asyncio/selector_events.py:280> took 0.169 seconds Executing <handle IOLoop._run_callback(functools.par...7eba43ea1d00>)) created at /home/linus/ISLP/islpenv/lib/python3.12/site-packages/tornado/platform/asyncio.py:235> took 0.170 seconds



```
[57]: seq1 = np.linspace(0, 10, 11)
    seq1

[57]: array([ 0.,  1.,  2.,  3.,  4.,  5.,  6.,  7.,  8.,  9., 10.])

[58]: seq2 = np.arange(0, 10)
    seq2

[58]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])

[59]: "Hello, world!"[3:6]
```

```
[60]: "Hello, world!"[slice(3, 6)]
[60]: 'lo,'
[61]: A = np.array(np.arange(16)).reshape((4, 4))
      print(A)
     A[1, 2]
     [[ 0 1 2 3]
      [4 5 6 7]
      [8 9 10 11]
      [12 13 14 15]]
[61]: 6
[62]: A[[1, 3]]
[62]: array([[ 4, 5, 6, 7],
             [12, 13, 14, 15]])
[63]: A[:, [0, 2]]
[63]: array([[ 0, 2],
             [4, 6],
             [8, 10],
             [12, 14]])
[64]: A[[1, 3], [0, 2]]
[64]: array([4, 14])
[65]: np.array([A[1, 0], A[3, 2]])
[65]: array([4, 14])
[66]: A[[1, 3]][:, [0, 2]]
[66]: array([[4, 6],
             [12, 14]])
[67]: idx = np.ix_([1, 3], [0, 2, 3])
      A[idx]
[67]: array([[ 4, 6, 7],
            [12, 14, 15]])
[68]: A[1:4:2, 0:3:2]
```

```
[68]: array([[ 4, 6],
             [12, 14]])
[69]: keep_rows = np.zeros(A.shape[0], bool)
      keep_rows
[69]: array([False, False, False, False])
[70]: keep_rows[[1, 3]] = True
      keep_rows
[70]: array([False, True, False, True])
[71]: np.all(keep_rows == np.array([0, 1, 0, 1]))
[71]: True
[72]: A[np.array([0, 1, 0, 1])]
[72]: array([[0, 1, 2, 3],
             [4, 5, 6, 7],
             [0, 1, 2, 3],
             [4, 5, 6, 7]])
[73]: A[keep_rows]
[73]: array([[ 4, 5, 6, 7],
             [12, 13, 14, 15]])
[74]: keep_cols = np.zeros(A.shape[1], bool)
      keep_cols
[74]: array([False, False, False, False])
[75]: keep_cols[[0, 2, 3]] = True
      keep_cols
[75]: array([ True, False, True, True])
[76]: idx_bool = np.ix_(keep_rows, keep_cols)
      idx_bool
[76]: (array([[1],
              [3]]),
       array([[0, 2, 3]]))
[77]: A[idx_bool]
```

```
[77]: array([[ 4, 6, 7],
             [12, 14, 15]])
[78]: idx_mixed = np.ix_([1, 3], keep_cols)
      idx_mixed
[78]: (array([[1],
               [3]]),
       array([[0, 2, 3]]))
[79]: A[idx_mixed]
[79]: array([[ 4, 6, 7],
              [12, 14, 15]])
     1.1 Reading in a data set
[80]: import pandas as pd
      Auto = pd.read_csv("Auto.csv")
      Auto
[80]:
            mpg
                 cylinders
                             displacement horsepower weight acceleration year
      0
           18.0
                          8
                                     307.0
                                                   130
                                                          3504
                                                                         12.0
                                                                                 70
      1
           15.0
                          8
                                     350.0
                                                   165
                                                          3693
                                                                         11.5
                                                                                 70
      2
                          8
           18.0
                                                                         11.0
                                                                                 70
                                     318.0
                                                   150
                                                          3436
      3
           16.0
                          8
                                     304.0
                                                   150
                                                          3433
                                                                         12.0
                                                                                 70
      4
           17.0
                          8
                                                                         10.5
                                     302.0
                                                   140
                                                          3449
                                                                                 70
      . .
      392 27.0
                          4
                                     140.0
                                                          2790
                                                                         15.6
                                                                                 82
                                                   86
      393 44.0
                          4
                                                                         24.6
                                      97.0
                                                    52
                                                          2130
                                                                                 82
      394 32.0
                          4
                                     135.0
                                                    84
                                                          2295
                                                                         11.6
                                                                                 82
      395 28.0
                          4
                                     120.0
                                                    79
                                                          2625
                                                                         18.6
                                                                                 82
      396 31.0
                                     119.0
                                                                         19.4
                                                    82
                                                          2720
                                                                                 82
           origin
                                          name
      0
                1
                    chevrolet chevelle malibu
      1
                1
                            buick skylark 320
      2
                1
                           plymouth satellite
      3
                1
                                amc rebel sst
      4
                 1
                                   ford torino
      392
                1
                              ford mustang gl
      393
                 2
                                     vw pickup
      394
                1
                                dodge rampage
      395
                                  ford ranger
                 1
      396
                 1
                                    chevy s-10
```

[397 rows x 9 columns]

```
[81]: Auto = pd.read_csv("Auto.data", sep="\s+")
      Auto
     <>:1: SyntaxWarning: invalid escape sequence '\s'
     <>:1: SyntaxWarning: invalid escape sequence '\s'
     /tmp/ipykernel_14647/4041205627.py:1: SyntaxWarning: invalid escape sequence
     '\s'
       Auto = pd.read_csv("Auto.data", sep="\s+")
[81]:
                 cylinders
                             displacement horsepower
                                                       weight
                                                                acceleration
                                                                               year
            mpg
      0
           18.0
                          8
                                     307.0
                                                130.0
                                                       3504.0
                                                                         12.0
                                                                                 70
                          8
      1
           15.0
                                     350.0
                                                165.0
                                                       3693.0
                                                                         11.5
                                                                                 70
      2
           18.0
                          8
                                                       3436.0
                                                                         11.0
                                     318.0
                                                150.0
                                                                                 70
      3
           16.0
                          8
                                     304.0
                                                150.0
                                                       3433.0
                                                                         12.0
                                                                                 70
      4
           17.0
                          8
                                     302.0
                                                 140.0
                                                       3449.0
                                                                         10.5
                                                                                 70
                                                86.00
      392 27.0
                                     140.0
                                                        2790.0
                                                                         15.6
                                                                                 82
                          4
                                                                         24.6
      393 44.0
                          4
                                      97.0
                                                52.00
                                                       2130.0
                                                                                 82
      394 32.0
                          4
                                     135.0
                                                84.00
                                                        2295.0
                                                                         11.6
                                                                                 82
      395
          28.0
                          4
                                                                         18.6
                                     120.0
                                                79.00
                                                        2625.0
                                                                                 82
      396 31.0
                                     119.0
                                                82.00 2720.0
                                                                         19.4
                                                                                 82
           origin
                                          name
      0
                1
                    chevrolet chevelle malibu
      1
                 1
                            buick skylark 320
      2
                1
                           plymouth satellite
      3
                 1
                                amc rebel sst
      4
                 1
                                   ford torino
      . .
      392
                1
                              ford mustang gl
      393
                 2
                                     vw pickup
      394
                 1
                                dodge rampage
      395
                 1
                                   ford ranger
      396
                 1
                                    chevy s-10
      [397 rows x 9 columns]
[82]:
     Auto["horsepower"]
[82]: 0
             130.0
             165.0
      1
      2
             150.0
      3
             150.0
             140.0
      4
```

```
392
             86.00
      393
             52.00
      394
             84.00
      395
             79.00
      396
             82.00
      Name: horsepower, Length: 397, dtype: object
[83]: np.unique(Auto["horsepower"])
[83]: array(['100.0', '102.0', '103.0', '105.0', '107.0', '108.0', '110.0',
             '112.0', '113.0', '115.0', '116.0', '120.0', '122.0', '125.0',
             '129.0', '130.0', '132.0', '133.0', '135.0', '137.0', '138.0',
             '139.0', '140.0', '142.0', '145.0', '148.0', '149.0', '150.0',
             '152.0', '153.0', '155.0', '158.0', '160.0', '165.0', '167.0',
             '170.0', '175.0', '180.0', '190.0', '193.0', '198.0', '200.0',
             '208.0', '210.0', '215.0', '220.0', '225.0', '230.0', '46.00',
             '48.00', '49.00', '52.00', '53.00', '54.00', '58.00', '60.00',
             '61.00', '62.00', '63.00', '64.00', '65.00', '66.00', '67.00',
             '68.00', '69.00', '70.00', '71.00', '72.00', '74.00', '75.00',
             '76.00', '77.00', '78.00', '79.00', '80.00', '81.00', '82.00',
             '83.00', '84.00', '85.00', '86.00', '87.00', '88.00', '89.00',
             '90.00', '91.00', '92.00', '93.00', '94.00', '95.00', '96.00',
             '97.00', '98.00', '?'], dtype=object)
[84]: Auto = pd.read csv("Auto.data", na values=["?"], sep="\s+")
      Auto["horsepower"].sum()
     <>:1: SyntaxWarning: invalid escape sequence '\s'
     <>:1: SyntaxWarning: invalid escape sequence '\s'
     /tmp/ipykernel_14647/3247743814.py:1: SyntaxWarning: invalid escape sequence
       Auto = pd.read_csv("Auto.data", na_values=["?"], sep="\s+")
[84]: 40952.0
[85]: Auto.shape
[85]: (397, 9)
      Auto_new = Auto.dropna()
[86]:
           mpg
                 cylinders
                            displacement horsepower weight
                                                               acceleration
                                                                             year \
      0
           18.0
                         8
                                   307.0
                                                130.0
                                                       3504.0
                                                                       12.0
                                                                                70
                         8
      1
           15.0
                                   350.0
                                                165.0
                                                       3693.0
                                                                       11.5
                                                                                70
      2
                         8
                                                       3436.0
                                                                       11.0
           18.0
                                   318.0
                                                150.0
                                                                                70
      3
           16.0
                         8
                                   304.0
                                                150.0 3433.0
                                                                       12.0
                                                                               70
      4
           17.0
                         8
                                                140.0
                                                       3449.0
                                                                       10.5
                                                                                70
                                   302.0
      . .
```

```
393 44.0
                         4
                                     97.0
                                                 52.0 2130.0
                                                                        24.6
                                                                                82
      394 32.0
                         4
                                    135.0
                                                 84.0 2295.0
                                                                        11.6
                                                                                82
      395 28.0
                         4
                                    120.0
                                                 79.0 2625.0
                                                                        18.6
                                                                                82
      396 31.0
                         4
                                    119.0
                                                 82.0 2720.0
                                                                        19.4
                                                                                82
           origin
                                         name
      0
                   chevrolet chevelle malibu
                1
                1
                           buick skylark 320
      1
      2
                1
                          plymouth satellite
                                amc rebel sst
      3
                1
      4
                1
                                  ford torino
      . .
      392
                1
                             ford mustang gl
      393
                2
                                    vw pickup
      394
                               dodge rampage
                1
      395
                1
                                  ford ranger
      396
                1
                                   chevy s-10
      [392 rows x 9 columns]
[87]: Auto new.shape
[87]: (392, 9)
[88]: Auto = Auto_new
      Auto.columns
[88]: Index(['mpg', 'cylinders', 'displacement', 'horsepower', 'weight',
             'acceleration', 'year', 'origin', 'name'],
            dtype='object')
[89]: Auto[:3]
[89]:
          {	t mpg} cylinders displacement horsepower weight acceleration year \
      0 18.0
                                  307.0
                                              130.0 3504.0
                                                                      12.0
                                                                              70
                       8
      1 15.0
                       8
                                  350.0
                                              165.0 3693.0
                                                                      11.5
                                                                              70
      2 18.0
                                                                      11.0
                       8
                                  318.0
                                              150.0 3436.0
                                                                              70
         origin
                                       name
      0
              1 chevrolet chevelle malibu
              1
                         buick skylark 320
      1
      2
              1
                        plymouth satellite
[90]: idx_80 = Auto["year"] > 80
      Auto[idx_80]
```

140.0

4

86.0 2790.0

15.6

82

392 27.0

[90]:		mpg	cylinders	displacement	horsepower	weight	acceleration	year	\
	338	27.2	4	135.0	84.0	2490.0	15.7	81	
	339	26.6	4	151.0	84.0	2635.0	16.4	81	
	340	25.8	4	156.0	92.0	2620.0	14.4	81	
	341	23.5	6	173.0	110.0	2725.0	12.6	81	
	342	30.0	4	135.0	84.0	2385.0	12.9	81	
	343	39.1	4	79.0	58.0	1755.0	16.9	81	
	344	39.0	4	86.0	64.0	1875.0	16.4	81	
	345	35.1	4	81.0	60.0	1760.0	16.1	81	
	346	32.3	4	97.0	67.0	2065.0	17.8	81	
	347	37.0	4	85.0	65.0	1975.0	19.4	81	
	348	37.7	4	89.0	62.0	2050.0	17.3	81	
	349	34.1	4	91.0	68.0	1985.0	16.0	81	
	350	34.7	4	105.0	63.0	2215.0	14.9	81	
	351	34.4	4	98.0	65.0	2045.0	16.2	81	
	352	29.9	4	98.0	65.0	2380.0	20.7	81	
	353	33.0	4	105.0	74.0	2190.0	14.2	81	
	355	33.7	4	107.0	75.0	2210.0	14.4	81	
	356	32.4	4	108.0	75.0	2350.0	16.8	81	
	357	32.9	4	119.0	100.0	2615.0	14.8	81	
	358	31.6	4	120.0	74.0	2635.0	18.3	81	
	359	28.1	4	141.0	80.0	3230.0	20.4	81	
	360	30.7	6	145.0	76.0	3160.0	19.6	81	
	361	25.4	6	168.0	116.0	2900.0	12.6	81	
	362	24.2	6	146.0	120.0	2930.0	13.8	81	
	363	22.4	6	231.0	110.0	3415.0	15.8	81	
	364	26.6	8	350.0	105.0	3725.0	19.0	81	
	365	20.2	6	200.0	88.0	3060.0	17.1	81	
	366	17.6	6	225.0	85.0	3465.0	16.6	81	
	367	28.0	4	112.0	88.0	2605.0	19.6	82	
	368	27.0	4	112.0	88.0	2640.0	18.6	82	
	369	34.0	4	112.0	88.0	2395.0	18.0	82	
	370	31.0	4	112.0	85.0	2575.0	16.2	82	
	371	29.0	4	135.0	84.0	2525.0	16.0	82	
	372	27.0	4	151.0	90.0	2735.0	18.0	82	
	373	24.0	4	140.0	92.0	2865.0	16.4	82	
	374	36.0	4	105.0	74.0	1980.0	15.3	82	
	375	37.0	4	91.0	68.0	2025.0	18.2	82	
	376	31.0	4	91.0	68.0	1970.0	17.6	82	
	377	38.0	4	105.0	63.0	2125.0	14.7	82	
	378	36.0	4	98.0	70.0	2125.0	17.3	82	
	379	36.0	4	120.0	88.0	2160.0	14.5	82	
	380	36.0	4	107.0	75.0	2205.0	14.5	82	
	381	34.0	4	108.0	70.0	2245.0	16.9	82	
	382	38.0	4	91.0	67.0	1965.0	15.0	82	
	383	32.0	4	91.0	67.0	1965.0	15.7	82	
	384	38.0	4	91.0	67.0	1995.0	16.2	82	

385	25.0	6	181.0	110.0	2945.0
386	38.0	6	262.0	85.0	3015.0
387	26.0	4	156.0	92.0	2585.0
388	22.0	6	232.0		2835.0
389	32.0	4	144.0	96.0	2665.0
390	36.0	4	135.0	84.0	2370.0
391	27.0	4	151.0	90.0	2950.0
392	27.0	4	140.0	86.0	2790.0
393	44.0	4	97.0	52.0	2130.0
394	32.0	4	135.0	84.0	2295.0
395	28.0	4	120.0		2625.0
396	31.0	4	119.0	82.0	2720.0
	origin			name	
338	1		plymouth	reliant	
339	1		buick	skylark	
340	1		dodge aries wa	ngon (sw)	
341	1		chevrolet	_	
	1				
342				reliant	
343	3		•	starlet	
344	1		plymou	th champ	
345	3		honda ci	vic 1300	
346	3			subaru	
347	3		datsur	210 mpg	
348	3			a tercel	
349	3			da glc 4	
350	1		plymouth h		
351	1		ford e	escort 4w	
352	1		ford e	scort 2h	
353	2		volkswag	gen jetta	
355	3		-	prelude	
356	3			corolla	
	3		•		
357				sun 200sx	
358	3			nazda 626	
359	2	J	peugeot 505s turb	oo diesel	
360	2		volv	o diesel	
361	3		toyota	cressida	
362	3		datsun 81	0 maxima	
363	1			century	
	1			•	
364	_		oldsmobile cu		
365	1		_	ranada gl	
366	1		chrysler lebar	on salon	
367	1		chevrolet	cavalier	
368	1		chevrolet cavali	er wagon	
369	1		chevrolet cavalie	_	
370	1		ontiac j2000 se h		
371	1	P.	•		
3/1	1		doage	aries se	

16.4

17.0

14.5

14.7

13.9

13.0

17.3

15.6

24.6

11.6

18.6

19.4

82

82

82

82

82

82

82

82

82

82

82 82

```
372
          1
                                 pontiac phoenix
373
          1
                           ford fairmont futura
374
           2
                            volkswagen rabbit l
375
          3
                              mazda glc custom 1
376
          3
                                mazda glc custom
377
                         plymouth horizon miser
          1
378
          1
                                  mercury lynx 1
          3
                                nissan stanza xe
379
          3
380
                                    honda accord
381
          3
                                  toyota corolla
           3
382
                                     honda civic
383
          3
                              honda civic (auto)
384
          3
                                   datsun 310 gx
385
                           buick century limited
          1
386
          1
              oldsmobile cutlass ciera (diesel)
387
           1
                     chrysler lebaron medallion
388
           1
                                  ford granada 1
389
           3
                                toyota celica gt
390
           1
                               dodge charger 2.2
391
           1
                                chevrolet camaro
392
          1
                                 ford mustang gl
          2
393
                                       vw pickup
394
          1
                                   dodge rampage
395
                                     ford ranger
          1
396
           1
                                      chevy s-10
```

[91]: Auto[["mpg", "horsepower"]]

```
[91]:
                  horsepower
            mpg
      0
            18.0
                        130.0
      1
            15.0
                        165.0
      2
            18.0
                        150.0
      3
            16.0
                        150.0
      4
            17.0
                        140.0
      . .
      392
           27.0
                         86.0
      393
           44.0
                         52.0
      394
           32.0
                         84.0
      395
           28.0
                         79.0
      396
           31.0
                         82.0
```

[392 rows x 2 columns]

```
[92]: Auto.index
```

[92]: Index([0, 2, 3, 4, 5, 6, 7, 8, 9,

```
387, 388, 389, 390, 391, 392, 393, 394, 395, 396],
            dtype='int64', length=392)
[93]: Auto_re = Auto.set_index("name")
      Auto re
[93]:
                                        cylinders
                                                   displacement horsepower
                                                                              weight \
                                   mpg
      name
                                                          307.0
      chevrolet chevelle malibu 18.0
                                                8
                                                                       130.0
                                                                              3504.0
      buick skylark 320
                                  15.0
                                                8
                                                          350.0
                                                                              3693.0
                                                                       165.0
      plymouth satellite
                                  18.0
                                                8
                                                          318.0
                                                                       150.0
                                                                              3436.0
      amc rebel sst
                                  16.0
                                                8
                                                          304.0
                                                                       150.0
                                                                              3433.0
      ford torino
                                  17.0
                                                8
                                                          302.0
                                                                       140.0 3449.0
                                                                        86.0 2790.0
      ford mustang gl
                                  27.0
                                                4
                                                          140.0
      vw pickup
                                                4
                                                           97.0
                                                                        52.0 2130.0
                                  44.0
      dodge rampage
                                  32.0
                                                4
                                                          135.0
                                                                        84.0 2295.0
      ford ranger
                                  28.0
                                                4
                                                          120.0
                                                                        79.0 2625.0
      chevy s-10
                                  31.0
                                                4
                                                          119.0
                                                                        82.0 2720.0
                                  acceleration year origin
     name
      chevrolet chevelle malibu
                                          12.0
                                                  70
                                                            1
      buick skylark 320
                                          11.5
                                                  70
                                                            1
      plymouth satellite
                                          11.0
                                                  70
                                                            1
      amc rebel sst
                                          12.0
                                                  70
                                                            1
      ford torino
                                          10.5
                                                  70
                                                            1
      ford mustang gl
                                          15.6
                                                  82
                                                            1
      vw pickup
                                          24.6
                                                  82
                                                            2
      dodge rampage
                                          11.6
                                                  82
                                                            1
      ford ranger
                                          18.6
                                                  82
                                                            1
      chevy s-10
                                          19.4
                                                  82
                                                            1
      [392 rows x 8 columns]
[94]: Auto_re.columns
[94]: Index(['mpg', 'cylinders', 'displacement', 'horsepower', 'weight',
             'acceleration', 'year', 'origin'],
            dtype='object')
```

```
[96]: rows = ["amc rebel sst", "ford torino"]
Auto_re.loc[rows]
```

[95]: Auto_re.shape

[95]: (392, 8)

```
[96]:
                            cylinders displacement horsepower weight \
                       mpg
      name
       amc rebel sst
                      16.0
                                     8
                                               304.0
                                                            150.0
                                                                   3433.0
       ford torino
                      17.0
                                     8
                                               302.0
                                                            140.0 3449.0
                      acceleration year origin
       name
       amc rebel sst
                               12.0
                                       70
                                                1
       ford torino
                               10.5
                                       70
                                                1
[97]: Auto_re.iloc[[3, 4]]
[97]:
                             cylinders displacement horsepower
                       mpg
       amc rebel sst
                      16.0
                                     8
                                               304.0
                                                            150.0
                                                                   3433.0
       ford torino
                      17.0
                                     8
                                               302.0
                                                            140.0
                                                                   3449.0
                      acceleration year
                                           origin
       name
       amc rebel sst
                               12.0
                                       70
                                                1
       ford torino
                               10.5
                                       70
                                                1
      Auto_re.iloc[:, [0, 2, 3]]
[98]:
[98]:
                                    mpg displacement horsepower
      name
       chevrolet chevelle malibu 18.0
                                                307.0
                                                             130.0
       buick skylark 320
                                   15.0
                                                350.0
                                                             165.0
       plymouth satellite
                                   18.0
                                                318.0
                                                             150.0
       amc rebel sst
                                   16.0
                                                304.0
                                                             150.0
       ford torino
                                                302.0
                                                             140.0
                                   17.0
                                                              86.0
       ford mustang gl
                                   27.0
                                                140.0
                                                 97.0
                                                              52.0
       vw pickup
                                   44.0
       dodge rampage
                                   32.0
                                                135.0
                                                              84.0
       ford ranger
                                   28.0
                                                120.0
                                                              79.0
       chevy s-10
                                   31.0
                                                119.0
                                                              82.0
       [392 rows x 3 columns]
[99]: Auto_re.iloc[[3, 4], [0, 2, 3]]
[99]:
                       mpg
                            displacement horsepower
       name
       amc rebel sst 16.0
                                    304.0
                                                150.0
                      17.0
                                    302.0
       ford torino
                                                140.0
[100]: Auto_re.loc["ford galaxie 500", ["mpg", "origin"]]
```

Γ100]: mpg origin name ford galaxie 500 15.0 1 ford galaxie 500 14.0 1 ford galaxie 500 14.0 1 [101]: | idx_80 = Auto_re["year"] > 80 Auto_re.loc[idx_80] [101]: cylinders displacement horsepower \ mpg name27.2 plymouth reliant 4 135.0 84.0 buick skylark 26.6 4 151.0 84.0 4 dodge aries wagon (sw) 25.8 156.0 92.0 chevrolet citation 23.5 6 173.0 110.0 plymouth reliant 4 135.0 30.0 84.0 4 toyota starlet 39.1 79.0 58.0 plymouth champ 39.0 4 86.0 64.0 honda civic 1300 35.1 4 81.0 60.0 4 subaru 32.3 97.0 67.0 datsun 210 mpg 37.0 4 85.0 65.0 toyota tercel 37.7 4 89.0 62.0 mazda glc 4 34.1 4 91.0 68.0 4 plymouth horizon 4 34.7 105.0 63.0 ford escort 4w 34.4 4 98.0 65.0 ford escort 2h 29.9 4 98.0 65.0 4 volkswagen jetta 74.0 33.0 105.0 4 honda prelude 33.7 107.0 75.0 4 toyota corolla 32.4 108.0 75.0 4 datsun 200sx 32.9 119.0 100.0 mazda 626 31.6 4 120.0 74.0 4 peugeot 505s turbo diesel 28.1 141.0 80.0 30.7 6 145.0 76.0 volvo diesel 6 toyota cressida 25.4 168.0 116.0 6 datsun 810 maxima 24.2 146.0 120.0 22.4 6 buick century 231.0 110.0 oldsmobile cutlass ls 26.6 8 350.0 105.0 ford granada gl 20.2 6 200.0 88.0

chrysler lebaron salon

chevrolet cavalier wagon

chevrolet cavalier 2-door

pontiac j2000 se hatchback

chevrolet cavalier

dodge aries se

pontiac phoenix

ford fairmont futura

volkswagen rabbit l

17.6

28.0

27.0

34.0

31.0

29.0

27.0

24.0

36.0

6

4

4

4

4

4

4

4

225.0

112.0

112.0

112.0

112.0

135.0

151.0

140.0

105.0

85.0

88.0

88.0

88.0

85.0

84.0

90.0

92.0

74.0

	27.0	4	0.1	^	CO 0
mazda glc custom l	37.0	4	91.		68.0
mazda glc custom	31.0	4	91.		68.0
plymouth horizon miser	38.0	4 4	105. 98.		63.0 70.0
mercury lynx l nissan stanza xe	36.0 36.0	4			88.0
			120.		
honda accord	36.0	4	107.		75.0
toyota corolla	34.0	4	108.		70.0
honda civic	38.0	4	91.		67.0
honda civic (auto)	32.0	4	91.		67.0
datsun 310 gx	38.0	4	91.		67.0
buick century limited	25.0	6	181.		110.0
oldsmobile cutlass ciera (diesel)	38.0	6	262.		85.0
chrysler lebaron medallion	26.0	4	156.		92.0
ford granada l	22.0	6	232.		112.0
toyota celica gt	32.0	4	144.		96.0
dodge charger 2.2	36.0	4	135.		84.0
chevrolet camaro	27.0	4	151.		90.0
ford mustang gl	27.0	4	140.		86.0
vw pickup	44.0	4	97.		52.0
dodge rampage	32.0	4	135.		84.0
ford ranger	28.0	4	120.		79.0
chevy s-10	31.0	4	119.	0	82.0
	weight	acceleration	year	origin	
			•	_	
name	0400 0	45.7	04	4	
plymouth reliant	2490.0	15.7	81	1	
plymouth reliant buick skylark	2635.0	16.4	81	1	
plymouth reliant buick skylark dodge aries wagon (sw)	2635.0 2620.0	16.4 14.4	81 81	1 1	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation	2635.0 2620.0 2725.0	16.4 14.4 12.6	81 81 81	1 1 1	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant	2635.0 2620.0 2725.0 2385.0	16.4 14.4 12.6 12.9	81 81 81 81	1 1 1 1	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet	2635.0 2620.0 2725.0 2385.0 1755.0	16.4 14.4 12.6 12.9 16.9	81 81 81 81	1 1 1 1 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0	16.4 14.4 12.6 12.9 16.9	81 81 81 81 81	1 1 1 1 3 1	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0	16.4 14.4 12.6 12.9 16.9 16.4	81 81 81 81 81 81	1 1 1 1 3 1 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1	81 81 81 81 81 81 81	1 1 1 3 1 3 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0 1975.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8	81 81 81 81 81 81 81	1 1 1 3 1 3 3 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0 1975.0 2050.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4	81 81 81 81 81 81 81 81	1 1 1 3 1 3 3 3 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0 1975.0 2050.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3	81 81 81 81 81 81 81 81 81	1 1 1 3 1 3 3 3 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0 1975.0 2050.0 1985.0 2215.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9	81 81 81 81 81 81 81 81 81 81	1 1 1 3 1 3 3 3 3 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4 ford escort 4w	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 2065.0 1975.0 2050.0 1985.0 2215.0 2045.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9	81 81 81 81 81 81 81 81 81 81	1 1 1 3 1 3 3 3 3 1 1	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4 ford escort 4w ford escort 2h	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 2065.0 1975.0 2050.0 1985.0 2215.0 2045.0 2380.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9 16.2 20.7	81 81 81 81 81 81 81 81 81 81 81	1 1 1 3 1 3 3 3 3 1 1 1	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4 ford escort 4w ford escort 2h volkswagen jetta	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0 1975.0 2050.0 1985.0 2215.0 2045.0 2380.0 2190.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9 16.2 20.7	81 81 81 81 81 81 81 81 81 81 81 81	1 1 1 3 1 3 3 3 3 1 1 1 1 2	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4 ford escort 4w ford escort 2h volkswagen jetta honda prelude	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 2065.0 1975.0 2050.0 1985.0 2215.0 2045.0 2380.0 2190.0 2210.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9 16.2 20.7 14.2	81 81 81 81 81 81 81 81 81 81 81 81	1 1 1 3 1 3 3 3 3 1 1 1 1 2 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4 ford escort 4w ford escort 2h volkswagen jetta honda prelude toyota corolla	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 2065.0 1975.0 2050.0 1985.0 2215.0 2380.0 2190.0 2350.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9 16.2 20.7 14.2 14.4	81 81 81 81 81 81 81 81 81 81 81 81 81	1 1 1 3 1 3 3 3 3 1 1 1 1 2 3 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4 ford escort 4w ford escort 2h volkswagen jetta honda prelude toyota corolla datsun 200sx	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0 1975.0 2050.0 1985.0 2215.0 2380.0 2190.0 2210.0 2350.0 2615.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9 16.2 20.7 14.2 14.4 16.8	81 81 81 81 81 81 81 81 81 81 81 81 81 8	1 1 1 3 1 3 3 3 3 1 1 1 2 3 3 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4 ford escort 4w ford escort 2h volkswagen jetta honda prelude toyota corolla datsun 200sx mazda 626	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0 1975.0 2050.0 1985.0 2215.0 2380.0 2190.0 2210.0 2350.0 2615.0 2635.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9 16.2 20.7 14.2 14.4 16.8 14.8	81 81 81 81 81 81 81 81 81 81 81 81 81 8	1 1 1 3 1 3 3 3 3 1 1 1 2 3 3 3 3	
plymouth reliant buick skylark dodge aries wagon (sw) chevrolet citation plymouth reliant toyota starlet plymouth champ honda civic 1300 subaru datsun 210 mpg toyota tercel mazda glc 4 plymouth horizon 4 ford escort 4w ford escort 2h volkswagen jetta honda prelude toyota corolla datsun 200sx	2635.0 2620.0 2725.0 2385.0 1755.0 1875.0 1760.0 2065.0 1975.0 2050.0 1985.0 2215.0 2380.0 2190.0 2210.0 2350.0 2615.0	16.4 14.4 12.6 12.9 16.9 16.4 16.1 17.8 19.4 17.3 16.0 14.9 16.2 20.7 14.2 14.4 16.8	81 81 81 81 81 81 81 81 81 81 81 81 81 8	1 1 1 3 1 3 3 3 3 1 1 1 2 3 3 3	

2900.0	12.6	81	3
2930.0	13.8	81	3
3415.0	15.8	81	1
3725.0	19.0	81	1
3060.0	17.1	81	1
3465.0	16.6	81	1
2605.0	19.6	82	1
2640.0	18.6	82	1
2395.0	18.0	82	1
2575.0	16.2	82	1
2525.0	16.0	82	1
2735.0	18.0	82	1
2865.0	16.4	82	1
1980.0	15.3	82	2
2025.0	18.2	82	3
1970.0	17.6	82	3
2125.0	14.7	82	1
2125.0	17.3	82	1
2160.0	14.5	82	3
2205.0	14.5	82	3
2245.0	16.9	82	3
1965.0	15.0	82	3
1965.0	15.7	82	3
1995.0	16.2	82	3
2945.0	16.4	82	1
3015.0	17.0	82	1
2585.0	14.5	82	1
2835.0	14.7	82	1
2665.0	13.9	82	3
2370.0	13.0	82	1
2950.0	17.3	82	1
2790.0	15.6	82	1
2130.0	24.6	82	2
2295.0	11.6	82	1
2625.0	18.6	82	1
2720.0	19.4	82	1
	2930.0 3415.0 3725.0 3060.0 3465.0 2605.0 2640.0 2395.0 2575.0 2525.0 2735.0 2865.0 1980.0 2025.0 1970.0 2125.0 2125.0 2160.0 2205.0 1965.0 1995.0 1995.0 2945.0 3015.0 2585.0 2835.0 2665.0 2370.0 2950.0 2130.0 2295.0	2930.0 13.8 3415.0 15.8 3725.0 19.0 3060.0 17.1 3465.0 16.6 2605.0 19.6 2640.0 18.6 2395.0 18.0 2575.0 16.2 2525.0 16.0 2735.0 18.0 2865.0 16.4 1980.0 15.3 2025.0 18.2 1970.0 17.6 2125.0 14.7 2125.0 17.3 2160.0 14.5 2245.0 16.9 1965.0 15.7 1995.0 16.2 2945.0 16.4 3015.0 17.0 2585.0 14.5 2835.0 14.7 2665.0 13.9 2370.0 13.0 2950.0 17.3 2790.0 15.6 2130.0 24.6 2295.0 11.6 2625.0 18.6	2930.0 13.8 81 3415.0 15.8 81 3725.0 19.0 81 3060.0 17.1 81 3465.0 16.6 81 2605.0 19.6 82 2640.0 18.6 82 2395.0 18.0 82 2575.0 16.2 82 2525.0 16.0 82 2735.0 18.0 82 2865.0 16.4 82 1980.0 15.3 82 2025.0 18.2 82 1970.0 17.6 82 2125.0 14.7 82 2125.0 17.3 82 2125.0 14.7 82 2245.0 16.9 82 1965.0 15.0 82 1965.0 15.7 82 1995.0 16.2 82 2945.0 16.4 82 2945.0 16.4 82 2855.0 14.7 82 2855.0 14.7 <t< td=""></t<>

[102]: Auto_re.loc[idx_80, ["weight", "origin"]]

[102]:		weight	origin
	name		
	plymouth reliant	2490.0	1
	buick skylark	2635.0	1
	dodge aries wagon (sw)	2620.0	1
	chevrolet citation	2725.0	1
	plymouth reliant	2385.0	1
	toyota starlet	1755.0	3

plymouth champ	1875.0	1
honda civic 1300	1760.0	3
subaru	2065.0	3
datsun 210 mpg	1975.0	3
toyota tercel	2050.0	3
•	1985.0	3
mazda glc 4		
plymouth horizon 4	2215.0	1
ford escort 4w	2045.0	1
ford escort 2h	2380.0	1
volkswagen jetta	2190.0	2
honda prelude	2210.0	3
toyota corolla	2350.0	3
datsun 200sx	2615.0	3
mazda 626	2635.0	3
peugeot 505s turbo diesel	3230.0	2
volvo diesel	3160.0	2
toyota cressida	2900.0	3
datsun 810 maxima	2930.0	3
	3415.0	1
buick century		_
oldsmobile cutlass ls	3725.0	1
ford granada gl	3060.0	1
chrysler lebaron salon	3465.0	1
chevrolet cavalier	2605.0	1
chevrolet cavalier wagon	2640.0	1
chevrolet cavalier 2-door	2395.0	1
pontiac j2000 se hatchback	2575.0	1
dodge aries se	2525.0	1
pontiac phoenix	2735.0	1
ford fairmont futura	2865.0	1
volkswagen rabbit l	1980.0	2
mazda glc custom 1	2025.0	3
mazda glc custom	1970.0	3
plymouth horizon miser	2125.0	1
mercury lynx 1	2125.0	1
nissan stanza xe	2160.0	3
honda accord	2205.0	3
toyota corolla	2245.0	3
honda civic	1965.0	3
honda civic (auto)	1965.0	3
datsun 310 gx	1995.0	3
buick century limited	2945.0	1
oldsmobile cutlass ciera (diesel)	3015.0	1
chrysler lebaron medallion	2585.0	1
ford granada l	2835.0	1
toyota celica gt	2665.0	3
dodge charger 2.2	2370.0	1
chevrolet camaro	2950.0	1
CHEATOTER CAMATA	2300.0	1

```
      ford mustang gl
      2790.0
      1

      vw pickup
      2130.0
      2

      dodge rampage
      2295.0
      1

      ford ranger
      2625.0
      1

      chevy s-10
      2720.0
      1
```

[103]: Auto_re.loc[lambda df: df["year"] > 80, ["weight", "origin"]]

[103]:		weight	origin
	name		
	plymouth reliant	2490.0	1
	buick skylark	2635.0	1
	dodge aries wagon (sw)	2620.0	1
	chevrolet citation	2725.0	1
	plymouth reliant	2385.0	1
	toyota starlet	1755.0	3
	plymouth champ	1875.0	1
	honda civic 1300	1760.0	3
	subaru	2065.0	3
	datsun 210 mpg	1975.0	3
	toyota tercel	2050.0	3
	mazda glc 4	1985.0	3
	plymouth horizon 4	2215.0	1
	ford escort 4w	2045.0	1
	ford escort 2h	2380.0	1
	volkswagen jetta	2190.0	2
	honda prelude	2210.0	3
	toyota corolla	2350.0	3
	datsun 200sx	2615.0	3
	mazda 626	2635.0	3
	peugeot 505s turbo diesel	3230.0	2
	volvo diesel	3160.0	2
	toyota cressida	2900.0	3
	datsun 810 maxima	2930.0	3
	buick century	3415.0	1
	oldsmobile cutlass ls	3725.0	1
	ford granada gl	3060.0	1
	chrysler lebaron salon	3465.0	1
	chevrolet cavalier	2605.0	1
	chevrolet cavalier wagon	2640.0	1
	chevrolet cavalier 2-door	2395.0	1
	pontiac j2000 se hatchback	2575.0	1
	dodge aries se	2525.0	1
	pontiac phoenix	2735.0	1
	ford fairmont futura	2865.0	1
	volkswagen rabbit l	1980.0	2
	mazda glc custom l	2025.0	3

```
mazda glc custom
                                    1970.0
                                                 3
plymouth horizon miser
                                    2125.0
                                                 1
mercury lynx l
                                    2125.0
                                                 1
                                                 3
nissan stanza xe
                                    2160.0
honda accord
                                    2205.0
                                                 3
toyota corolla
                                    2245.0
                                                 3
                                                 3
honda civic
                                    1965.0
honda civic (auto)
                                                 3
                                    1965.0
datsun 310 gx
                                                 3
                                    1995.0
buick century limited
                                    2945.0
                                                 1
oldsmobile cutlass ciera (diesel)
                                    3015.0
                                                 1
chrysler lebaron medallion
                                    2585.0
                                                 1
ford granada 1
                                    2835.0
                                                 1
                                                 3
toyota celica gt
                                    2665.0
dodge charger 2.2
                                    2370.0
                                                 1
                                                 1
chevrolet camaro
                                    2950.0
ford mustang gl
                                                 1
                                    2790.0
                                                 2
vw pickup
                                    2130.0
                                                 1
dodge rampage
                                    2295.0
ford ranger
                                    2625.0
                                                 1
chevy s-10
                                    2720.0
                                                 1
```

[104]:		weight	origin
	name		
	toyota starlet	1755.0	3
	plymouth champ	1875.0	1
	honda civic 1300	1760.0	3
	subaru	2065.0	3
	datsun 210 mpg	1975.0	3
	toyota tercel	2050.0	3
	mazda glc 4	1985.0	3
	plymouth horizon 4	2215.0	1
	ford escort 4w	2045.0	1
	volkswagen jetta	2190.0	2
	honda prelude	2210.0	3
	toyota corolla	2350.0	3
	datsun 200sx	2615.0	3
	mazda 626	2635.0	3
	volvo diesel	3160.0	2
	chevrolet cavalier 2-door	2395.0	1
	pontiac j2000 se hatchback	2575.0	1
	volkswagen rabbit l	1980.0	2
	mazda glc custom l	2025.0	3
	mazda glc custom	1970.0	3

```
plymouth horizon miser
                                           2125.0
                                                        1
       mercury lynx 1
                                           2125.0
                                                        1
       nissan stanza xe
                                                        3
                                           2160.0
                                                        3
       honda accord
                                           2205.0
                                                        3
       toyota corolla
                                           2245.0
       honda civic
                                           1965.0
                                                        3
       honda civic (auto)
                                                        3
                                           1965.0
       datsun 310 gx
                                           1995.0
                                                        3
       oldsmobile cutlass ciera (diesel)
                                                        1
                                           3015.0
       toyota celica gt
                                           2665.0
                                                        3
       dodge charger 2.2
                                                        1
                                           2370.0
                                                        2
       vw pickup
                                           2130.0
       dodge rampage
                                           2295.0
                                                        1
       chevy s-10
                                           2720.0
                                                        1
[105]: Auto_re.loc[
           lambda df: (df["displacement"] < 300)</pre>
           & (df.index.str.contains("ford") | df.index.str.contains("datsun")),
           ["weight", "origin"],
       ]
```

[105]:		weight	origin
	name		
	ford maverick	2587.0	1
	datsun pl510	2130.0	3
	datsun pl510	2130.0	3
	ford torino 500	3302.0	1
	ford mustang	3139.0	1
	datsun 1200	1613.0	3
	ford pinto runabout	2226.0	1
	ford pinto (sw)	2395.0	1
	datsun 510 (sw)	2288.0	3
	ford maverick	3021.0	1
	datsun 610	2379.0	3
	ford pinto	2310.0	1
	datsun b210	1950.0	3
	ford pinto	2451.0	1
	datsun 710	2003.0	3
	ford maverick	3158.0	1
	ford pinto	2639.0	1
	datsun 710	2545.0	3
	ford pinto	2984.0	1
	ford maverick	3012.0	1
	ford granada ghia	3574.0	1
	datsun b-210	1990.0	3
	ford pinto	2565.0	1
	datsun f-10 hatchback	1945.0	3

```
ford granada
                        3525.0
                                      1
ford mustang ii 2+2
                        2755.0
                                      1
datsun 810
                        2815.0
                                      3
ford fiesta
                        1800.0
                                      1
datsun b210 gx
                        2070.0
                                      3
ford fairmont (auto)
                        2965.0
                                      1
ford fairmont (man)
                        2720.0
                                      1
datsun 510
                        2300.0
                                      3
datsun 200-sx
                                      3
                        2405.0
ford fairmont 4
                        2890.0
                                      1
datsun 210
                        2020.0
                                      3
datsun 310
                        2019.0
                                      3
ford fairmont
                        2870.0
                                      1
datsun 510 hatchback
                        2434.0
                                      3
datsun 210
                                      3
                        2110.0
                                      3
datsun 280-zx
                        2910.0
                                      3
datsun 210 mpg
                        1975.0
ford escort 4w
                        2045.0
                                      1
ford escort 2h
                        2380.0
                                      1
datsun 200sx
                                      3
                        2615.0
datsun 810 maxima
                                      3
                        2930.0
ford granada gl
                                      1
                        3060.0
ford fairmont futura
                                      1
                        2865.0
datsun 310 gx
                        1995.0
                                      3
ford granada 1
                        2835.0
ford mustang gl
                        2790.0
                                      1
ford ranger
                        2625.0
```

1.2 for loops

```
[106]: total = 0
    for value in [3, 2, 9]:
        total += value
    print("total is: {0}".format(total))

total is: 14

[107]: total = 0
    for value in [3, 2, 9]:
        for weight in [3, 2, 1]:
            total += weight * value
    print("total is: {0}".format(total))

total is: 84

[108]: total = 0
    for value, weight in zip([3, 2, 9], [0.2, 0.3, 0.5]):
        total += weight * value
```

```
print("weighted average is: {0}".format(total))
      weighted average is: 5.7
[109]: rng = np.random.default_rng(1)
      A = rng.standard_normal((127, 5))
      Α
[109]: array([[ 3.45584192e-01, 8.21618144e-01, 3.30437076e-01,
              -1.30315723e+00, 9.05355867e-01],
              [ 4.46374572e-01, -5.36953235e-01, 5.81118104e-01,
               3.64572396e-01, 2.94132497e-01],
              [ 2.84222413e-02, 5.46712987e-01, -7.36454087e-01,
              -1.62909948e-01, -4.82119313e-01],
              [ 5.98846213e-01, 3.97221075e-02, -2.92456751e-01,
              -7.81908462e-01, -2.57192241e-01],
              [8.14218052e-03, -2.75602905e-01, 1.29406381e+00,
                1.00672432e+00, -2.71116248e+00],
              [-1.88901325e+00, -1.74772092e-01, -4.22190412e-01,
               2.13642997e-01, 2.17321931e-01],
              [ 2.11783876e+00, -1.11202076e+00, -3.77605007e-01,
               2.04277161e+00, 6.46702996e-01],
              [ 6.63063372e-01, -5.14006372e-01, -1.64807517e+00,
                1.67464744e-01, 1.09014088e-01],
              [-1.22735205e+00, -6.83226662e-01, -7.20436797e-02,
              -9.44751623e-01, -9.82699679e-02],
              [ 9.54830275e-02, 3.55862371e-02, -5.06291658e-01,
               5.93748072e-01, 8.91166954e-01],
              [ 3.20848305e-01, -8.18230227e-01, 7.31652284e-01,
              -5.01440018e-01, 8.79160618e-01],
              [-1.07178742e+00, 9.14467203e-01, -2.00634546e-02,
              -1.24874889e+00, -3.13899472e-01],
              [5.41022788e-02, 2.72791339e-01, -9.82188125e-01,
              -1.10737305e+00, 1.99584533e-01],
              [-4.66749617e-01, 2.35505612e-01, 7.59519522e-01,
              -1.64878737e+00, 2.54388117e-01],
              [ 1.22464697e+00, -2.97526844e-01, -8.10814583e-01,
               7.52243827e-01, 2.53446516e-01],
              [8.95883071e-01, -3.45215710e-01, -1.48181827e+00,
              -1.10010765e-01, -4.45828153e-01],
              [7.75323822e-01, 1.93632848e-01, -1.63084923e+00,
              -1.19516308e+00, 8.83789037e-01],
              [6.79765017e-01, -6.40243366e-01, -1.04879657e-03,
               4.45573554e-01, 4.68404336e-01],
              [ 8.76242196e-01, 2.56485627e-01, -9.48283390e-02,
              -2.58848065e-01, 1.05574280e+00],
              [-2.25085428e+00, -1.38655325e-01, 3.30001040e-02,
              -1.42534896e+00, 3.32813613e-01],
```

```
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[ 3.82929583e-01, -8.75721143e-01, -1.51431863e+00,
 1.75338412e+00, -1.11292193e-01],
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 6.16878755e-01, 2.54789782e+00],
[-1.00092485e+00, -1.25069576e+00, 5.88968934e-01,
-8.40721590e-01, -5.06025484e-01],
[-3.48117467e-01, 5.32002086e-01, -4.05302361e-01,
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```

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[-1.19946058e+00, 5.17082195e-01, 1.01840866e+00,
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[-1.39388831e-01, 5.74166620e-02, -2.02749360e-01,
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[-3.49467146e-01, 1.00625575e+00, -6.11475615e-01,
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[ 3.57868890e-01, -4.28238208e-01, 5.44832109e-02,
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[ 9.12899205e-01, -2.80412144e-01, 3.80250758e-02,
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```
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 1.79696202e-01, -1.88207089e+00],
```

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              -2.79748758e-01, -7.04489515e-01],
              [8.51641715e-01, -9.14444983e-01, -2.72908493e+00,
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               3.74863045e-01, -1.58085545e+00],
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               1.84244761e+00, -2.14524000e-01],
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              -4.51551059e-01, 9.50756951e-01]])
[110]: A.shape
[110]: (127, 5)
[111]: M = rng.choice([0, np.nan], p=[0.8, 0.2], size=A.shape)
      М
[111]: array([[ 0., 0., 0., 0., nan],
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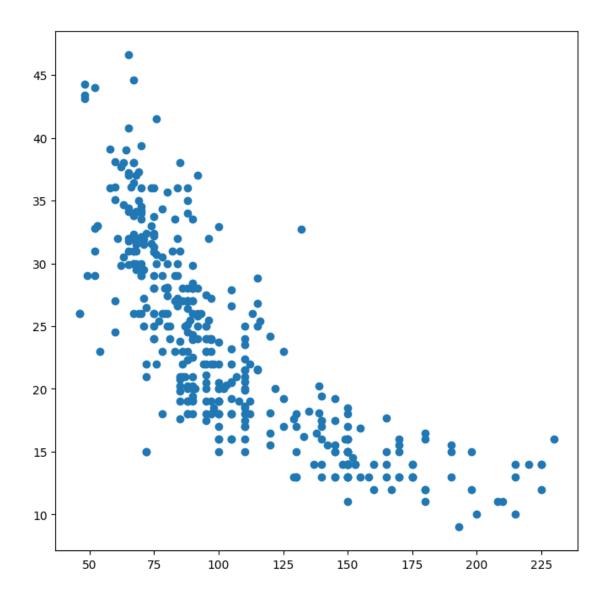
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              [ 4.75867438e-01, -3.23721814e-01, 2.72916704e+00,
               1.84244761e+00, -2.14524000e-01],
              [-3.29131254e-01, 1.69017655e+00, -1.88335978e+00,
              -4.51551059e-01, 9.50756951e-01]])
[113]: D = pd.DataFrame(A, columns=["food", "bar", "pickle", "snack", "popcorn"])
      D
```

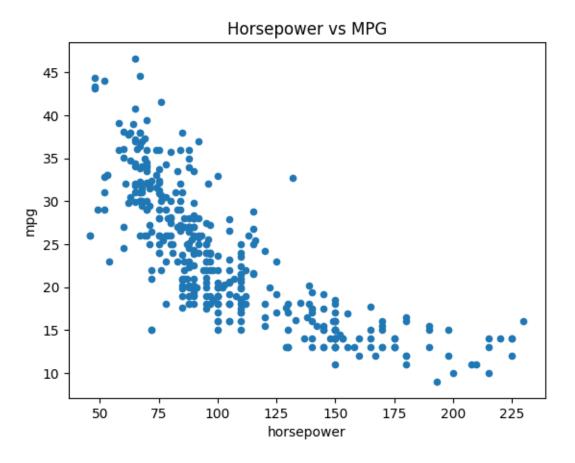
-1.48124023e+00, -1.98986032e+00],

```
[113]:
               food
                           bar
                                  pickle
                                             snack
                                                     popcorn
            0.345584 0.821618 0.330437 -1.303157
      0
                                                         NaN
      1
                 NaN -0.536953 0.581118 0.364572
                                                    0.294132
      2
                 NaN 0.546713
                                     NaN -0.162910 -0.482119
      3
           0.598846
                                     NaN -0.781908
                           NaN
                                                         NaN
            0.008142 -0.275603
                                1.294064
                                               NaN -2.711162
      . .
      122
                 NaN -1.421741
                                0.011192
                                               NaN
                                                   0.128476
      123 0.887647 -0.243649 0.730347 0.720844
                                                         NaN
      124 1.716248 0.778838
                                     NaN -0.680824 -0.845306
      125  0.475867  -0.323722  2.729167  1.842448  -0.214524
      126 -0.329131 1.690177 -1.883360 -0.451551 0.950757
      [127 rows x 5 columns]
[114]: D[:3]
[114]:
              food
                        bar
                                pickle
                                           snack
                                                   popcorn
         0.345584 0.821618
                             0.330437 -1.303157
                                                       NaN
      1
              NaN -0.536953 0.581118 0.364572
                                                  0.294132
      2
              NaN 0.546713
                                   NaN -0.162910 -0.482119
[115]: for col in D.columns:
           template = "Column {0} has {1: .2%} missing values"
          print(template.format(col, np.isnan(D[col]).mean()))
      Column food has 16.54% missing values
      Column bar has 25.98% missing values
      Column pickle has 29.13% missing values
      Column snack has 21.26% missing values
      Column popcorn has 22.83% missing values
[116]: fig, ax = subplots(figsize=(8, 8))
      ax.plot(Auto["horsepower"].values, Auto["mpg"].values, "o");
```



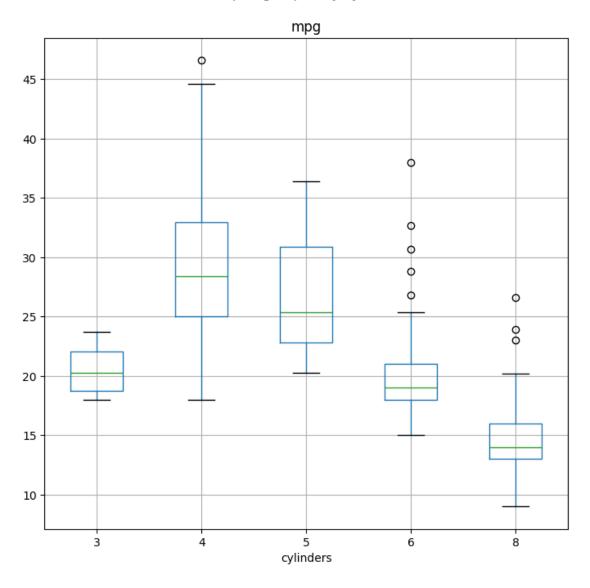
```
[117]: ax = Auto.plot.scatter("horsepower", "mpg")
ax.set_title("Horsepower vs MPG")
```

[117]: Text(0.5, 1.0, 'Horsepower vs MPG')

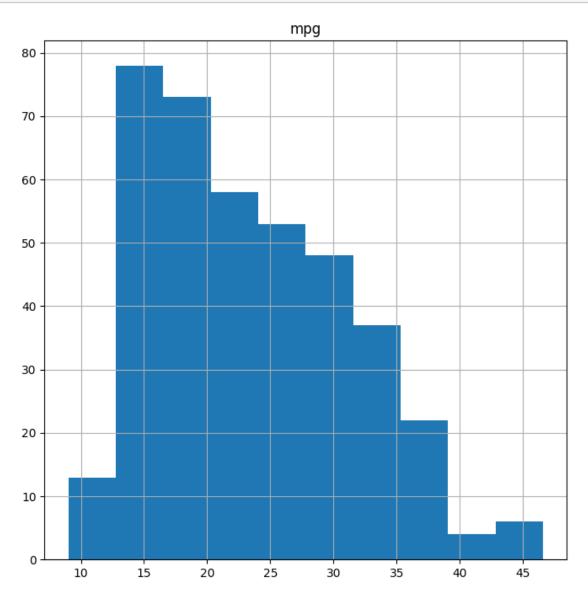


```
[118]: fig = ax.figure
    fig.savefig("hp_mpg.png")
[119]: fig, axes = subplots(ncols=3, figsize=(15, 5))
    Auto.plot.scatter("horsepower", "mpg", ax=axes[1])
[119]: <Axes: xlabel='horsepower', ylabel='mpg'>
```

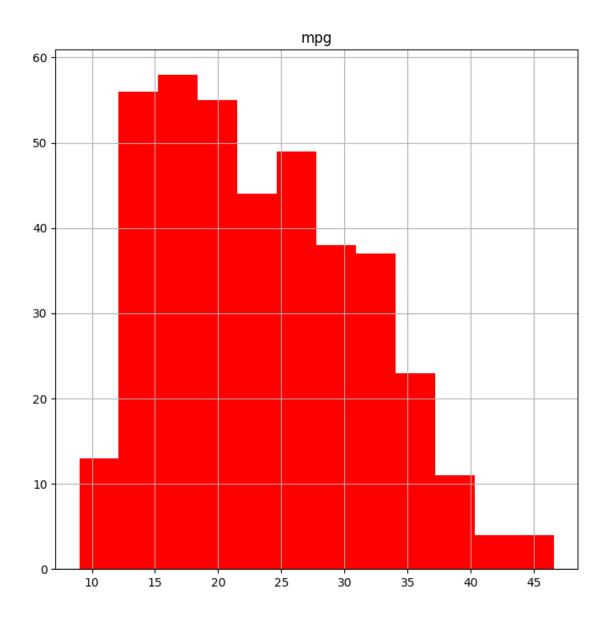
Boxplot grouped by cylinders



```
[122]: fig, ax = subplots(figsize=(8, 8));
Auto.hist("mpg", ax=ax);
```



```
[123]: fig, ax = subplots(figsize=(8, 8))
Auto.hist("mpg", color="red", bins=12, ax=ax);
```



[124]: Auto.hist?

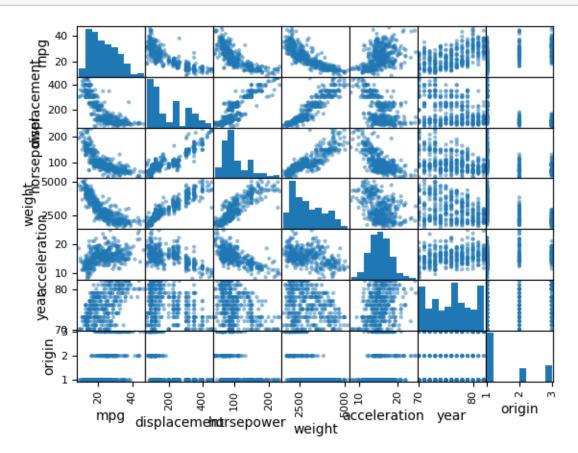
```
Signature:
Auto.hist(
    column: 'IndexLabel | None' = None,
    by=None,
    grid: 'bool' = True,
    xlabelsize: 'int | None' = None,
    xrot: 'float | None' = None,
    ylabelsize: 'int | None' = None,
    yrot: 'float | None' = None,
    sa=None,
    sharex: 'bool' = False,
```

```
sharey: 'bool' = False,
   figsize: 'tuple[int, int] | None' = None,
   layout: 'tuple[int, int] | None' = None,
   bins: 'int | Sequence[int]' = 10,
   backend: 'str | None' = None,
   legend: 'bool' = False,
    **kwargs,
Docstring:
Make a histogram of the DataFrame's columns.
A `histogram` is a representation of the distribution of data.
This function calls :meth: `matplotlib.pyplot.hist`, on each series in
the DataFrame, resulting in one histogram per column.
.. _histogram: https://en.wikipedia.org/wiki/Histogram
Parameters
_____
data : DataFrame
   The pandas object holding the data.
column : str or sequence, optional
   If passed, will be used to limit data to a subset of columns.
by : object, optional
    If passed, then used to form histograms for separate groups.
grid : bool, default True
    Whether to show axis grid lines.
xlabelsize : int, default None
    If specified changes the x-axis label size.
xrot : float, default None
   Rotation of x axis labels. For example, a value of 90 displays the
   x labels rotated 90 degrees clockwise.
ylabelsize : int, default None
    If specified changes the y-axis label size.
yrot : float, default None
    Rotation of y axis labels. For example, a value of 90 displays the
   y labels rotated 90 degrees clockwise.
ax : Matplotlib axes object, default None
    The axes to plot the histogram on.
sharex : bool, default True if ax is None else False
    In case subplots=True, share x axis and set some x axis labels to
    invisible; defaults to True if ax is None otherwise False if an ax
    Note that passing in both an ax and sharex=True will alter all x axis
    labels for all subplots in a figure.
sharey : bool, default False
    In case subplots=True, share y axis and set some y axis labels to
```

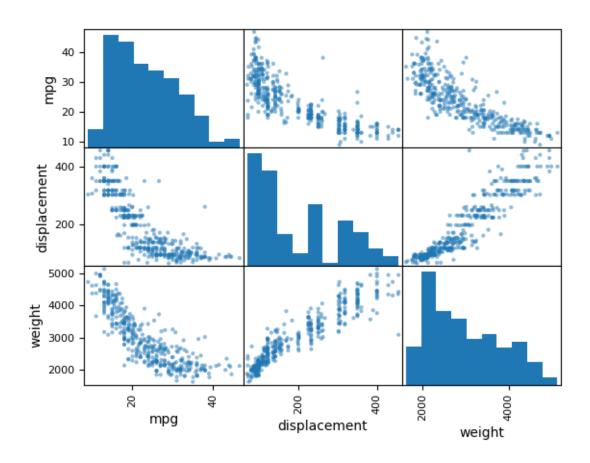
invisible.

```
figsize : tuple, optional
    The size in inches of the figure to create. Uses the value in
    `matplotlib.rcParams` by default.
layout : tuple, optional
    Tuple of (rows, columns) for the layout of the histograms.
bins: int or sequence, default 10
   Number of histogram bins to be used. If an integer is given, bins + 1
   bin edges are calculated and returned. If bins is a sequence, gives
   bin edges, including left edge of first bin and right edge of last
   bin. In this case, bins is returned unmodified.
backend : str, default None
    Backend to use instead of the backend specified in the option
    ``plotting.backend``. For instance, 'matplotlib'. Alternatively, to
    specify the ``plotting.backend`` for the whole session, set
    ``pd.options.plotting.backend``.
legend : bool, default False
   Whether to show the legend.
**kwargs
    All other plotting keyword arguments to be passed to
    :meth: `matplotlib.pyplot.hist`.
Returns
matplotlib.AxesSubplot or numpy.ndarray of them
See Also
_____
matplotlib.pyplot.hist : Plot a histogram using matplotlib.
Examples
This example draws a histogram based on the length and width of
some animals, displayed in three bins
.. plot::
    :context: close-figs
   >>> data = {'length': [1.5, 0.5, 1.2, 0.9, 3],
              'width': [0.7, 0.2, 0.15, 0.2, 1.1]}
   >>> index = ['pig', 'rabbit', 'duck', 'chicken', 'horse']
   >>> df = pd.DataFrame(data, index=index)
   >>> hist = df.hist(bins=3)
          ~/ISLP/islpenv/lib/python3.12/site-packages/pandas/plotting/_core.py
Type:
          method
```

[125]: pd.plotting.scatter_matrix(Auto);



```
[126]: pd.plotting.scatter_matrix(Auto[["mpg", "displacement", "weight"]]);
```



```
[127]: Auto[["mpg", "weight"]].describe()
[127]:
                      mpg
                                weight
              392.000000
                            392.000000
       count
               23.445918
                           2977.584184
       mean
       std
                7.805007
                            849.402560
                9.000000
                           1613.000000
       min
               17.000000
                           2225.250000
       25%
       50%
               22.750000
                           2803.500000
       75%
               29.000000
                           3614.750000
               46.600000
       max
                          5140.000000
       Auto[["cylinders"]].describe()
[128]:
[128]:
               cylinders
                      392
       count
       unique
                        5
                        4
       top
       freq
                      199
```

```
[129]: Auto[["mpg"]].describe()
[129]:
                     mpg
       count 392.000000
       mean
               23.445918
       std
                7.805007
       min
                9.000000
       25%
               17.000000
       50%
               22.750000
       75%
               29.000000
       max
               46.600000
[130]: allDone()
```

<IPython.lib.display.Audio object>