Marketing Exercise

Import notebook functions

```
from notebookfuncs import *
```

Import standard libraries

```
import numpy as np
import pandas as pd
from matplotlib.pyplot import subplots
```

New imports

```
import statsmodels.api as sm
```

Import statsmodel.objects

```
from statsmodels.stats.outliers_influence import variance_inflation_factor as VIF
from statsmodels.stats.outliers_influence import summary_table
from statsmodels.stats.anova import anova_lm
```

Import ISLP objects

```
import ISLP
from ISLP import models
from ISLP import load_data
from ISLP.models import ModelSpec as MS, summarize, poly
```

Inspecting objects and namespaces

dir()

```
['Audio',
 'ISLP',
 'In',
 'InteractiveShell',
 'MS',
 'Out',
 'VIF',
 '_',
 '__builtin__',
 '__builtins__',
'__doc__',
'__loader__',
 '__name__',
'__package__',
 '__session__',
 '__spec__',
 '_dh',
 '_i',
 '_i1',
 '_i2',
 '_i3',
 '_i4',
 '_i5',
 '_i6',
 _
'_ih',
 '_ii',
 '_iii',
 '_oh',
 'allDone',
 'anova_lm',
```

```
'display',
 'exit',
 'get_ipython',
 'load_data',
 'models',
 'np',
 'open',
 'pd',
 'poly',
 'quit',
 'sm',
 'subplots',
 'summarize',
 'summary_table']
Advertising = pd.read_csv("Advertising.csv")
# Drop first column
Advertising = Advertising.iloc[:, 1:]
Advertising.head()
```

| | TV | Radio | Newspaper | Sales |
|---|-------|-------|-----------|-------|
| 0 | 230.1 | 37.8 | 69.2 | 22.1 |
| 1 | 44.5 | 39.3 | 45.1 | 10.4 |
| 2 | 17.2 | 45.9 | 69.3 | 9.3 |
| 3 | 151.5 | 41.3 | 58.5 | 18.5 |
| 4 | 180.8 | 10.8 | 58.4 | 12.9 |

Advertising.describe()

| | TV | Radio | Newspaper | Sales |
|----------------------|------------|------------|------------|------------|
| count | 200.000000 | 200.000000 | 200.000000 | 200.000000 |
| mean | 147.042500 | 23.264000 | 30.554000 | 14.022500 |
| std | 85.854236 | 14.846809 | 21.778621 | 5.217457 |
| \min | 0.700000 | 0.000000 | 0.300000 | 1.600000 |
| 25% | 74.375000 | 9.975000 | 12.750000 | 10.375000 |
| 50% | 149.750000 | 22.900000 | 25.750000 | 12.900000 |
| 75% | 218.825000 | 36.525000 | 45.100000 | 17.400000 |
| max | 296.400000 | 49.600000 | 114.000000 | 27.000000 |

Is there a relationship between sales and advertising budget?

```
y = Advertising["Sales"]
cols = list(Advertising.columns)
cols.remove("Sales")
X = MS(cols).fit_transform(Advertising)
model = sm.OLS(y, X)
results = model.fit()
print("F-value", results.fvalue)
print("F-pvalue", results.f_pvalue)
summarize(results)
```

F-value 570.2707036590944 F-pvalue 1.575227256092416e-96

| | coef | std err | t | P> t |
|---------------|---------|---------|--------|------|
| intercept | 2.9389 | 0.312 | 9.422 | 0.00 |
| TV | 0.0458 | 0.001 | 32.809 | 0.00 |
| Radio | 0.1885 | 0.009 | 21.893 | 0.00 |
| Newspaper | -0.0010 | 0.006 | -0.177 | 0.86 |

dir(models)

```
['Column',
    'Feature',
    'FeatureSelector',
    'ModelSpec',
    'Stepwise',
    'StringIO',
    '__builtins__',
    '__cached__',
    '__doc__',
    '__file__',
    '__loader__',
    '__name__',
    '__package__',
    '__path__',
    '__spec__',
    'bs',
```

```
'build_columns',
'columns',
'contrast',
'derived_feature',
'generic_selector',
'min_max_strategy',
'model_spec',
'np',
'ns',
'pca',
'pd',
'poly',
'sklearn_selected',
'sklearn_selection_path',
'sklearn_sm',
'sklearn_wrap',
'strategy',
'summarize']
```

• The p-value corresponding to the F-statistic is very low. Thus, clear evidence of a relationship between sales and advertising budget.

dir(results)

```
['HCO_se',
'HC1_se',
'HC2_se',
'HC3_se',
'_HCCM',
'__class__',
'__delattr__',
'__dict__',
'__dir__',
'__eq__',
'__eq__',
'__getattribute__',
'__getstate__',
'__getstate__',
'__gt__',
'__ninit__',
```

```
'__init_subclass__',
'__le__',
'__lt__',
'__module__',
'__ne__',
'__new__',
'__reduce__',
'__reduce_ex__',
'__repr__',
'__setattr__',
'__sizeof__',
'__str__',
'__subclasshook__',
'__weakref__',
'_abat_diagonal',
'_cache',
'_data_attr',
'_data_in_cache',
'_get_robustcov_results',
'_get_wald_nonlinear',
'_is_nested',
'_transform_predict_exog',
'_use_t',
'_wexog_singular_values',
'aic',
'bic',
'bse',
'centered_tss',
'compare_f_test',
'compare_lm_test',
'compare_lr_test',
'condition_number',
'conf_int',
'conf_int_el',
'cov HCO',
'cov_HC1',
'cov_HC2',
'cov_HC3',
'cov_kwds',
'cov_params',
'cov_type',
'df_model',
'df_resid',
```

```
'diagn',
'eigenvals',
'el_test',
'ess',
'f_pvalue',
'f_test',
'fittedvalues',
'fvalue',
'get_influence',
'get_prediction',
'get_robustcov_results',
'info_criteria',
'initialize',
'k_constant',
'llf',
'load',
'model',
'mse_model',
'mse_resid',
'mse_total',
'nobs',
'normalized_cov_params',
'outlier_test',
'params',
'predict',
'pvalues',
'remove_data',
'resid',
'resid_pearson',
'rsquared',
'rsquared_adj',
'save',
'scale',
'ssr',
'summary',
'summary2',
't_test',
't_test_pairwise',
'tvalues',
'uncentered_tss',
'use_t',
'wald_test',
'wald_test_terms',
```

'wresid']

How strong is the relationship?

results.summary()

| Dep. Variable: | | Sales | \mathbf{R} | R-squared: | | 0.897 |
|--------------------------|---------------------------------------|----------------------------------|--|----------------------------------|-----------------------------------|----------------------------------|
| Model: | | OLS | OLS Adj. R-squa | | uared: | 0.896 |
| Method: | Method: | | \mathbf{res} \mathbf{F} | -statistic | : | 570.3 |
| Date: | Tue | e, 24 Sep 2 | 2024 P | rob (F-s | tatistic): | 1.58e-96 |
| Time: | | 12:50:55 | \mathbf{L} | og-Likeli | ihood: | -386.18 |
| No. Observation | ons: | 200 | A | IC: | | 780.4 |
| Df Residuals: | | 196 | В | SIC: | | 793.6 |
| Df Model: | | 3 | | | | |
| Covariance Type: | | nonrobus | t | | | |
| coef | | | | | | |
| | coef | std err | t | $\mathbf{P} > \mathbf{t} $ | [0.025] | 0.975] |
| intercept | coef 2.9389 | std err 0.312 | t 9.422 | P > t 0.000 | [0.025 2.324 | 0.975] 3.554 |
| intercept TV | | | | | • | |
| - | 2.9389 | 0.312 | 9.422 | 0.000 | 2.324 | 3.554 |
| ${f TV}$ | 2.9389 0.0458 | 0.312 0.001 | 9.422 32.809 | 0.000 | 2.324 0.043 | 3.554 0.049 |
| TV Radio | 2.9389 0.0458 0.1885 | 0.312 0.001 0.009 | 9.422 32.809 21.893 -0.177 | 0.000 0.000 0.000 | 2.324 0.043 0.172 -0.013 | 3.554 0.049 0.206 |
| TV Radio Newspaper | 2.9389 0.0458 0.1885 -0.0010 | 0.312 0.001 0.009 0.006 | 9.422 32.809 21.893 -0.177 Durbin | 0.000 0.000 0.000 0.860 | 2.324 0.043 0.172 -0.013 | 3.554 0.049 0.206 0.011 |

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Cond. No.

454.

6.332

y.mean()

14.0225

results.resid.std()

Kurtosis:

1.6727572743844117

```
(results.resid.std() / y.mean()) * 100
```

11.929094486606608

• The residual standard error (RSE) is 1.67 and the mean value of the response is 14.023 which translates to a percentage error of roughly 11.93%

```
("R-squared", results.rsquared, "Adjusted R-squared", results.rsquared adj)
```

('R-squared', 0.8972106381789522, 'Adjusted R-squared', 0.8956373316204668)

• The R2 explains about 90% of the variance in Sales.

Which media are associated with Sales?

• The low p-values for Radio and TV suggest that only they are related to Sales.

How large is the association between each medium and sales?

```
results.conf_int(alpha=0.05)
```

| | 0 | 1 |
|-----------|-----------|----------|
| intercept | 2.323762 | 3.554016 |
| TV | 0.043014 | 0.048516 |
| Radio | 0.171547 | 0.205513 |
| Newspaper | -0.012616 | 0.010541 |

- The confidence intervals for TV and Radio are narrow and far from zero. This provides evidence that these media are related to sales.
- The interval for Newspaper includes zero indicating that it is not statistically significant given values of TV and Radio.

```
vals = [VIF(X, i) for i in range(1, X.shape[1])]
print(vals)
```

[1.00461078493965, 1.1449519171055353, 1.1451873787239288]

- The VIF scores are 1.005, 1.145 and 1.145 respectively for TV, radio and newspaper. These suggest no evidence of collinearity as an explination for wide standard errors for newspaper.
- In order to assess the association of each medium individually on sales, we can perform three separate linear regressions.

```
TV = MS(["TV"]).fit_transform(Advertising)
model = sm.OLS(y, TV)
results = model.fit()
print(summarize(results))
Radio = MS(["Radio"]).fit_transform(Advertising)
model = sm.OLS(y, Radio)
results = model.fit()
print(summarize(results))
Newspaper = MS(["Newspaper"]).fit_transform(Advertising)
model = sm.OLS(y, Newspaper)
results = model.fit()
print(summarize(results))
```

```
coef std err
                                  P>|t|
                                 t
intercept 7.0326
                    0.458 15.360
                                      0.0
TV
           0.0475
                    0.003 17.668
                                      0.0
             coef std err
                                 t P>|t|
intercept
                    0.563 16.542
          9.3116
                                      0.0
Radio
           0.2025
                     0.020
                             9.921
                                      0.0
                                  t P>|t|
              coef std err
intercept
          12.3514
                     0.621
                            19.876 0.000
                             3.300 0.001
Newspaper
            0.0547
                     0.017
```

Looking at the p-values, there is evidence of a strong association b/w TV and sales and radio and sales. There is evidence of a mild association between Newspaper and sales when TV and radio are ignored.

How accurately can we predict future sales?

• Given that \$100,000 is spent on TV advertising, and \$20,000 is spent on Radio advertising, we need to compute the 95% Confidence intervals for each city (i.e., the mean) and the prediction interval for a particular city (also at 95% confidence intervals).

Fit the regression dropping the Newspaper column as insignificant

```
y = Advertising["Sales"]
cols = list(Advertising.columns)
cols.remove("Sales")
cols.remove("Newspaper")
X = MS(cols).fit_transform(Advertising)
model = sm.OLS(y, X)
results = model.fit()
print("F-value", results.fvalue)
print("F-pvalue", results.f_pvalue)
summarize(results)
```

F-value 859.6177183058211 F-pvalue 4.8273618513354486e-98

| | coef | std err | t | P> t |
|-----------|--------|---------|--------|------|
| intercept | 2.9211 | 0.294 | 9.919 | 0.0 |
| TV | 0.0458 | 0.001 | 32.909 | 0.0 |
| Radio | 0.1880 | 0.008 | 23.382 | 0.0 |

results.summary()

| Dep. Variable: | Sales | R-squared: | 0.897 |
|-------------------|------------------|---------------------|----------|
| Model: | OLS | Adj. R-squared: | 0.896 |
| Method: | Least Squares | F-statistic: | 859.6 |
| Date: | Tue, 24 Sep 2024 | Prob (F-statistic): | 4.83e-98 |
| Time: | 12:50:56 | Log-Likelihood: | -386.20 |
| No. Observations: | 200 | AIC: | 778.4 |
| Df Residuals: | 197 | BIC: | 788.3 |
| Df Model: | 2 | | |
| Covariance Type: | nonrobust | | |

| | \mathbf{coef} | std err | \mathbf{t} | $\mathbf{P} \gt \mathbf{t} $ | [0.025] | 0.975] |
|-----------|-----------------|--------------------------|--------------|-------------------------------|---------|--------|
| intercept | 2.9211 | 0.294 | 9.919 | 0.000 | 2.340 | 3.502 |
| ${f TV}$ | 0.0458 | 0.001 | 32.909 | 0.000 | 0.043 | 0.048 |
| Radio | 0.1880 | 0.008 | 23.382 | 0.000 | 0.172 | 0.204 |

| Omnibus: | 60.022 | Durbin-Watson: | 2.081 |
|----------------|--------|-----------------------|----------|
| Prob(Omnibus): | 0.000 | Jarque-Bera (JB): | 148.679 |
| Skew: | -1.323 | Prob(JB): | 5.19e-33 |
| Kurtosis: | 6.292 | Cond. No. | 425. |

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
design = MS(["TV", "Radio"])
new_df = pd.DataFrame({"TV": [100], "Radio": [20]})
print(new_df)
new_X = design.fit_transform(new_df)
new_predictions = results.get_prediction(new_X)
new_predictions.predicted_mean
```

```
TV Radio
0 100 20
array([11.25646595])
```

We predict the confidence intervals at 95% as follows:

array([[7.92961607, 14.58331584]])

```
new_predictions.conf_int(alpha=0.05)
array([[10.98525445, 11.52767746]])
```

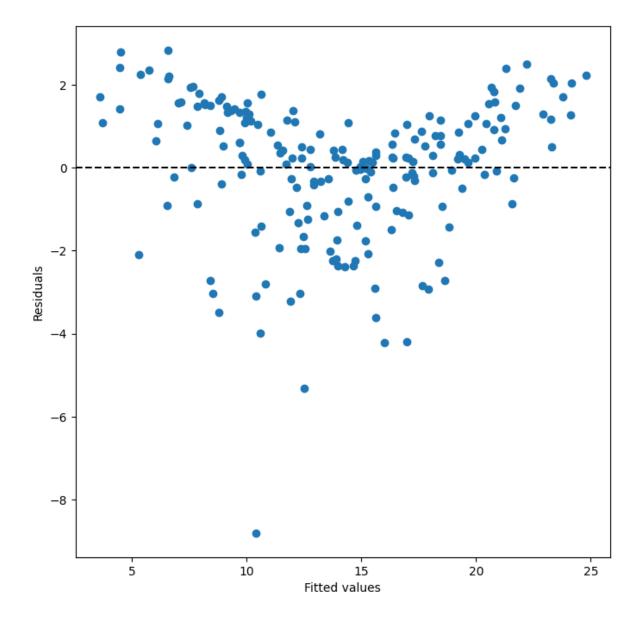
We predict the prediction interval for a particular city as follows:

```
new_predictions.conf_int(alpha=0.05, obs=True)
```

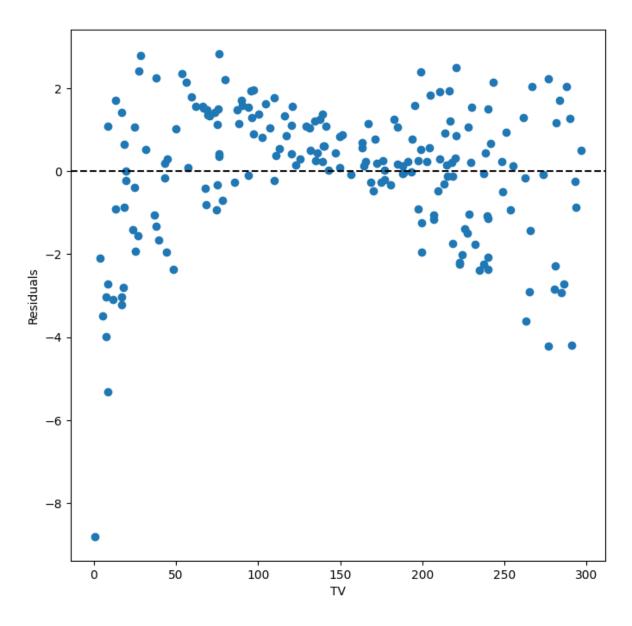
• Both intervals are centered at 11,256 but the prediction intervals are wider reflecting the additional uncertainty around sales for a particular city as against the average sales for many locations.

Is the relationship linear?

```
_, ax = subplots(figsize=(8, 8))
ax.scatter(results.fittedvalues, results.resid)
ax.set_xlabel("Fitted values")
ax.set_ylabel("Residuals")
ax.axhline(0, c="k", ls="--")
```

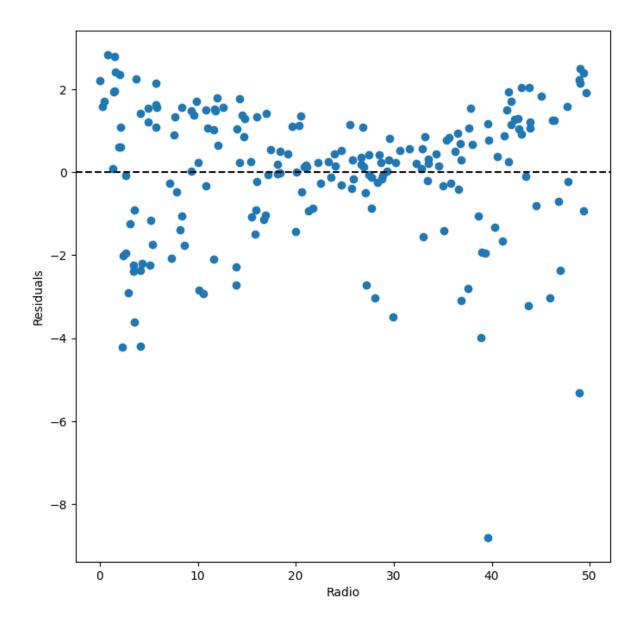


```
_, ax = subplots(figsize=(8, 8))
ax.scatter(Advertising["TV"], results.resid)
ax.set_xlabel("TV")
ax.set_ylabel("Residuals")
ax.axhline(0, c="k", ls="--")
```



```
_, ax = subplots(figsize=(8, 8))
ax.scatter(Advertising["Radio"], results.resid)
```

```
ax.set_xlabel("Radio")
ax.set_ylabel("Residuals")
ax.axhline(0, c="k", ls="--")
```



• There is evidence of non-linearity in the model from the residuals plotted against the fitted values. Looking at the residuals versus predictors plots, it appears that TV is a better candidate for quadratification.

```
X = MS([poly("TV", degree=2, raw=True), "Radio"]).fit_transform(Advertising)
model = sm.OLS(y, X)
results = model.fit()
summarize(results)
```

| | coef | std err | t | P> t |
|---------------------------------|---------|----------|--------|------|
| intercept | 1.2876 | 0.359000 | 3.588 | 0.0 |
| poly(TV, degree=2, raw=True)[0] | 0.0784 | 0.005000 | 15.736 | 0.0 |
| poly(TV, degree=2, raw=True)[1] | -0.0001 | 0.000017 | -6.775 | 0.0 |
| Radio | 0.1930 | 0.007000 | 26.465 | 0.0 |

results.summary()

| Dep. Variable: | Sales | R-squared: | 0.917 |
|-------------------|------------------|---------------------|-----------|
| Model: | OLS | Adj. R-squared: | 0.915 |
| Method: | Least Squares | F-statistic: | 719.0 |
| Date: | Tue, 24 Sep 2024 | Prob (F-statistic): | 1.80e-105 |
| Time: | 12:50:58 | Log-Likelihood: | -365.16 |
| No. Observations: | 200 | AIC: | 738.3 |
| Df Residuals: | 196 | BIC: | 751.5 |
| Df Model: | 3 | | |
| Covariance Type: | nonrobust | | |

| | coef | std err | t | \mathbf{P} > $ \mathbf{t} $ | 0.025 | $\boldsymbol{0.975}]$ |
|---------------------------------|---------|----------|--------|-------------------------------|--------|-----------------------|
| intercept | 1.2876 | 0.359 | 3.588 | 0.000 | 0.580 | 1.995 |
| poly(TV, degree=2, raw=True)[0] | 0.0784 | 0.005 | 15.736 | 0.000 | 0.069 | 0.088 |
| poly(TV, degree=2, raw=True)[1] | -0.0001 | 1.68e-05 | -6.775 | 0.000 | -0.000 | -8.05e-05 |
| Radio | 0.1930 | 0.007 | 26.465 | 0.000 | 0.179 | 0.207 |
| Omnibus: 19.524 | 1 Durb | in-Watso | n: | 2.136 | | |
| D 1 (O 1) 0 000 | т | D / | TD) | 44 710 | | |

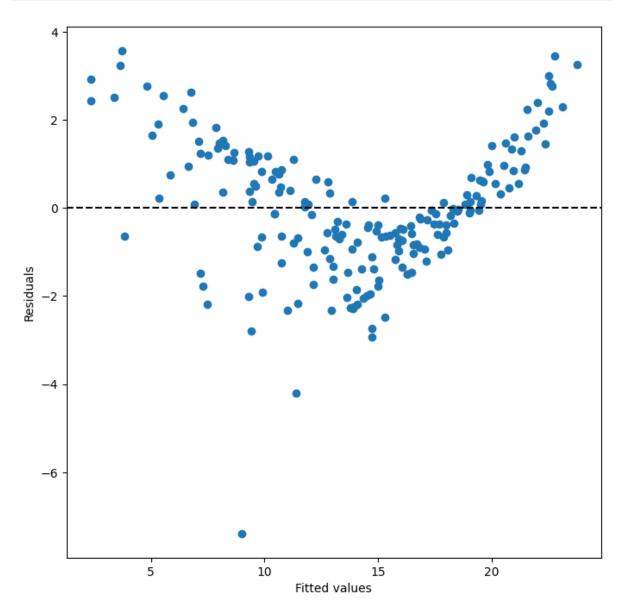
| Omnibus: | 19.524 | Durbin-Watson: | 2.136 |
|----------------|--------|-------------------|------------|
| Prob(Omnibus): | 0.000 | Jarque-Bera (JB): | 44.712 |
| Skew: | -0.413 | Prob(JB): | 1.95e-10 |
| Kurtosis: | 5.164 | Cond. No. | 1.29e + 05 |

Notes:

^[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

^[2] The condition number is large, 1.29e+05. This might indicate that there are strong multicollinearity or other numerical problems.

```
_, ax = subplots(figsize=(8, 8))
ax.scatter(results.fittedvalues, results.resid)
ax.set_xlabel("Fitted values")
ax.set_ylabel("Residuals")
ax.axhline(0, c="k", ls="--")
```



While the fit has improved as seen from the R2 increasing by 2 percentage points, there is still some non-linearity visible in the residuals plot against fitted values.

References:

 $https://www.kellogg.northwestern.edu/faculty/weber/emp/_session_3/nonlinearities.htm \\ https://online.stat.psu.edu/stat462/node/120/$

Is there synergy among the advertising media?

Synergy implies an interaction effect. That's what we test out now.

```
X = MS([poly("TV", raw=True, degree=2), "Radio", ("TV", "Radio")]).fit_transform(
         Advertising
)
model = sm.OLS(y, X)
results = model.fit()
summarize(results)
```

| | coef | std err | t | P> t |
|---------------------------------|---------|----------|---------|------|
| intercept | 5.1371 | 0.193000 | 26.663 | 0.0 |
| poly(TV, degree=2, raw=True)[0] | 0.0509 | 0.002000 | 22.810 | 0.0 |
| poly(TV, degree=2, raw=True)[1] | -0.0001 | 0.000007 | -15.920 | 0.0 |
| Radio | 0.0352 | 0.006000 | 5.959 | 0.0 |
| TV:Radio | 0.0011 | 0.000035 | 31.061 | 0.0 |
| | | | | |

results.summary()

| Dep. Variable: | Sales | R-squared: | 0.986 |
|-------------------|------------------|---------------------|-----------|
| Model: | OLS | Adj. R-squared: | 0.986 |
| Method: | Least Squares | F-statistic: | 3432. |
| Date: | Tue, 24 Sep 2024 | Prob (F-statistic): | 1.79e-179 |
| Time: | 12:50:59 | Log-Likelihood: | -186.86 |
| No. Observations: | 200 | AIC: | 383.7 |
| Df Residuals: | 195 | BIC: | 400.2 |
| Df Model: | 4 | | |
| Covariance Type: | nonrobust | | |

| | \mathbf{coef} | std err | \mathbf{t} | $\mathbf{P} > \mathbf{t} $ | [0.025] | 0.975] |
|---------------------------------|-----------------|--------------------------|--------------|-----------------------------|---------|-----------|
| intercept | 5.1371 | 0.193 | 26.663 | 0.000 | 4.757 | 5.517 |
| poly(TV, degree=2, raw=True)[0] | 0.0509 | 0.002 | 22.810 | 0.000 | 0.047 | 0.055 |
| poly(TV, degree=2, raw=True)[1] | -0.0001 | 6.89 e - 06 | -15.920 | 0.000 | -0.000 | -9.61e-05 |
| Radio | 0.0352 | 0.006 | 5.959 | 0.000 | 0.024 | 0.047 |
| TV:Radio | 0.0011 | 3.47e-05 | 31.061 | 0.000 | 0.001 | 0.001 |

| Omnibus: | 169.759 | Durbin-Watson: | 2.204 |
|----------------|---------|-----------------------|------------|
| Prob(Omnibus): | 0.000 | Jarque-Bera (JB): | 4031.167 |
| Skew: | -2.988 | Prob(JB): | 0.00 |
| Kurtosis: | 24.166 | Cond. No. | 1.70e + 05 |

Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.7e+05. This might indicate that there are strong multicollinearity or other numerical problems.
 - Finally, when we add an interaction term TV * Radio to the model, we can see that the residual fit exhibits no pattern. And the R2 is 98.6%.

Compute VIFs and List Comprehension

```
vals = [VIF(X, i) for i in range(1, X.shape[1])]
print(vals)
```

[18.787830609925035, 15.885268501061871, 3.9253174186837008, 6.940088238444382]

```
vif = pd.DataFrame({"vif": vals}, index=X.columns[1:])
print(vif)
("VIF Range:", np.min(vif), np.max(vif))
```

```
vif
poly(TV, degree=2, raw=True)[0] 18.787831
poly(TV, degree=2, raw=True)[1] 15.885269
Radio 3.925317
TV:Radio 6.940088
```

('VIF Range:', 3.9253174186837008, 18.787830609925035)

- The VIF ranges are high. These can be reduced by transforming variables to mean 0.
- https://stats.stackexchange.com/questions/23538/quadratic-term-and-variance-inflation-factor-in-ols-estimation

```
Advertising["TV"] = Advertising["TV"] - Advertising["TV"].mean()

Advertising["Radio"] = Advertising["Radio"] - Advertising["Radio"].mean()
```

```
X = MS([poly("TV", raw=True, degree=2), "Radio", ("TV", "Radio")]).fit_transform(
         Advertising
)
model = sm.OLS(y, X)
results = model.fit()
summarize(results)
```

| | coef | std err | t | P> t |
|---------------------------------|---------|----------|---------|------|
| intercept | 14.7525 | 0.067000 | 219.634 | 0.0 |
| poly(TV, degree=2, raw=True)[0] | 0.0437 | 0.001000 | 84.111 | 0.0 |
| poly(TV, degree=2, raw=True)[1] | -0.0001 | 0.000007 | -15.920 | 0.0 |
| Radio | 0.1935 | 0.003000 | 64.526 | 0.0 |
| TV:Radio | 0.0011 | 0.000035 | 31.061 | 0.0 |

results.summary()

| Dep. Variable: | Sales | R-squared: | 0.986 |
|-------------------|------------------|---------------------|-----------|
| Model: | OLS | Adj. R-squared: | 0.986 |
| Method: | Least Squares | F-statistic: | 3432. |
| Date: | Tue, 24 Sep 2024 | Prob (F-statistic): | 1.79e-179 |
| Time: | 12:50:59 | Log-Likelihood: | -186.86 |
| No. Observations: | 200 | AIC: | 383.7 |
| Df Residuals: | 195 | BIC: | 400.2 |
| Df Model: | 4 | | |
| Covariance Type: | nonrobust | | |

| | coef | std err | t | $\mathbf{P} > \mathbf{t} $ | [0.025] | 0.975] |
|---------------------------------|-----------------------|---|---------|-----------------------------|---------|-----------|
| intercept | 14.7525 | 0.067 | 219.634 | 0.000 | 14.620 | 14.885 |
| poly(TV, degree=2, raw=True)[0] | 0.0437 | 0.001 | 84.111 | 0.000 | 0.043 | 0.045 |
| poly(TV, degree=2, raw=True)[1] | -0.0001 | 6.89 e - 06 | -15.920 | 0.000 | -0.000 | -9.61e-05 |
| Radio | 0.1935 | 0.003 | 64.526 | 0.000 | 0.188 | 0.199 |
| TV:Radio | 0.0011 | 3.47e-05 | 31.061 | 0.000 | 0.001 | 0.001 |

| Omnibus: | 169.759 | Durbin-Watson: | 2.204 |
|----------------|---------|-------------------|------------|
| Prob(Omnibus): | 0.000 | Jarque-Bera (JB): | 4031.167 |
| Skew: | -2.988 | Prob(JB): | 0.00 |
| Kurtosis: | 24.166 | Cond. No. | 1.49e + 04 |

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 1.49e+04. This might indicate that there are strong multicollinearity or other numerical problems.

```
vals = [VIF(X, i) for i in range(1, X.shape[1])]
print(vals)
```

[1.0172717815970211, 1.017084612216564, 1.013513326764562, 1.0075840215785734]

```
vif = pd.DataFrame({"vif": vals}, index=X.columns[1:])
print(vif)
("VIF Range:", np.min(vif), np.max(vif))
```

```
vif
poly(TV, degree=2, raw=True)[0] 1.017272
poly(TV, degree=2, raw=True)[1] 1.017085
Radio 1.013513
TV:Radio 1.007584
```

('VIF Range:', 1.0075840215785734, 1.0172717815970211)

```
allDone()
```

<IPython.lib.display.Audio object>