# Marketing

February 21, 2025

# 1 Marketing Exercise

# 1.1 Import notebook functions

```
[1]: from notebookfuncs import *
```

# 1.2 Import standard libraries

```
[2]: import numpy as np
import pandas as pd
from matplotlib.pyplot import subplots
```

# 1.3 New imports

```
[3]: import statsmodels.api as sm
```

# 1.4 Import statsmodel.objects

# 1.5 Import ISLP objects

```
[5]: import ISLP
from ISLP import models
from ISLP import load_data
from ISLP.models import ModelSpec as MS, summarize, poly
```

Inspecting objects and namespaces

```
[6]: dir()
```

```
'Latex',
'MS',
'Markdown',
'Math',
'Out',
'VIF',
'__builtin__',
'__builtins__',
'__doc__',
'__loader__',
'__name__',
'__package__',
'__spec__',
'_dh',
'_i',
'_i1',
'_i2',
'_i3',
'_i4',
'_i5',
'_i6',
'_ih',
'_ii',
_
'_iii',
'_oh',
'allDone',
'anova_lm',
'display',
'exit',
'get_ipython',
'load_data',
'models',
'np',
'open',
'pd',
'poly',
'printlatex',
'printmd',
'quit',
'sm',
'subplots',
'summarize',
'summary_table']
```

```
[7]: Advertising = pd.read_csv("Advertising.csv")
      # Drop first column
      Advertising = Advertising.iloc[:, 1:]
      Advertising.head()
 [7]:
            TV
                Radio
                       Newspaper
                                  Sales
                            69.2
         230.1
                 37.8
                                    22.1
      0
          44.5
                 39.3
                            45.1
                                    10.4
      1
      2
          17.2
                 45.9
                            69.3
                                    9.3
      3 151.5
                 41.3
                            58.5
                                    18.5
      4 180.8
                 10.8
                            58.4
                                   12.9
 [8]: Advertising.describe()
 [8]:
                     TV
                              Radio
                                       Newspaper
                                                       Sales
                         200.000000
                                      200.000000
                                                  200.000000
      count
             200.000000
             147.042500
                          23.264000
                                       30.554000
                                                   14.022500
     mean
      std
              85.854236
                          14.846809
                                       21.778621
                                                    5.217457
     min
               0.700000
                           0.000000
                                       0.300000
                                                    1.600000
      25%
              74.375000
                           9.975000
                                       12.750000
                                                   10.375000
      50%
             149.750000
                                       25.750000
                          22.900000
                                                   12.900000
      75%
             218.825000
                          36.525000
                                       45.100000
                                                   17.400000
      max
             296.400000
                          49.600000 114.000000
                                                   27.000000
     1.6 Is there a relationship between sales and advertising budget?
 [9]: y = Advertising["Sales"]
      cols = list(Advertising.columns)
      cols.remove("Sales")
      X = MS(cols).fit_transform(Advertising)
      model = sm.OLS(y, X)
      results = model.fit()
      print("F-value", results.fvalue)
      print("F-pvalue", results.f_pvalue)
      summarize(results)
     F-value 570.2707036590944
     F-pvalue 1.575227256092416e-96
 [9]:
                        std err
                                         P>|t|
                   coef
                 2.9389
      intercept
                           0.312
                                   9.422
                                            0.00
      TV
                 0.0458
                           0.001 32.809
                                            0.00
      Radio
                 0.1885
                           0.009
                                  21.893
                                            0.00
      Newspaper -0.0010
                           0.006 -0.177
                                            0.86
[10]: dir(models)
```

```
[10]: ['Column',
        'Feature',
        'FeatureSelector',
        'ModelSpec',
        'Stepwise',
        'StringIO',
        '__builtins__',
'__cached__',
        '__doc__',
'__file__',
        '__loader__',
        '__name__',
        '__package__',
        '__path__',
'__spec__',
        'bs',
        'build_columns',
        'columns',
        'contrast',
        'derived_feature',
        'generic_selector',
        'min_max_strategy',
        'model_spec',
        'np',
        'ns',
        'pca',
        'pd',
        'poly',
        'sklearn_selected',
        'sklearn_selection_path',
        'sklearn_sm',
        'sklearn_wrap',
        'strategy',
        'summarize']
```

• The p-value corresponding to the F-statistic is very low. Thus, clear evidence of a relationship between sales and advertising budget.

# [11]: dir(results)

```
'__dir__',
'__doc__',
'__eq__',
'__format__',
'__ge__',
'__getattribute__',
'__getstate__',
'__gt__',
'__hash__',
'__init__',
'__init_subclass__',
'__le__',
'__lt___',
'__module__',
'__ne__',
'__new__',
'__reduce__',
'__reduce_ex__',
'__repr__',
'__setattr__',
'__sizeof__',
'__str__',
'__subclasshook__',
'__weakref__',
'_abat_diagonal',
' cache',
'_data_attr',
'_data_in_cache',
'_get_robustcov_results',
'_get_wald_nonlinear',
'_is_nested',
'_transform_predict_exog',
'_use_t',
'_wexog_singular_values',
'aic',
'bic',
'bse',
'centered_tss',
'compare_f_test',
'compare_lm_test',
'compare_lr_test',
'condition_number',
'conf_int',
'conf_int_el',
'cov_HCO',
'cov_HC1',
'cov_HC2',
```

```
'cov_HC3',
'cov_kwds',
'cov_params',
'cov_type',
'df_model',
'df_resid',
'diagn',
'eigenvals',
'el_test',
'ess',
'f_pvalue',
'f_test',
'fittedvalues',
'fvalue',
'get_influence',
'get_prediction',
'get_robustcov_results',
'info_criteria',
'initialize',
'k_constant',
'llf',
'load',
'model',
'mse_model',
'mse_resid',
'mse_total',
'nobs',
'normalized_cov_params',
'outlier_test',
'params',
'predict',
'pvalues',
'remove_data',
'resid',
'resid_pearson',
'rsquared',
'rsquared_adj',
'save',
'scale',
'ssr',
'summary',
'summary2',
't_test',
't_test_pairwise',
'tvalues',
'uncentered_tss',
'use_t',
```

```
'wald_test',
'wald_test_terms',
'wresid']
```

# 1.7 How strong is the relationship?

Covariance Type:

[12]: results.summary()

[12]:

Dep. Variable:	Sales	R-squared:	0.897
Model:	OLS	Adj. R-squared:	0.896
Method:	Least Squares	F-statistic:	570.3
Date:	Fri, 21 Feb 2025	Prob (F-statistic):	1.58e-96
Time:	15:47:55	Log-Likelihood:	-386.18
No. Observations:	200	AIC:	780.4
Df Residuals:	196	BIC:	793.6
Df Model:	3		

	$\mathbf{coef}$	std err	t	$\mathbf{P} >  \mathbf{t} $	[0.025]	0.975]	_
intercept	2.9389	0.312	9.422	0.000	2.324	3.554	
$\mathbf{TV}$	0.0458	0.001	32.809	0.000	0.043	0.049	
Radio	0.1885	0.009	21.893	0.000	0.172	0.206	
Newspaper	-0.0010	0.006	-0.177	0.860	-0.013	0.011	

nonrobust

Omnibus:	60.414	Durbin-Watson:	2.084
Prob(Omnibus):	0.000	Jarque-Bera (JB):	151.241
Skew:	-1.327	Prob(JB):	1.44e-33
Kurtosis:	6.332	Cond. No.	454.

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[13]: y.mean()

[13]: 14.0225

[14]: results.resid.std()

[14]: 1.6727572743844117

[15]: (results.resid.std() / y.mean()) \* 100

[15]: 11.929094486606608

• The residual standard error (RSE) is 1.67 and the mean value of the response is 14.023 which translates to a percentage error of roughly 11.93%

```
[16]: ("R-squared", results.rsquared, "Adjusted R-squared", results.rsquared_adj)
```

[16]: ('R-squared', 0.8972106381789522, 'Adjusted R-squared', 0.8956373316204668)

• The R2 explains about 90% of the variance in Sales.

### 1.8 Which media are associated with Sales?

• The low p-values for Radio and TV suggest that only they are related to Sales.

### 1.9 How large is the association between each medium and sales?

```
[17]: results.conf_int(alpha=0.05)

[17]: 0 1
intercept 2.323762 3.554016
TV 0.043014 0.048516
Radio 0.171547 0.205513
Newspaper -0.012616 0.010541
```

- The confidence intervals for TV and Radio are narrow and far from zero. This provides evidence that these media are related to sales.
- The interval for Newspaper includes zero indicating that it is not statistically significant given values of TV and Radio.

```
[18]: vals = [VIF(X, i) for i in range(1, X.shape[1])]
print(vals)
```

#### [1.00461078493965, 1.1449519171055353, 1.1451873787239288]

- The VIF scores are 1.005, 1.145 and 1.145 respectively for TV, radio and newspaper. These suggest no evidence of collinearity as an explnation for wide standard errors for newspaper.
- In order to assess the association of each medium individually on sales, we can perform three separate linear regressions.

```
[19]: TV = MS(["TV"]).fit_transform(Advertising)
    model = sm.OLS(y, TV)
    results = model.fit()
    print(summarize(results))
    Radio = MS(["Radio"]).fit_transform(Advertising)
    model = sm.OLS(y, Radio)
    results = model.fit()
    print(summarize(results))
    Newspaper = MS(["Newspaper"]).fit_transform(Advertising)
    model = sm.OLS(y, Newspaper)
    results = model.fit()
    print(summarize(results))
```

```
std err
                                    P>|t|
             coef
                                  t
intercept 7.0326
                     0.458
                                       0.0
                            15.360
TV
           0.0475
                     0.003 17.668
                                       0.0
             coef
                   std err
                                  t
                                    P>|t|
intercept 9.3116
                     0.563 16.542
                                       0.0
```

```
Radio
           0.2025
                     0.020
                              9.921
                                       0.0
                                   t P>|t|
              coef
                    std err
intercept
           12.3514
                      0.621
                             19.876
                                     0.000
Newspaper
            0.0547
                      0.017
                               3.300 0.001
```

Looking at the p-values, there is evidence of a strong association b/w TV and sales and radio and sales. There is evidence of a mild association between Newspaper and sales when TV and radio are ignored.

# 1.10 How accurately can we predict future sales?

• Given that \$100,000 is spent on TV advertising, and \$20,000 is spent on Radio advertising, we need to compute the 95% Confidence intervals for each city (i.e., the mean) and the prediction interval for a particular city (also at 95% confidence intervals).

### 1.10.1 Fit the regression dropping the Newspaper column as insignificant

```
[20]: y = Advertising["Sales"]
    cols = list(Advertising.columns)
    cols.remove("Sales")
    cols.remove("Newspaper")
    X = MS(cols).fit_transform(Advertising)
    model = sm.OLS(y, X)
    results = model.fit()
    print("F-value", results.fvalue)
    print("F-pvalue", results.f_pvalue)
    summarize(results)
```

F-value 859.6177183058211 F-pvalue 4.8273618513354486e-98

```
[20]:
                   coef
                         std err
                                          P>|t|
                                        t
      intercept 2.9211
                            0.294
                                             0.0
                                    9.919
      TV
                 0.0458
                            0.001
                                  32.909
                                             0.0
      Radio
                 0.1880
                            0.008
                                  23.382
                                             0.0
```

[21]: results.summary()

[21]:

Dep. Variable:	Sales	R-squared:	0.897
Model:	OLS	Adj. R-squared:	0.896
Method:	Least Squares	F-statistic:	859.6
Date:	Fri, 21 Feb 2025	Prob (F-statistic):	4.83e-98
Time:	15:47:56	Log-Likelihood:	-386.20
No. Observations:	200	AIC:	778.4
Df Residuals:	197	BIC:	788.3
Df Model:	2		
Covariance Type:	nonrobust		

	$\mathbf{coef}$	$\operatorname{std}$ err	$\mathbf{t}$	$\mathbf{P} \gt  \mathbf{t} $	[0.025]	0.975]
intercept	2.9211	0.294	9.919	0.000	2.340	3.502
${f TV}$	0.0458	0.001	32.909	0.000	0.043	0.048
Radio	0.1880	0.008	23.382	0.000	0.172	0.204
Omnibus:		60.022	Durbii	n:	2.081	
Prob(On	mibus):	0.000	Jarque	e-Bera (d	<b>JB</b> ): 1	148.679
Skew:		-1.323	Prob(	JB):	5	.19e-33
Kurtosis:	1	6.292	Cond.	No.		425.

#### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
[22]: design = MS(["TV", "Radio"])
  new_df = pd.DataFrame({"TV": [100], "Radio": [20]})
  print(new_df)
  new_X = design.fit_transform(new_df)
  new_predictions = results.get_prediction(new_X)
  new_predictions.predicted_mean

    TV Radio
    0 100 20

[22]: array([11.25646595])
```

### 1.10.2 We predict the confidence intervals at 95% as follows:

```
[23]: new_predictions.conf_int(alpha=0.05)

[23]: array([[10.98525445, 11.52767746]])
```

### 1.10.3 We predict the prediction interval for a particular city as follows:

```
[24]: new_predictions.conf_int(alpha=0.05, obs=True)
```

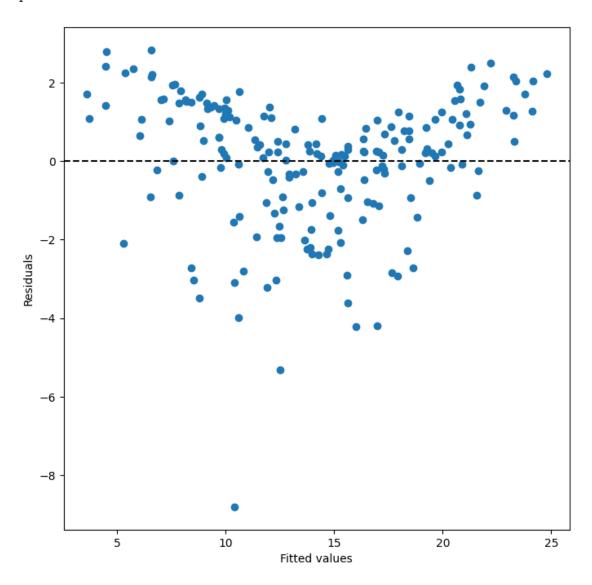
```
[24]: array([[ 7.92961607, 14.58331584]])
```

• Both intervals are centered at 11,256 but the prediction intervals are wider reflecting the additional uncertainty around sales for a particular city as against the average sales for many locations.

### 1.10.4 Is the relationship linear?

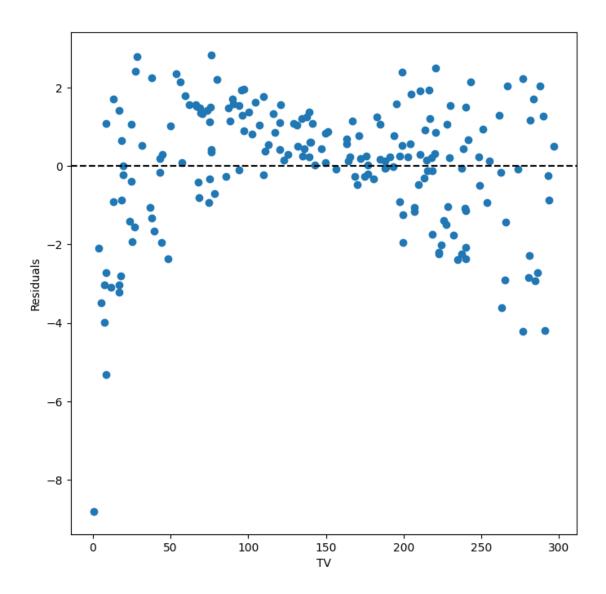
```
[25]: __, ax = subplots(figsize=(8, 8))
    ax.scatter(results.fittedvalues, results.resid)
    ax.set_xlabel("Fitted values")
    ax.set_ylabel("Residuals")
    ax.axhline(0, c="k", ls="--")
```

[25]: <matplotlib.lines.Line2D at 0x752ab85c63c0>



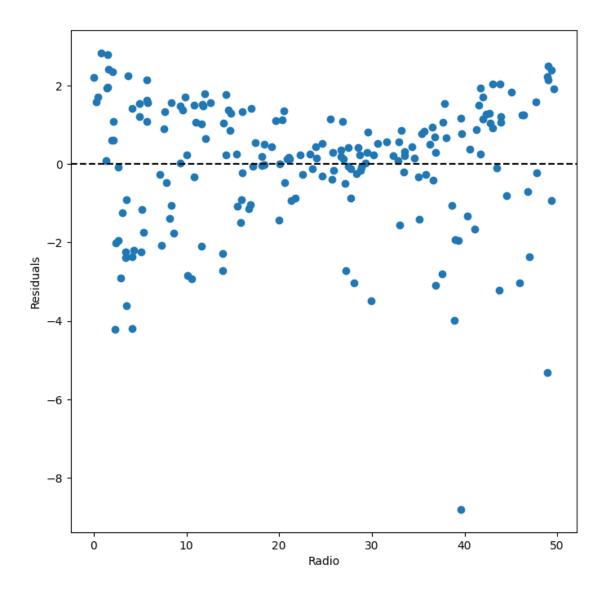
```
[26]: __, ax = subplots(figsize=(8, 8))
ax.scatter(Advertising["TV"], results.resid)
ax.set_xlabel("TV")
ax.set_ylabel("Residuals")
ax.axhline(0, c="k", ls="--")
```

[26]: <matplotlib.lines.Line2D at 0x752ab85c4170>



```
[27]: __, ax = subplots(figsize=(8, 8))
    ax.scatter(Advertising["Radio"], results.resid)
    ax.set_xlabel("Radio")
    ax.set_ylabel("Residuals")
    ax.axhline(0, c="k", ls="--")
```

[27]: <matplotlib.lines.Line2D at 0x752ab5d36600>



• There is evidence of non-linearity in the model from the residuals plotted against the fitted values. Looking at the residuals versus predictors plots, it appears that TV is a better candidate for quadratification.

```
[28]: X = MS([poly("TV", degree=2, raw=True), "Radio"]).fit_transform(Advertising)
model = sm.OLS(y, X)
results = model.fit()
summarize(results)
```

```
[28]:
                                                                    P>|t|
                                           coef
                                                   std err
                                                                 t
      intercept
                                         1.2876
                                                 0.359000
                                                             3.588
                                                                       0.0
      poly(TV, degree=2, raw=True)[0]
                                                            15.736
                                         0.0784
                                                 0.005000
                                                                       0.0
      poly(TV, degree=2, raw=True)[1] -0.0001
                                                 0.000017
                                                                       0.0
                                                            -6.775
      Radio
                                         0.1930
                                                 0.007000
                                                            26.465
                                                                       0.0
```

# [29]: results.summary()

[29]:

Dep. Variable:	Sales	R-squared:	0.917
Model:	OLS	Adj. R-squared:	0.915
Method:	Least Squares	F-statistic:	719.0
Date:	Fri, 21 Feb 2025	Prob (F-statistic):	1.80e-105
Time:	15:47:57	Log-Likelihood:	-365.16
No. Observations:	200	AIC:	738.3
Df Residuals:	196	BIC:	751.5
Df Model:	3		
Covariance Type:	nonrobust		

	coef	std err	t	$P> \mathbf{t} $	[0.025]	0.975
intercept	1.2876	0.359	3.588	0.000	0.580	1.995
poly(TV, degree=2, raw=True)[0]	0.0784	0.005	15.736	0.000	0.069	0.088
poly(TV, degree=2, raw=True)[1]	-0.0001	1.68e-05	-6.775	0.000	-0.000	-8.05e-05
Radio	0.1930	0.007	26.465	0.000	0.179	0.207

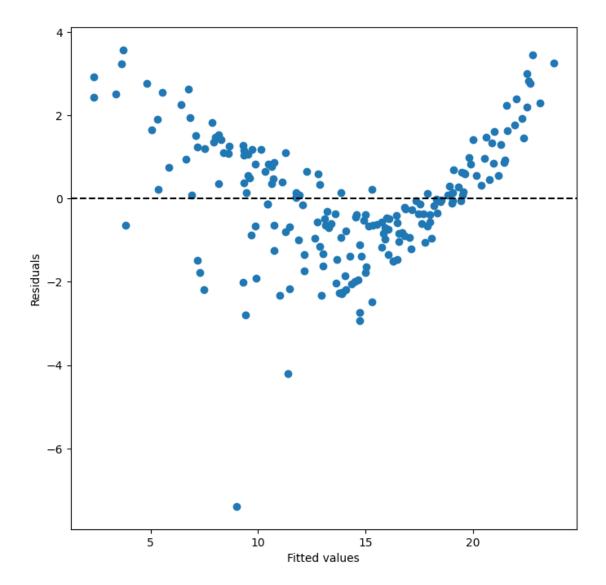
Omnibus:	19.524	Durbin-Watson:	2.136
Prob(Omnibus):	0.000	Jarque-Bera (JB):	44.712
Skew:	-0.413	Prob(JB):	1.95e-10
Kurtosis:	5.164	Cond. No.	1.29e + 05

#### Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.29e+05. This might indicate that there are strong multicollinearity or other numerical problems.

```
[30]: __, ax = subplots(figsize=(8, 8))
ax.scatter(results.fittedvalues, results.resid)
ax.set_xlabel("Fitted values")
ax.set_ylabel("Residuals")
ax.axhline(0, c="k", ls="--")
```

[30]: <matplotlib.lines.Line2D at 0x752ab5de63c0>



While the fit has improved as seen from the R2 increasing by 2 percentage points, there is still some non-linearity visible in the residuals plot against fitted values.

# References:

https://www.kellogg.northwestern.edu/faculty/weber/emp/\_session\_3/nonlinearities.

https://online.stat.psu.edu/stat462/node/120/

# 1.10.5 Is there synergy among the advertising media?

Synergy implies an interaction effect. That's what we test out now.

```
→fit_transform(
           Advertising
      model = sm.OLS(y, X)
      results = model.fit()
      summarize(results)
[31]:
                                             coef
                                                                       P>|t|
                                                    std err
                                                                    t
      intercept
                                          5.1371
                                                   0.193000
                                                              26.663
                                                                          0.0
      poly(TV, degree=2, raw=True)[0]
                                          0.0509
                                                   0.002000
                                                              22.810
                                                                          0.0
      poly(TV, degree=2, raw=True)[1] -0.0001
                                                   0.000007 - 15.920
                                                                          0.0
      Radio
                                          0.0352
                                                   0.006000
                                                                5.959
                                                                          0.0
      TV:Radio
                                          0.0011
                                                   0.000035
                                                              31.061
                                                                          0.0
[32]:
      results.summary()
[32]:
                Dep. Variable:
                                          Sales
                                                       R-squared:
                                                                               0.986
                                           OLS
                Model:
                                                       Adj. R-squared:
                                                                               0.986
                Method:
                                      Least Squares
                                                       F-statistic:
                                                                               3432.
                                                       Prob (F-statistic):
                Date:
                                     Fri, 21 Feb 2025
                                                                             1.79e-179
                Time:
                                         15:47:57
                                                       Log-Likelihood:
                                                                              -186.86
                No. Observations:
                                           200
                                                       AIC:
                                                                               383.7
                Df Residuals:
                                                       BIC:
                                           195
                                                                               400.2
                Df Model:
                                            4
                Covariance Type:
                                        nonrobust
                                              coef
                                                      std err
                                                                  \mathbf{t}
                                                                        P > |t|
                                                                                 [0.025]
                                                                                          0.975
       intercept
                                             5.1371
                                                       0.193
                                                                26.663
                                                                         0.000
                                                                                 4.757
                                                                                           5.517
                                                                22.810
       poly(TV, degree=2, raw=True)[0]
                                             0.0509
                                                       0.002
                                                                         0.000
                                                                                 0.047
                                                                                           0.055
       poly(TV, degree=2, raw=True)[1]
                                             -0.0001
                                                      6.89e-06
                                                               -15.920
                                                                         0.000
                                                                                 -0.000
                                                                                         -9.61e-05
       Radio
                                             0.0352
                                                       0.006
                                                                5.959
                                                                         0.000
                                                                                 0.024
                                                                                           0.047
       TV:Radio
                                             0.0011
                                                      3.47e-05
                                                                31.061
                                                                         0.000
                                                                                 0.001
                                                                                           0.001
                    Omnibus:
                                        169.759
                                                  Durbin-Watson:
                                                                          2.204
                    Prob(Omnibus):
                                         0.000
                                                  Jarque-Bera (JB):
                                                                         4031.167
                    Skew:
                                         -2.988
                                                  Prob(JB):
                                                                           0.00
                    Kurtosis:
                                                  Cond. No.
                                        24.166
                                                                        1.70e + 05
```

[31]: X = MS([poly("TV", raw=True, degree=2), "Radio", ("TV", "Radio")]).

#### Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.7e+05. This might indicate that there are strong multicollinearity or other numerical problems.
  - Finally, when we add an interaction term TV \* Radio to the model, we can see that the residual fit exhibits no pattern. And the R2 is 98.6%.

# 1.10.6 Compute VIFs and List Comprehension

```
[33]: vals = [VIF(X, i) for i in range(1, X.shape[1])]
      print(vals)
     [18.787830609925035, 15.885268501061871, 3.9253174186837008, 6.940088238444382]
[34]: vif = pd.DataFrame({"vif": vals}, index=X.columns[1:])
      print(vif)
      ("VIF Range:", np.min(vif), np.max(vif))
                                             vif
     poly(TV, degree=2, raw=True)[0]
                                       18.787831
     poly(TV, degree=2, raw=True)[1]
                                       15.885269
     Radio
                                        3.925317
     TV:Radio
                                        6.940088
[34]: ('VIF Range:', 3.9253174186837008, 18.787830609925035)
        • The VIF ranges are high. These can be reduced by transforming variables to mean 0.
        • https://stats.stackexchange.com/questions/23538/quadratic-term-and-variance-inflation-fac
[35]: Advertising["TV"] = Advertising["TV"] - Advertising["TV"].mean()
      Advertising["Radio"] = Advertising["Radio"] - Advertising["Radio"].mean()
[36]: X = MS([poly("TV", raw=True, degree=2), "Radio", ("TV", "Radio")]).
       →fit_transform(
          Advertising
      model = sm.OLS(y, X)
      results = model.fit()
      summarize(results)
[36]:
                                          coef
                                                 std err
                                                                 t P>|t|
                                        14.7525 0.067000 219.634
      intercept
                                                                      0.0
      poly(TV, degree=2, raw=True)[0]
                                        0.0437 0.001000
                                                            84.111
                                                                      0.0
      poly(TV, degree=2, raw=True)[1]
                                       -0.0001 0.000007 -15.920
                                                                      0.0
      Radio
                                        0.1935 0.003000
                                                            64.526
                                                                      0.0
      TV:Radio
                                        0.0011 0.000035
                                                            31.061
                                                                      0.0
[37]: results.summary()
[37]:
```

Dep. Variable:	Sales	R-squared:	0.986
Model:	OLS	Adj. R-squared:	0.986
Method:	Least Squares	F-statistic:	3432.
Date:	Fri, 21 Feb 2025	Prob (F-statistic):	1.79e-179
Time:	15:47:57	Log-Likelihood:	-186.86
No. Observations:	200	AIC:	383.7
Df Residuals:	195	BIC:	400.2
Df Model:	4		
Covariance Type:	nonrobust		

	$\mathbf{coef}$	$\operatorname{std}$ err	$\mathbf{t}$	$\mathbf{P} \gt  \mathbf{t} $	[0.025]	0.975]
intercept	14.7525	0.067	219.634	0.000	14.620	14.885
poly(TV, degree=2, raw=True)[0]	0.0437	0.001	84.111	0.000	0.043	0.045
poly(TV, degree=2, raw=True)[1]	-0.0001	6.89 e - 06	-15.920	0.000	-0.000	-9.61e-05
Radio	0.1935	0.003	64.526	0.000	0.188	0.199
TV:Radio	0.0011	3.47e-05	31.061	0.000	0.001	0.001

Omnibus:	169.759	<b>Durbin-Watson:</b>	2.204
Prob(Omnibus):	0.000	Jarque-Bera (JB):	4031.167
Skew:	-2.988	Prob(JB):	0.00
Kurtosis:	24.166	Cond. No.	1.49e + 04

#### Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 1.49e+04. This might indicate that there are strong multicollinearity or other numerical problems.

```
[38]: vals = [VIF(X, i) for i in range(1, X.shape[1])]
      print(vals)
```

[1.0172717815970211, 1.017084612216564, 1.013513326764562, 1.0075840215785734]

```
[39]: vif = pd.DataFrame({"vif": vals}, index=X.columns[1:])
      print(vif)
      ("VIF Range:", np.min(vif), np.max(vif))
```

```
vif
```

poly(TV, degree=2, raw=True)[0] 1.017272 poly(TV, degree=2, raw=True)[1] 1.017085 Radio 1.013513 TV:Radio 1.007584

[39]: ('VIF Range:', 1.0075840215785734, 1.0172717815970211)

# [40]: allDone()

<IPython.lib.display.Audio object>