

AppliedEx13

February 21, 2025

1 Applied: Exercise 13

2 Import notebook funcs

```
[1]: from notebookfuncs import *
```

2.1 Import libraries

```
[2]: from ISLP import load_data
from ISLP import confusion_table
from ISLP.models import (ModelSpec as MS , summarize)
from summarytools import dfSummary
import numpy as np
from scipy.stats import skew
from scipy.stats import boxcox
from scipy.optimize import curve_fit
import klib
import seaborn as sns
import matplotlib.pyplot as plt
import matplotlib.ticker as mtick
import statsmodels.api as sm
from statsmodels.tools.tools import add_constant
import pandas as pd
from sklearn.metrics import confusion_matrix, classification_report
from sklearn.metrics import ConfusionMatrixDisplay
from sklearn.discriminant_analysis import (LinearDiscriminantAnalysis as LDA ,
↳ QuadraticDiscriminantAnalysis as QDA)
from sklearn.naive_bayes import GaussianNB
from sklearn.neighbors import KNeighborsClassifier
```

2.2 Exercise 13

This question should be answered using the Weekly data set, which is part of the ISLP package. This data is similar in nature to the Smarket data from this chapter's lab, except that it contains 1,089 weekly returns for 21 years, from the beginning of 1990 to the end of 2010.

```
[3]: Weekly = load_data("Weekly")
Weekly["LogVolume"] = np.log(Weekly["Volume"])
Weekly = klib.convert_datatypes(Weekly)
print(Weekly.dtypes)
Weekly.head()
```

```
Year          int16
Lag1          float32
Lag2          float32
Lag3          float32
Lag4          float32
Lag5          float32
Volume        float32
Today         float32
Direction     category
LogVolume     float32
dtype: object
```

```
[3]:   Year  Lag1  Lag2  Lag3  Lag4  Lag5  Volume  Today  Direction  \
0  1990  0.816  1.572 -3.936 -0.229 -3.484  0.154976 -0.270      Down
1  1990 -0.270  0.816  1.572 -3.936 -0.229  0.148574 -2.576      Down
2  1990 -2.576 -0.270  0.816  1.572 -3.936  0.159837  3.514       Up
3  1990  3.514 -2.576 -0.270  0.816  1.572  0.161630  0.712       Up
4  1990  0.712  3.514 -2.576 -0.270  0.816  0.153728  1.178       Up

   LogVolume
0  -1.864485
1  -1.906672
2  -1.833598
3  -1.822446
4  -1.872571
```

```
[4]: # Calculate skew for Volume, LogVolume, sqrt(Volume), sqrt4(Volume), Volume ^ 2
print("Skew for Volume: ", skew(Weekly["Volume"], axis=0, bias=True))
print("Skew for LogVolume: ", skew(Weekly["LogVolume"], axis=0, bias=True))
print("Skew for Sqrt(Volume): ", skew(np.sqrt(Weekly["Volume"]), axis=0,
    ↪ bias=True))
print("Skew for Sqrt4(Volume): ", skew(np.sqrt(np.sqrt(Weekly["Volume"])),
    ↪ axis=0, bias=True))
print("Skew for Volume ** 2: ", skew(Weekly["Volume"] ** 2, axis=0, bias=True))
```

```
Skew for Volume:  1.6181865242606417
Skew for LogVolume:  0.05204035343976238
Skew for Sqrt(Volume):  0.8527756846731206
Skew for Sqrt4(Volume):  0.4482314175369111
Skew for Volume ** 2:  3.03324753476614
```

We transform column *Volume* to *LogVolume* since this is the most symmetrical among the transformations *sqrt*, *sqrt4* and *log* (as evidenced by its low skew value).

Alternatively, we could use the [Box-Cox](#) series of transformations to convert Volume to a normally distributed variable.

```
[5]: Weekly["BoxCoxVolume"], lambda_vol = boxcox(Weekly["Volume"])
      print("lambda: :", lambda_vol)
      print("Skew for BoxCoxVolume: ", skew(Weekly["BoxCoxVolume"], axis=0,
      ↪ bias=True))
```

```
lambda: : -0.02702330888725645
Skew for BoxCoxVolume:  0.010558441792967627
```

Here, we see that the value of lambda_vol is almost zero and hence, the BoxCox transformation is the log transformation approximately.

```
[6]: Weekly.shape
```

```
[6]: (1089, 11)
```

2.2.1 (a)

Produce some numerical and graphical summaries of the Weekly data. Do there appear to be any patterns?

```
[7]: dfSummary(Weekly)
```

```
[7]: <pandas.io.formats.style.Styler at 0x718640a3c530>
```

```
[8]: klib.corr_plot(Weekly);
```

Feature-correlation (pearson)



We can see that the correlation between Year and LogVolume is 0.98 which is much higher than the correlation between Year and Volume which is 0.84. That's because log transformation is non-linear and the original relation was non-linear as seen from the plot below. The same applies for BoxCoxVolume since it is approximately the log transformation of Volume.

```
[9]: Weekly["Week"] = np.arange(1, Weekly.shape[0] + 1)
Years_Break = Weekly.groupby("Year").first()
plt.figure(figsize=(16, 16))
plt.subplot(3,1,1)
plt.plot(Weekly["Volume"], label="Volume", c="r");
plt.xticks(ticks=Years_Break.Week, labels=Years_Break.index);
plt.gca().yaxis.set_major_formatter(mtick.PercentFormatter())

# objective function
def objective(x, a, b, c, d, e):
```

```

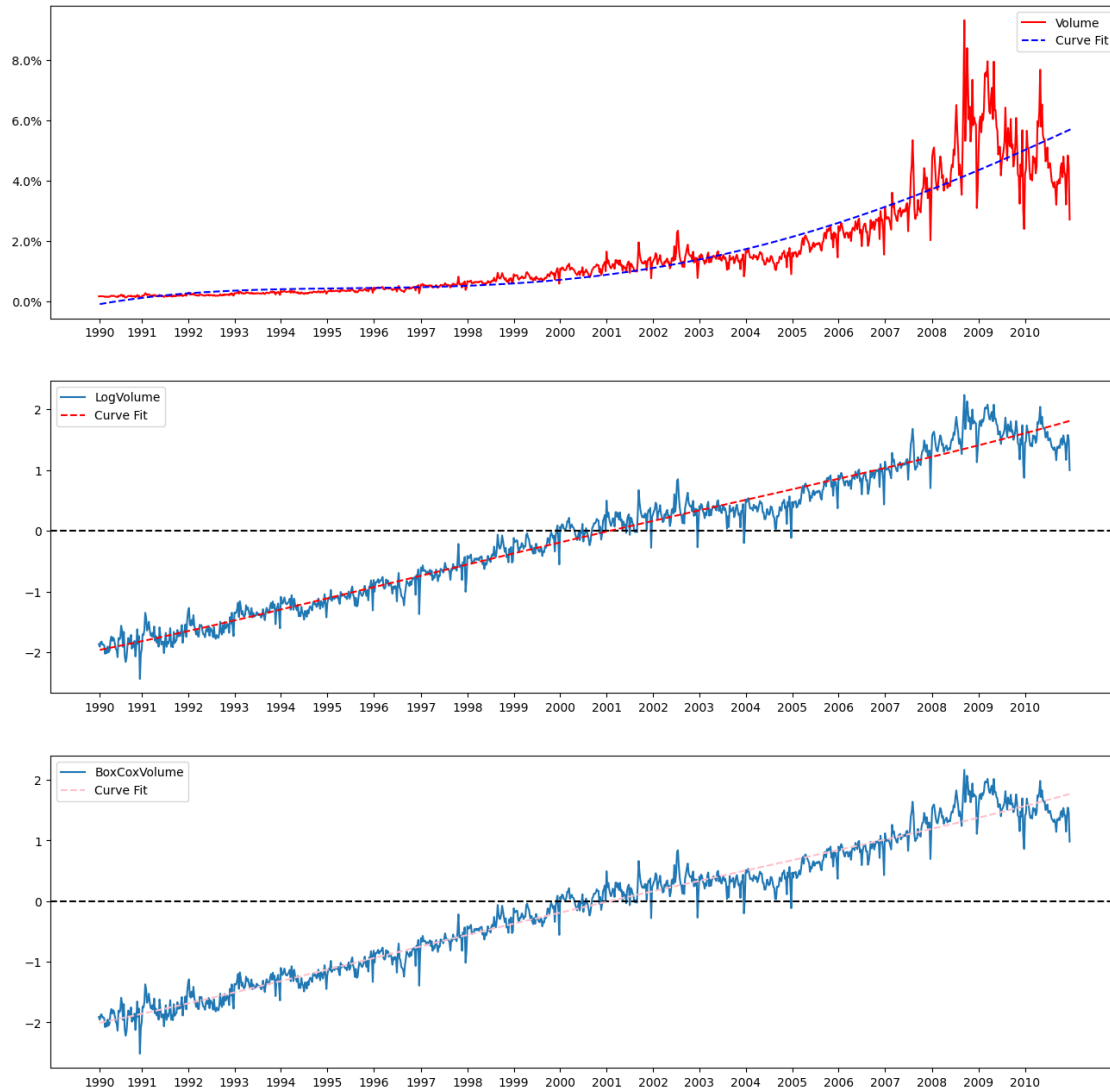
    return a * x + b * x ** 2 + c * x ** 3 + d * x ** 4 + e

# fit curve
popt, _ = curve_fit(objective, Weekly["Week"],Weekly["Volume"])
a, b, c, d, e = popt
y_new = objective(Weekly["Week"], a , b, c, d, e)
plt.plot(Weekly["Week"], y_new, "--", color="blue", label="Curve Fit")
plt.legend();

plt.subplot(3,1,2)
plt.plot(Weekly["LogVolume"], label="LogVolume");
plt.xticks(ticks=Years_Break.Week,labels=Years_Break.index);
plt.axhline(y=0, color="black", linestyle="--")
popt, _ = curve_fit(objective, Weekly["Week"],Weekly["LogVolume"])
a, b, c, d, e = popt
y_new = objective(Weekly["Week"], a , b, c, d, e)
plt.plot(Weekly["Week"], y_new, "--", color="red", label="Curve Fit")
plt.legend();

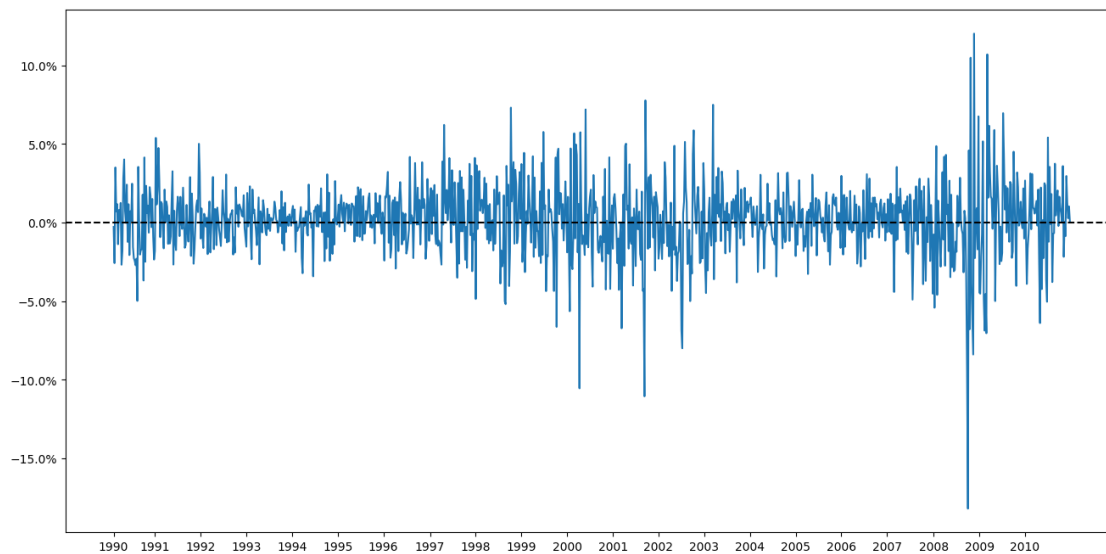
plt.subplot(3,1,3)
plt.plot(Weekly["BoxCoxVolume"], label="BoxCoxVolume");
plt.xticks(ticks=Years_Break.Week,labels=Years_Break.index);
plt.axhline(y=0, color="black", linestyle="--")
popt, _ = curve_fit(objective, Weekly["Week"],Weekly["BoxCoxVolume"])
a, b, c, d, e = popt
y_new = objective(Weekly["Week"], a , b, c, d, e)
plt.plot(Weekly["Week"], y_new, "--", color="pink", label="Curve Fit")
plt.legend();

```



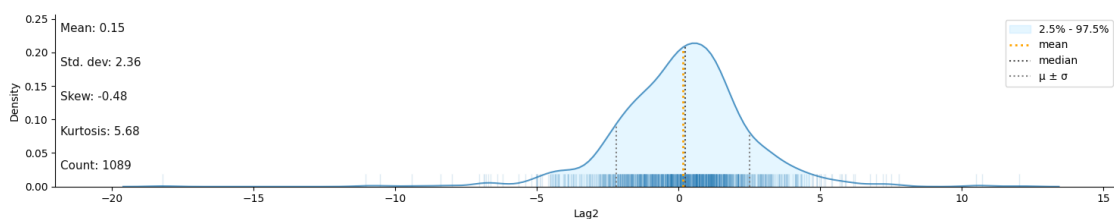
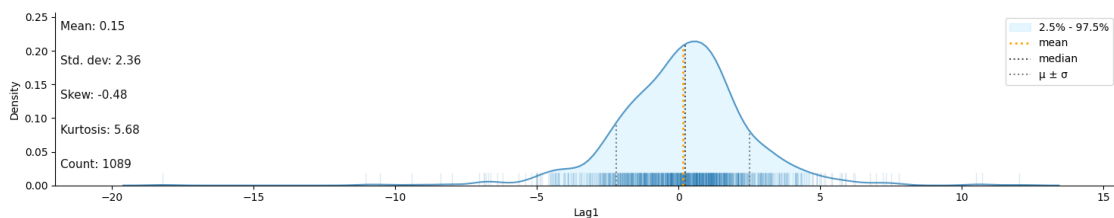
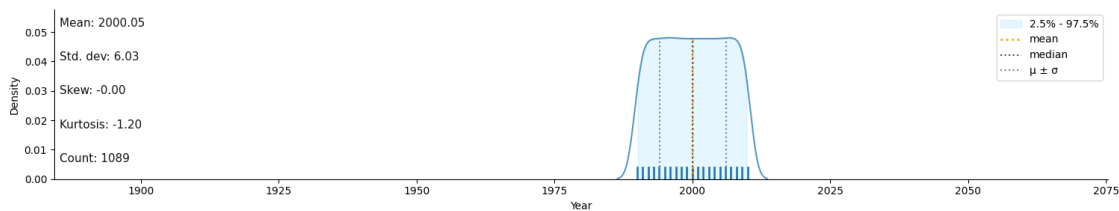
Here, we can see from the curve fit where we specified a cubic objective function, the Volume chart displays non-linearity but the LogVolume and BoxCoxVolume fits are straight lines.

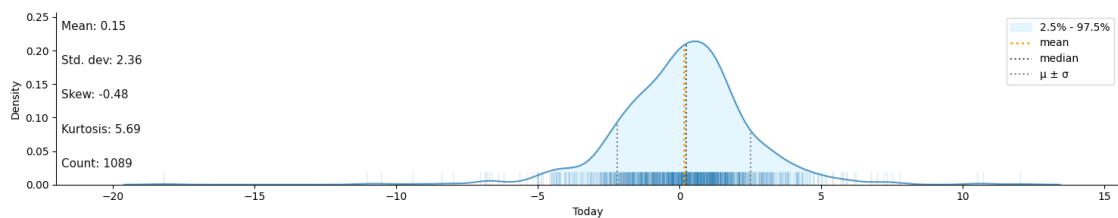
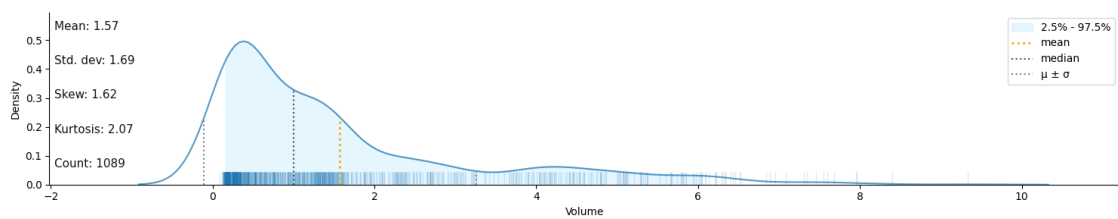
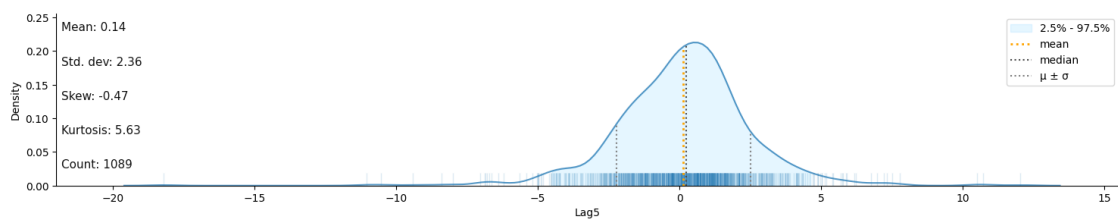
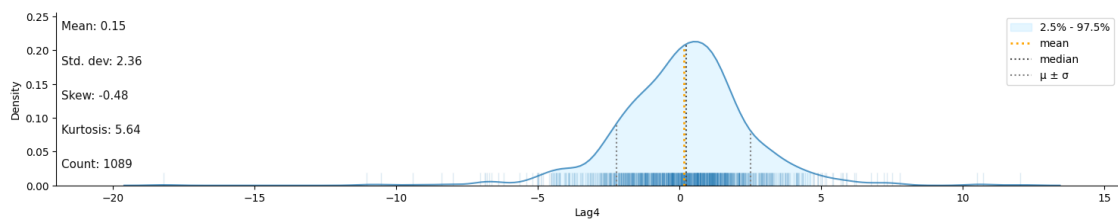
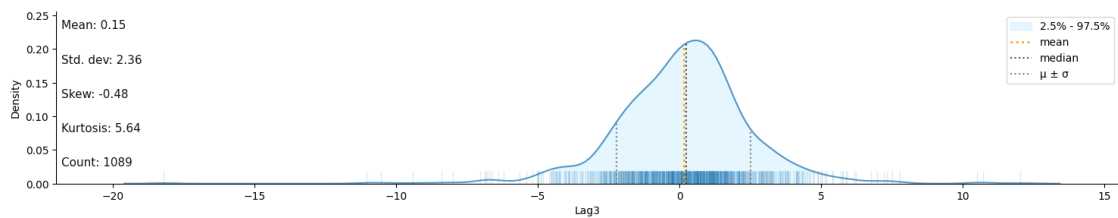
```
[10]: plt.figure(figsize=(16, 8))
plt.plot(Weekly["Week"],Weekly["Today"])
plt.xticks(ticks=Years_Break.Week,labels=Years_Break.index)
plt.gca().yaxis.set_major_formatter(mtick.PercentFormatter())
plt.axhline(y=0, color="k", linestyle="--");
```

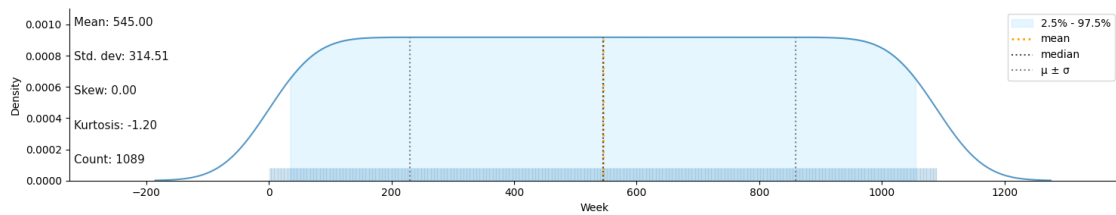
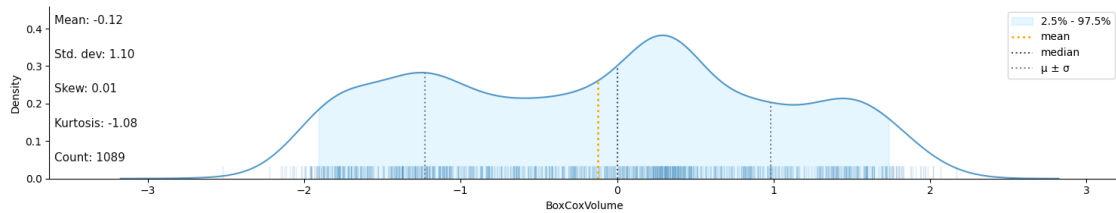
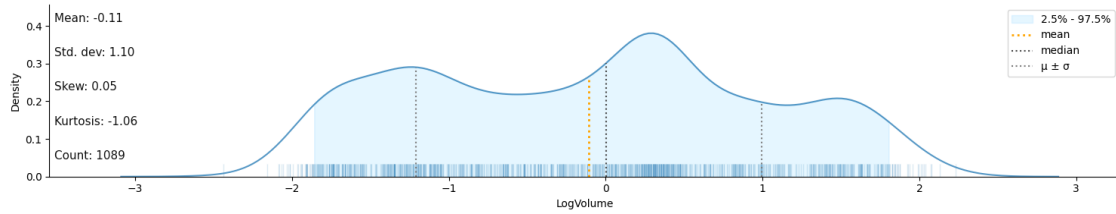


Here, we can see that the market go through periods of low and high volatility. Events such as market crashes exhibit high variance/volatility.

```
[11]: klib.dist_plot(Weekly);
```







Skewness Skewness is a measure of asymmetry or distortion of symmetric distribution. It measures the deviation of the given distribution of a random variable from a symmetric distribution, such as normal distribution. A normal distribution is without any skewness, as it is symmetrical on both sides.

Kurtosis Negative kurtosis, also known as platykurtic, is a measure of a distribution's thin tails, meaning that outliers are infrequent:

Explanation Kurtosis is a statistical measure that describes the shape of a distribution's tails in relation to its overall shape. It measures how often outliers occur, or the "tailedness" of the distribution.

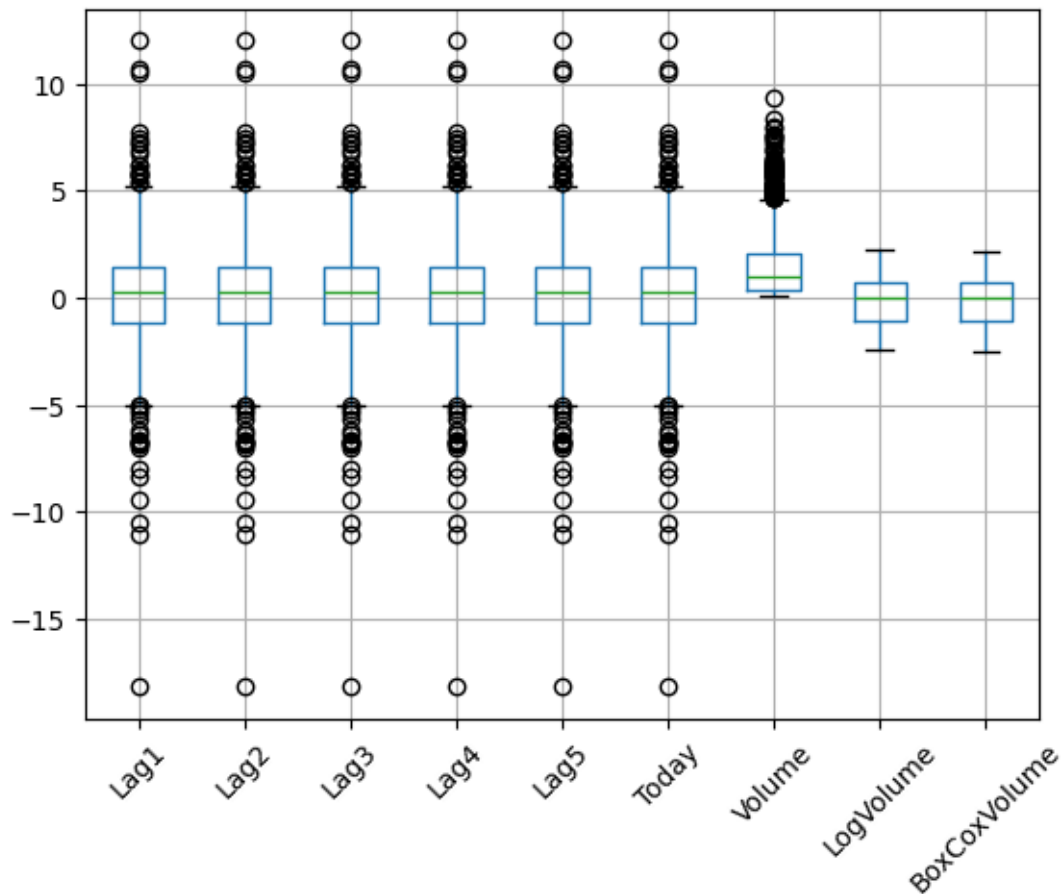
Kurtosis types A distribution with a kurtosis of 3 is considered mesokurtic, meaning it has a medium tail. A distribution with a kurtosis greater than 3 is leptokurtic, meaning it has a fat tail and a lot of outliers. A distribution with a kurtosis less than 3 is platykurtic, meaning it has a thin tail and infrequent outliers.

Kurtosis vs peakedness Kurtosis measures "tailedness," not "peakedness". A distribution can have a lower peak with high kurtosis, or a sharply peaked distribution with low kurtosis.

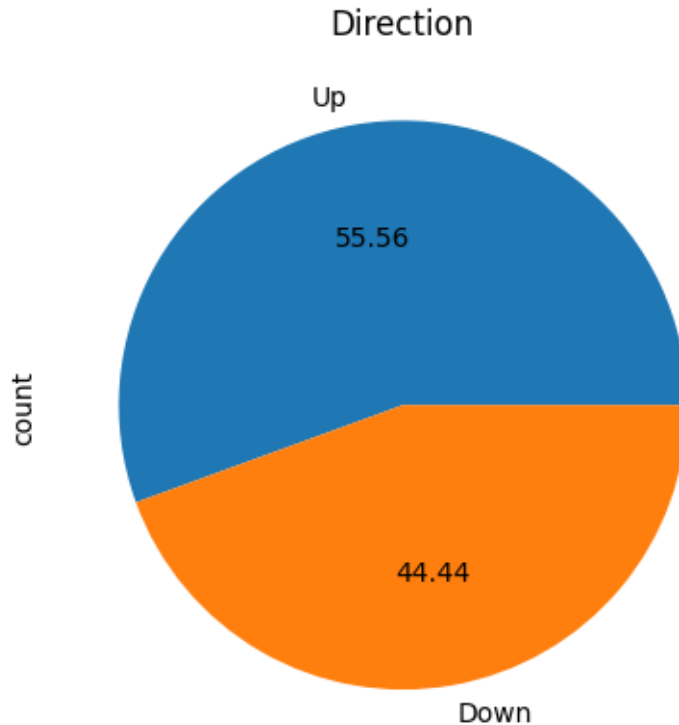
Calculating kurtosis Kurtosis is calculated mathematically as the standardized fourth moment of a distribution.

We can verify the above conclusion from kurtosis definition by plotting the boxplots for the continuous variables, Lag1 - Lag5, Today and LogVolume.

```
[12]: Weekly.boxplot(column=["Lag1","Lag2","Lag3", "Lag4", "Lag5", "Today", "Volume",  
↪ "LogVolume", "BoxCoxVolume"], rot=45);
```



```
[13]: Weekly["Direction"].value_counts().plot(kind="pie", autopct="%.  
↪ 2f", title="Direction");
```



```
[14]: nic_classifier_pct = Weekly["Direction"].value_counts()[0] / len(Weekly)
```

/tmp/ipykernel_35629/3312589537.py:1: FutureWarning: Series.__getitem__ treating keys as positions is deprecated. In a future version, integer keys will always be treated as labels (consistent with DataFrame behavior). To access a value by position, use `ser.iloc[pos]`

```
nic_classifier_pct = Weekly["Direction"].value_counts()[0] / len(Weekly)
```

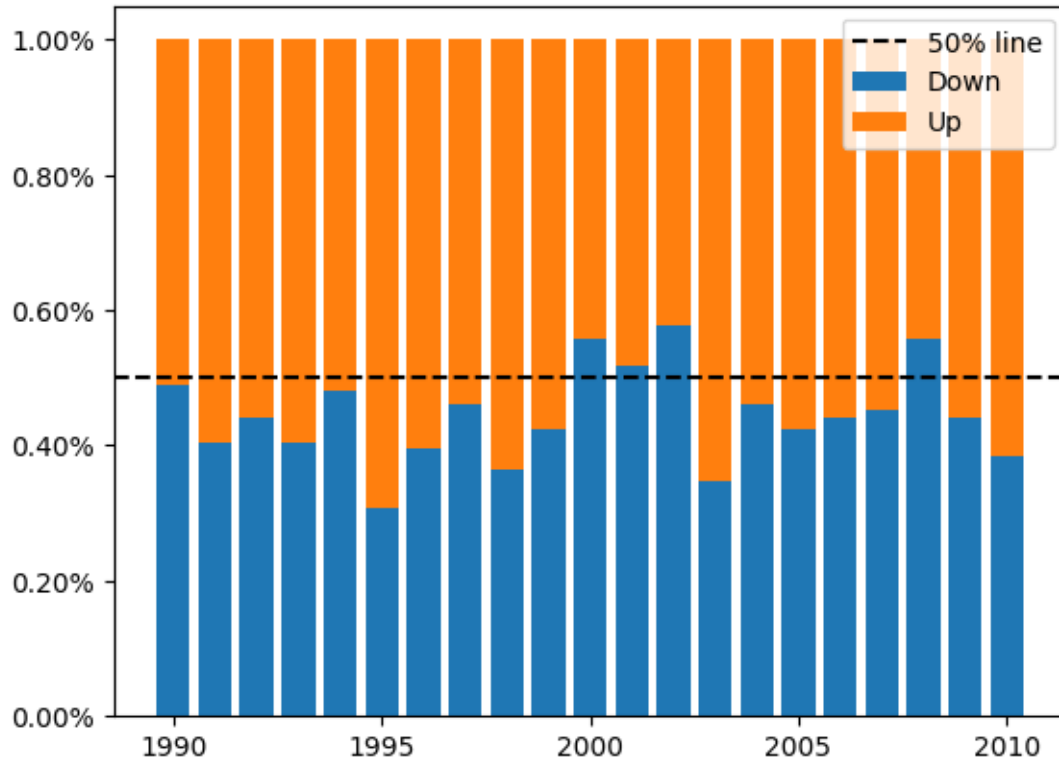
```
[14]: 0.5555555555555556
```

- Thus, we see from the pie-chart, that if we classify all responses as 'Up', we would still achieve an accuracy level of 55.56%. This is the base level which we have to improve upon.

```
[15]: bar_df = Weekly.groupby(["Year", "Direction"], observed=False).size().
      ↪reset_index(name="Counts")
downs = bar_df[bar_df.Direction == "Down"].Counts.values
ups = bar_df[bar_df.Direction == "Up"].Counts.values
downs_pct = np.divide(downs, np.add(downs, ups))
ups_pct = np.divide(ups, np.add(downs, ups))
years = bar_df["Year"].unique();
```

```
[16]: fig, ax = plt.subplots()
ax.bar(years, downs_pct, label="Down")
```

```
ax.bar(years,ups_pct, bottom=downs_pct, label="Up");
ax.axhline(y=0.5, color="k", linestyle="--", label="50% line");
ax.yaxis.set_major_formatter(mtick.PercentFormatter())
ax.legend();
```



The bar-chart displays the percentage of Ups and Downs in a year from 1990 – 2010. The Ups dominate for most years except four.

2.2.2 (b)

Use the full data set to perform a logistic regression with Direction as the response and the five lag variables plus Volume as predictors. Use the summary function to print the results. Do any of the predictors appear to be statistically significant? If so, which ones?

```
[17]: # Try to avoid using ISLP classes for anything else but to load data since it
      ↪ may not transfer well to
      # actual usage in data analysis projects
      # drop columns Today, Direction, Year, Week , Volume, LogVolume
      # We use BoxCoxVolume to regress against since it has the lowest skew value
      ↪ amongst all the transformations of the feature Volume
      allvars = Weekly[Weekly.columns.difference(['Today', 'Direction', 'Year',
      ↪ "Week", "Volume", "LogVolume"])]
```

```
# add constant term of 1s
X = add_constant(allvars)
# Convert 'Down' and 'Up' to 0s and 1s respectively
y = Weekly.Direction == 'Up'
# Use Binomial family for Logistic Regression
family = sm.families.Binomial()
glm = sm.GLM(y, X, family=family)
results = glm.fit()
summarize(results)
```

```
[17]:
```

	coef	std err	z	P> z
const	0.2247	0.062	3.606	0.000
BoxCoxVolume	-0.0515	0.056	-0.920	0.358
Lag1	-0.0413	0.026	-1.565	0.118
Lag2	0.0584	0.027	2.178	0.029
Lag3	-0.0161	0.027	-0.603	0.547
Lag4	-0.0279	0.026	-1.055	0.291
Lag5	-0.0146	0.026	-0.552	0.581

```
[18]: results.summary()
```

```
[18]:
```

Dep. Variable:	Direction	No. Observations:	1089
Model:	GLM	Df Residuals:	1082
Model Family:	Binomial	Df Model:	6
Link Function:	Logit	Scale:	1.0000
Method:	IRLS	Log-Likelihood:	-742.94
Date:	Tue, 11 Feb 2025	Deviance:	1485.9
Time:	14:08:50	Pearson chi2:	1.09e+03
No. Iterations:	4	Pseudo R-squ. (CS):	0.009426
Covariance Type:	nonrobust		

	coef	std err	z	P> z	[0.025	0.975]
const	0.2247	0.062	3.606	0.000	0.103	0.347
BoxCoxVolume	-0.0515	0.056	-0.920	0.358	-0.161	0.058
Lag1	-0.0413	0.026	-1.565	0.118	-0.093	0.010
Lag2	0.0584	0.027	2.178	0.029	0.006	0.111
Lag3	-0.0161	0.027	-0.603	0.547	-0.068	0.036
Lag4	-0.0279	0.026	-1.055	0.291	-0.080	0.024
Lag5	-0.0146	0.026	-0.552	0.581	-0.066	0.037

```
[19]: results.model.endog_names
```

```
[19]: 'Direction'
```

```
[20]: results.params
```

```
[20]: const          0.224750
BoxCoxVolume      -0.051454
```

```
Lag1          -0.041254
Lag2           0.058360
Lag3          -0.016059
Lag4          -0.027884
Lag5          -0.014559
dtype: float64
```

```
[21]: results.pvalues[results.pvalues < 0.05]
```

```
[21]: const      0.000311
      Lag2      0.029378
      dtype: float64
```

From the above, it can be deduced that **Lag2** is the only significant variable that predicts **Direction**. The positive coefficient for **Lag2** suggests that if the market had a positive return today, it is more likely that the market will rise once more in two days and vice versa. We can also see that the confidence intervals of the other parameters **Lag1**, **Lag3**, **Lag4**, **Lag5** and **LogVolume** span the value 0 and thus are not significant.

2.3 (c)

Compute the confusion matrix and overall fraction of correct predictions. Explain what the confusion matrix is telling you about the types of mistakes made by logistic regression.

```
[22]: predictions = results.predict()
      predictions.shape
```

```
[22]: (1089,)
```

```
[23]: labels = np.array(['Down']*len(Weekly))
      print(labels.shape)
      labels[predictions > 0.5] = "Up"
```

```
(1089,)
```

```
[24]: ct = confusion_table(Weekly["Direction"],
                           labels)
      print(ct)
```

Truth	Down	Up
Predicted		
Down	61	423
Up	52	553

The diagonal elements of the confusion matrix indicate correct predictions, while the off-diagonals represent incorrect predictions.

```
[25]: correct_up_preds = ct["Up"]["Up"]
      correct_down_preds = ct["Down"]["Down"]
```

```

print(f"Hence our model correctly predicted that the market would go up on {correct_up_preds} days and that it would go down on {correct_down_preds} days, for a total of {ct["Up"]["Up"]} + {ct["Down"]["Down"]} = {ct["Up"]["Up"] + ct["Down"]["Down"]} correct predictions. The np.mean() function can be used to compute the fraction of days for which the prediction was correct.")
correct_pred_perc = (ct["Up"]["Up"] + ct["Down"]["Down"]) * 100 / (ct["Up"]["Up"] + ct["Down"]["Down"] + ct["Down"]["Up"] + ct["Up"]["Down"])
print(f"In this case, logistic regression correctly predicted the movement of the market {correct_pred_perc:.1f}% of the time.")

```

Hence our model correctly predicted that the market would go up on 553 days and that it would go down on 61 days, for a total of $553 + 61 = 614$ correct predictions. The `np.mean()` function can be used to compute the fraction of days for which the prediction was correct. In this case, logistic regression correctly predicted the movement of the market 56.4% of the time.

```

[26]: accuracy = np.mean(labels == Weekly.Direction),
      ↪ (correct_up_preds+correct_down_preds) / len(Weekly)

```

```

[26]: (0.5638200183654729, 0.5638200183654729)

```

```

[27]: print(f"This accuracy of {accuracy[0]*100:.2f}% is not much better than the no information classifier's (NIC) accuracy of {nic_classifier_pct *100:.2f}% when we just guess that the market will go up all the time and achieve an accuracy level of {nic_classifier_pct*100:.2f}%.")

```

This accuracy of 56.38% is not much better than the no information classifier's (NIC) accuracy of 55.56% when we just guess that the market will go up all the time and achieve an accuracy level of 55.56%.

```

[28]: print(f"100 - {accuracy[0]*100:.1f} = {100 - accuracy[0]*100:.1f}% is the training error rate.")

```

$100 - 56.4 = 43.6\%$ is the training error rate.

As we have seen previously, the training error rate is often overly optimistic — it tends to underestimate the test error rate. In order to better assess the accuracy of the logistic regression model in this setting, we can fit the model using part of the data, and then examine how well it predicts the held out data. This will yield a more realistic error rate, in the sense that in practice we will be interested in our model's performance not on the data that we used to fit the model, but rather on days in the future for which the market's movements are unknown.

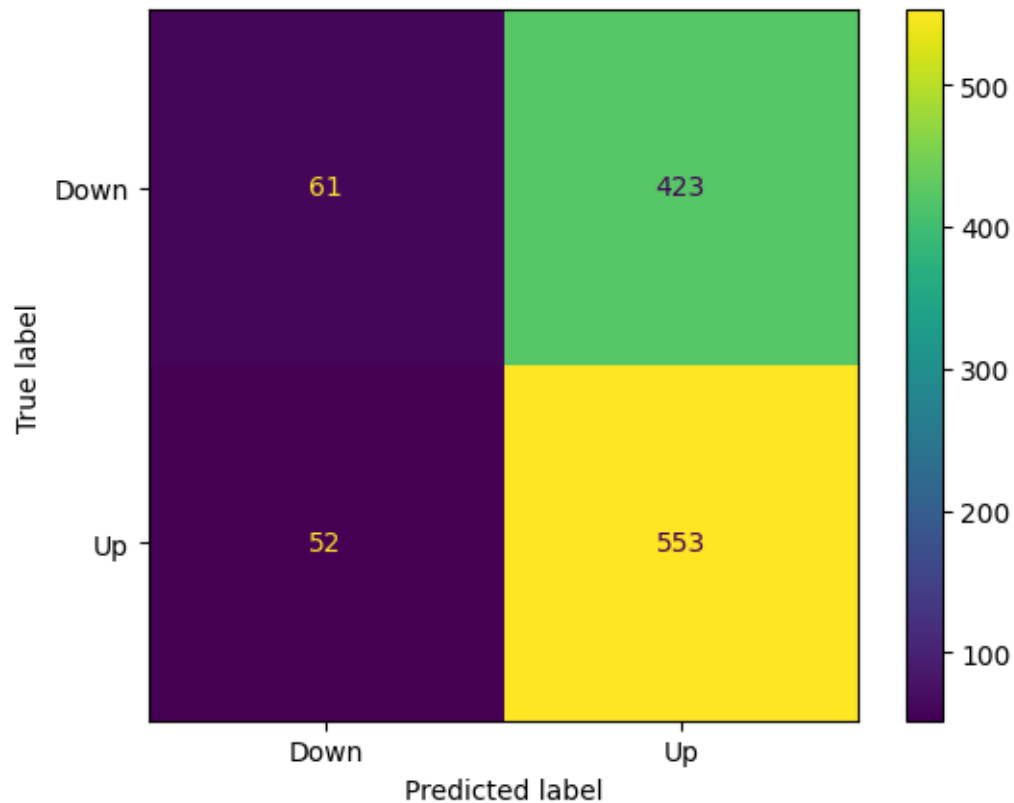
```

[29]: print(classification_report(Weekly["Direction"],
                                labels,
                                digits = 3))
cm = confusion_matrix(Weekly["Direction"],
                      labels)

```

```
disp = ConfusionMatrixDisplay(confusion_matrix=cm,
                              display_labels=["Down", "Up"])
disp.plot();
```

	precision	recall	f1-score	support
Down	0.540	0.126	0.204	484
Up	0.567	0.914	0.700	605
accuracy			0.564	1089
macro avg	0.553	0.520	0.452	1089
weighted avg	0.555	0.564	0.479	1089



```
[30]: # Getting individual values for
true_negatives, false_positives, false_negatives, true_positives = cm.ravel()
```

```
[31]: support_up = np.sum(Weekly["Direction"] == "Up")
support_down = Weekly.shape[0] - support_up
predicted_up = np.sum(labels == "Up")
```



```

predicted_down = np.sum(labels == "Down")
predicted_correctly_up = true_positives
precision_up = predicted_correctly_up / predicted_up
predicted_correctly_down = true_negatives
precision_down = predicted_correctly_down / predicted_down
print(f"Support (Up, Down): {support_up}, {support_down}")
print(f"Precision (Up, Down): {precision_up:.3f}, {precision_down:.3f}")
print(f"Precision Average (Macro, Weighted): {(precision_up + precision_down)/2:
↪.3f}, {(precision_up * support_up + precision_down * support_down)/
↪(support_up + support_down):.3f}")
recall_up = true_positives / support_up
recall_down = true_negatives / support_down
print(f"Recall (Up, Down): {recall_up:.3f}, {recall_down:.3f}")
print(f"Recall Average (Macro, Weighted): {(recall_up + recall_down)/2:
↪.3f}, {(recall_up * support_up + recall_down * support_down)/(support_up +
↪support_down):.3f}")
f1_score_up = 2 * precision_up * recall_up / (precision_up + recall_up)
f1_score_down = 2 * precision_down * recall_down / (precision_down + recall_down)
print(f"F1 score (Up, Down): {f1_score_up:.3f}, {f1_score_down:.3f}")
print(f"F1 score Average (Macro, Weighted): {(f1_score_up + f1_score_down)/2:
↪.3f}, {(f1_score_up * support_up + f1_score_down * support_down)/(support_up +
↪support_down):.3f}")

```

```

Support (Up, Down): 605, 484
Precision (Up, Down): 0.567, 0.540
Precision Average (Macro, Weighted): 0.553, 0.555
Recall (Up, Down): 0.914, 0.126
Recall Average (Macro, Weighted): 0.520,0.564
F1 score (Up, Down): 0.700, 0.204
F1 score Average (Macro, Weighted): 0.452,0.479

```

2.3.1 (d)

Now fit the logistic regression model using a training data period from 1990 to 2008, with Lag2 as the only predictor. Compute the confusion matrix and the overall fraction of correct predictions for the held out data (that is, the data from 2009 and 2010).

```

[32]: train = (Weekly.Year <= 2008)
      Weekly_train = Weekly.loc[train]
      Weekly_test = Weekly.loc[~train];

```

```

[33]: Weekly_train.shape

```

```

[33]: (985, 12)

```

```

[34]: Weekly_test.shape

```

```

[34]: (104, 12)

```

```
[35]: X_train , X_test = Weekly_train["Lag2"], Weekly_test["Lag2"]
      # add constant term of 1s
      X_train = add_constant(X_train)
      X_test = add_constant(X_test)
      y_train , y_test = Weekly_train["Direction"] == "Up", Weekly_test["Direction"] == "Up"
      glm_train = sm.GLM(y_train , X_train, family=sm.families.Binomial())
      results = glm_train.fit()
      probs = results.predict(exog=X_test);
```

```
[36]: D = Weekly.Direction
      L_train , L_test = D.loc[train], D.loc[~train]
```

```
[37]: labels = np.array(['Down']*L_test.shape[0])
      labels[probs > 0.5] = 'Up'
      confusion_table(labels , L_test)
```

```
[37]: Truth      Down  Up
      Predicted
      Down      9   5
      Up       34  56
```

```
[38]: accuracy = np.mean(labels == L_test)
```

```
[38]: 0.625
```

```
[39]: test_error = np.mean(labels != L_test)
```

```
[39]: 0.375
```

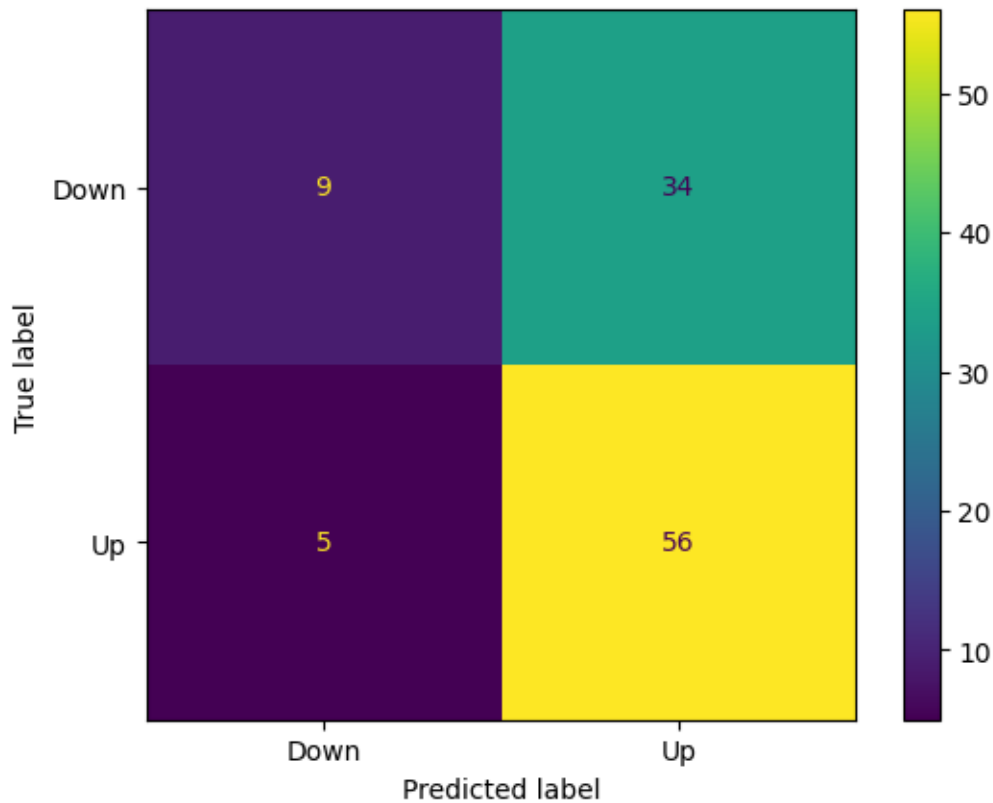
```
[40]: print(f"Here we see the accuracy is {accuracy * 100:g}%.")
      print(f"The test error is {test_error * 100:g}%.")
```

Here we see the accuracy is 62.5%.
The test error is 37.5%.

```
[41]: print(classification_report(Weekly_test["Direction"],
                                  labels,
                                  digits = 3, output_dict=False))
      cm = confusion_matrix(Weekly_test["Direction"],
                              labels)
      disp = ConfusionMatrixDisplay(confusion_matrix=cm,
                                     display_labels=["Down", "Up"])
      disp.plot();
```

	precision	recall	f1-score	support
Down	0.643	0.209	0.316	43
Up	0.622	0.918	0.742	61

accuracy			0.625	104
macro avg	0.633	0.564	0.529	104
weighted avg	0.631	0.625	0.566	104



2.3.2 (e)

Repeat (d) using LDA.

```
[42]: lda = LDA(store_covariance=True)
```

```
[42]: LinearDiscriminantAnalysis(store_covariance=True)
```

Since the LDA estimator automatically adds an intercept, we should remove the column corresponding to the intercept in both `X_train` and `X_test`. We can also directly use the labels rather than the Boolean vectors `y_train`.

```
[43]: X_lda_train , X_lda_test = [M.drop(columns =['const']) for M in [X_train ,
↪X_test ]]
```

```
[44]: lda.fit(X_lda_train , L_train)
lda.means_
```

```
[44]: array([[ -0.03568254],
          [ 0.2603659 ]], dtype=float32)
```

The above means indicate that when **Lag2** is negative, the market direction is Down two days later and vice versa.

The estimated prior probabilities are stored in the `priors_` attribute. The package **sklearn** typically uses this trailing `_` to denote a quantity estimated when using the `fit()` method. We can be sure of which entry corresponds to which label by looking at the `classes_` attribute.

```
[45]: lda.classes_
```

```
[45]: array(['Down', 'Up'], dtype='<U4')
```

```
[46]: priors = lda.priors_
```

```
[46]: array([0.44771573, 0.55228424], dtype=float32)
```

```
[47]: str_down = f"{priors[0]:.3f}"
str_up = f"{priors[1]:.3f}"
```

```
[47]: '0.552'
```

```
[48]: printmd("The LDA output indicates that  $\hat{\pi}_{Down} = " + str\_down + "\backslash$ 
↪and  $\hat{\pi}_{Up} = " + str\_up$ )
```

The LDA output indicates that $\hat{\pi}_{Down} = 0.448$ and $\hat{\pi}_{Up} = 0.552$

The linear discriminant vectors can be found in the `scalings_` attribute:

```
[49]: lda.scalings_
```

```
[49]: array([[0.44141617]], dtype=float32)
```

These values provide the linear combination of **Lag2** that are used to form the LDA decision rule. In other words, these are the multipliers of the elements of $X = x$ in (4.24).

$$\delta_k = x^T \Sigma^{-1} \mu_k + \frac{\mu_k^T \Sigma^{-1} \mu_k}{2} + \log(\pi_k)$$

If $-0.44 \times \text{Lag2}$ is large, then the LDA classifier will predict a market increase, and if it is small, then the LDA classifier will predict a market decline.

```
[50]: lda.xbar_
```

```
[50]: array([0.12782034], dtype=float32)
```

```
[51]: lda_pred = lda.predict(X_lda_test)
```

```
[51]: array(['Up', 'Up', 'Down', 'Down', 'Up', 'Up', 'Up', 'Down', 'Down',
          'Down', 'Down', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up',
          'Up', 'Down', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up',
          'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up',
          'Up', 'Up', 'Up', 'Down', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up',
          'Up', 'Up', 'Up', 'Up', 'Down', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up',
          'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Down', 'Up',
          'Down', 'Up', 'Up', 'Up', 'Up', 'Down', 'Down', 'Up', 'Up', 'Up',
          'Up', 'Up', 'Down', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up',
          'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up', 'Up'],
          dtype='<U4')
```

```
[52]: np.all(lda_pred == labels)
```

```
[52]: True
```

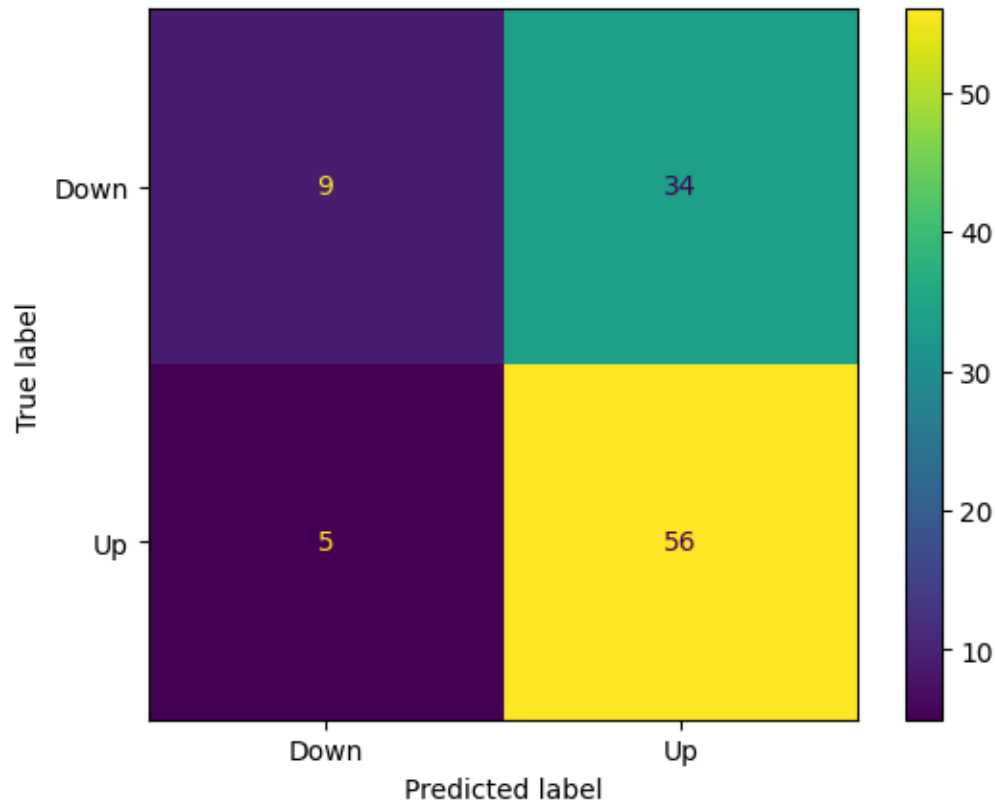
As we observed in our comparison of classification methods (Section 4.5), the LDA and logistic regression predictions are almost identical.

```
[53]: confusion_table(L_test, lda_pred)
```

```
[53]: Truth      Down  Up
Predicted
Down          9  34
Up            5  56
```

```
[54]: print(classification_report(L_test,
                                   lda_pred,
                                   digits = 3, output_dict=False))
cm = confusion_matrix(L_test,
                      lda_pred)
ConfusionMatrixDisplay(confusion_matrix=cm,
                      display_labels=["Down", "Up"]).plot();
```

	precision	recall	f1-score	support
Down	0.643	0.209	0.316	43
Up	0.622	0.918	0.742	61
accuracy			0.625	104
macro avg	0.633	0.564	0.529	104
weighted avg	0.631	0.625	0.566	104



2.3.3 (f)

Repeat (d) using QDA.

2.3.4 (g)

Repeat (d) using KNN with $K = 1$.

2.3.5 (h)

Repeat (d) using naive Bayes.

2.3.6 (i)

Which of these methods appears to provide the best results on this data?

2.3.7 (j)

Experiment with different combinations of predictors, including possible transformations and interactions, for each of the methods. Report the variables, method, and associated confusion matrix that appears to provide the best results on the held out data. Note that you should also experiment with values for K in the KNN classifier.

```
[55]: allDone();
```

```
<IPython.lib.display.Audio object>
```