KNNDistances

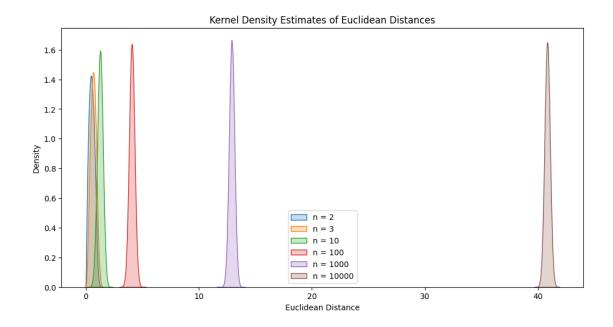
February 21, 2025

1 KNN Distances

1.1 Import notebook funcs

```
[1]: from notebookfuncs import *
[2]: import torch
     import matplotlib.pyplot as plt
     import seaborn as sns
     def generate_n_dimensional_tensor(n, num_points=1000):
       """Generates an n-dimensional tensor of random numbers.
       Args:
         n: The desired number of dimensions.
         num_points: The number of data points to generate.
       Returns:
         An n-dimensional PyTorch tensor.
       return torch.rand(num_points, n)
     def euclidean_distance(p1, p2):
       """Calculates the Euclidean distance between two tensors.
      Args:
        p1: The first tensor.
        p2: The second tensor.
       Returns:
         The Euclidean distance between the two tensors.
      return torch.norm(p1 - p2, dim=-1)
     def plot_distance_histograms(distances_list, dimensions):
       """Plots histograms of the Euclidean distances on a single plot.
```

```
Arqs:
    distances\_list: A list of lists, each containing distances for a specific \Box
 \hookrightarrow dimension.
    dimensions: A list of dimensions.
 plt.figure(figsize=(12, 6))
 for i, (distances, n) in enumerate(zip(distances_list, dimensions)):
    sns.kdeplot(distances, fill=True, label=f"n = {n}")
 plt.xlabel("Euclidean Distance")
 plt.ylabel("Density")
 plt.title("Kernel Density Estimates of Euclidean Distances")
 plt.legend()
 plt.show()
# Define the desired dimensions
dimensions = [2, 3, 10, 100, 1000, 10000]
# Generate and print the arrays
distances list = []
for n in dimensions:
  tensor = generate_n_dimensional_tensor(n)
 num_points = tensor.shape[0]
  distances = []
  for i in range(num_points):
    for j in range(i + 1, num_points):
      distance = euclidean_distance(tensor[i], tensor[j]).item()
      distances.append(distance)
  distances_list.append(distances)
plot_distance_histograms(distances_list, dimensions)
```



[5]: printlatex("\$\\text{The Curse of Dimensionality } \\implies \\text{ As }n \\to_\\infty, \\text{ distances between points increase.}\$")

The Curse of Dimensionality \implies As $n \to \infty$, distances between points increase.

Reference: 1. https://www.cs.cornell.edu/courses/cs4780/2022fa/slides/KNN_annotated.pdf

[4]: allDone();

<IPython.lib.display.Audio object>