Introduction to Simulation



- □ Simulation: Key Questions
- □ Introduction to Simulation
- Common Mistakes in Simulation
- Other Causes of Simulation Analysis Failure
- Checklist for Simulations
- □ Terminology
- Types of Models

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Simulation: Key Questions

- What are the common mistakes in simulation and why most simulations fail?
- What language should be used for developing a simulation model?
- What are different types of simulations?
- □ How to schedule events in a simulation?
- □ How to verify and validate a model?
- □ How to determine that the simulation has reached a steady state?
- How long to run a simulation?

Simulation: Key Questions (Cont)

- □ How to generate uniform random numbers?
- How to verify that a given random number generator is good?
- □ How to select seeds for random number generators?
- ☐ How to generate random variables with a given distribution?
- □ What distributions should be used and when?

Introduction to Simulation

The best advice to those about to embark on a very large simulation is often the same as Punch's famous advice to those about to marry: Don't!

-Brately, Fox, and Schrage (1987)

Common Mistakes in Simulation

- 1. Inappropriate Level of Detail:
 - More detail \Rightarrow More time \Rightarrow More Bugs \Rightarrow More CPU
 - ⇒ More parameters ≠ More accurate
- 2. Improper Language
 - General purpose ⇒ More portable, More efficient, More time
- 3. Unverified Models: Bugs
- 4. Invalid Models: Model vs. reality
- 5. Improperly Handled Initial Conditions
- 6. Too Short Simulations: Need confidence intervals
- 7. Poor Random Number Generators: Safer to use a well-known generator
- 8. Improper Selection of Seeds: Zero seeds, Same seeds for all streams

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Other Causes of Simulation Analysis Failure

- 1. Inadequate Time Estimate
- 2. No Achievable Goal
- 3. Incomplete Mix of Essential Skills
 - (a) Project Leadership
 - (b) Modeling and
 - (c) Programming
 - (d) Knowledge of the Modeled System
- 4. Inadequate Level of User Participation
- 5. Obsolete or Nonexistent Documentation
- 6. Inability to Manage the Development of a Large Complex Computer Program Need software engineering tools
- 7. Mysterious Results

Checklist for Simulations

- 1. Checks before developing a simulation:
 - (a) Is the goal of the simulation properly specified?
 - (b) Is the level of detail in the model appropriate for the goal?
 - (c) Does the simulation team include personnel with project leadership, modeling, programming, and computer systems backgrounds?
 - (d) Has sufficient time been planned for the project?
- 2. Checks during development:
 - (a) Has the random number generator used in the simulation been tested for uniformity and independence?
 - (b) Is the model reviewed regularly with the end user?
 - (c) Is the model documented?

Checklist for Simulations (Cont)

- 3. Checks after the simulation is running:
 - (a) Is the simulation length appropriate?
 - (b) Are the initial transients removed before computation?
 - (c) Has the model been verified thoroughly?
 - (d) Has the model been validated before using its results?
 - (e) If there are any surprising results, have they been validated?
 - (f) Are all seeds such that the random number streams will not overlap?

Terminology

□ State Variables: Define the state of the system

Can restart simulation from state variables

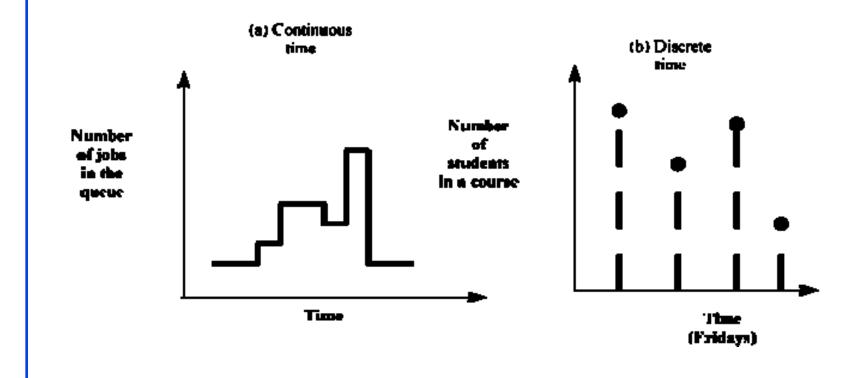
E.g., length of the job queue.

Event: Change in the system state.

E.g., arrival, beginning of a new execution, departure

Types of Models

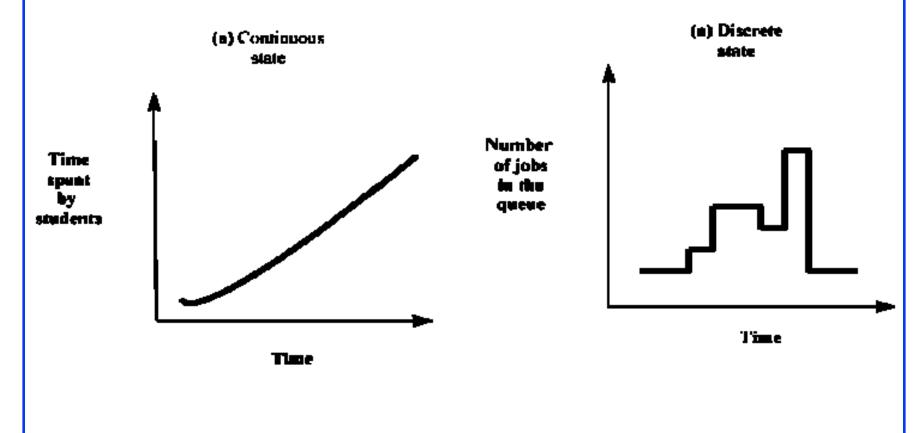
- □ Continuous Time Model: State is defined at all times
- □ Discrete Time Models: State is defined only at some instants



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Types of Models (Cont)

- □ Continuous State Model: State variables are continuous
- □ Discrete State Models: State variables are discrete



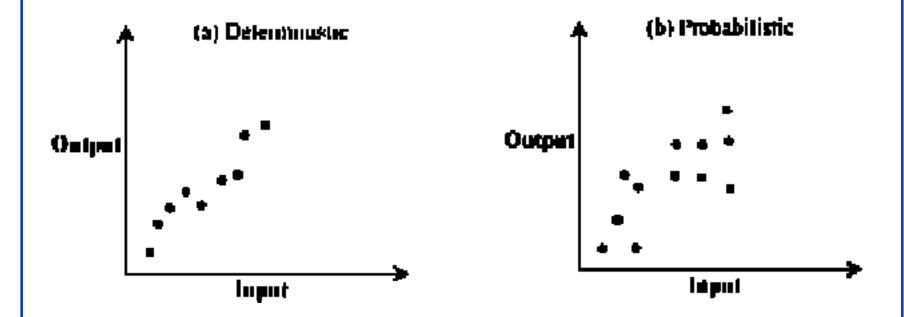
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Types of Models (Cont)

- □ Discrete state = Discrete event model
- □ Continuous state = Continuous event model
- □ Continuity of time ≠ Continuity of state
- □ Four possible combinations:
- 1. discrete state/discrete time
- 2. discrete state/continuous time
- 3. continuous state/discrete time
- 4. continuous state/continuous time models

Types of Models (Cont)

□ Deterministic and Probabilistic Models:

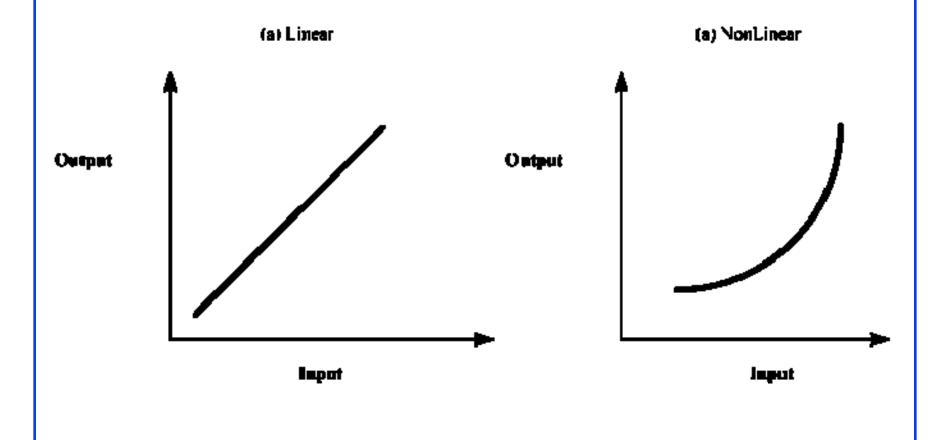


□ Static and Dynamic Models:

CPU scheduling model vs. $E = mc^2$.

Linear and Nonlinear Models

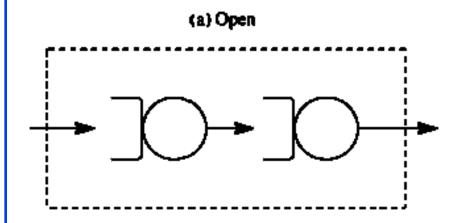
 \Box Output = fn(Input)

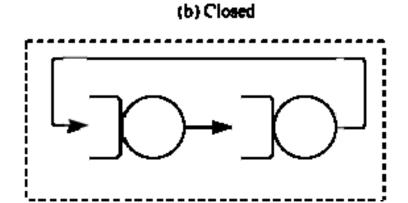


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Open and Closed Models

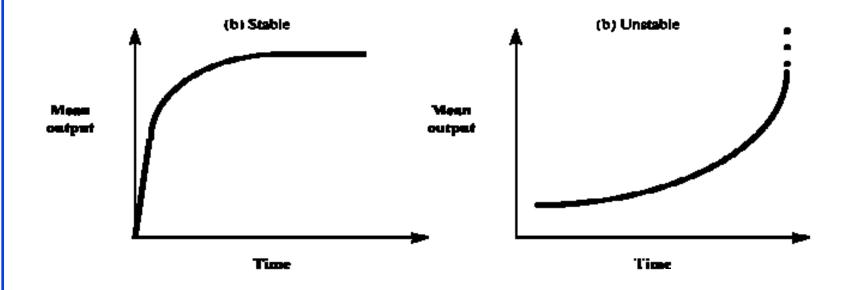
 \square External input \Rightarrow open





Stable and Unstable Models

- \square Stable \Rightarrow Settles to steady state
- \square Unstable \Rightarrow Continuously changing.



Computer System Models

- Continuous time
- □ Discrete state
- Probabilistic
- Dynamic
- Nonlinear
- Open or closed
- □ Stable or unstable

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Selecting a Language for Simulation

- 1. Simulation language
- 2. General purpose
- 3. Extension of a general purpose language
- 4. Simulation package

Simulation Languages

- □ Save development time
- Built-in facilities for time advancing, event scheduling, entity manipulation, random variate generation, statistical data collection, and report generation
- More time for system specific issues
- Very readable modular code

General Purpose Language

- Analyst's familiarity
- □ Easy availability
- Quick startup
- □ Time for routines for event handling, random number generation
- □ Other Issues: Efficiency, flexibility, and portability
- □ Recommendation: Learn at least one simulation language.

Extensions of a General Purpose Language

- □ Examples: GASP (for FORTRAN)
 - > Collection of routines to handle simulation tasks
 - > Compromise for efficiency, flexibility, and portability.

Simulation Packages

Example: QNET4, and RESQ

- □ Input dialog
- □ Library of data structures, routines, and algorithms
- □ Big time savings
- □ Inflexible \Rightarrow Simplification

Types of Simulation Languages

- **□** Continuous Simulation Languages:
 - > CSMP, DYNAMO
 - Differential equations
 - Used in chemical engineering
- **□** Discrete-event Simulation Languages:
 - SIMULA and GPSS
- **□** Combined:
 - > SIMSCRIPT and GASP.
 - Allow discrete, continuous, as well as combined simulations.

Types of Simulations

- Emulation: Using hardware or firmware
 E.g., Terminal emulator, processor emulator
 Mostly hardware design issues
- 2. Monte Carlo Simulation
- 3. Trace-Driven Simulation
- 4. Discrete Event Simulation

Types of Simulation (Cont)

Monte Carlo method [Origin: after Count Montgomery de Carlo, Italian gambler and random-number generator (1792-1838).] A method of jazzing up the action in certain statistical and number-analytic environments by setting up a book and inviting bets on the outcome of a computation.

- The Devil's DP Dictionary McGraw Hill (1981)

Monte Carlo Simulation

- □ Static simulation (No time axis)
- □ To model probabilistic phenomenon
- Need pseudorandom numbers
- □ Used for evaluating non-probabilistic expressions using probabilistic methods.

Monte Carlo: Example

$$I = \int_0^2 e^{-x^2} dx$$
$$x \sim \text{Uniform}(0, 2)$$

Density function $f(x) = \frac{1}{2}$ iff $0 \le x \le 2$

$$y = 2e^{-x^2}$$

Monte Carlo: Example (Cont)

$$E(y) = \int_{0}^{2} 2e^{-x^{2}} f(x) dx$$

$$= \int_{0}^{2} 2e^{-x^{2}} \frac{1}{2} dx$$

$$= \int_{0}^{2} e^{-x^{2}} dx$$

$$= I$$

 $x_i \sim \text{Uniform}(0,2)$

$$y_{i} = 2e^{-x_{i}^{2}}$$

$$I = E(y) = \frac{1}{n} \sum_{i=1}^{n} y_{i}$$

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Trace-Driven Simulation

- ☐ Trace = Time ordered record of events on a system
- Trace-driven simulation = Trace input
- □ Used in analyzing or tuning resource management algorithms
 Paging, cache analysis, CPU scheduling, deadlock prevention
 dynamic storage allocation
- **Example**: Trace = Page reference patterns
- Should be independent of the system under study

 E.g., trace of pages fetched depends upon the working set size and page replacement policy
 - > Not good for studying other page replacement policies
 - > Better to use pages referenced

Advantages of Trace-Driven Simulations

- 1. Credibility
- 2. Easy Validation: Compare simulation with measured
- 3. Accurate Workload: Models correlation and interference
- 4. Detailed Trade-Offs:

Detailed workload ⇒ Can study small changes in algorithms

5. Less Randomness:

Trace \Rightarrow deterministic input \Rightarrow Fewer repetitions

- 6. Fair Comparison: Better than random input
- 7. Similarity to the Actual Implementation:

Trace-driven model is similar to the system

⇒ Can understand complexity of implementation

Disadvantages of Trace-Driven Simulations

- 1. Complexity: More detailed
- 2. Representativeness: Workload changes with time, equipment
- 3. Finiteness: Few minutes fill up a disk
- 4. Single Point of Validation: One trace = one point
- 5. Detail
- 6. Trade-Off: Difficult to change workload

Discrete Event Simulations

- Concentration of a chemical substance
 - ⇒ Continuous event simulations
- \square Number of jobs \Rightarrow Discrete event
- □ Discrete state ≠ discrete time

Components of Discrete Event Simulations

- 1. Event Scheduler
 - (a) Schedule event X at time T.
 - (b) Hold event X for a time interval dt.
 - (c) Cancel a previously scheduled event X.
 - (d) Hold event X indefinitely
 - (e) Schedule an indefinitely held event.
- 2. Simulation Clock and a Time Advancing Mechanism
 - (a) Unit-time approach
 - (b) Event-driven approach

Components of Discrete Events Sims (Cont)

3. System State Variables

Global = Number of jobs

Local = CPU time required for a job

4. Event Routines: One per event.

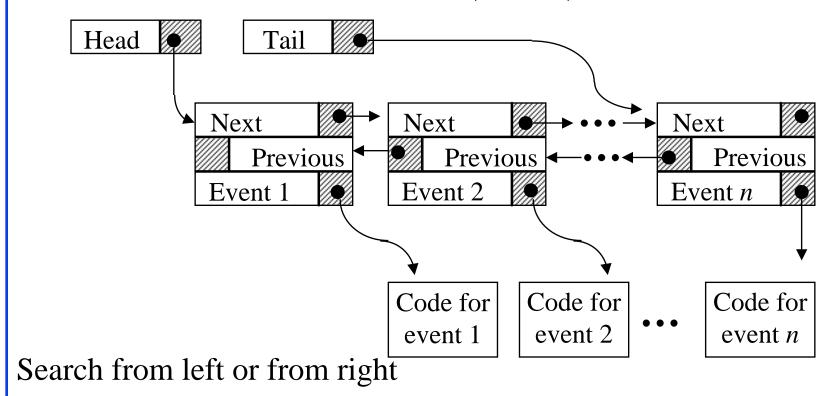
E.g., job arrivals, job scheduling, and job departure

- 5. Input Routines: Get model parameters Very parameters in a range.
- 6. Report Generator
- 7. Initialization Routines: Set the initial state. Initialize seeds.
- 8. Trace Routines: On/off feature
- 9. Dynamic Memory Management: Garbage collection
- 10. Main Program

Event-Set Algorithms

Event Set = Ordered linked list of future event notices Insert vs. Execute next

1. Ordered Linked List: SIMULA, GPSS, and GASP IV

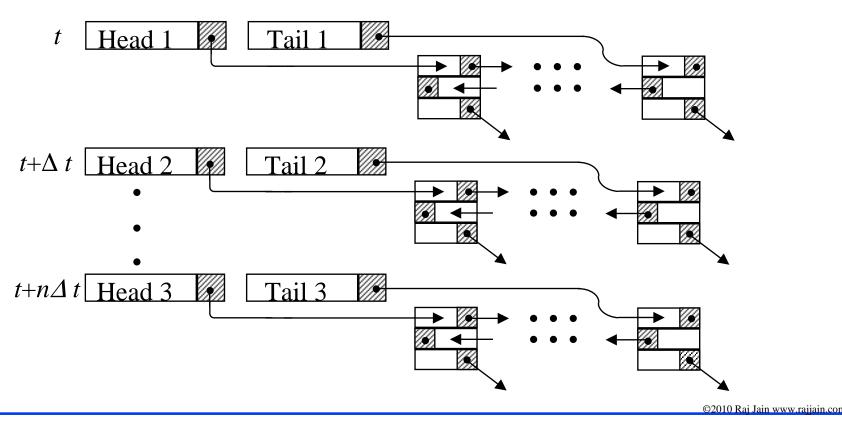


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Event-Set Algorithms (Cont)

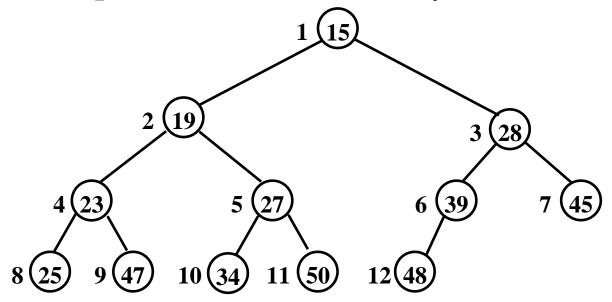
2. Indexed Linear List:

- \rightarrow Array of indexes \Rightarrow No search to find the sub-list
- \triangleright Fixed or variable Δt . Only the first list is kept sorted



Event-Set Algorithms (Cont)

- 3. Calendar Queues: All events of Jan 1 on one page. 1995 or 1996.
- 4. Tree Structures: Binary tree $\Rightarrow \log_2 n$
- 5. **Heap**: Event is a node in binary tree



(a) Tree representation of a heap.

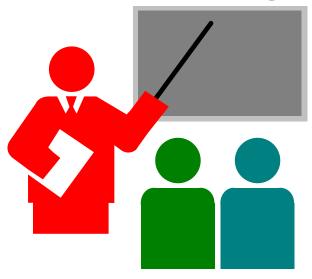
Event-Set Algorithms(Cont)

i 1 2 3 4 5 6 7 8 9 10 11 12

A[i] 15 19 28 23 27 39 45 25 47 34 50 48

- > Event time for each node is smaller than that of its Children
 - \Rightarrow **R**oot is next
- > Heap can be stored as arrays
- > Children of node in position i are in positions 2i and 2i+1
- 6. **k-ary heaps**: k-ary trees
 - > 20-120 events: Index linear
 - > 120+ events: Heaps

Summary



- 1. Common Mistakes: Detail, Invalid, Short
- 2. Discrete Event, Continuous time, nonlinear models
- 3. Monte Carlo Simulation: Static models
- 4. Trace driven simulation: Credibility, difficult trade-offs
- 5. Even Set Algorithms: Linked list, indexed linear list, heaps

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Exercise 24.1

For each of the following models, identify all classifications that apply to it:

a.
$$y(t)=t+0.2$$

b.
$$y(t)=t^2$$

c. $y(t+1)=y(t)+\Delta$, Δ is not an integer.

d.
$$n(t+1)=2n(t)+3$$

$$e. y(t)=\sin(wt)$$

f.
$$\bar{y}(t+1) = \bar{y}(t) + \Delta$$

Exercise 24.2

Which type of simulation would you use for the following problems:

- 1. To model destination address reference patterns in a network traffic, given that the pattern depends upon a large number of factors.
- 2. To model scheduling in a multiprocessor system, given that the request arrivals have a known distribution.
- 3. To determine the value of π

Exercise 24.3

What is unit-time approach and why is it not generally used?

Homework

For each of the following models, identify all classifications that apply to it:

1.
$$\bar{y}(t+1) = \bar{y}(t) + a$$

2.
$$y(t+1) = y(t) + 3$$

3.
$$y(t) = t^1.5$$

4.
$$y(t) = a + bt + ct^2$$

5.
$$n(t+1) = 3n(t) + 5$$

6.
$$y(t) = cos(wt + \psi)$$