Homework 6

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Question 1

```
##
                    AgeGroup Race
                                     Shots
                                             InsuranceType MedAssist Location
         Age
##
   Min. :11.00
                    0:482
                             0:232
                                     1:153
                                             0:204
                                                           0:311
                                                                      1:216
                                                           1:204
                                                                      2: 0
##
   1st Qu.:13.00
                    1: 33
                             1:194
                                     2:164
                                             1:171
   Median :15.00
                             2: 29
                                     3:198
                                             2: 25
                                                                      3: 0
## Mean :14.92
                             3: 60
                                             3:115
                                                                      4:299
##
   3rd Qu.:17.00
##
  Max. :21.00
  LocationType
##
  0:216
##
   1:299
##
##
##
##
         Age
                    AgeGroup Race
                                     Shots
                                             InsuranceType MedAssist Location
##
   Min. :11.00
                    0:123
                             0:169
                                     1:117
                                             0: 12
                                                           0:353
                                                                      1:365
                                                                      2: 0
##
   1st Qu.:17.00
                    1:242
                             1:102
                                     2:128
                                             1:188
                                                           1: 12
                                                                      3: 0
  Median :19.00
                             2: 10
                                     3:120
                                             2: 9
  Mean :19.46
                             3: 84
                                             3:156
                                                                      4: 0
   3rd Qu.:22.00
##
##
   Max.
           :26.00
##
  LocationType
##
   0:365
##
   1: 0
##
##
##
##
                    AgeGroup Race
                                     Shots
                                             InsuranceType MedAssist Location
##
         Age
   Min. :11.00
                    0: 96
                             0:331
                                     1:170
                                             0: 59
                                                           0:474
                                                                      1:217
   1st Qu.:19.00
                    1:437
                             1:147
                                     2:144
                                             1:364
                                                           1: 59
                                                                      2:165
                                                                      3: 89
   Median :22.00
                             2: 13
                                     3:219
                                             2: 50
##
  Mean
          :21.43
                             3: 42
                                             3: 60
                                                                      4: 62
   3rd Qu.:24.00
## Max.
           :26.00
##
  LocationType
##
  0:382
##
   1:151
##
##
##
##
```

Question 2

The treatment is received the vaccine at OB-GYN facilities and the control is received the vaccine at facilities other than OB-GYN. Among these variables, Age, Race, InsuranceType, Location are covariates. Shots contains some information about outcome, information in AgeGroup and LocationType overlap with Age and Location. There are NAs when using MedAssist to calculate propensity scores. So Shots, MedAssist, AgeGroup and LocationType are not regarded as covariates.

```
##
         Age
                     AgeGroup Race
                                        Shots
                                                InsuranceType MedAssist Location
##
    Min.
           :11.00
                     0:96
                               0:331
                                        1:170
                                                0: 59
                                                               0:474
                                                                          1:217
                                                               1: 59
##
    1st Qu.:19.00
                     1:437
                               1:147
                                        2:144
                                                1:364
                                                                          2:165
    Median :22.00
                                        3:219
                                                2: 50
                                                                          3: 89
##
                               2: 13
##
    Mean
           :21.43
                               3: 42
                                                3: 60
                                                                          4: 62
##
    3rd Qu.:24.00
            :26.00
##
    Max.
##
    LocationType
    0:382
##
    1:151
##
##
##
##
##
##
                                               InsuranceType MedAssist Location
         Age
                    AgeGroup Race
                                      Shots
##
    Min.
           :11.0
                    0:605
                              0:401
                                       1:270
                                               0:216
                                                              0:664
                                                                         1:581
##
    1st Qu.:14.0
                    1:275
                              1:296
                                      2:292
                                               1:359
                                                               1:216
                                                                         2: 0
##
    Median:16.0
                              2: 39
                                      3:318
                                               2: 34
                                                                         3:
                                                                             0
                              3:144
                                               3:271
                                                                         4:299
##
    Mean
           :16.8
##
    3rd Qu.:19.0
##
           :26.0
   Max.
##
    LocationType
    0:581
##
##
    1:299
##
##
##
##
```

Based on levels of baseline characteristics in treatment group and control group, we can get the eligibility criteria. The eligibility criteria are age between 11-26, Race equals to 0, 1, 2 or 3, InsuranceType equals to 0, 1, 2 or 3, Location equals to 1 or 4 and MedAssist equals to 0 or 1.

Question 3

According to the eligibility criteria, subjects with LocationType equals to 2 or 3 in treatment group 1, should be excluded. Descriptive statistics of analytic sample are shown below:

##	Age	AgeGroup	Race	Shots	${\tt InsuranceType}$	${\tt MedAssist}$	Location
##	Min. :11.0	0:605	0:401	1:270	0:216	0:664	1:581
##	1st Qu.:14.0	1:275	1:296	2:292	1:359	1:216	2: 0
##	Median :16.0		2: 39	3:318	2: 34		3: 0
##	Mean :16.8		3:144		3:271		4:299

```
3rd Qu.:19.0
##
    Max.
           :26.0
    LocationType
##
    0:581
##
##
    1:299
##
##
##
##
##
         Age
                     AgeGroup Race
                                        Shots
                                                 InsuranceType MedAssist Location
##
           :11.00
                     0: 47
                               0:173
                                        1: 92
                                                 0: 18
                                                                0:261
                                                                           1:217
    Min.
                                        2: 74
                                                                           2: 0
##
    1st Qu.:19.00
                     1:232
                               1: 65
                                                 1:190
                                                                1: 18
    Median :22.00
                                  4
                                        3:113
                                                                           3:
                                                                               0
##
                               2:
                                                 2: 14
##
    Mean
           :21.59
                               3: 37
                                                 3: 57
                                                                           4: 62
##
    3rd Qu.:24.00
##
    Max.
            :26.00
##
    LocationType
##
    0:217
    1: 62
##
##
##
##
##
```

I redefine the PracticeType variable into binary variable PracticeType_bin. I let PracticeType equals to 2 be treatment group 1 and PracticeType equals to 0 or 1 be control group. Besides, I also exclude subjects with LocationType equals to 2 or 3 in treatment group 1. Descriptive statistics are different.

Numbers of subjects in different level of AgeGroup Race, Shots, Completed, InsuranceType, MedAssist, Location and LocationType are different. Compare to study sample, analytic sample do not have subjects with Location equals to 2 or 3, and mean, 1st and 3rd quantiles of age are different too.

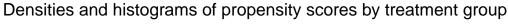
Question 4

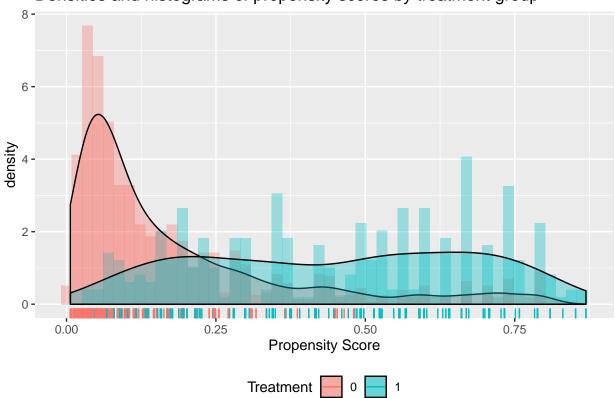
```
##
  glm(formula = PracticeType_bin ~ Age + Race + InsuranceType +
##
       Location, family = binomial, data = q3_data)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    3Q
                                            Max
           -0.6181 -0.3636
  -1.7610
                              -0.1536
                                         2.5668
##
## Coefficients:
##
                  Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                  -7.63403
                               0.59058 - 12.926
                                               < 2e-16 ***
                   0.30458
                               0.02359
                                        12.910
                                                < 2e-16 ***
## Age
## Race1
                  -0.42717
                               0.19278
                                        -2.216
                                                0.02671
## Race2
                               0.60269
                  -1.19596
                                        -1.984
                                                0.04721 *
## Race3
                  -0.64490
                               0.24149
                                        -2.670
                                                0.00757 **
## InsuranceType1 1.02725
                               0.32631
                                                0.00164 **
                                         3.148
## InsuranceType2 1.17159
                               0.45552
                                         2.572 0.01011 *
```

```
## InsuranceType3 0.59322
                              0.37287
                                        1.591 0.11162
## Location4
                   0.43685
                              0.24447
                                        1.787
                                               0.07395 .
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 1279.34
                               on 1158
                                        degrees of freedom
## Residual deviance: 953.17
                               on 1150
                                        degrees of freedom
  AIC: 971.17
##
## Number of Fisher Scoring iterations: 5
```

The propensity scores in the analytic sample is shown above.

Question 5

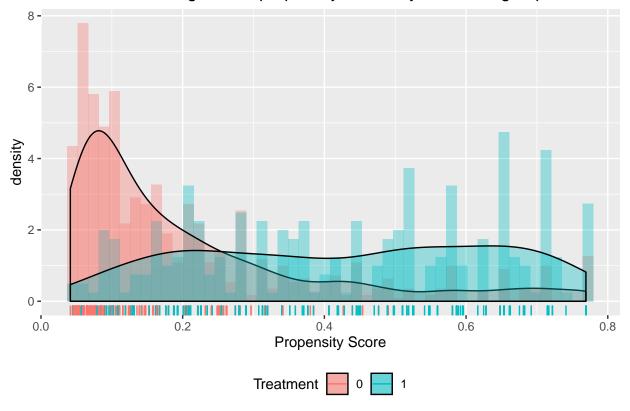




According to the plot, we can find that propensity score of treatment group 1 and treatment group 0 do not overlap when propensity scores are near 1, so we need to trim data.

There are 147 observations have been eliminated and there are 1012 observations left.





According to the plot above, we can find that propensity score of treatment group 1 and treatment group 0 overlap now, which means trimming can improve covariate balance, improving internal validity, so efficiency is improved. But trimming will hurts external validity(generalizability).

Question 6

##	Stratified by PracticeType_bin					oin
##		0		1		SMD
##	n	742		270		
##	Age (mean (SD))	17.58	(3.53)	21.46	(3.27)	1.141
##	Race (%)					0.223
##	0	371	(50.0)	164	(60.7)	
##	1	234	(31.5)	65	(24.1)	
##	2	18	(2.4)	4	(1.5)	
##	3	119	(16.0)	37	(13.7)	
##	<pre>InsuranceType (%)</pre>					0.492
##	0	130	(17.5)	18	(6.7)	
##	1	341	(46.0)	184	(68.1)	
##	2	34	(4.6)	11	(4.1)	
##	3	237	(31.9)	57	(21.1)	
##	Location (%)					0.252
##	1	516	(69.5)	217	(80.4)	
##	2	0	(0.0)	0	(0.0)	
##	3	0	(0.0)	0	(0.0)	
##	4	226	(30.5)	53	(19.6)	

We want SMD to be small. According to the table above, we can find that SMD of Race and Location is close to 0.2, which mean these two covariates balance relatively well. While SMD of age and Location are relatively large, which means these two covariates do not balance well.

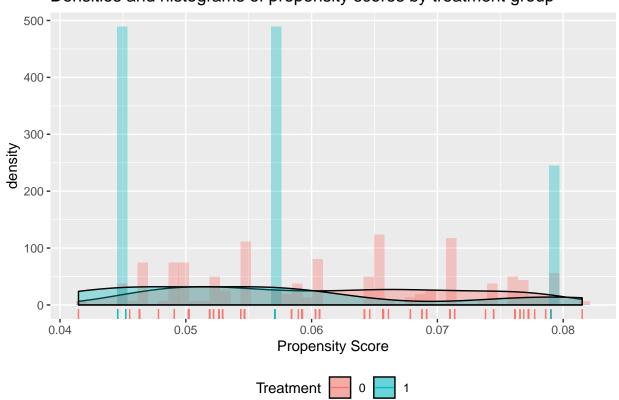
Question 7

```
20%
                      40%
                                  60%
                                              80%
## 0.08192037 0.14166779 0.24136248 0.47664191
##
      subclass
##
         0
                  2
                       3
                           4
##
     0 198 186 154 128
                         76
         5
             21
                 43
                    74 127
##
```

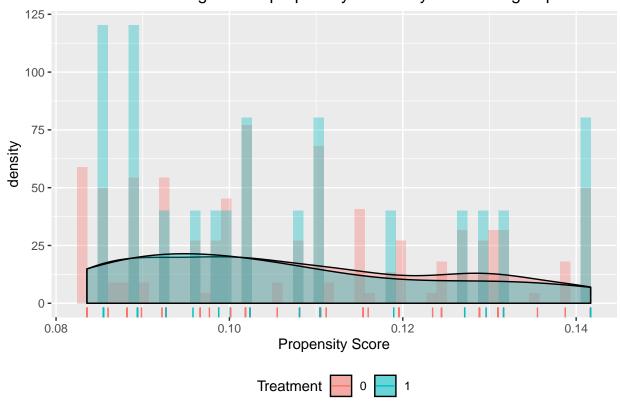
I choose 20%, 40%, 60% and 80% quantiles as breaks. Breaks are 0.082, 0.142, 0.241, 0.477. As these breaks do not violate positivity assumption, they are valid.

Plots of propensity scores with these breaks are shown below:

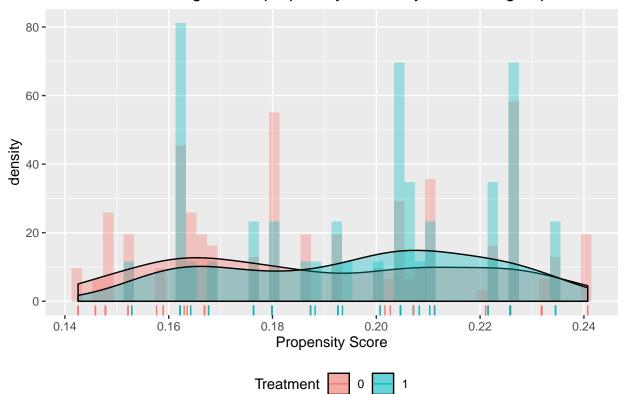
Densities and histograms of propensity scores by treatment group

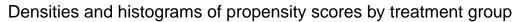


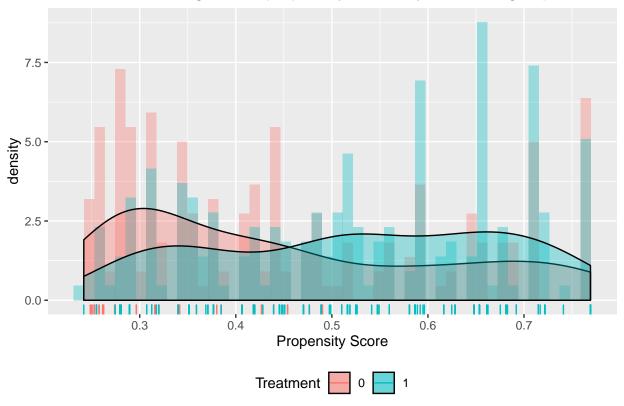
Densities and histograms of propensity scores by treatment group



Densities and histograms of propensity scores by treatment group







According to above plots, we can find that propensity score of treatment group and control group overlap better, which means covariates are balanced better.

##		Stratif	ied by	Practio	ceType_b	in
##		0		1		SMD
##	n	198		5		
##	Age (mean (SD))	14.27	(1.45)	13.60	(1.52)	0.450
##	Race (%)					0.587
##	0	84	(42.4)	2	(40.0)	
##	1	69	(34.8)	1	(20.0)	
##	2	8	(4.0)	0	(0.0)	
##	3	37	(18.7)	2	(40.0)	
##	InsuranceType (%	()				0.741
##	0	74	(37.4)	1	(20.0)	
##	1	53	(26.8)	3	(60.0)	
##	2	6	(3.0)	0	(0.0)	
##	3	65	(32.8)	1	(20.0)	
##	Location (%)					0.553
##	1	109	(55.1)	4	(80.0)	
##	2	0	(0.0)	0	(0.0)	
##	3	0	(0.0)	0	(0.0)	
##	4	89	(44.9)	1	(20.0)	
##		Stratif	ied by	Practio	ceType_b	in
##		0	J	1	V	SMD
##	n	186		21		

```
Age (mean (SD))
##
                        16.06 (1.52) 16.05 (1.24)
                                                       0.012
                                                       0.587
##
     Race (%)
##
        0
                           85 (45.7)
                                          11 (52.4)
##
                           60 (32.3)
                                           7 (33.3)
        1
        2
                                           2 (9.5)
##
                            3 (1.6)
##
        3
                           38 (20.4)
                                           1 (4.8)
##
     InsuranceType (%)
                                                       0.063
                           37 (19.9)
                                           4 (19.0)
##
##
        1
                           66 (35.5)
                                           7 (33.3)
                                           1 (4.8)
##
        2
                            9 (4.8)
##
        3
                           74 (39.8)
                                           9 (42.9)
                                                       0.092
##
     Location (%)
                          125 (67.2)
                                          15 (71.4)
##
        1
        2
##
                            0 (0.0)
                                           0 (0.0)
##
        3
                            0 (0.0)
                                           0 (0.0)
##
        4
                           61 (32.8)
                                           6 (28.6)
##
                       Stratified by PracticeType_bin
##
                                       1
                                                      SMD
##
                          154
                                           43
##
     Age (mean (SD))
                        17.83 (1.56) 18.26 (1.62)
                                                       0.267
     Race (%)
##
                                                       0.216
                                          24 (55.8)
##
        0
                           86 (55.8)
##
        1
                           48 (31.2)
                                          13 (30.2)
##
        2
                            3 (1.9)
                                           0 (0.0)
        3
##
                           17 (11.0)
                                           6 (14.0)
##
                                                       0.168
     InsuranceType (%)
##
                           16 (10.4)
                                           5 (11.6)
##
        1
                           75 (48.7)
                                          20 (46.5)
##
        2
                            8 (5.2)
                                           1 (2.3)
##
        3
                           55 (35.7)
                                          17 (39.5)
##
                                                       0.350
     Location (%)
                          102 (66.2)
##
        1
                                          35 (81.4)
##
        2
                            0(0.0)
                                           0(0.0)
##
        3
                            0(0.0)
                                           0(0.0)
##
                           52 (33.8)
                                           8 (18.6)
##
                       Stratified by PracticeType_bin
##
##
                          128
                                           74
##
     Age (mean (SD))
                        20.39 (1.75) 20.88 (1.76)
                                                       0.278
##
     Race (%)
                                                       0.131
        0
##
                           68 (53.1)
                                          36 (48.6)
                           40 (31.2)
                                          25 (33.8)
##
        1
##
        2
                            3 (2.3)
                                           1 (1.4)
##
        3
                           17 (13.3)
                                          12 (16.2)
##
     InsuranceType (%)
                                                       0.195
##
        0
                            2 (1.6)
                                           3 (4.1)
##
        1
                           79 (61.7)
                                          47 (63.5)
##
        2
                           11 (8.6)
                                           4 (5.4)
##
        3
                           36 (28.1)
                                          20 (27.0)
##
                                                       0.143
     Location (%)
##
        1
                          104 (81.2)
                                          64 (86.5)
                                           0 (0.0)
##
        2
                            0 (0.0)
```

```
## 3 0 (0.0) 0 (0.0)
## 4 24 (18.8) 10 (13.5)
```

According to tables above, we can find that SMDs decrease a lot in each subclass. Except subclass 1, most of SMDs are smaller than or near 0.2, which means covariates are balanced well in these subclasses. SMDs in subclass 1 are relatively high, which means covariates are not balanced well.

Question 8

The point estimate of the marginal average causal effect is 0.065. The confidence interval is (-0.054, 0.184). Interpretation:

As the point estimate of the marginal average causal effect is 0.065, the estimated true marginal average causal effect is 0.065.

As the confidence interval is (-0.054, 0.184), it means with 95% confidence, we can conclude that the true marginal average causal effect falls between -0.054 and 0.184.

Question 9

g-formula for observational studies:

$$\begin{split} E[Y_1] - E[Y_0] &= \sum_C E(Y_1|C=c) Pr(C=c) - \sum_C E(Y_0|C=c) Pr(C=c) (IE) \\ &= \sum_C E(Y_1|A=1,C=c) Pr(C=c) - \sum_C E(Y_0|A=1,C=c) Pr(C=c) (RA) \\ &= \sum_{C,U} E(Y_1|A=1,C=c,U=u) Pr(C=c,U=u) - \sum_{C,U} E(Y_0|A=0,C=c,U=u) Pr(C=c,U=u) (IE+C) \\ &= E(Y|A=1) - E(Y|A=0) \end{split}$$

```
##
## Call:
## lm(formula = Completed ~ PracticeType_bin + Age + Race + InsuranceType +
##
       Location, data = q8 data)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
##
   -0.5291 -0.3404 -0.2461 0.5851
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     0.631520
                                 0.100443
                                            6.287 4.81e-10 ***
## PracticeType_bin 0.100831
                                 0.036918
                                            2.731 0.006421 **
## Age
                    -0.018211
                                 0.004444
                                           -4.098 4.51e-05 ***
## Race1
                    -0.114444
                                 0.033860
                                           -3.380 0.000753 ***
## Race2
                     0.037180
                                 0.100115
                                            0.371 0.710440
## Race3
                    -0.031418
                                 0.042309
                                           -0.743 0.457901
## InsuranceType1
                     0.069881
                                 0.051355
                                            1.361 0.173899
## InsuranceType2
                     0.181203
                                 0.078531
                                            2.307 0.021234 *
## InsuranceType3
                     0.049890
                                 0.059672
                                            0.836 0.403315
## Location4
                    -0.083875
                                 0.043978
                                           -1.907 0.056782
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.458 on 1002 degrees of freedom
## Multiple R-squared: 0.04086, Adjusted R-squared: 0.03224
## F-statistic: 4.743 on 9 and 1002 DF, p-value: 3.362e-06
```

The beta of PracticeType_bin is 0.1, which means given coavariates are the same, E[Y|A=1] - E[Y|A=0] is 0.1. If 1)consistency, SUTVA, exchangeability and positivity assumptions are meet, 2)there is no interaction between treatment and covariates and 3)the outcome is continous, then this would be the same as the true marginal average causal effect which I estimate in question 8 as well as the average causa effect get from g-formula.

However, the estimated marginal average causal effect calculated in question 8 is not the same as what we get from linear model. Following are some possible reasons: 1) there is interaction between treatment and covariates, 2) using linear regression to fit model of binary outcome might cause bias, 3) the estimated marginal ACE is slightly different from true marginal ACE.

```
knitr::opts_chunk$set(echo = FALSE)
library(tidyverse)
library(personalized)
library(tableone)
gard_data = read.table("./gardasil.dat",header = T) %>%
  select(-Completed)
gard_data$id = c(1:nrow(gard_data))
#head(gard_data)
q1_data = gard_data %>%
  mutate(AgeGroup = as.factor(AgeGroup),
         Race = as.factor(Race),
         Shots = as.factor(Shots),
         InsuranceType = as.factor(InsuranceType),
         MedAssist = as.factor(MedAssist),
         Location = as.factor(Location),
         LocationType = as.factor(LocationType))
summary(q1_data[q1_data$PracticeType==0,c(1:8)])
summary(q1_data[q1_data$PracticeType==1,c(1:8)])
summary(q1_data[q1_data$PracticeType==2,c(1:8)])
q2_data = q1_data %>%
  mutate(PracticeType_bin = ifelse(PracticeType==2,1,0)) %>%
  select(-PracticeType)
summary(q2_data[q2_data$PracticeType_bin==1,c(1:8)])
summary(q2_data[q2_data$PracticeType_bin==0,c(1:8)])
q3_data = q2_data %>%
 filter(Location %in% c(1,4))
summary(q3 data[q3 data$PracticeType bin==0,c(1:8)])
summary(q3_data[q3_data$PracticeType_bin==1,c(1:8)])
ps.model<-glm(PracticeType_bin~Age + Race + InsuranceType + Location,data=q3_data, family = binomial)
summary(ps.model)
ps <- predict(ps.model, type="response")</pre>
x = q3_{data}
prop.func <- function(x, trt){</pre>
  # fit propensity score model
  propens.model <- glm(trt ~ Age + Race + InsuranceType + Location, data=x, family = binomial)</pre>
```

```
pi.x <- predict(propens.model, type = "response")</pre>
  pi.x
check.overlap(x = x,
               trt = q3_data$PracticeType_bin,
               type = "both",
               propensity.func = prop.func)
trim_data = x[ps>=min(ps[q3_data$PracticeType_bin==1]) & ps <= max(ps[q3_data$PracticeType_bin==0]),]
ps.model<-glm(PracticeType_bin ~ Age + Race + InsuranceType + Location, data=trim_data, family = binomi
ps <- predict(ps.model, type="response")</pre>
x = trim_data
prop.func <- function(x, trt){</pre>
  # fit propensity score model
  propens.model <- glm(trt~Age + Race + InsuranceType + Location, data=x, family = binomial)</pre>
  pi.x <- predict(propens.model, type = "response")</pre>
  pi.x
check.overlap(x = x,
               trt = trim_data$PracticeType_bin,
               type = "both",
               propensity.func = prop.func)
vars <- c("Age" , "Race", "InsuranceType" ,"Location")</pre>
## Construct a table
cov_bal <- CreateTableOne(vars = vars, strata = "PracticeType_bin", data = trim_data, test = FALSE)</pre>
## Show table with SMD
print(cov_bal, smd = TRUE)
#creating subclasses
subclass.breaks = quantile(ps, c(.20, .40, .60, .80)) # bins (initial try - modify as needed)
subclass.breaks
subclass = ps
subclass = as.numeric(ps>subclass.breaks[1])
subclass[which(ps>subclass.breaks[1]& ps<=subclass.breaks[2])]<- 1</pre>
subclass[which(ps>subclass.breaks[2]& ps<=subclass.breaks[3])]<- 2</pre>
subclass[which(ps>subclass.breaks[3]& ps<=subclass.breaks[4])]<- 3</pre>
subclass[which(ps>subclass.breaks[4])]<- 4</pre>
#looking at sample sizes within each subclass
table(trim_data$PracticeType_bin, subclass)
prop.func <- function(x, trt) {</pre>
  ps[which(ps <= subclass.breaks[1])]</pre>
trim_data$ps <-ps</pre>
check.overlap(x = trim_data[which(trim_data$ps <=subclass.breaks[1]),],</pre>
               trt = trim_data$PracticeType_bin[which(trim_data$ps <= subclass.breaks[1])],</pre>
               type = "both",
               propensity.func = prop.func)
prop.func <- function(x, trt)</pre>
```

```
ps[which(ps>subclass.breaks[1]&ps<=subclass.breaks[2])]
}
trim_data$ps <-ps</pre>
check.overlap(x = trim_data[which(ps>subclass.breaks[1] %ps<=subclass.breaks[2]),],</pre>
              trt = trim_data$PracticeType_bin[which(ps>subclass.breaks[1]&ps<=subclass.breaks[2])],</pre>
              type = "both",
              propensity.func = prop.func)
prop.func <- function(x, trt)</pre>
{
  ps[which(ps>subclass.breaks[2]&ps<=subclass.breaks[3])]
trim_data$ps <-ps</pre>
check.overlap(x = trim_data[which(ps>subclass.breaks[2] ps<=subclass.breaks[3]),],</pre>
              trt = trim_data$PracticeType_bin[which(ps>subclass.breaks[2]&ps<=subclass.breaks[3])],</pre>
              type = "both",
              propensity.func = prop.func)
 prop.func <- function(x, trt)</pre>
   ps[which(ps>subclass.breaks[3])]
 }
 trim_data$ps <-ps</pre>
 check.overlap(x = trim_data[which(ps>subclass.breaks[3]),],
               trt = trim_data$PracticeType_bin[which(ps>subclass.breaks[3])],
               type = "both",
               propensity.func = prop.func)
tabUnmatched_s0 <- CreateTableOne(vars = vars, strata = "PracticeType_bin", data = trim_data[which(subc
tabUnmatched_s1 <- CreateTableOne(vars = vars, strata = "PracticeType_bin", data = trim_data[which(subc
tabUnmatched_s2 <- CreateTableOne(vars = vars, strata = "PracticeType_bin", data = trim_data[which(subc
tabUnmatched_s3 <- CreateTableOne(vars = vars, strata = "PracticeType_bin", data = trim_data[which(subc
## Show table with SMD
print(tabUnmatched_s0, smd = TRUE)
print(tabUnmatched_s1, smd = TRUE)
print(tabUnmatched_s2, smd = TRUE)
print(tabUnmatched_s3, smd = TRUE)
Completed_data <- read.table("./gardasil.dat",header = T) %>%
  mutate(id = c(1:nrow(gard_data))) %>%
  select(Completed, id)
q8_data = merge(Completed_data, trim_data)
ACEO <- mean(q8_data$Completed[which(subclass==0 & q8_data$PracticeType_bin==1)])-mean(q8_data$Complete
ACE1 <- mean(q8_data$Completed[which(subclass==1 & q8_data$PracticeType_bin==1)])-mean(q8_data$Complete
ACE2 <- mean(q8_data$Completed[which(subclass==2 & q8_data$PracticeType_bin==1)])-mean(q8_data$Complete
ACE3 <- mean(q8_data$Completed[which(subclass==3 & q8_data$PracticeType_bin==1)])-mean(q8_data$Complete
ACE4 <- mean(q8_data$Completed[which(subclass==4 & q8_data$PracticeType_bin==1)])-mean(q8_data$Complete
```

```
ace <- (nrow(q8_data[which(subclass==0),])/nrow(q8_data))*ACEO+
    (nrow(q8_data[which(subclass==1),])/nrow(q8_data))*ACE1+
    (nrow(q8_data[which(subclass==2),])/nrow(q8_data))*ACE2+
    (nrow(q8_data[which(subclass==3),])/nrow(q8_data))*ACE3+
    (nrow(q8_data[which(subclass==4),])/nrow(q8_data))*ACE4
v01 <- var(q8_data$Completed[which(subclass==0 & q8_data$PracticeType_bin==1)])
v00 <- var(q8_data$Completed[which(subclass==0 & q8_data$PracticeType_bin==0)])
v11 <- var(q8_data$Completed[which(subclass==1 & q8_data$PracticeType_bin==1)])
v10 <- var(q8_data$Completed[which(subclass==1 & q8_data$PracticeType_bin==0)])
v21 <- var(q8_data$Completed[which(subclass==2 & q8_data$PracticeType_bin==1)])
v20 <- var(q8_data$Completed[which(subclass==2 & q8_data$PracticeType_bin==0)])
v31 <- var(q8_data$Completed[which(subclass==3 & q8_data$PracticeType_bin==1)])
v30 <- var(q8_data$Completed[which(subclass==3 & q8_data$PracticeType_bin==0)])
v41 <- var(q8_data$Completed[which(subclass==4 & q8_data$PracticeType_bin==1)])
v40 <- var(q8_data$Completed[which(subclass==4 & q8_data$PracticeType_bin==0)])
n0 <- nrow(q8_data[which(subclass==0),])</pre>
n1 <- nrow(q8_data[which(subclass==1),])</pre>
n2 <- nrow(q8_data[which(subclass==2),])</pre>
n3 <- nrow(q8_data[which(subclass==3),])</pre>
n4 <- nrow(q8_data[which(subclass==4),])</pre>
n01 <- nrow(q8_data[which(subclass==0& q8_data$PracticeType_bin==1),])
n11 <- nrow(q8_data[which(subclass==1& q8_data$PracticeType_bin==1),])
n21 <- nrow(q8_data[which(subclass==2& q8_data$PracticeType_bin==1),])
n31 <- nrow(q8_data[which(subclass==3& q8_data$PracticeType_bin==1),])
n41 <- nrow(q8_data[which(subclass==4& q8_data$PracticeType_bin==1),])
n00 <- nrow(q8_data[which(subclass==0& q8_data$PracticeType_bin==0),])
n10 <- nrow(q8_data[which(subclass==1& q8_data$PracticeType_bin==0),])
n20 <- nrow(q8_data[which(subclass==2& q8_data$PracticeType_bin==0),])
n30 <- nrow(q8_data[which(subclass==3& q8_data$PracticeType_bin==0),])
n40 <- nrow(q8_data[which(subclass==4& q8_data$PracticeType_bin==0),])
 varace <-(n1)^2/nrow(q8_data)^2*((v11/n11)+(v10/n10))+(n2)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3) + (n2)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3) + (n2)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(n3)^2/nrow(q8_data)^2*((v21/n21)+(v20/n20))+(v20/n20)^2*((v21/n21)+(v20/n20))+(v20/n20)^2*((v21/n21)+(v20/n20))+(v20/n20)^2*((v21/n20)+(v20/n20))+(v20/n20)^2*((v21/n20)+(v20/n20))+(v20/n20)^2*((v21/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/n20)+(v20/
sdace<-sqrt(varace)</pre>
CIL=ace-sdace*2
CIU=ace+sdace*2
#glm.model <- glm(Completed~PracticeType_bin + Age + Race + InsuranceType + Location, data=q8_data, fam
lm.model = lm(Completed~PracticeType_bin + Age + Race + InsuranceType + Location, data=q8_data)
#summary(glm.model)
summary(lm.model)
```