

# Automatic Relation-aware Graph Network Proliferation

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## Abstract

*Graph neural architecture search has sparked much attention as Graph Neural Networks (GNNs) have shown powerful reasoning capability in many relational tasks. However, the currently used graph search space overemphasizes learning node features and neglects mining hierarchical relational information. Moreover, due to diverse mechanisms in the message passing, the graph search space is much larger than that of CNNs. This hinders the straightforward application of classical search strategies for exploring complicated graph search space. We propose Automatic Relation-aware Graph Network Proliferation (ARGNP) for efficiently searching GNNs with a relation-guided message passing mechanism. Specifically, we first devise a novel dual relation-aware graph search space that comprises both node and relation learning operations. These operations can extract hierarchical node/relational information and provide anisotropic guidance for message passing on a graph. Second, analogous to cell proliferation, we design a network proliferation search paradigm to progressively determine the GNN architectures by iteratively performing network division and differentiation. The experiments on six datasets for four graph learning tasks demonstrate that GNNs produced by our method are superior to the current state-of-the-art hand-crafted and search-based GNNs. Codes are available at <https://github.com/phython96/ARGNP>.*

## 1. Introduction

Graph neural networks (GNNs), as a dominant paradigm to handle graph-structured data, have significantly promoted the performance in many relation reasoning tasks, such as molecular prediction [7, 15, 18, 24], social network analysis [35, 40], 3D point cloud recognition [30, 31, 47, 54],

object detection [19, 22], semantic segmentation [23, 33, 53], few-shot learning [26, 50, 60], etc. Despite their great success, the architectures of GNNs are usually manually designed, which requires tremendous expert knowledge and intensive trial and error. To explore advanced GNN architectures and reduce the human intervention, researchers attempt to automate the design process with the help of neural architecture search (NAS) [17, 36, 43, 64, 65] and have achieved superior performance. This is known as graph neural architecture search, where there are two most critical components: (1) graph search space and (2) search strategy.

The graph search space defines which graph neural networks can be represented in principle, determining the upper bound of networks' reasoning capability. Current graph search space mainly focuses on designing node-learning operations, which is categorized into macro search space [32, 43] and micro search space [11, 17, 36, 65]. The former explores the combinations of existing message passing mechanisms (i.e., using general-purpose GNNs as candidate operations), while the latter emphasizes the construction for novel ones (i.e., designing fine-grained operations such as node aggregating and feature combining functions). However, they all neglect mining the latent hierarchical relational information associated with edges. In fact, relational information can provide anisotropic guidance for message aggregation of neighboring nodes, which is critical for constructing relation-guided message passing mechanisms. Motivated by this, in this paper, we explore designing micro graph search space from the perspective of learning both hierarchical relation and node features.

The search strategy details how to explore search space, determining the search efficiency and effect. Some early works [17, 64, 65] apply reinforcement learning (RL) based strategy to search for GNNs by building, training, and evaluating various graph neural architectures from scratch, which is extremely time-consuming. Recently, due to the high computational efficiency, one-shot differentiable strategies [11, 32, 36] have attracted a lot of interest, which

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consists of three stages: supernet training, subnet searching, and subnet retraining. They boost the search efficiency from the parameter sharing among subnets and supernet. Using the auxiliary supernet can avoid training each child graph neural architecture individually, but this may cause severe subnet interference [62, 63]. Besides, it is limited in searching large GNN architectures due to the quadratic complexity of storing and training the supernet. As a compromise, researchers introduce the cell trick where the architecture is a stack of several same building blocks [11, 32, 36, 39]. This shifts the searching objective from the whole architecture to small cells but seriously narrows the original search space. The above limitations, *i.e.* the subnet interference, the high space-time complexity and the shrink of search space, bring a severe negative impact for graph neural architecture search.

In this paper, we propose the Automatic Relation-aware Graph Network Proliferation (ARGNP) to efficiently search the optimal GNN architectures with a relation-guided message passing mechanism. First, we design a dual relation-aware graph search space comprising both relation and node search space, as shown in Figure 2. The relation search space introduces diverse relation-mining operations to extract relational information hidden in edge-connected nodes. It allows arbitrary valid connection modes among relation-mining operations and forms the hierarchical relation-learning structure. Different connection modes result in the group of relation features with different message-passing preferences, which favors different graph tasks. The node search space defines a series of node-learning operations which implements the anisotropic message aggregation under the guidance of relation features.

Second, analogous to cell proliferation, we devise a novel search paradigm called *network proliferation* to progressively explore the graph search space. Instead of directly optimizing the global supernet, we search the final graph neural architecture by iteratively performing network division and network differentiation. Figure 1 shows one iteration process. During network division, each intermediate feature vertex is divided into two parts. One retains original operations and connections while the other builds a local supernet. Network differentiation aims to differentiate the local supernet into a specific subnet. Theoretically, we proved that such a search paradigm achieves the linear space-time complexity. This enables our search to thoroughly free from the cell trick. The network proliferation decomposes the training of global supernet into sequential local supernets optimization, which alleviates the interference among child graph neural architectures.

Our contributions are summarized as follows: (1) A novel dual relation-aware graph search space comprising both node and relation search space. It can derive GNNs with a relation-guided message passing mechanism. (2) A

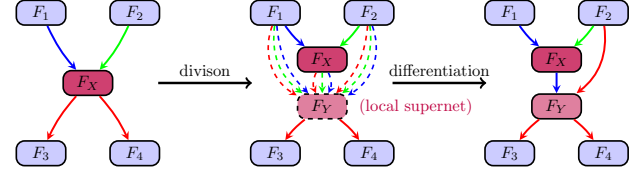


Figure 1. **One iteration of the proposed network proliferation search paradigm.**  $F_{(\cdot)}$  denotes the intermediate feature vertex in an architecture. The edges with different colors are associated with different operations.  $F_Y$  is the newly divided part of  $F_X$ , which joins  $F_1$ ,  $F_2$  and  $F_X$  to build a local supernet.

network proliferation search paradigm. It sequentially performs network division and differentiation to explore the optimal GNN architecture within linear space-time complexity. (3) Experiment results on six datasets for four classical graph learning tasks show that our method outperforms human-crafted and other search-based GNNs by a large margin. The code will be released publicly.

## 2. Related Work

**Graph Neural Networks (GNNs)** have been successfully applied to operate on the graph-structure data [8, 9, 14, 20, 28, 52, 58, 61]. Current GNNs are constructed on message passing mechanisms and can be categorized into two groups, isotropic and anisotropic. Isotropic GNNs [20, 28, 58] aim at extending the original convolution operation to graphs. Anisotropic GNNs enhance the original models with anisotropic operations on graphs [44], such as gating and attention mechanism [8, 41, 42, 52, 61]. Anisotropic methods usually achieve better performance, since they can weigh the importance of edges according to the node features and implement the adaptive feature aggregation.

**Neural Architecture Search (NAS)** aims at automatically finding the optimal neural architectures specific to dataset [4, 10, 13, 31, 37, 39, 39, 45, 56, 66]. Search space and strategy are the most essential components in NAS. Search space defines which architectures can be represented in principle. Search strategy details how to explore the search space. Methods can be mainly categorized into three groups, *i.e.*, reinforcement learning (RL) [4, 45, 66], evolutionary algorithms (EA) [38, 48, 49] and gradient-based (GB) [10, 13, 31, 37, 39, 59]. Benefiting from the high efficiency, gradient-based differentiable search strategies attracted the attention of increasing researchers.

**Graph Neural Architecture Search (GNAS)** is proposed to automatically find the best GNNs for the given specific graph task. The current GNAS methods [11, 17, 36, 43, 64, 65] mainly focus on designing graph search space by introducing neighbor aggregation, activation functions, *etc.*, but neglect the importance of relation mining. To our best knowledge, we are the first to take mining relational information into account during devising graph search space.

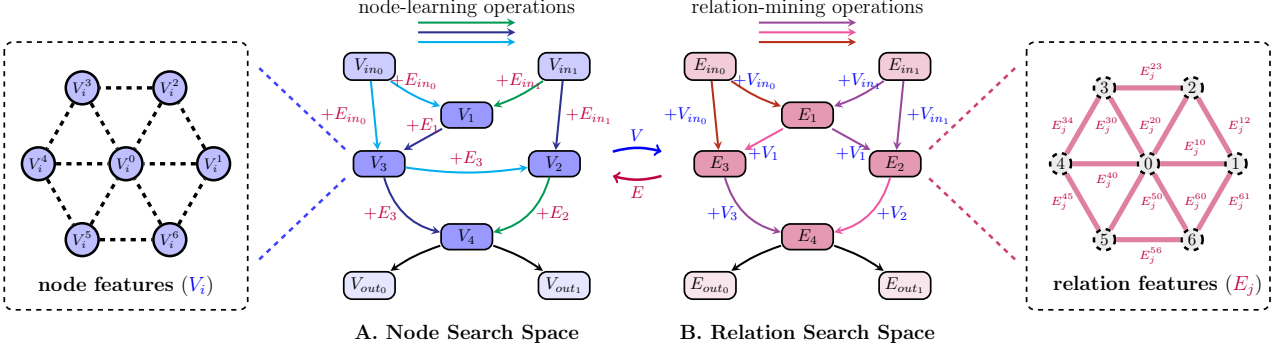


Figure 2. **Our dual relation-aware graph search space.** It comprises node and relation search space. The vertex  $V_i$  and vertex  $E_j$  denote a group of node and relation features on the graph, respectively.  $+E_j$  means that learning node features require the guidance of relation features.  $+V_i$  means that the node features are required when extracting relational information.

### 3. Method

#### 3.1. Preliminaries

A graph neural architecture uses graph-structured data as input and outputs high-dimensional node and edge features (relation features). The input data can be represented as  $\{G, V_{in}, E_{in}\}$ , where  $G$  is the input graph structure with  $n$  nodes and  $m$  edges,  $V_{in} \in \mathbb{R}^{n \times d_v}$  denotes the input node features,  $E_{in} \in \mathbb{R}^{m \times d_e}$  denotes the input edge features,  $d_v$  and  $d_e$  denote the feature dimension. Notably, if there is no original edge feature in the dataset, we initialize  $E_{in}$  with  $[1, \dots, 1] \in \mathbb{R}^{m \times 1}$  for subsequent relation learning. Our dual relation-aware graph search space comprises both node and edge search space. The derived computation structure of node or relation search space is a directed acyclic graph (DAG). To avoid confusion, the node and edge in the DAG is renamed to “vertex” and “link”, where “vertex” denotes an intermediate features ( $V_i$  or  $E_j$ ), the “link” is associated with an operation  $o$  or a mixture operation  $\bar{o}$ .

#### 3.2. Relation-aware Graph Search Space

In this subsection, we detail how our dual relation-aware graph search space is devised. As shown in Figure 2, it comprises node search space and relation search space. These two spaces are not individual in essence, instead, they communicate information with each other. The relational information is extracted from node features. In turn, it provides anisotropic guidance for learning better node features.

**Node search space.** The computation structure derived by node search space is a directed acyclic graph, which consists of an ordered sequence of  $N+4$  vertices, which constitutes the set  $\{V_{in_0}, V_{in_1}, V_1, \dots, V_N, V_{out_0}, V_{out_1}\}$ . Each vertex is a latent representation denoted as  $V_i$  (i.e., node features in a GNN layer, as shown in the left of Figure 2), where  $i$  is its topological order in the DAG. In order to be compatible with the cell trick, we introduce two input vertices and two output vertices.  $V_{in_0}$  and  $V_{in_1}$  are the outputs of previous two cells while  $V_{out_0}$  and  $V_{out_1}$

are the inputs of post two cells. In fact, our method can thoroughly free from the cell trick. In this situation, we have  $V_{in_0} = V_{in_1}, V_{out_0} = V_{out_1}$ . Each directed link  $(i, j)$  in the DAG is associated with one node-learning operation  $\mathcal{O}_V^{(i,j)}$ , that transforms the information from  $V_i$  to  $V_j$ , guided by relation features  $E_i$ . The transformed information is denoted as  $V_{i \rightarrow j} = \mathcal{O}_V^{(i,j)}(V_i, E_i, f_{i,j})$ , where  $f_{i,j}$  is an aggregating function which takes multiset as input, such as *mean*, *max*, *sum*, *std*, etc. We leverage feature-wise linear modulation (FiLM) mechanism [9] to implement the anisotropic guidance of message propagation. This allows the model to dynamically up-weight and down-weight node features based on the relational information. Specifically, we compute an element-wise affine transformation  $\gamma$  and  $\beta$  based on the input relation features  $E_i$  and use it to modulate the incoming messages during message passing. Given a node  $t$  on the graph, its transformed feature  $V_{i \rightarrow j}^t$  is formulated as follows

$$V_{i \rightarrow j}^t = f_{i,j}(\{\gamma_{s,t} \odot V_i^s + \beta_{s,t} | s \in \mathcal{N}(t)\}), \quad (1)$$

$$\gamma_{s,t}, \beta_{s,t} = g(E_i^{s,t}; \theta),$$

where  $g(\cdot)$  is a two-layer multilayer perceptron to compute affine transformation with the learnable parameters  $\theta$ ,  $\mathcal{N}(t)$  denotes the set of neighbors of target node  $t$  on the graph. Following previous works [11, 32, 36, 39], we allow two inputs for each intermediate vertex, i.e.,  $V_i = V_{p_1 \rightarrow i} + V_{p_2 \rightarrow i}$ , where  $p_1, p_2 \in \{in_0, in_1, 1, 2, \dots, i-1\}$ . For each node-learning operation, its aggregating function is optional. Different aggregating function  $f_{i,j}$  captures different types of information. For example, *sum* captures the structural information [58], *max* captures the representative information, *mean* and *std* captures the statistical information from the neighboring nodes. The node search space has 8 candidate node-learning operations: *V\_MAX*, *V\_SUM*, *V\_MEAN*, *V\_STD*, *V\_GEM2*, *V\_GEM3*, *skip-connect*, and *zero* operation. We detail all eight node-learning operation options in the supplementary material.

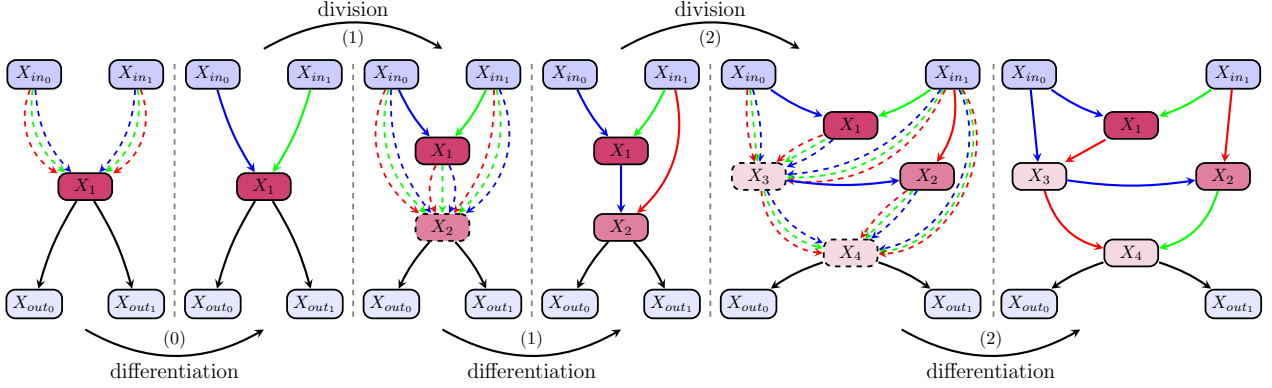


Figure 3. **Illustration of network proliferation search paradigm.** It comprises two procedures of network division and differentiation. The edges with different colors are associated with different operations. A group of dashed edges denotes a mixture operation. A local supernet comprises of three mixture operations pointing to one feature vertex. (i) denotes the  $i$ -th iteration.

**Relation search space.** The computation structure derived by relation search space is also a directed acyclic graph with the same number of vertices. Each vertex  $E_i$  is a latent relation representation (*i.e.*, edge features in a GNN layer, as shown in the right of Figure 2). The directed link  $(i, j)$  in the DAG is associated with a relation-mining operation  $o_{\mathcal{E}}^{(i,j)}$ . It extracts relational information from node features  $V_i$ . The extracted information is joined with  $E_i$  to obtain higher order relation representation  $E_{i \rightarrow j} = o_{\mathcal{E}}^{(i,j)}(V_i, E_i, h_{i,j})$ .  $h_{i,j}$  is a relation-mining function, such as *subtraction*, *hardmard product*, *gauss kernel*, *etc.* Given a specific edge  $(s, t)$  on the graph,  $E_{i \rightarrow j}^{s,t}$  can be computed using feature-wise linear modulation (FiLM):

$$\begin{aligned} E_{i \rightarrow j}^{s,t} &= \gamma_{s,t} \odot E_i^{s,t} + \beta_{s,t}, \\ \gamma_{s,t}, \beta_{s,t} &= h_{i,j}(V_i^s, V_i^t; \theta), \end{aligned} \quad (2)$$

where  $\gamma_{s,t}, \beta_{s,t}$  is the affine transformation learned by  $h_{i,j}$ ,  $\theta$  is the learnable parameters. This allows adaptive relational information fusion. Similar to node search space, we assume that each intermediate vertex has only two inputs, *i.e.*,  $E_i = E_{p_1 \rightarrow i} + E_{p_2 \rightarrow i}$ , where  $p_1, p_2 \in \{in_0, in_1, 1, 2, \dots, i-1\}$ . Different relation-mining operations focus on extracting different types of relational information. For example, *subtraction* captures the relative change while *hardmard product* emphasizes on the commonalities between the edge-connected nodes. The relation search space has 8 candidate relation-mining operations: *E\_SUB*, *E\_GAUSS*, *E\_HAD*, *E\_MAX*, *E\_SUM*, *E\_MEAN*, *skip-connect*, and *zero* operation. Eight candidate options of the relation-mining function are detailed in the supplementary material.

### 3.3. Network Proliferation Search Paradigm

We detail how the proposed network proliferation search paradigm explores a single search space (*e.g.*, node or rela-

#### Algorithm 1 Network Proliferation Search Paradigm

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**Input:** a search algorithm  $\mathcal{A}$ , architecture size  $\mathcal{S}$   
**Output:** a graph neural architecture defined by  $\{\mathbb{V}, \mathbb{L}\}$   
**Define:**  $e(X_s, X_t, O)$  is a link from  $X_s$  to  $X_t$  with an operation  $O$ , where  $O \in \{o, \bar{o}\}$ ,  $\bar{o}$  is the mixture operation

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1:  $\mathbb{V} \leftarrow \{X_1\}$ 
2:  $\mathbb{L} \leftarrow \{e(X_{in_0}, X_1, \bar{o}), e(X_{in_1}, X_1, \bar{o})\}$ 
3: while True do
4:   // network differentiation
5:    $\mathbb{V}_r \leftarrow \mathbb{V} \cup \{X_{in_0}, X_{in_1}\}$ 
6:   Create a graph neural architecture  $\mathcal{G}$  from  $\{\mathbb{V}_r, \mathbb{L}\}$ 
7:   Initialize  $\mathcal{G}$  with new parameters
8:   Perform search algorithm:  $\mathbb{L} \leftarrow \mathcal{A}(\mathcal{G})$ 
9:   if  $len(\mathbb{V}) \geq \mathcal{S}$  then
10:    return  $\{\mathbb{V}_r, \mathbb{L}\}$ 
11:   // network division
12:    $\mathbb{V}_{tmp} \leftarrow \mathbb{V}, \mathbb{L}_{tmp} \leftarrow \mathbb{L}, l \leftarrow len(\mathbb{V})$ 
13:   for  $X_i$  in  $\mathbb{V}_{tmp}$  do
14:      $\mathbb{V} \leftarrow \mathbb{V} \cup \{X_{i+l}\}$ 
15:      $\mathbb{L} \leftarrow \mathbb{L} \cup \{e(X_i, X_{i+l}, \bar{o})\}$ 
16:     for  $e(X_s, X_t, O)|_{t=i}$  in  $\mathbb{L}_{tmp}$  do
17:        $\mathbb{L} \leftarrow \mathbb{L} \cup \{e(X_s, X_{i+l}, \bar{o})\}$ 
18:    $\mathbb{L}_{tmp} \leftarrow \mathbb{L}$ 
19:   for  $e(X_s, X_t, O)|_{s \in \mathbb{V}_{tmp}, s+l \neq t}$  in  $\mathbb{L}_{tmp}$  do
20:      $\mathbb{L} \leftarrow \mathbb{L} \cup \{e(X_{s+l}, X_t, O)\} / \{e(X_s, X_t, O)\}$ 

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tion search space) for simplicity. Since our dual relation-aware graph search space comprising node and relation search space is symmetric, it can be generalized to search the whole dual space simultaneously.

Motivated by the observation that a well-performed small architecture can provide a good skeleton for building a larger one (shown in Figure 4), we can efficiently obtain the expected large architecture through iterative search





Figure 4. **Boxplots of 8-layer architectures on ZINC.** “R” and “S” denote the random and SGAS [31] search strategies, respectively. *e.g.*, architecture “RS” is constructed by sequentially performing random search, network division and SGAS search. The architecture size after the first and the second search is 4 and 8. Comparing “RR” with “SR”, “RS” with “SS”, we find that a pre-searched architecture is useful for subsequent search.

based on the current small architecture. We detail this procedure in Figure 3 and Algorithm 1. Each iterative search comprises of two subprocedures, *i.e.*, network division, and network differentiation. Network division builds a  $2\times$  larger architecture based on the current architecture, where each feature vertex is divided into two parts. One part that retains original operations and connections is called parent vertex ( $X_p$ ), whose role is to provide the architecture skeleton. The other one is called newly divided vertex ( $X_n$ ), which joins  $X_p$  and  $X_p$ ’s two input vertices  $X_{p_1}, X_{p_2}$  to build a local supernet. We define the mixture operation is parameterized by architectural parameters  $\alpha^{(i,j)}$  as a softmax mixture over all the possible operations within the operation space  $\mathcal{O}$ , *i.e.*,  $\bar{o}^{(i,j)}(X_i) = \frac{\exp(\alpha_o^{(i,j)})}{\sum_{o' \in \mathcal{O}} \exp(\alpha_{o'}^{(i,j)})} o(X_i)$ . The local supernet contains three mixture operations, which is represented as follows,

$$X_n = \bar{o}^{(p,n)}(X_p) + \bar{o}^{(p_1,n)}(X_{p_1}) + \bar{o}^{(p_2,n)}(X_{p_2}). \quad (3)$$

Since the local supernet contains  $C_3^2 \times |\mathcal{O}|$  candidate local subnets, we need to discretize it to one specific subnet. This is called network differentiation. During this procedure, we can adopt any search algorithms [12, 21, 32, 39, 57, 59], that can discretize the supernet to the subnet. After the network differentiation, each mixture operation in the architecture is replaced with one specific operation. The algorithm terminates until the size of the architecture reaches the pre-defined threshold.

Next, we analyze the complexity of our network proliferation search paradigm. The running time and occupied memory are proportional to the number of operations. It requires  $\log(N)$  iterations for searching for architecture with  $N$  feature vertices. During the  $i$ -th iteration, there are  $2^{i-1} \times 2$  operations and  $2^{i-1} \times 3$  mixture operations, *i.e.*,  $2^i + 3 \times 2^{i-1}|\mathcal{O}|$  operations in total. So the whole complexity is  $O(\sum_{i=1}^{\log(N)} 2^i + 3 \times 2^{i-1}|\mathcal{O}|) = O(N|\mathcal{O}|)$ . Compared with vanilla DARTS [39] ( $O(N^2|\mathcal{O}|)$  complexity), our method reduces the complexity from quadratic to linear. This enables ours to directly search for large neu-

ral architectures without relying on the cell trick, and this also enlarges the global search space. For example, we try to search for an architecture with  $N = 16, |\mathcal{O}| = 8$ . In general, due to the high complexity, the DARTS stacks 4 cells with 4 feature vertices in each of them, resulting in  $3.0 \times 10^9$  candidate architectures. Compared with vanilla DARTS, our search paradigm can explore up to  $3.4 \times 10^{36}$  candidate architectures using comparable resources.

## 4. Experiments

### 4.1. Experimental Setups

**Dataset.** We evaluate our method on six datasets, *i.e.*, ZINC [25], CLUSTER [16], CIFAR10 [29], TSP [16], ModelNet10 [55], ModelNet40 [55] across four different graph learning tasks (node classification, edge classification, graph classification and graph regression). ZINC is one popular real-world molecular dataset of 250K graphs, whose task is graph property regression, out of which we select 12K for efficiency following works [11, 14, 16]. CLUSTER is the node classification tasks generated via Stochastic Block Models [1], which are used to model communications in social networks by modulating the intra-community and extra-community connections. CIFAR10 is the original classical image classification dataset and converted into graphs using superpixel [2] algorithm to test graph classification task. TSP dataset is based on the classical *Travelling Salesman Problem*, which tests edge classification on 2D Euclidean graphs to identify edges belonging to the optimal TSP solution. ModelNet is a dataset for 3D object recognition with two variants, ModelNet10 and ModelNet40, which comprise objects from 10 and 40 classes, respectively. We sample 1024 points for each object as input and use  $k$ -NN algorithm to construct the edges ( $k = 9$  by default unless it is specified).

**Searching settings.** The original architecture is initialized with 2 feature vertices. We perform *network proliferation* for 4 iterations to obtain a sequence of GNN architectures with the size of  $\{2, 4, 8, 16\}$ . Specifically, we choose SGAS [31] as the search strategy that can differentiate the local supernet to a specific subnet. During the network differentiation, after warming up for 10 epochs, SGAS begins to simultaneously determine one node-learning operation and one relation-mining operation for every 5 epochs. Thus, the search epoch is set to  $\{25, 25, 45, 85\}$  for 4 sequential iterations. To carry out the architecture search, we hold out half of the training data as the validation set. For one-shot differentiable search strategies (SGAS [31] and DARTS [39]), there are operation weights  $w$  and architectural parameters  $\alpha$  to be optimized. We use momentum SGD to optimize the weights  $w$ , with initial learning rate  $\eta_w = 0.025$  (annealed down to zero following a cosine schedule without restart), momentum 0.9, and weight

Table 1. **Comparison with state-of-the-art architectures on the CLUSTER, ZINC, CIFAR10 and TSP datasets.**  $\textcircled{m}$  denotes the architecture is manually designed. The indicator E denotes whether the architecture can learn edge feature. The ARGNP without edge feature means that the relation space is removed from relation-aware graph search space. Note that mean and standard deviation are computed across 4 independently searched GNN architectures.

Architecture	E $\checkmark$	Node Level			Graph Level						Edge Level		
		CLUSTER			ZINC			CIFAR10			TSP		
		Metric (AA %) $\uparrow$	Params (M)	Search (day)	Metric (MAE) $\downarrow$	Params (M)	Search (day)	Metric (OA %) $\uparrow$	Params (M)	Search (day)	Metric (F1) $\uparrow$	Params (M)	Search (day)
GCN [28]	$\times$	$68.50 \pm 0.98$	0.50	$\textcircled{m}$	$0.367 \pm 0.011$	0.50	$\textcircled{m}$	$56.34 \pm 0.38$	0.10	$\textcircled{m}$	$0.630 \pm 0.001$	0.10	$\textcircled{m}$
GIN [58]	$\times$	$64.72 \pm 1.55$	0.52	$\textcircled{m}$	$0.526 \pm 0.051$	0.51	$\textcircled{m}$	$55.26 \pm 1.53$	0.10	$\textcircled{m}$	$0.656 \pm 0.003$	0.10	$\textcircled{m}$
GraphSage [20]	$\times$	$63.84 \pm 0.11$	0.50	$\textcircled{m}$	$0.398 \pm 0.002$	0.51	$\textcircled{m}$	$65.77 \pm 0.31$	0.10	$\textcircled{m}$	$0.665 \pm 0.003$	0.10	$\textcircled{m}$
GAT [52]	$\times$	$70.59 \pm 0.45$	0.53	$\textcircled{m}$	$0.384 \pm 0.007$	0.53	$\textcircled{m}$	$64.22 \pm 0.46$	0.11	$\textcircled{m}$	$0.671 \pm 0.002$	0.10	$\textcircled{m}$
GatedGCN [8]	$\checkmark$	$76.08 \pm 0.34$	0.50	$\textcircled{m}$	$0.214 \pm 0.013$	0.51	$\textcircled{m}$	$67.31 \pm 0.31$	0.10	$\textcircled{m}$	$0.838 \pm 0.002$	0.53	$\textcircled{m}$
PNA [14]	$\times$	N/A	N/A	N/A	$0.320 \pm 0.032$	0.39	$\textcircled{m}$	$70.46 \pm 0.44$	0.11	$\textcircled{m}$	N/A	N/A	N/A
PNA [14]	$\checkmark$	N/A	N/A	N/A	$0.188 \pm 0.004$	0.39	$\textcircled{m}$	$70.47 \pm 0.72$	0.11	$\textcircled{m}$	N/A	N/A	N/A
DGN [5]	$\times$	N/A	N/A	N/A	$0.219 \pm 0.010$	0.39	$\textcircled{m}$	$72.70 \pm 0.54$	0.11	$\textcircled{m}$	N/A	N/A	N/A
DGN [5]	$\checkmark$	N/A	N/A	N/A	$0.168 \pm 0.003$	0.39	$\textcircled{m}$	$72.84 \pm 0.42$	0.11	$\textcircled{m}$	N/A	N/A	N/A
GNAS-MP [11]	$\times$	$74.77 \pm 0.15$	1.61	0.80	$0.242 \pm 0.005$	1.20	0.40	$70.10 \pm 0.44$	0.43	3.20	$0.742 \pm 0.002$	1.20	2.10
ARGNP (2)	$\times$	$61.61 \pm 0.27$	0.07	0.04	$0.430 \pm 0.003$	0.09	0.01	$66.55 \pm 0.13$	0.10	0.11	$0.655 \pm 0.003$	0.09	0.05
ARGNP (4)	$\times$	$64.06 \pm 0.45$	0.14	0.07	$0.303 \pm 0.013$	0.14	0.01	$66.65 \pm 0.39$	0.18	0.14	$0.668 \pm 0.003$	0.17	0.06
ARGNP (8)	$\times$	$68.73 \pm 0.12$	0.25	0.20	$0.239 \pm 0.009$	0.27	0.02	$67.37 \pm 0.32$	0.33	0.48	$0.674 \pm 0.002$	0.29	0.21
ARGNP (16)	$\times$	$71.92 \pm 0.29$	0.53	0.71	$0.221 \pm 0.004$	0.51	0.06	$67.10 \pm 0.51$	0.58	1.77	$0.684 \pm 0.002$	0.56	0.76
ARGNP (2)	$\checkmark$	$64.99 \pm 0.31$	0.08	0.06	$0.318 \pm 0.009$	0.08	0.01	$69.14 \pm 0.30$	0.10	0.17	$0.773 \pm 0.001$	0.08	0.08
ARGNP (4)	$\checkmark$	$74.75 \pm 0.25$	0.15	0.09	$0.197 \pm 0.006$	0.15	0.01	$71.83 \pm 0.32$	0.17	0.23	$0.821 \pm 0.001$	0.14	0.10
ARGNP (8)	$\checkmark$	$76.32 \pm 0.03$	0.29	0.31	$0.155 \pm 0.003$	0.28	0.04	$73.72 \pm 0.32$	0.33	0.84	$0.841 \pm 0.001$	0.30	0.39
ARGNP (16)	$\checkmark$	<b><math>77.35 \pm 0.05</math></b>	0.52	1.10	<b><math>0.136 \pm 0.002</math></b>	0.52	0.15	<b><math>73.90 \pm 0.15</math></b>	0.64	2.95	<b><math>0.855 \pm 0.001</math></b>	0.62	1.23

decay  $3 \times 10^{-4}$ . We use Adam [27] as the optimizer for  $\alpha$ , with initial learning rate  $\eta_\alpha = 3 \times 10^{-4}$ , momentum  $\beta = (0.5, 0.999)$  and weight decay  $10^{-3}$ .

**Training settings.** We follow all the training settings (data splits, optimizer, metrics, *etc.*) in work [11, 16]. Specifically, we adopt Adam [27] with the same learning rate decay for all runs. The learning rate is initialized with  $10^{-3}$ , which is reduced by half if the validation loss stops decreasing after 20 epochs. The weight decay is set to 0. The dropout is set to 0.5 to alleviate the overfitting. Our architectures are all trained for 400 epochs with a batch size of 32. We report the mean and standard deviation of the metric on the test dataset of 4 discovered architectures. These experiments are run on a single NVIDIA GeForce RTX 3090 GPU.

## 4.2. Results and Analysis

In Table 1 and Table 2, we compare our ARGNP with the state-of-the-art hand-crafted and search-based GNN architectures on the CLUSTER, ZINC, CIFAR10, TSP, ModelNet10, and ModelNet40 datasets. The evaluation metric is the average accuracy (AA) for CLUSTER, mean absolute error (MAE) for ZINC, F1-score (F1) for TSP. For CIFAR10, ModelNet10, and ModelNet40, we use the overall accuracy (OA) as the evaluation metric. To make a fair comparison, we also report the architecture parameters, the search cost, and the mean and standard deviation of all the metrics. We can see that, on all the six datasets for four classical graph learning tasks, the GNN architec-

tures discovered by our ARGNP surpass the state-of-the-art architectures by a large margin in terms of both mean and standard deviation. Compared with the state-of-the-art search-based method GNAS-MP [11], our searched architecture can easily achieve better performance with only  $\frac{1}{10} \sim \frac{1}{4}$  parameters. This benefits from that the relation-aware graph search space can mine hierarchical relation information (such as local structural similarity) to guide anisotropic message passing. Moreover, the network proliferation search paradigm can efficiently and effectively explore the proposed search space. We visualize the best-performed GNN architecture with the size of 4 in Figure 5, which is searched on the ModelNet40 dataset. Other examples are provided in the supplementary material.

## 4.3. Ablation of Search Space

We study the influence of the relation search space in our proposed relation-aware graph search. First, we construct a search space variant by removing the relation search space. Then we perform GNN architecture search on this variant using the network proliferation search paradigm and obtain a sequence of GNN architectures with the size of  $\{2, 4, 8, 16\}$ . These GNN architectures are evaluated on six datasets. For a fair comparison, we increase the dimension of the node features to keep the architectural parameters comparable. As shown in Table 1 and Table 2, the best performance of the search space variant without relation learning descends by a large margin. Under all the differ-

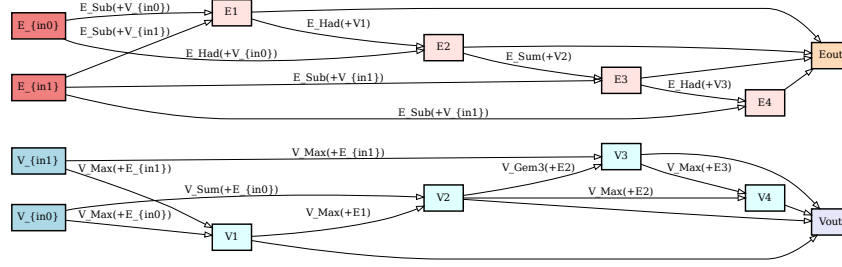


Figure 5. The best GNN architecture with the network size of 4 searched on the ModelNet40 dataset.

Table 2. Comparison with state-of-the-art architectures on the ModelNet10 and ModelNet40 datasets at 3D point cloud recognition task. L denotes the size of GNN architecture.

Architecture	ModelNet10		ModelNet40		Params (M)	Search (Day)
	L (#)	E (✓)	Metric (OA %) ↑	Metric (OA %) ↑		
3DmFV [6]	/	/	95.2	91.6	45.77	Ⓜ
PointNet++ [46]	/	/	N/A	90.7	1.48	Ⓜ
PCNN [3]	/	/	N/A	92.3	8.20	Ⓜ
PointCNN [34]	/	/	N/A	92.2	0.60	Ⓜ
DGCNN [54]	/	/	N/A	92.2	1.84	Ⓜ
KPConv [51]	/	/	N/A	92.9	14.3	Ⓜ
SGAS [31]	9	✓	N/A	92.93±0.19	8.87	0.19
ARGNP	2 ×	✓	93.20±0.24	91.11±0.24	1.80	0.03
ARGNP	4 ×	✓	93.86±0.25	91.30±0.22	2.27	0.04
ARGNP	8 ×	✓	94.23±0.22	91.85±0.18	3.20	0.15
ARGNP	2	✓	95.07±0.31	92.47±0.23	2.50	0.04
ARGNP	4	✓	95.35±0.23	92.80±0.19	3.05	0.06
ARGNP	8	✓	<b>95.87±0.22</b>	<b>93.33±0.15</b>	4.15	0.20

ent network size settings, relation learning can significantly improve the capability of graph reasoning. Interestingly, this improvement is also observed on the CLUSTER, CIFAR10, and ModelNet datasets which don't have original edge features. Taking the CLUSTER dataset as an example, it aims at identifying the community clusters, where the graphs represent the community networks. The edges play a role in connecting two nodes and have no original meaningful features. In this case, relation learning can mine hierarchical relational information by extracting local structural similarities between nodes. This can help distinguish between intra-community and extra-community connections for learning better discriminative node features.

#### 4.4. Ablation of Search Paradigm

To investigate the effectiveness of our *Network Proliferation Search Paradigm (NPSP)*, we conduct the ablation experiments on ZINC dataset around *network size*, *search strategy*, *whether to use cell trick* and *whether to use NPSP*. We run 14 different experiments and report the results in Table 3. We observe the following phenomena. First, *the cell trick improves the search efficiency but weakens the expressive capability of graph search space*. This results from its

Table 3. Performance of the relation-aware graph search space under different settings. Cell is an indicator of whether to use the cell trick. NPSP is an indicator of whether to use the network proliferation search. OOM denotes out of memory.

ZINC								
#	Method	L (#)	Search Strategy	Cell (✓)	NPSP (✓)	Metric (MAE) ↓	Params (M)	Search (Day)
1	R-space	8	Random	×	×	0.303±0.058	0.27	0.
2	R-space	8	DARTS	✓	×	0.160±0.005	0.28	0.17
3	R-space	8	DARTS	×	×	0.157±0.008	0.28	0.30
4	R-space	8	DARTS	×	✓	<b>0.150±0.006</b>	0.29	<b>0.08</b>
5	R-space	8	SGAS	✓	×	0.165±0.008	0.30	0.13
6	R-space	8	SGAS	×	×	0.161±0.008	0.30	0.25
7	R-space	8	SGAS	×	✓	<b>0.155±0.003</b>	0.28	<b>0.06</b>
8	R-space	16	Random	×	×	0.185±0.024	0.51	0.
9	R-space	16	DARTS	✓	×	0.144±0.004	0.57	0.38
10	R-space	16	DARTS	×	×	N/A	N/A	OOM
11	R-space	16	DARTS	×	✓	<b>0.139±0.005</b>	0.56	<b>0.24</b>
12	R-space	16	SGAS	✓	×	0.140±0.003	0.60	0.32
13	R-space	16	SGAS	×	×	N/A	N/A	OOM
14	R-space	16	SGAS	×	✓	<b>0.136±0.002</b>	0.52	<b>0.21</b>

original assumption where the GNN architecture is a stack of the same building cells that narrows our relation-aware graph search space. Therefore, the search strategy with the cell trick performs worse than that without it, which is demonstrated by the contrast between exp 2 and exp 3, exp 5 and exp 6. Second, *our NPSP can both significantly improve the search efficiency and search effect with different search strategies*. The performance improvement benefits from that the NPSP can alleviate the subnet interference and mitigate the shrink of search space by breaking away from the cell assumption. The efficiency improvement lies in that NPSP shifts the training object from global supernet to sequential local supernets. They are supported by exp 4, 7, 11, and 14, where NPSP achieves the best performance with less time cost under all the experimental settings.

#### 4.5. Visualizing Hierarchical Features

To better demonstrate the effectiveness of the relation learning, we provide relation and node features visualization on ModelNet40 dataset. During the inference, we feed forward one 3D pointcloud object into the network with

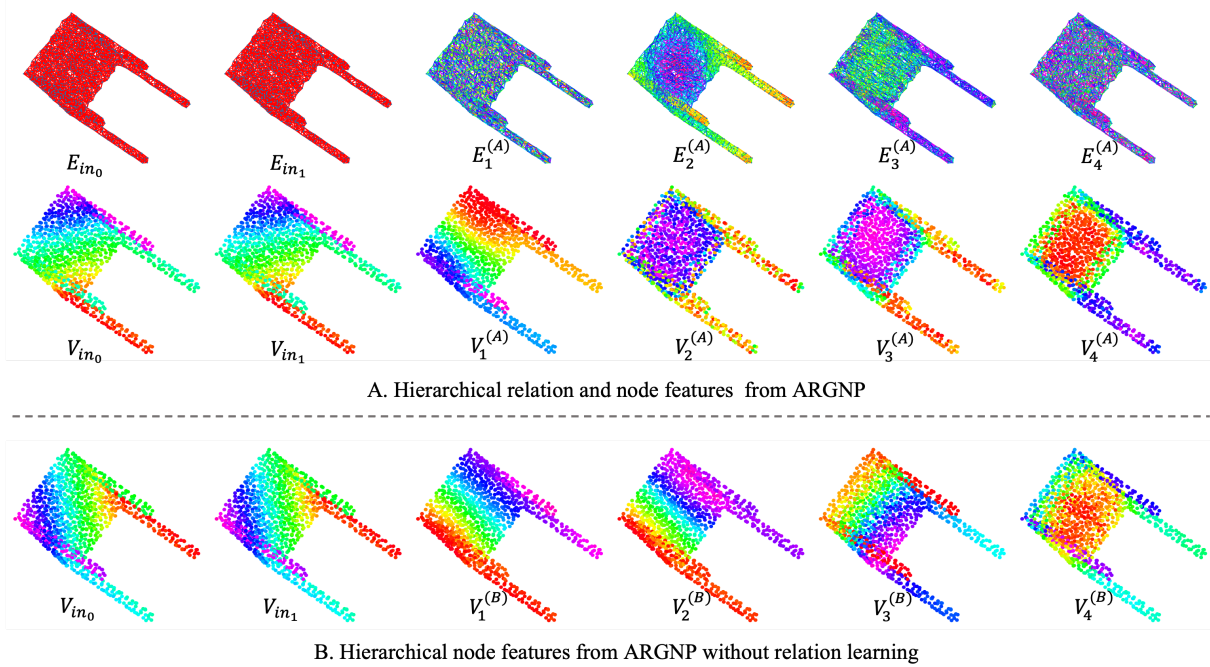


Figure 6. **Visualization of the learned hierarchical features for 3D point cloud recognition** (taking table as an example). Relation features with different edge color distribution have different message passing preferences. Node features with different node color distribution represent different clustering effects.

the input  $\{V_{in_0}, V_{in_1}, E_{in_0}, E_{in_1}\}$ , where  $V_{in_0} = V_{in_1} \in \mathbb{R}^{1024 \times 3}$  are the 3D coordinates and  $E_{in_0} = E_{in_1} = \mathbf{1} \in \mathbb{R}^{(1024 \times 9) \times 1}$  are the pseudo relation features. The hierarchical node/relation features generated from each layer is denoted as  $\{V_1, \dots, V_4\}$  and  $\{E_1, \dots, E_4\}$ , respectively. For better visualization on the point cloud graph, we reduce the feature dimension to 1 through principal component analysis (PCA). The edges with a similar color are considered to have the same message passing preferences, while the nodes with a similar color are considered to belong to a similar cluster. A visualization example from ARGNP and a version without relation learning architecture are shown in Figure 6A and 6B, respectively.

As shown in Figure 6A, ARGNP can capture the structural information and well discriminate different parts of the object (e.g., the legs, desktop, and border of the table in  $V_4^{(A)}$ ). In contrast, as shown in Figure 6B, the original GNN without relation learning architecture can only gradually propagate the node information through the input graph based on 3D coordinates. As a result, the similar nodes that are distant in the 3D space can not be well clustered (e.g., 4 legs of the table in  $V_4^{(B)}$ ). The above comparison shows that the relation features can guide better message passing mechanisms to learn more effective node features. To show the role of the relation learning more specifically, accompanied with the searched GNN in Figure 5, we analyze the features in Figure 6A. For example, the  $E_1^{(A)}$  is learned by

*subtraction* operation. The *subtraction* operation is similar to an “border detection” operation that can discriminate the directions between two nodes. In this way, the ARGNP can directly distinguish groups of parallel components of an object (e.g., legs, parallel borders, etc. in  $V_2^{(A)}$ ). However, without using the relation features, it requires numerous rounds of message passing which may cause the over smoothing problem. With the help of relation learning, the components with similar structures can be well clustered.

## 5. Conclusion

This paper proposes the automatic relation-aware graph network proliferation (ARGNP) method to design the optimal GNN architectures by devising a novel relation-aware graph search space and a network proliferation search paradigm. The search space significantly improves the upper bound of the discovered GNN’s reasoning capability while the proliferation search paradigm promotes search efficiency and effectiveness. Experiments show that ARGNP achieves superior performance for four tasks on six datasets.

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