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1 Homework: Implementing Deep Neural Networks in Tensor-Flow

1.0.1 Goals:

- Introduce the basics of TensorFlow
- Implement the digit classifier using the low level TensorFlow API
- Test Deep Neural Networks on real datasets and benchmark the results

2 Introduction to TensorFlow

TensorFlow is a dynamic graph computation engine, that allows automatic differentiation of each node. Tensorflow is the default computational backend of the Keras library. It can also be used directly from Python to build deep learning models.

- https://www.tensorflow.org
- https://www.tensorflow.org/tutorials/quickstart/advanced

TensorFlow builds where nodes may be: - **constant:** constants tensors, such as training data; - **Variables:** any tensor that is meant to be updated when training, such as parameters of the models.

```
[]: #pip install tensorflow

[]: import tensorflow as tf
   a = tf.constant(3)
   a

[]: <tf.Tensor: shape=(), dtype=int32, numpy=3>

[]: c = tf.Variable(0)
   b = tf.constant(2)
   c = a + b
   c
```

```
[]: A = tf.constant([[0, 1], [2, 3]], dtype=tf.float32)
[]: <tf.Tensor: shape=(2, 2), dtype=float32, numpy=
     array([[0., 1.],
            [2., 3.]], dtype=float32)>
    A tf. Tensor can be converted to numpy the following way:
[ ]: A.numpy()
[]: array([[0., 1.],
            [2., 3.]], dtype=float32)
[]: b = tf.Variable([1, 2], dtype=tf.float32)
[]: <tf.Variable 'Variable:0' shape=(2,) dtype=float32, numpy=array([1., 2.],
     dtype=float32)>
[]: tf.reshape(b, (-1, 1))
[]: <tf.Tensor: shape=(2, 1), dtype=float32, numpy=
     array([[1.],
            [2.]], dtype=float32)>
[]: tf.matmul(A, tf.reshape(b, (-1, 1)))
[]: <tf.Tensor: shape=(2, 1), dtype=float32, numpy=
     array([[2.],
            [8.]], dtype=float32)>
    2.0.1 Exercise
    Write a function that computes the squared Euclidean norm of an 1D tensorf input x:
       • Use element wise arithmetic operations (+, -, *, /, **)
       • Use tf.reduce_sum to compute the sum of the element of a Tensor.
[]: x = tf.Variable([1, -4], dtype=tf.float32)
     Х
[]: <tf.Variable 'Variable:0' shape=(2,) dtype=float32, numpy=array([1., -4.],
     dtype=float32)>
[]: def squared_norm(x):
         return tf.reduce_sum(x ** 2)
[]: # %load solutions/tf_squared_norm.py
```

```
[]: squared_norm(x)
[]: <tf.Tensor: shape=(), dtype=float32, numpy=17.0>
[]: squared_norm(x).numpy()
[]: 17.0
```

2.0.2 Autodiff and Gradient Descent

```
[]: x = tf.Variable([1, -4], dtype=tf.float32)

with tf.GradientTape() as tape:
    result = squared_norm(x)
    #tf.GradientTape for automatic differentiation;
    # computing the gradient of a computation with respect to some inputs

variables = [x]
    gradients = tape.gradient(result, variables)
    gradients
```

[]: [<tf.Tensor: shape=(2,), dtype=float32, numpy=array([2., -8.], dtype=float32)>]

```
[]: grad_x = gradients[0]
```

[]: x

We can apply a gradient step to modify x in place by taking one step of gradient descent:

```
[]: x.assign_sub(0.1 * grad_x) x.numpy()
```

[]: array([0.8, -3.2], dtype=float32)

Execute the following gradient descent step many times consecutively to watch the decrease of the objective function and the values of x converging to the minimum of the $squared_norm$ function.

Hit [ctrl]-[enter] several times to execute the same Jupyter notebook cell over and over again.

```
[]: with tf.GradientTape() as tape:
    objective = squared_norm(x)

x.assign_sub(0.1 * tape.gradient(objective, [x])[0])
```

```
print(f"objective = {objective.numpy():e}")
print(f"x = {x.numpy()}")

objective = 1.088000e+01
x = [ 0.64 -2.56]
```

2.0.3 Device-aware Memory Allocation

To explicitly place tensors on a device, use context managers:

```
[]: with tf.device("CPU:0"):
    x_cpu = tf.constant(3)

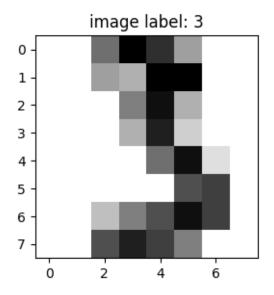
# with tf.device("GPU:0"):
    # x_gpu = tf.constant(3)
    x_cpu.device
```

[]: '/job:localhost/replica:0/task:0/device:CPU:0'

2.1 Building a Digits Classifier in TensorFlow

2.1.1 Dataset:

 $\bullet \ \ http://scikit-learn.org/stable/modules/generated/sklearn.datasets.load_digits.html \# sklearn.datasets.load_digits.html \# sklearn.d$



2.1.2 Preprocessing

- Normalization
- Train / test split

[]: (((1527, 64), (1527,)), ((270, 64), (270,)))

TensorFlow provides dataset abstraction which makes it is to iterate over the data batch by batch:

```
[]: def gen_dataset(x, y, batch_size=128):
    dataset = tf.data.Dataset.from_tensor_slices((x, y))
    dataset = dataset.shuffle(buffer_size=10000, seed=42)
    dataset = dataset.batch(batch_size=batch_size)
    return dataset

[]: dataset = gen_dataset(X_train, y_train)
    dataset

[]: <_BatchDataset element_spec=(TensorSpec(shape=(None, 64), dtype=tf.float32,
    name=None), TensorSpec(shape=(None,), dtype=tf.int32, name=None))>
[]: batch_x, batch_y = next(iter(dataset))
    batch_x.shape
[]: TensorShape([128, 64])
[]: batch_y.shape
[]: TensorShape([128])
```

2.1.3 Build a model using TensorFlow

- Using TensorFlow, build a similar model (one hidden layer) as you previously did;
- The input will be a batch coming from X_train, and the output will be a batch of ints;
- The output do not need be normalized as probabilities, the softmax will be moved to the loss function.

```
def init_weights(shape):
    return tf.Variable(tf.random.normal(shape, stddev=0.01))

def accuracy(y_pred, y):
    return np.mean(np.argmax(y_pred, axis=1) == y)

def test_model(model, x, y):
    dataset = gen_dataset(x, y)
    preds, targets = [], []

for batch_x, batch_y in dataset:
        preds.append(model(batch_x).numpy())
        targets.append(batch_y.numpy())

preds, targets = np.concatenate(preds), np.concatenate(targets)
    return accuracy(preds, targets)
```

Define your model there, and then execute the following cell to train your model. Don't hesitate to tweak the hyperparameters.

```
[]: # hyperparams
     batch_size = 32
     hid_size = 15
     learning_rate = 0.5
     num_epochs = 10
     input_size = X_train.shape[1]
     output_size = 10
     # build the model and weights
     class MyModel:
         def __init__(self, input_size, hid_size, output_size):
             # randomly initialize all the internal variables of the model:
             self.W_h = init_weights([input_size, hid_size])
             self.b_h = init_weights([hid_size])
             self.W_o = init_weights([hid_size, output_size])
             self.b_o = init_weights([output_size])
         def __call__(self, inputs):
             # this method should implement the forward pass with
             # tensorflow operations: compute the outputs, that is the
             # unnormalized predictions of the network for a give batch
             # of inputs vectors.
             # No need to implement the softmax operations as we will
             # move it the loss function instead.
             # Hint: you can use tf.matmul, tf.tanh, tf.sigmoid,
             # arithmetic operations and so on.
            h = tf.nn.sigmoid(tf.matmul(inputs, self.W_h) + self.b_h)
            return tf.matmul(h, self.W_o) + self.b_o
    model = MyModel(input_size, hid_size, output_size)
[]: # %load solutions/tf_model.py
     logits = model(X_test[:1])
     logits.numpy()
[]: array([[ 0.00737174, -0.00769683, -0.00192661, -0.0135047 , 0.01407218,
              0.0494116, 0.02454551, -0.01039417, -0.00279989, -0.00879737]],
           dtype=float32)
[]: y_test[:1]
[]: array([2], dtype=int32)
```

```
[]: test_model(model, X_test, y_test)
```

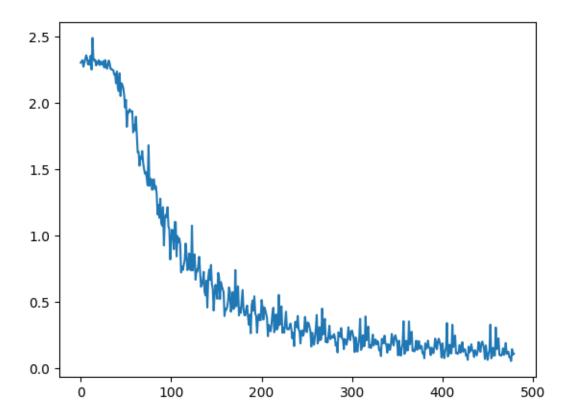
[]: 0.11481481481481481

The following implements a training loop in Python. Note the use of tf.GradientTape to automatically compute the gradients of the loss w.r.t. the different parameters of the model:

```
[]: losses = []
     for e in range(num_epochs):
         train_dataset = gen_dataset(X_train, y_train, batch_size=batch_size)
         for batch_x, batch_y in train_dataset:
             # tf.GradientTape records the activation to compute the gradients:
             with tf.GradientTape() as tape:
                 logits = model(batch x)
                 loss = tf.reduce_mean(tf.nn.
      sparse_softmax_cross_entropy_with_logits(batch_y, logits))
                 losses.append(loss.numpy())
             # Here we ask for the gradients of dL/dW_h, etc.
             dW_h, db_h, dW_o, db_o = tape.gradient(
                 loss, [model.W_h, model.b_h, model.W_o, model.b_o])
             # Update the weights as a Stochastic Gradient Descent would do:
             model.W h.assign sub(learning rate * dW h)
             model.b_h.assign_sub(learning_rate * db_h)
             model.W_o.assign_sub(learning_rate * dW_o)
             model.b_o.assign_sub(learning_rate * db_o)
         train_acc = test_model(model, X_train, y_train)
         test_acc = test_model(model, X_test, y_test)
         print("Epoch {}, train_acc = {}, test_acc = {}".format(e, round(train_acc,_
      \rightarrow4), round(test_acc, 4)))
    plt.plot(losses)
```

```
Epoch 0, train_acc = 0.4977, test_acc = 0.4593
Epoch 1, train_acc = 0.8003, test_acc = 0.7556
Epoch 2, train_acc = 0.8841, test_acc = 0.8815
Epoch 3, train_acc = 0.9384, test_acc = 0.937
Epoch 4, train_acc = 0.9555, test_acc = 0.9519
Epoch 5, train_acc = 0.9679, test_acc = 0.9481
Epoch 6, train_acc = 0.9745, test_acc = 0.9519
Epoch 7, train_acc = 0.9777, test_acc = 0.9593
Epoch 8, train_acc = 0.9823, test_acc = 0.9593
Epoch 9, train_acc = 0.9836, test_acc = 0.9593
```

[]: [<matplotlib.lines.Line2D at 0x7b966ca80640>]



```
[]: test_model(model, X_test, y_test)

[]: 0.9592592592593

[]: test_model(model, X_train, y_train)
```

[]: 0.9836280288146693

2.2 Now it is your turn for more exercises

- add L2 regularization with $\lambda = 10^{-4}$
- train with 3 and 4 layers: only pass the layer sizes as hyperparameter to the model class constructor (__init__ method)
- you may use tensorboard (https://www.tensorflow.org/how_tos/summaries_and_tensorboard/) to monitor loss and display graph
- Can you test implemented DL model on a real genomics dataset? Examples may include disease outcome prediction or subtype classification using gene expression data. Define your scientific problem and your analysis goal and evaluate the performance. How does the performance compare with logistic regression, SVM or other methods?

Note: Feel free to modify nonlinear activition functions, loss functions, model architecture and regularization to see if there is any impact on the performance.

```
[]: # Modify MyModel:
     # Add L2 regularization with lambda=1e-4
     # Pass the layer sizes as hyperparameter to the model class constructor, so it_{\sqcup}
     ⇔can train with 3 and 4 layes
     class MyModel:
         def __init__(self, layer_sizes, 12_lambda=1e-4):
             self.layers = [] # List to store layers, where each layer consists of
      ⇔weights and biases
             # Create layers based on the size list provided
             for i in range(len(layer_sizes) - 1): # Loop through each pair of ⊔
      ⇔consecutive layers
                 # Append a dictionary to `self.layers` where:
                 # 'W' is a weight matrix initialized with normally distributed_
      ⇔random values
                 # 'b' is a bias vector initialized to zeros
                 self.layers.append({
                     'W': tf. Variable(tf.random.normal([layer sizes[i],
      ⇔layer_sizes[i+1]], stddev=0.01, dtype=tf.float32)),
                     'b': tf.Variable(tf.zeros([layer sizes[i+1]], dtype=tf.
      →float32)) # Zero-initialized biases for the layer
                 })
             # Store the L2 regularization strength
             self.12_lambda = 12_lambda
         # Callable method to compute the output of the network for given inputs
         def call (self, inputs):
             x = inputs # Ensure inputs are of type float32 for computation
             # Process input through all layers except the last using sigmoid_
      →activation function
             for layer in self.layers[:-1]:
                 x = tf.nn.sigmoid(tf.matmul(x, layer['W']) + layer['b']) # Apply_
      ⇔sigmoid activation to the linear transformation
             # For the last layer, only perform the linear transformation
             x = tf.matmul(x, self.layers[-1]['W']) + self.layers[-1]['b']
             return x # Return the final output of the network
         # Method to calculate the L2 loss (regularization term) for the network's \Box
      \hookrightarrow weights
         def get_12_loss(self):
             12 loss = 0 # Initialize L2 loss to zero
             for layer in self.layers: # Iterate through each layer
                 12_loss += tf.reduce_sum(tf.square(layer['W'])) # Sum the squares_
      →of all weight matrices
```

```
[]: ##### Test for our new class
     # Initialize the model with a hypothetical layer configuration
    model = MyModel(layer_sizes=[10, 20, 5]) # 10 input features, 20 neurons in_
      → the hidden layer, 5 output neurons
     # Generate synthetic data
    np.random.seed(0)
    X_test = np.random.normal(size=(100, 10)) # 100 samples, 10 features each
     # Convert X_test to a TensorFlow tensor
    X_test_tensor = tf.convert_to_tensor(X_test, dtype=tf.float32)
     # Use the model to predict
    outputs = model(X_test_tensor)
     # Print the outputs and the L2 loss
    #print("Outputs:", outputs.numpy()) # Convert TensorFlow tensor to numpy array_
     ⇔for printing
    print("L2 Loss:", model.get_12_loss().numpy()) # Calculate and print the L2_1
      ⇔regularization loss
```

L2 Loss: 3.1652737e-06

```
[]: # Use tensorboard monitor loss and display graph
from tensorflow.summary import create_file_writer

logdir = "./logs"
writer = create_file_writer(logdir)

with writer.as_default():
    for epoch in range(num_epochs):
        # Run training and record loss
        tf.summary.scalar('loss', loss, step=epoch)
```

Test implemented DL model on a real genomics dataset

Drive already mounted at /content/drive; to attempt to forcibly remount, call drive.mount("/content/drive", force_remount=True).

```
[]: from sklearn.preprocessing import LabelEncoder
     # Assume all columns except 'cell_type' are features
     X = df.drop('cell_type', axis=1).values
     y = df['cell_type'].values
     # Encode the categorical target variable
     label_encoder = LabelEncoder()
     y_encoded = label_encoder.fit_transform(y)
     # Split the data into training and testing sets
     X_train, X_test, y_train, y_test = train_test_split(X, y_encoded, test_size=0.
      →2, random_state=42)
[]: (X_train.shape, y_train.shape), (X_test.shape, y_test.shape)
[]: (((9204, 2436), (9204,)), ((2301, 2436), (2301,)))
[]: X_train.shape[1]
[]: 2436
[]: # Test again for our new MyModel
     X_train_tensor=tf.convert_to_tensor(X_train, dtype=tf.float32)
     New_Model=MyModel([X_train.shape[1], 64, 6])
     # Use the model to predict
     outputs = New_Model(X_train_tensor)
     # Print the outputs and the L2 loss
     #print("Outputs:", outputs.numpy()) # Convert TensorFlow tensor to numpy array_
     ⇔for printing
     print("L2 Loss:", model.get_12_loss().numpy()) # Calculate and print the L2_1
      →regularization lossModel(X_train)
    L2 Loss: 3.1652737e-06
[]: def gen_dataset(x, y, batch_size=128):
         """ Generate batches of data from x and y arrays. """
        dataset = tf.data.Dataset.from_tensor_slices((x, y))
        dataset = dataset.batch(batch_size)
        return dataset
     def closest_class(logits, classes):
         """ Map each logit to the closest class. """
         # Expand logits and classes to enable broadcasting
        logits = tf.expand_dims(logits, -1) # Expand logits shape for broadcasting
         classes = tf.constant(classes, dtype=logits.dtype) # Ensure same dtype
         # Calculate the absolute differences
        differences = tf.abs(logits - classes)
```

```
# Find the index of the minimum difference for each logit
    closest_indices = tf.argmin(differences, axis=-1)
    # Map indices to classes
    return tf.gather(classes, closest_indices)
def test_model(model, x, y):
    dataset = gen_dataset(x, y)
    preds, targets = [], []
    for batch_x, batch_y in dataset:
        # Ensure batch_x is of the correct dtype if the model expects float64, u
 → change dtype to tf.float64
        batch_x = tf.cast(batch_x, dtype=tf.float32)
        logits = model(batch_x)
       # Since logits are used directly in np.argmax, ensure logits are a_
 →numpy array of the right type
        logits = logits.numpy() # Ensures conversion to numpy array if notu
 \hookrightarrow already
        y_pred = np.argmax(logits, axis=1) # Finds the index of the maximum_
 → logit which represents the class
        predicted_classes = closest_class(y_pred, [0, 1, 2, 3, 4, 5])
        preds.extend(predicted classes.numpy().flatten())
        targets.extend(batch_y.numpy().flatten())
    # Calculate accuracy
    accuracy = np.mean(np.array(preds) == np.array(targets))
    return accuracy
```

```
[]: train_acc = test_model(New_Model, X_train, y_train)
train_acc
```

[]: 0.022381573229030855

```
[]: import tensorflow as tf
import numpy as np
import matplotlib.pyplot as plt

def train(model, X_train, y_train, X_test, y_test, epochs, batch_size):
    optimizer = tf.optimizers.Adam() # Optimizer for updating the weights
    epoch_losses = [] # List to store average losses for each epoch

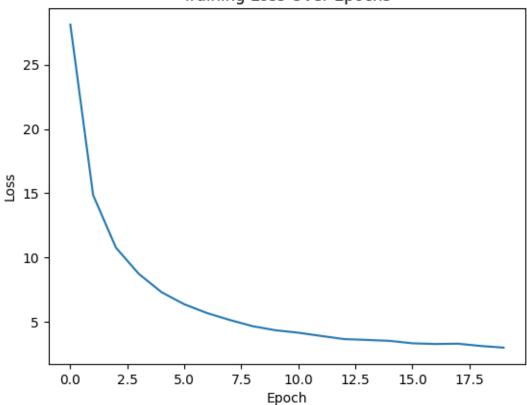
for epoch in range(epochs):
    losses = [] # List to store losses for each batch within an epoch
    total_loss_this_epoch = 0
    for i in range(0, X_train.shape[0], batch_size):
        with tf.GradientTape() as tape:
```

```
inputs = tf.convert_to_tensor(X_train[i:i + batch_size],__
→dtype=tf.float32)
               labels = tf.convert_to_tensor(y_train[i:i + batch_size],__
→dtype=tf.float32)
               # One-hot encode the labels if needed (uncomment if your_
⇔problem is multi-class classification)
               # labels = tf.one_hot(labels, depth=6) # Adjust depth_
→according to your number of classes
               logits = model(inputs) # Get the model output for the inputs
               # Ensure logits and labels have the same shape
               if logits.shape[-1] == 1:
                   labels = tf.expand_dims(labels, axis=-1)
               else:
                   labels = tf.one_hot(tf.cast(labels, tf.int32), depth=logits.
\hookrightarrowshape [-1])
               # Calculate the data loss using sigmoid cross-entropy
               data_loss = tf.reduce_mean(tf.nn.
sigmoid_cross_entropy_with_logits(labels=labels, logits=logits))
               reg_loss = model.get_12_loss() # Regularization loss from the_
⊶model
               total_loss = data_loss + reg_loss # Total loss includes both_
⇔data and regularization loss
               total_loss_this_epoch += total_loss
           # Calculate gradients of total loss with respect to model parameters
           gradients = tape.gradient(total_loss, [var for layer in model.
⇒layers for var in [layer['W'], layer['b']]])
           # Apply gradients to update model parameters
           optimizer.apply_gradients(zip(gradients, [var for layer in model.
→layers for var in [layer['W'], layer['b']]]))
      losses.append(total_loss_this_epoch.numpy()) # Append the total loss_
⇔of the current epoch to the losses list
       # Logging the average loss every epoch
      print(f"Epoch {epoch}, Loss: {total_loss_this_epoch.numpy()}") # Print_\( \)
⇔total loss of the epoch
      train_acc = test_model(model, X_train, y_train)
      test acc = test model(model, X test, y test)
      print("Train_acc = {}, Test_acc = {}".format(round(train_acc, 4),__
→round(test_acc, 4)))
```

```
Epoch 0, Loss: 28.1090145111084
Train_acc = 0.6269, Test_acc = 0.6236
Epoch 1, Loss: 14.864154815673828
Train_acc = 0.856, Test_acc = 0.8588
Epoch 2, Loss: 10.781656265258789
Train_acc = 0.8558, Test_acc = 0.8583
Epoch 3, Loss: 8.75383472442627
Train_acc = 0.9198, Test_acc = 0.9266
Epoch 4, Loss: 7.324617862701416
Train_acc = 0.9326, Test_acc = 0.9435
Epoch 5, Loss: 6.386359691619873
Train_acc = 0.9333, Test_acc = 0.9435
Epoch 6, Loss: 5.703063488006592
Train_acc = 0.9359, Test_acc = 0.9444
Epoch 7, Loss: 5.163925647735596
Train_acc = 0.9343, Test_acc = 0.9439
Epoch 8, Loss: 4.684501647949219
Train_acc = 0.9349, Test_acc = 0.9452
Epoch 9, Loss: 4.369673252105713
Train_acc = 0.9393, Test_acc = 0.9474
Epoch 10, Loss: 4.180036544799805
Train_acc = 0.9374, Test_acc = 0.9461
Epoch 11, Loss: 3.929189682006836
Train_acc = 0.9661, Test_acc = 0.97
Epoch 12, Loss: 3.68708872795105
Train_acc = 0.9757, Test_acc = 0.9809
Epoch 13, Loss: 3.620755434036255
Train acc = 0.9773, Test acc = 0.9809
Epoch 14, Loss: 3.5464797019958496
Train_acc = 0.9682, Test_acc = 0.9683
Epoch 15, Loss: 3.3581504821777344
Train_acc = 0.9657, Test_acc = 0.9704
```

```
Epoch 16, Loss: 3.302844762802124
Train_acc = 0.9637, Test_acc = 0.9661
Epoch 17, Loss: 3.327347755432129
Train_acc = 0.9786, Test_acc = 0.9757
Epoch 18, Loss: 3.1493752002716064
Train_acc = 0.9855, Test_acc = 0.9839
Epoch 19, Loss: 3.0225138664245605
Train_acc = 0.9849, Test_acc = 0.9848
```

Training Loss Over Epochs



```
[]: len(losses)
```

[]: 480

```
[]: # Assume y_encoded is a NumPy array
unique_values = np.unique(y_encoded)
num_unique_values = len(unique_values)

print("Number of unique values:", num_unique_values)
print(unique_values)
```

Number of unique values: 6

```
[0 1 2 3 4 5]
```

```
[]: train_acc = test_model(New_Model, X_train, y_train)
[]: train_acc
[]: 0.9848978704910908
[]: test_acc = test_model(New_Model, X_test, y_test)
     test_acc
[]: 0.9847892220773576
[]: from sklearn.model_selection import train_test_split
     from sklearn.linear_model import LogisticRegression
     from sklearn.metrics import classification_report, confusion_matrix, __
     →accuracy_score
     from sklearn.preprocessing import StandardScaler
     # Standardize the data (zero mean, unit variance)
     scaler = StandardScaler()
     X_train = scaler.fit_transform(X_train)
     X_test = scaler.transform(X_test)
     # Initialize the Logistic Regression model
     log_reg = LogisticRegression(max_iter=10000)
     # Train the model
     log_reg.fit(X_train, y_train)
     # Make predictions
     y_pred_log = log_reg.predict(X_test)
     # Evaluate the model
     accuracy = accuracy_score(y_test, y_pred_log)
     print("Accuracy:", accuracy)
     print("Confusion Matrix:\n", confusion_matrix(y_test, y_pred_log))
     print("Classification Report:\n", classification_report(y_test, y_pred_log))
    Accuracy: 0.9826162538026945
    Confusion Matrix:
     [[ 543
                              0
                                   17
               0
                         0
                             0
                                  07
         0 1425
                   0
                       10
         1
              0
                  43
                        0
                             0
                                  07
                      200
                             0
                                  0]
         4
             19
                   0
     0
                        2
                             7
                                  0]
         1
              1
     Γ
         1
              0
                        0
                                 43]]
    Classification Report:
                   precision
                                recall f1-score
                                                    support
```

0	0.99	1.00	0.99	544
1	0.99	0.99	0.99	1435
2	1.00	0.98	0.99	44
3	0.94	0.90	0.92	223
4	1.00	0.64	0.78	11
5	0.98	0.98	0.98	44
accuracy			0.98	2301
macro avg	0.98	0.91	0.94	2301
weighted avg	0.98	0.98	0.98	2301

As observed from the output of both the deep learning algorithm and the logistic regression model, we achieved a similar accuracy rate of approximately 0.98 on the test sets. This indicates that both approaches are highly effective for this classification task.