

Assignment I

The plot of kernel estimation for Japanese pine saplings data with $\sigma = 0.05$ and $\sigma = 0.1$ is shown in Figure 1. The point pattern for Japanese black pine saplings is kind of random and is slightly clustered in the north-west. As the value of σ increases, the output trend tends to be smoother, and the overall estimated values decrease as well.

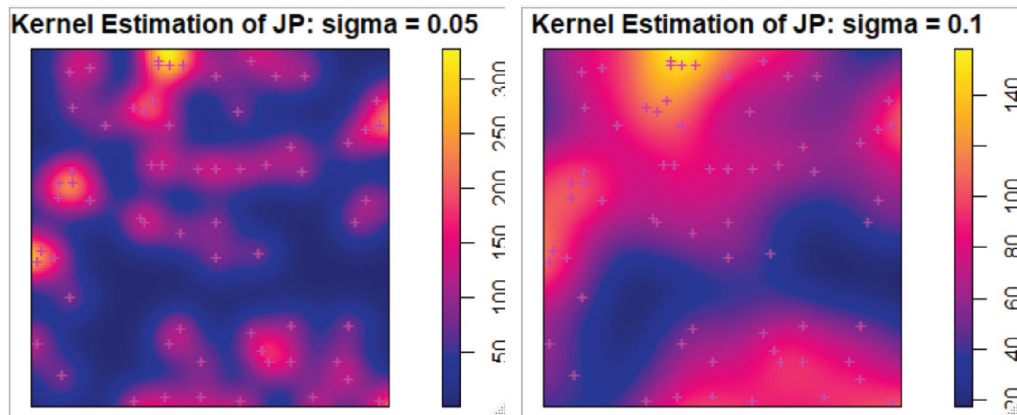


Figure 1. Plot of kernel estimation for Japanese pine saplings data with $\sigma = 0.05$ and $\sigma = 0.1$, respectively.

Assignment II

The plots of G_{hat} , F_{hat} , K_{hat} , and L_{hat} for Japanese pine saplings data are shown in Figure 2 and Figure 3. The point pattern for Japanese pine saplings is random given the evidence that (1) both of the empirical distribution functions $G(r)$ and $F(r)$ are aligned with the theoretical ones that derived from a Poisson process, and (2) the empirical values of $K(r)$ and $L(r)$ are both below the theoretical values under CSR.

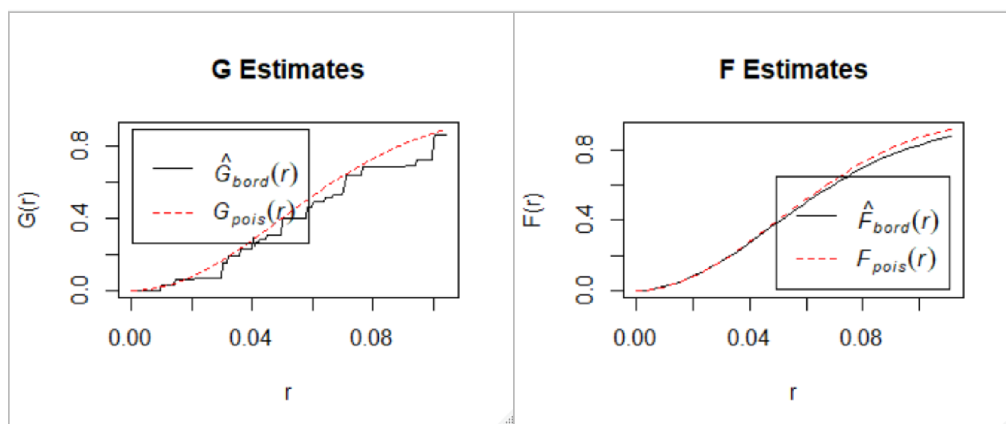


Figure 2. G_{hat} and F_{hat} for Japanese pine saplings data (without specifying $xlim$ argument).

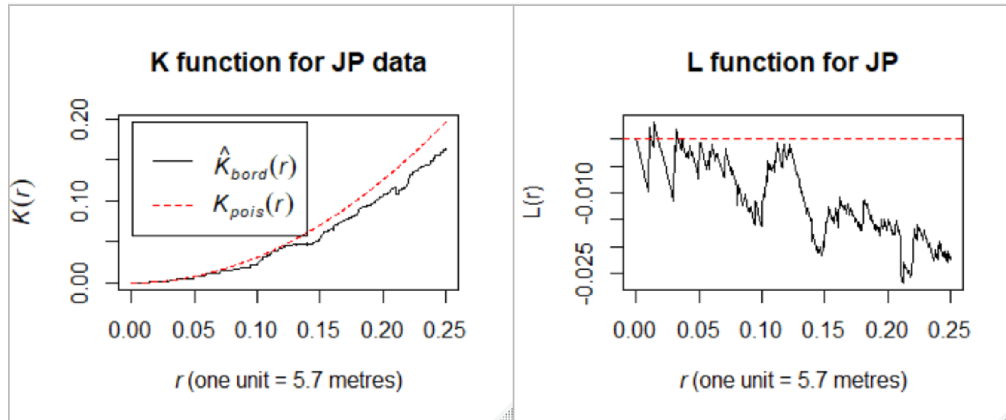


Figure 3. K hat and L hat for Japanese pine saplings data (without specifying $xlim$ argument).

Assignment III

The plot of G hat and F hat with simulating bounds for Japanese pine saplings data is shown in [Figure 4](#). The empirical values for $G(r)$ and $F(r)$ both fall within the envelopes formed by the upper and lower bounds of simulation, and therefore the point pattern for Japanese pine saplings data is random.

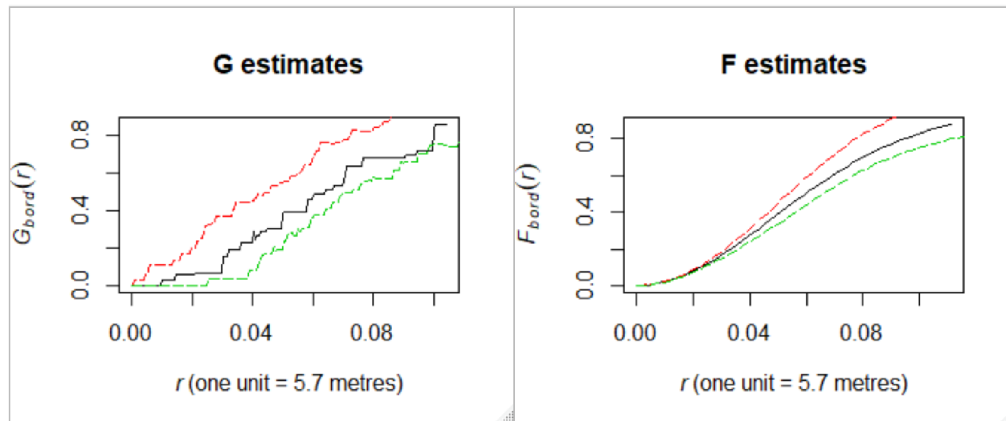


Figure 4. Plot of G hat and F hat with simulating bounds for Japanese pine saplings data.

Assignment IV

The plot of K hat with simulating bounds for Japanese pine saplings data is shown in [Figure 5](#). The empirical values for $K(r)$ fall within the envelopes formed by the upper and lower bounds of simulation, and therefore the point pattern for Japanese pine saplings data is random.

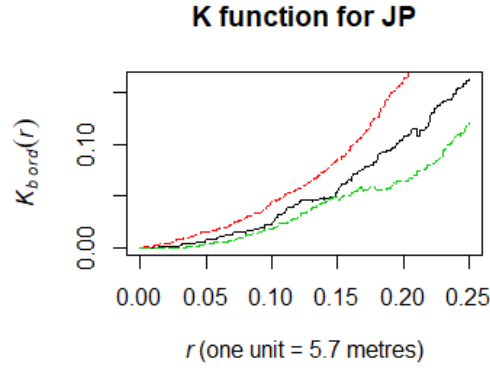


Figure 5. Plot of $Khat$ with simulating bounds for Japanese pine saplings data.

Assignment V

The plot of kernel estimation for California redwood tree saplings data with $\sigma = 0.05$ and $\sigma = 0.1$ is shown in Figure 6. The California redwood tree saplings are clustered in the north-east and the mid-west of the region.

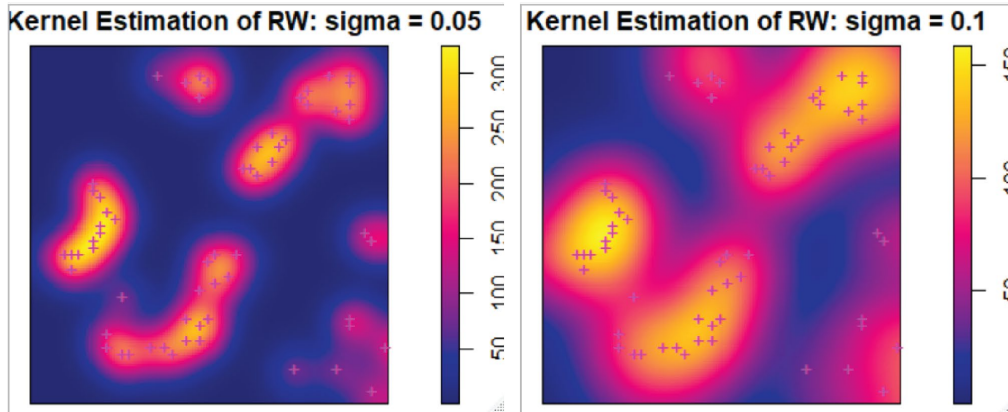


Figure 6. Plot of kernel estimation for California redwood tree saplings data with $\sigma = 0.05$ and $\sigma = 0.1$, respectively.

The plots of $Ghat$, $Fhat$, $Khat$, and $Lhat$ for California redwood tree saplings data are shown in Figure 7 and Figure 8. The point pattern for California redwood tree saplings is clustered given the evidence that (1) the empirical distribution function $G(r)$ is above the theoretical one that derived from a Poisson process, while the empirical distribution function $F(r)$ is below the theoretical function, and (2) both the empirical function $K(r)$ and $L(r)$ are above the theoretical ones that derived from a Poisson process.

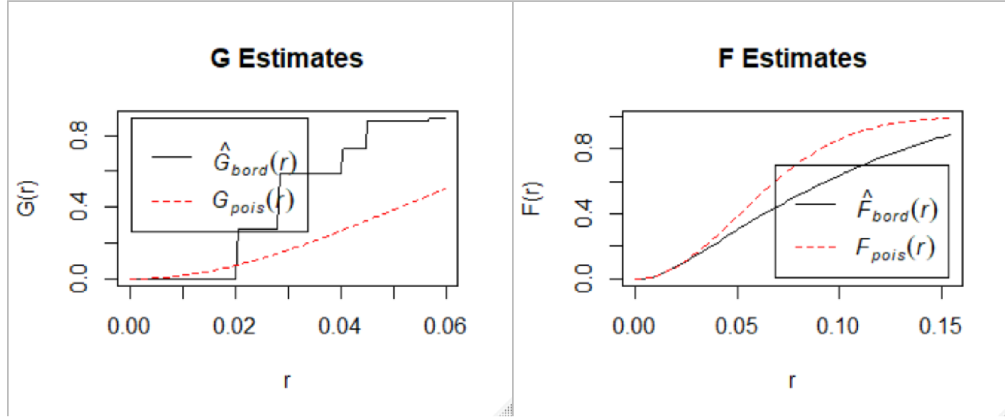


Figure 7. G_{hat} and F_{hat} for California redwood tree saplings data (without specifying $xlim$ argument).

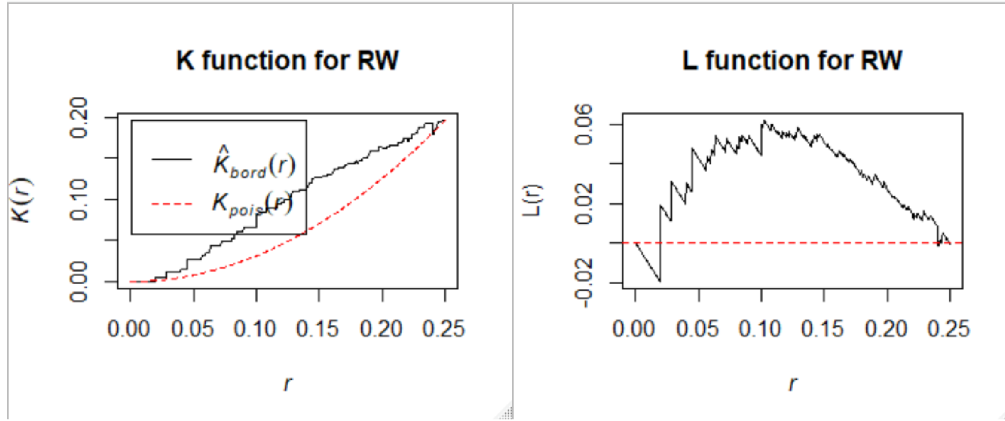


Figure 8. K_{hat} and L_{hat} for California redwood tree saplings data (without specifying $xlim$ argument).

The plot of F_{hat} and K_{hat} with simulating bounds for California redwood tree saplings data is shown in [Figure 9](#). The empirical values for $F(r)$ fall below the envelope formed by the upper and lower bounds of simulation, while those for $K(r)$ fall above the envelop; therefore, the point pattern for California redwood tree saplings data is clustered.

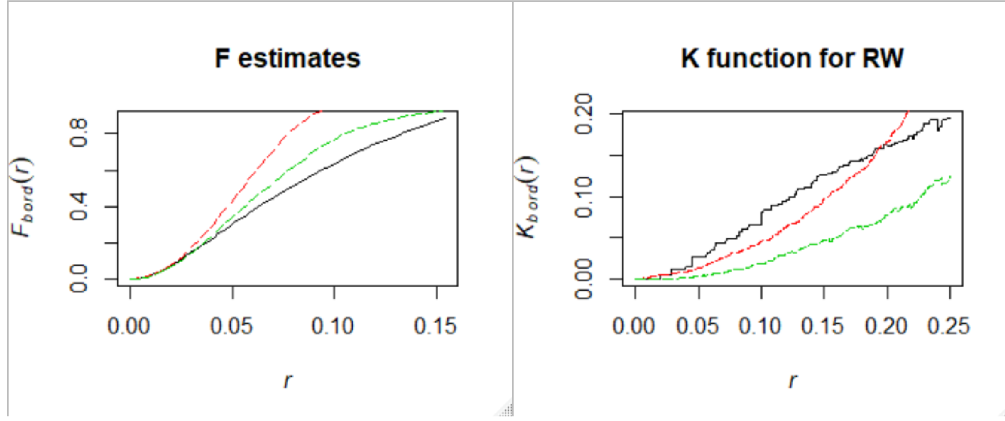


Figure 9. Plot of $Fhat$ and $Khat$ with simulating bounds for California redwood tree saplings data.

The plot of kernel estimation for regular point pattern with $\sigma = 0.05$ and $\sigma = 0.1$ is shown in Figure 10. The distribution of points is regular, without any clusters. As the σ increases, the edge effect tends to be more obvious.

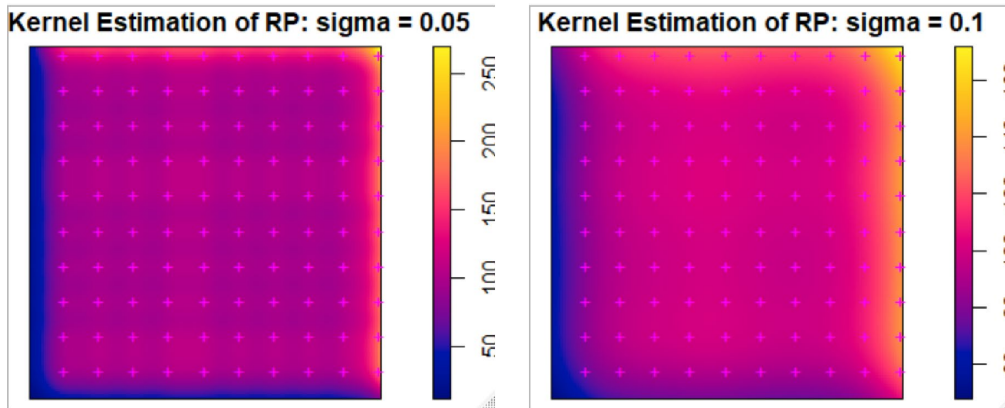


Figure 10. Plot of kernel estimation for regular point pattern with $\sigma = 0.05$ and $\sigma = 0.1$, respectively.

The plots of $Ghat$, $Fhat$, $Khat$, and $Lhat$ for Japanese pine saplings data are shown in Figure 11 and Figure 12. The point pattern is regular given the evidence that (1) the empirical distribution function $G(r)$ is below the theoretical one that derived from a Poisson process, while the empirical distribution function $F(r)$ is above the theoretical function, and (2) the empirical values of $K(r)$ and $L(r)$ are randomly distributed along the theoretical values under CSR.

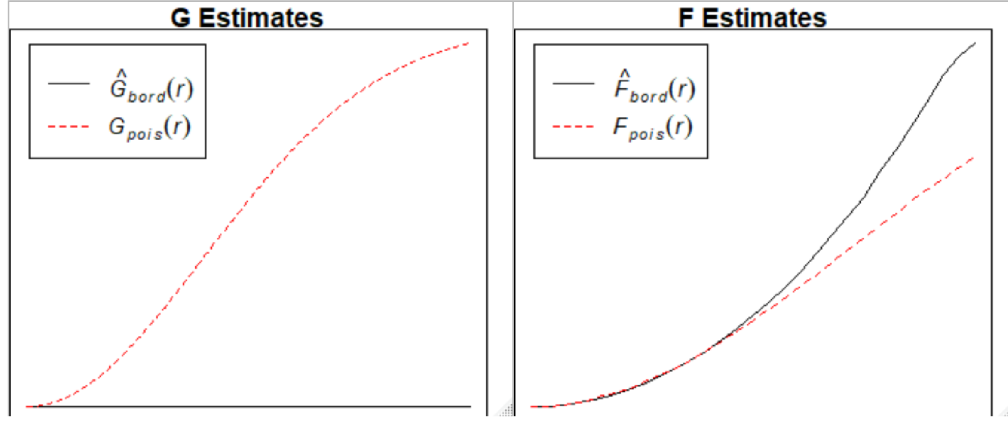


Figure 11. G_{hat} and F_{hat} for regular point pattern (without specifying $xlim$ argument).

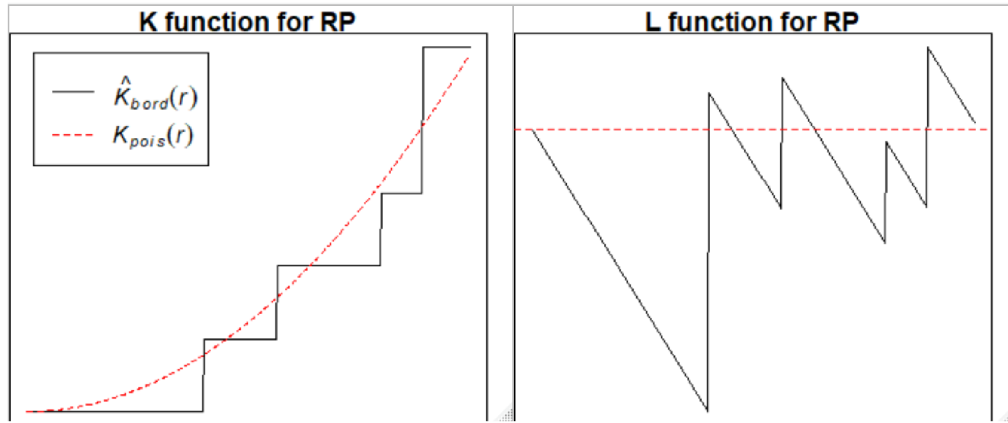


Figure 12. K_{hat} and L_{hat} for regular point pattern (without specifying $xlim$ argument).

The plot of F_{hat} and K_{hat} with simulating bounds for regular point pattern is shown in [Figure 13](#). The empirical values for $F(r)$ fall above the envelope formed by the upper and lower bounds of simulation, , while those for $K(r)$ fall somewhat below the envelop; therefore, the point pattern is regular.

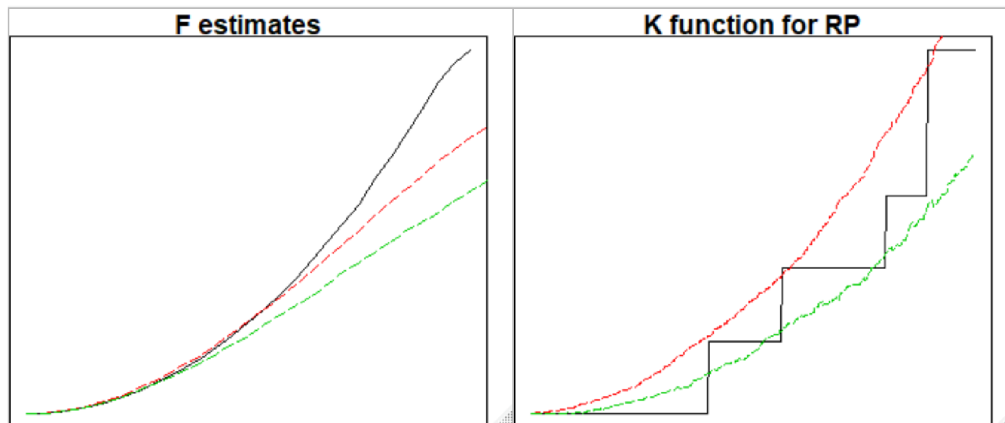


Figure 13. Plot of F_{hat} and K_{hat} with simulating bounds for regular point pattern.