Introduction to Occupancy Models

Statistical Toolbox for Analysing Citizen Science Data

Swantje Löbel

GFÖ Conference 2021, Pre-Meeting Workshop 29.08.2021



Introduction to Occupancy models

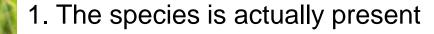
The **occurrence** of a species at a given location in your data is the result of two processes: 2. You detect the species in your survey 1. The species is actually present

Introduction to Occupancy models

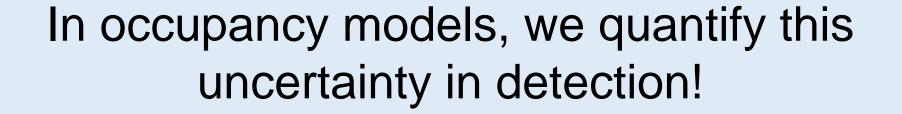
The **occurrence** of a species at a given location in your data is the result of two processes: 1. The species is actually present 2. You detect the species in your survey The **absence** of a species at a given location in your data is either the result of: 1. The species is actually absent 2. You did not detect the species in your survey

Introduction to Occupancy models

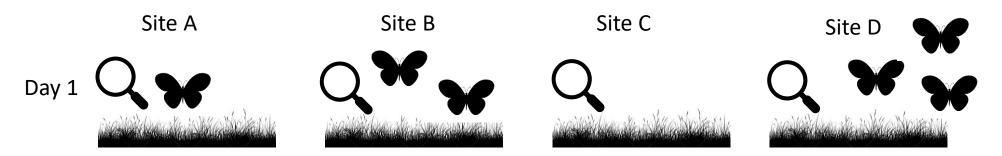
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2. You detect the species in your survey



Study design to estimate detection probability

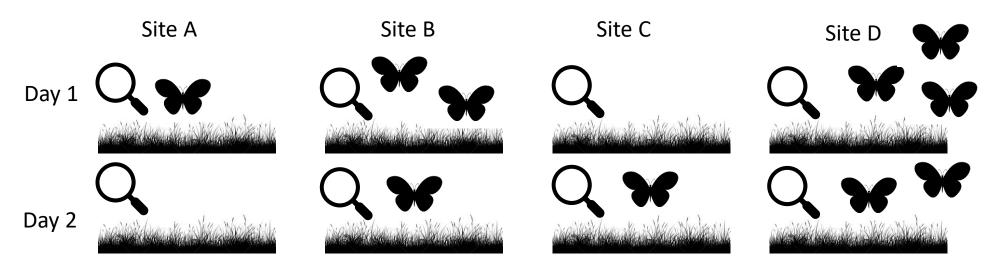


- We visit 4 sites each site is visited once
- At each site, we count the number of butterflies we see
- Can we separate detection rate from true occurrence rate?





Study design to estimate detection probability

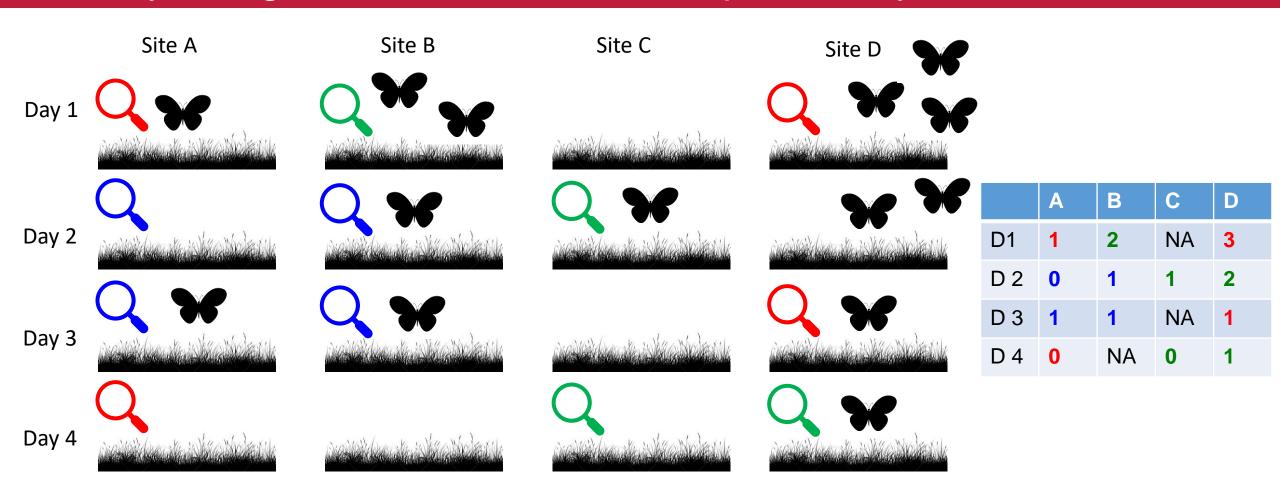


- We visit 4 sites each site is visited twice on different days
- At each site and on each day, we count the number of butterflies we see
- Can we separate detection rate from true occurrence rate?





Study design to estimate detection probability



Typical design while working with Citizen Science Data





Occupancy models

Assumptions:

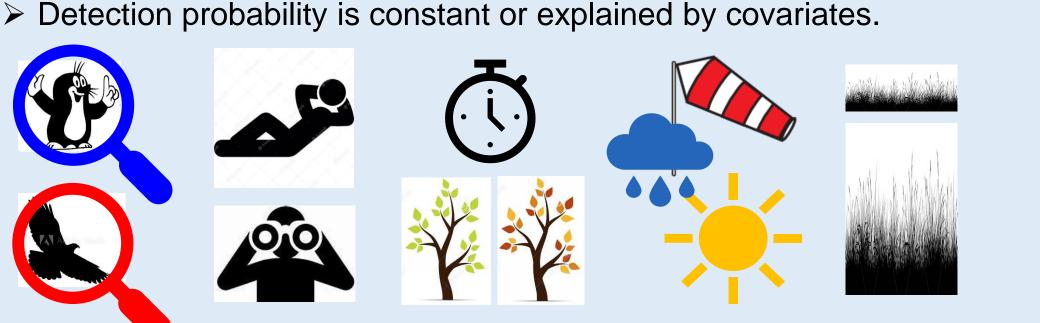
> Detection probability is constant or explained by covariates.





Assumptions:

Detection probability is constant or explained by covariates.



Observer

Sampling effort

Timing

Climate/ Wheather Habitat



Assumptions:

- > Detection probability is constant or explained by covariates.
- Closure: We require that the (true) presence/absence state of Site i does not change over the course of the study (or one season)!





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- No false positive errors
- > Independence of occurrence and independence
- > No residual spatial autocorrelation





Process or state model

$$Z_i \sim Bernoulli(\psi_i)$$

Ecological process yields true state (Z)

Latent variable – true species presence or absence

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- ightarrow simple Bernoulli model with an occurrence probability ($oldsymbol{\psi}$).
- Observation or detection model

$$y_{ij} \mid Z_i \sim Bernoulli(Z_i * p_{ij})$$

Observation model links the observations (y= our data) to the state variable (Z).

→ standard observation model is a Bernoulli model. **p** is the estimated detection probability.





Process or state model

$$Z_i \sim Bernoulli(\psi_i)$$

We can add linear predictors to both the occurrence probability ($m{\psi}$, psi) and detection probability ($m{p}$)

$$logit(\boldsymbol{\psi}_i) = \beta_0 + \beta_1 * occupancy.covar_i + ...$$

- ightarrow simple Bernoulli model with an occurrence probability ($oldsymbol{\psi}$).
- Observation or detection model

$$y_{ij} \mid Z_i \sim Bernoulli(Z_i * p_{ij})$$

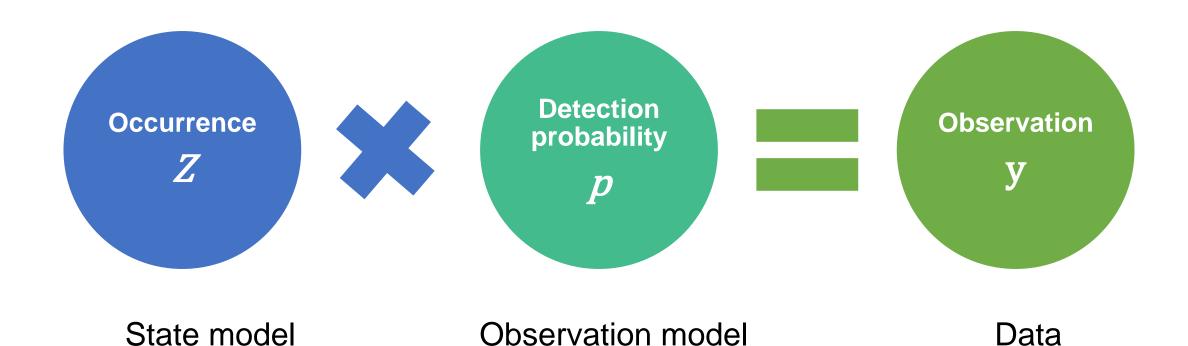
$$logit (\mathbf{p}_{ij}) = \alpha_0 + \alpha_1 * det.covar_{ij} + ...$$

ightarrow standard observation model is a Bernoulli model. $m{p}$ is the estimated detection probability.



You can include the same or separate covariates in the detection and occupancy components of the model!









The *unmarked* package

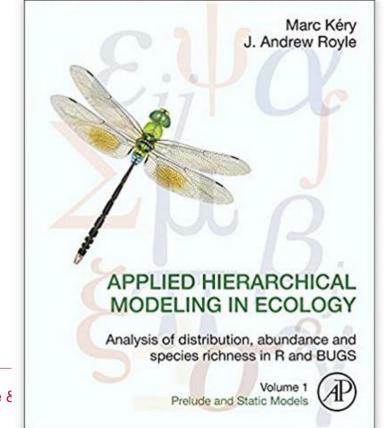
Authors: Ian Fiske, Richard Chandler, Andy Royle, Marc Kéry, David Miller, and Rebecca Hutchinson

"Fits hierarchical models of animal abundance and occurrence to data collected using survey methods such as point counts, site occupancy sampling, distance sampling, removal sampling, and double observer sampling. Parameters governing the state and observation processes can be modeled as

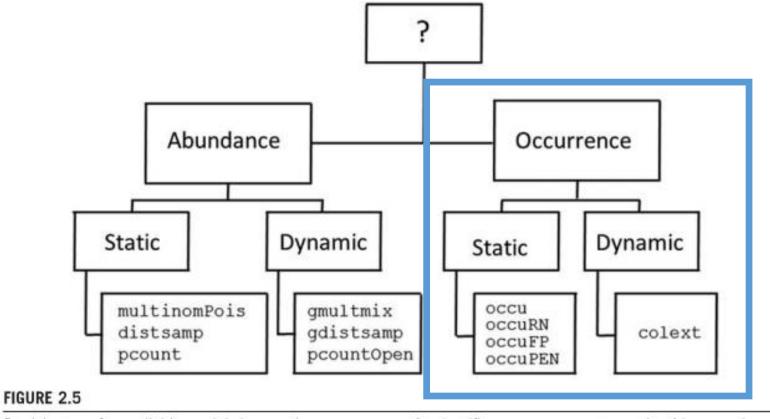
functions of covariates."

- easy to use for experienced R-Users
- Bayesian knowledge is not required (frequentists statistical package!)
- ➤ less flexible than coding in traditional BUGS-Language
- often less efficient while working with sparse detection-nondetection matrices





The *unmarked* package

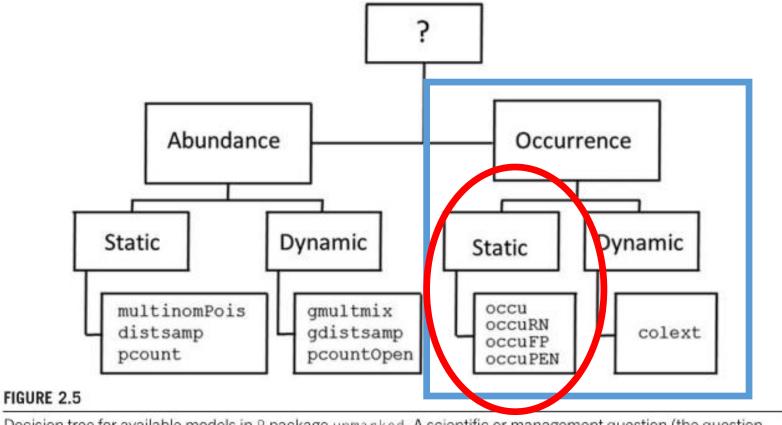


Decision tree for available models in R package unmarked. A scientific or management question (the question mark in the top square) first suggests a focus on either abundance or occurrence; second, the system is static or dynamic; and third, you use a particular sampling method; all of these determine the appropriate model for your study. (Figure courtesy of R. Chandler.)



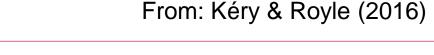


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(1) Processing and packaging the data into an "unmarked frame" using standard constructor functions that ensure data are in the proper format (unmarkedFrameOccu()).

Table 2.1 Typical data structure for the classes of HMs implemented in the unmarked package.

Observation Cova	
Date2	Date3
6	10
7	11
9	12
6	10
	6 7 9 6

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Table 2.1 Typical data structure for the classes of HMs implemented in the unmarked package.

	Detection Data		Site Covariate	Observation Covariate		riate	
	Visit1	Visit2	Visit3	Habitat	Date1	Date2	Date3
Site 1	1	1	1	Good	3	6	10
Site 2	0	0	0	Good	1	7	11
Site 3	1	0	0	Bad	2	9	12
Site 4	0	0	1	Bad	5	6	10



(1) Processing and packaging the data into an "unmarked frame" using standard constructor functions that ensure data are in the proper format (unmarkedFrameOccu()).

(2) Utilization of a standard model fitting function that produces parameter estimates, standard errors, AIC, and other summary statistics.





(1) Processing and packaging the data into an "unmarked frame" using standard constructor functions that ensure data are in the proper format (unmarkedFrameOccu()).

(2) Utilization of a standard model fitting function that produces parameter estimates, standard errors, AIC, and other summary statistics.

(3) Summary analyses that include producing model selection tables, goodness-of fit analyses (e.g., using parametric bootstrapping), and plotting predictions or fitted values.

```
fm <- occu( ~ Detection_Covariates ~ Occupancy_Covariates , data = umf)
fm0 <- occu(~ 1 ~ 1, data=umf)  # intercepts only
fm1 <- occu(~ wind ~ 1 , data=umf)  # covariates on detection
fm2 <- occu(~ 1 ~ habitat, data=umf)  # covariates on occupancy
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summary(fm3)</pre>
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                      call:
summary(fm3)
                      occu(formula = ~wind ~ habitat, data = umf)
                      Occupancy (logit-scale):
                                Estimate SE z P(>|z|)
                      (Intercept) -0.232 0.303 -0.765 4.44e-01
                      habitat 2.598 0.648 4.012 6.03e-05
                      Detection (logit-scale):
                                Estimate SE z P(>|z|)
```

(Intercept) -1.04 0.230 -4.53 5.83e-06

Swan wind -2.51 0.378 -6.65 3.02e-11



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pred.occ <- predict(fm3, type="state", newdata=newdat)</pre>
pred.det <- predict(fm3, type="det", newdata=newdat)</pre>
```





ranef(fm3)

State process $Z_i \sim Bernoulli(\psi_i)$

```
Mean Mode 2.5% 97.5%

[1,] 0.015231766 0 0 0

[2,] 0.017820736 0 0 0

[3,] 0.058991790 0 0 1

[4,] 1.000000000 1 1 1

[5,] 0.011251114 0 0 0

[6,] 0.072711276 0 0 1

[7,] 0.015363369 0 0 0

[8,] 0.058627194 0 0 1

[9,] 1.000000000 1 1 1
```

- ➤ These random effects are the presence/absence state at each site (Z), and their estimates represent our best guess of whether a particular site is occupied or not.
- ➤ These predictions of the random effects Z are also called **conditional** occupancy probability, where conditional means "given the observed data at that site".





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➤ If species was detected at a site, then Z is 1 with no uncertainty!!





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State process
$$Z_i \sim Bernoulli(\psi_i)$$

Mean Mode 2.5% 97.5% [1,] 0.015231766

Predicting Z at a site when species never detected

$$\Pr(z_i = 1 | \{y_i\} = 0) = \frac{\psi(1-p)^J}{(1-\psi) + \psi(1-p)^J}$$





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Model will predict some probability that the species was there





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Predicting Z at a site when species never detected

$$\Pr(z_i = 1 | \{y_i\} = 0) = \frac{\psi(1-p)^J}{(1-\psi) + \psi(1-p)^J}$$

- Model will predict some probability that the species was there
- \triangleright We have higher confidence in its presence (Z=1) despite the negative survey results (y=0,0,0) when
- 1. it is widespread overall (occurrence probability Ψ is high),
- 2. it is elusive (detection probability *p* is small),
- 3. the number of times we have looked for it (J) is small.





Derived parameters: Number of occupied sites

- ➤ In unmarked, we can obtain the number of occupied sites by summing over the estimates of the random effects z.
- Parametric bootstrapping can be used to obtain a confidence interval.





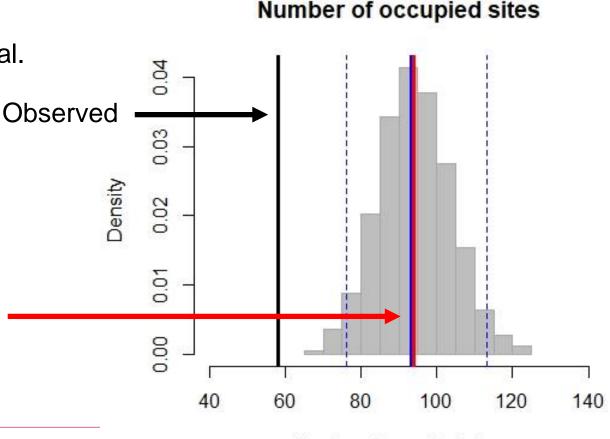
Derived parameters: Number of occupied sites

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Parametric bootstrapping can be used to obtain a confidence interval.

Species was only seen at 58 sites but was estimated to be present at ~ 93 sites by the model

True number of occupied sites = 94





Why Bootstrapping?

- For complicated functions, we often compute standard errors and confidence intervals using the method of bootstrapping
- Parametric bootstrapping we simulate data sets under the assumed model with parameters equal to the MLEs obtained from our observed data.
- For each simulated data set, we refit the model and obtain the (new) MLEs for the simulated data set. Each set of MLEs thus obtained is called a bootstrap sample, and together they form the bootstrap distribution.
- We can summarize to obtain quantities of interest. For example, the variance of the bootstrap samples is an estimate of the sampling variance. The 0.025 and 0.975 percentiles of the bootstrap distribution form a 95% confidence interval.





Fitting occupancy models in *JAGS*

What is JAGS?

- JAGS is 'Just Another Gibbs Sampler': a software package for performing Bayesian inference Using Gibbs Sampling
- Using a dialect of the BUGS language (WinBUGS, OpenBUGS, STAN)
- It estimates parameter posterior distributions for Bayesian statistical models, of (almost) arbitrary complexity, defined by the relationships between variables.
- JAGS uses MCMC simulation to converge on the posterior distribution of our parameters.





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We will access the **JAGS** functionalities within **R**. The package **rjags** provides an interface that allows us to handle pre-processing of data, the model estimation and the post-processing of results all together in one R session.





- (1) Get an idea of your data and your research question
- (2) Formulate a model and code it in the BUGS syntax





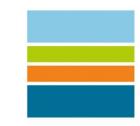
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- Most important elements of the syntax include:
 - x <- ... 'logical node' describes x as a deterministic function of some other variables
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- Most important elements of the syntax include:
 - x <- ... 'logical node' describes x as a deterministic function of some other variables
 - x ~ ... 'stochastic node' describes a probability distribution of x conditional on some other variables
- > Variety of in-build probability distributions: dnorm(mu,tau), dbin(p,n), dbern(p),...
- ➤ The BUGS language is not really vectorized we need loops to define the model for every element in vectors or multidimensional arrays.





10 basic steps of a Bayesian model analysis with JAGS

- (1) Get an idea of your data and your research question
- (2) Formulate a model and code it in the BUGS syntax
- (3) Think about the necessary prior distributions

Most ecologists use vague or uninformative priors, but be careful... priors might not always be as uninformative as you think!



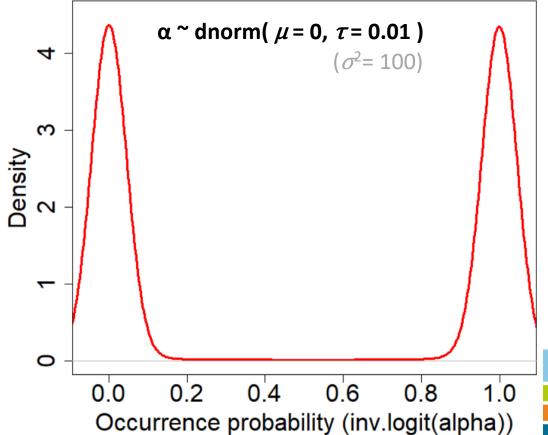


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Probability distributions in BUGS are defined by μ and precisions τ (= 1/ σ ²)!





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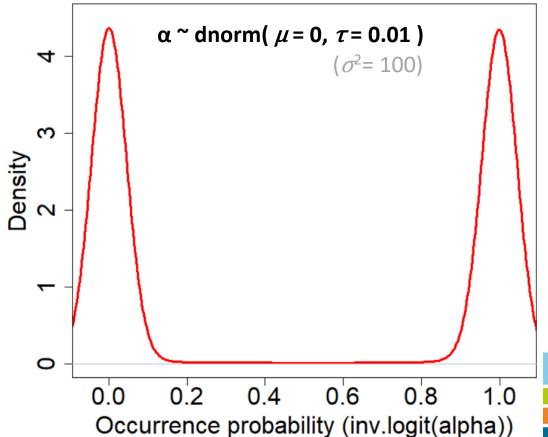
```
≈ flat priors at probability scale (for interept parameter in logistic models)
```

 $\alpha \sim dlogis(0, 1)$ Northrup & Gerber (2018)

mean.p ~ dunif(0, 1) Kéry & Royle (2016)
α <- ilogit(mean.p)</pre>

 $\alpha \sim dnorm(0, 0.5)$ Hobbs & Hooten (2015)

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Choice of priors for slope parameters is often less problematic, typical priors

 $\beta \sim \text{dnorm}(0, 0.1) \rightarrow \sigma^2 = 10$

 $\beta \sim dnorm(0, 0.01) \rightarrow \sigma^2 = 100$

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 $\beta \sim dnorm(0, 0.1)$ $\rightarrow \sigma^2 = 10$ $\beta \sim dnorm(0, 0.01)$ $\rightarrow \sigma^2 = 100$

The less information your data contains, the more impact has the choice of prior!

Recommendation: Perform a sensitivity analysis with different priors. If your posterior samples differ much – you should think further about your choice of prior.

```
cat(file = "StaticOcc_InterceptsOnly.txt","
model{
```

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```
cat(file = "StaticOcc_InterceptsOnly.txt","
model{
    ## Specify priors
    beta0.occ ~ dlogis(0,1)  ## prior on occupancy intercept
    alpha0.det ~ dlogis(0,1)  ## prior on detection intercept
```





```
cat(file = "StaticOcc_InterceptsOnly.txt","
model{

    ## Specify priors
    beta0.occ ~ dlogis(0,1)  ## prior on occupancy intercept
    alpha0.det ~ dlogis(0,1)  ## prior on detection intercept

    for (i in 1:nSites) {  ## Loop over Sites
        #--- True state model for the partially observed true state ---#
        z[i] ~ dbern(psi[i])  ## True occupancy z at site i
        logit(psi[i]) <- beta0.occ</pre>
```





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cat(file = "StaticOcc_InterceptsOnly.txt","
model{
   ## Specify priors
   beta0.occ ~ dlogis(0,1)
                                  ## prior on occupancy intercept
    alpha0.det ~ dlogis(0,1)
                                      ## prior on detection intercept
   for (i in 1:nSites) {
                           ## Loop over Sites
    #--- True state model for the partially observed true state ---#
     z[i] ~ dbern(psi[i])
                          ## True occupancy z at site i
      logit(psi[i]) <- beta0.occ</pre>
       for (j in 1:nVisits) { ## Loop over Visits
         #--- Observation model for the actual observations ---#
          y[i,j] ~ dbern(muy[i,j]) ## Detection-nondetection at i and j
          muy[i,j] <- z[i] * p[i,j]
          logit(p[i,j]) <- alpha0.det</pre>
         } #j
    } #i
```



- (1) Get an idea of your data and your research question
- (2) Formulate a model and code it in the BUGS syntax
- (3) Think about the necessary prior distributions
- (4) Assemble your data
 - format your data as a named list

```
BugsData <- list(y=y, nSites=dim(y)[1], nVisits=dim(y)[2])</pre>
```





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Swantje Löbel

- (4) Assemble your data
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- (4) Assemble your data
- (5) Generate (overdispersed) initial parameter values
- (6) Set the MCMC parameters (n.chains, n.iter, thin, ...)

```
n.chains = 3  # Number of chains (typically 3)
n.iter = 5000  # Total number of iterations (start with few)
n.burnin = 2500  # Burnin-length (Samples before will be discarded)
n.thin = 1  # e.g., thin = 1 → All samples are kept, thin = 10
→ every 10<sup>th</sup> sample will be kept
parameters.to.save = c(beta0.occ, alpha0.det, ...)
# Which parameters should be saved?
```



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- (6) Set the MCMC parameters (n.chains, n.iter, thin, ...)
- (7) Call and run JAGS





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- (5) Generate (overdispersed) initial parameter values
- (6) Set the MCMC parameters (n.chains, n.iter, thin, ...)
- (7) Call and run JAGS
- (8) Check your obtained posterior samples for convergence (traceplot, R-hat < 1.1)

```
traceplot(jagsModel)
gelman.plot(jagsModel)
```





- (1) Get an idea of your data and your research question
- (2) Formulate a model and code it in the BUGS syntax
- (3) Think about the necessary prior distributions
- (4) Assemble your data
- (5) Generate (overdispersed) initial parameter values
- (6) Set the MCMC parameters (n.chains, n.iter, thin, ...)
- (7) Call and run JAGS
- (8) Check your obtained posterior samples for convergence (traceplot, R-hat < 1.1)
- (9) If necessary, continue with further iterations until convergence
- (10) Inspect the posterior sample and analyse it with respect to your research question 1







