$$\forall h \in \mathcal{L}^2, \quad \mathbf{D}F(x) \cdot h = \langle (grad \ F)(x), h \rangle = \int (grad \ F)h$$
 (A.1)