

## ex1 - Lior Ziv

### Q1.a

I added another property which is not mentioned in your description, `suffTree{i}{4}` will hold the leaf index or an empty cell if it's an internal node.

### Q1.c.2

The degree is 2, The time complexity is polynomial  $O(n^2)$

### Q1.c.3

The actual time was = 43.9 seconds, the predicted time was 48.85 seconds.

### Q3.a

- I would suggest an algorithm that allows at most  $K$  mismatches.  
For a given read( $R$ ) and a sequence it builds a joint suffix tree and then work as follows:  
Find the largest common part(LCA) - lowest common ancestor, for each suffix of the sequence and  $R$ .  
After finding the LCA the strings split which means there is one mismatch(the next letter must be different)  
The next move will be taking  $R\{\text{splitPoint} + 1:\text{end}\}$ , `suffix{{splitPoint} + 1:end}` and start again running on the suffix tree from the root.  
For every split we add one mismatch and start again until  $r$  is empty. At the end we check if the amount of mismatches  $< K$  and only those suffixes are saved.

### pseudo code

- `k-mismatches(r,sequence,k):`  
  `ST = initialize(sequence,r)` one tree which contains both words  
  `result = {}`  
    – for each suffix in sequence:  
      \* `res = k-mismatchHelper(r,sequence,counter,k)`  
      \* `if(~isempty(res))` , add `res` to results
- `k-mismatchHelper(r,sequence,counter)`  
    – `if(isempty(r))` - return  
    – `splitPoint = find LCA(suffix,r)`

- $r = r\{\text{splitPoint} + 1 : \text{end}\}$ ,  $s = \text{suffix}\{\{\text{splitPoint} + 1 : \text{end}\}$
- raise mismatch counter by 1
- $\text{counter} = \text{k-mismatchHelper}(r, \text{sequence}, \text{counter})$
- if ( $\text{counter} < k$ )
  - \* return ( $\text{index}, \text{index} + \text{length}(r) - 1$ )
- return empty cell

### Q3.b

- The algorithm build a suffix tree for the sequence and the read  $r \rightarrow O(\text{length}(\text{sequence}) + \text{length}(r))$ , now the algorithm runs on each suffix with the read and might have  $k$  (up to  $r$  length) mismatches  $\rightarrow O(\text{length}(r))$   
combined the total **time complexity** is  $O(\text{length}(\text{sequence}) * \text{length}(r))$
- The algorithm build a suffix tree for the sequence and the read  $r \rightarrow O(\text{length}(\text{sequence}) + \text{length}(r))$  and for each suffix has to save at most an array with two indexes to save in results.  
combined the total **space complexity** is  $O(\text{length}(\text{sequence}) + \text{length}(r))$