

ex1 - Lior Ziv

1. show that for two sequences \vec{t}, \vec{s} with size n , there are at least 3^n possible alignments if we look at the possibilities when aligning two sequences we have 3 possibilities for each place:

- a letter from \vec{t} and a gap from \vec{s}
- a letter from \vec{s} and a gap from \vec{t}
- a letter from both \vec{t}, \vec{s}

so for each alignment we have n places to choose and for each place we have 3 options $\rightarrow 3 \cdot 3 \cdot 3 \dots 3$ n times $\rightarrow 3^n$

2. (a) Gap_penalty_value = -2 match = +1 mismatch = -1
sub_similarity(\vec{t}, \vec{s}) :

max = 0

optimal_loc = null

//initialize the gap lines

for i in range $|\vec{s}|$ SIM(i,0) += 0

for i in range $|\vec{t}|$ SIM(0,i) += Gap_penalty_value

//fills the SIM table

for i in range 1- $|\vec{s}|$:

- for j in range 1- $|\vec{t}|$:

– SIM(i,j) = max { SIM(i-1,j-1) + $\sigma(\vec{s}_i, \vec{t}_j)$, SIM(i-1,j) + Gap_penalty_value, SIM(i,j-1) + Gap_penalty_value }

– and mark the square you came from (in order to track back at the end)

//returns the best sub - sequence score and place in matrix

max, i_loc = max(SIM(i, $|\vec{t}|$) for i in range $|\vec{s}|$) (since the optimal seq is found at the last column - makes sure all t is included)

optimal_loc = (i_loc, $|\vec{t}|$)

return max, optimal_loc

in order to extract the sequence we need to track-back from the optimal_loc

(b)

Gap_penalty_value = -2 match = +1 mismatch = -1

sub_similarity(\vec{t}, \vec{s}) :

max = 0

optimal_loc = null

//initialize the gap lines

for i in range $|\vec{s}|$ SIM(i,0) += Gap_penalty_value

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for i in range  $|\vec{t}|$  SIM(0,j) += 0
//fills the SIM table
for i in range 1-  $|\vec{s}|$ :
    • for j in range 1-  $|\vec{t}|$ :
        - SIM(i,j) = max { SIM(i-1,j-1) +  $\sigma(\vec{s}_i, \vec{t}_j)$ , SIM(i-1,j) + Gap_penalty_value
            , SIM(i,j-1) + Gap_penalty_value }
        - and mark the square you came from (in order to track back at the
            end)

//returns the best sub - sequence score and place in matrix
max , j_loc= max(SIM( $|\vec{s}|$ ,i) for j in range  $|\vec{t}|$  (since the optimal seq is
found at the last line - makes sure all s is included)
optimal_loc = ( $|\vec{s}|$ ,j_loc)
return max,optimal_loc

in order to extract the sequence we need to track-back from the opti-
mal_loc

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