



# **Analytics in Managerial Economics**

**Estimating the effect of a Banking Regulation** 

## **Submitted By**

Ashesh Sasidharan (A0066946N)

Manisha Suryavanshi (A0176653W)

Yin Mingjun (A0082931E)

Zhang Qianru (A0176634X)

## **Table of Contents**

1.	Exe	cutive Summary	
		stract	
		y Findings	
1	1.3 Re	commendations	3
		odel Highlight & Assumption	
2.		eline Model	
3.	Rok	oustness Test: Propensity Score Match	5
4.		cebo Test – Exogenous Shocks in the System	
5.		ditional Hypothesis	
6.		o 10 and Bottom 10 group effects	
7.	Ref	erence	7
8.	Арр	oendix	8
8	8.1	Baseline Model	
8	8.2	Propensity Score Matching	8
8	8.3	Model for Placebo Test	11
8	8.4	Top Ten Grouping Effect	12
8	8.5	Additional Hypothesis	12

## 1. Executive Summary

#### 1.1 Abstract

This report focuses on estimating the announcement effect of **Volcker Rule** in reducing **Trading Asset Ratio** of Bank Holding Companies (BHC) with the help of Difference in Differences (DiD) methodology of Study. Timeframe of data used range from 2004, well before inception of VR to 2016 right before VR kicks into effect. Through this report, we aim to gain insights into potential effectiveness of the new regulation and the difference in magnitude of effects across different banks in the industry.

#### 1.2 Key Findings

- Volcker Rule is generally effective in enforcing banks to reduce Trading Asset. On average, there is 0.013% in trading assets across banking industry.
- ➤ While the average reduction in trading assets across banking industry is not significant, those affected BHC having greater than 3% in trading assets before VR have reduced their TAR portfolio by 2.33% more than non-affected BHCs.
- In particular, the **Top 10** banks with highest **TAR** portfolio before the VR announcement have responded strongly by reducing their asset ratio by approx. **6.54%** to the average of **2.33%**. Similar analysis on **Bottom 10** banks has shown a pared down response with only a reduction of **2.11%** to the average of **2.33%**.
- ➤ Looking at the overall risk-taking attitude of banks, controversially risk-taking appetite of banks generally **increase** across the industry after announcement of VR, despite **reduction** in trading assets.

#### 1.3 Recommendations

For the regulators, Although VR seems to be effective and viable regulation in forcing banks to reduce their Trading Asset Portfolio, especially for those Top performing BHCs with large trading asset size, they must incorporate more robust guideline to recede general risk-taking attitude of banks.

Our study has revealed that banks have most likely **shifted** their risk-taking appetite from **proprietary trading** to other **unaffected risky revenue generators**. This will potentially counteract and erode the effectiveness of VR if loosely enforced.

For BHCs with relatively large books, the magnitude of impact is higher than those with smaller **TAR** portfolio. For long term planning, those affected BHCs should transform their business strategically by spreading into **lower risk revenue generators** to buffer the effect, while also remaining competitive during this phase by maintaining their TAR portfolio as nearer to the limit regulated by **VR**.

#### 1.4 Model Feature & Assumptions

- ➤ Baseline model is tested for Robustness by taking into account distinct data schema by Inclusion & Exclusion of Fixed Effect (Both time and Bank), together with other control variable (Co-variates).
- Propensity score matching methodology is made use to scale down sample Bias problem. We also performed cross validation by choosing dataset spread across three quarter across different years.
- ➤ Placebo Test is also being accounted for by randomly assigning Banks to Control & Treatment group and cross validating our find that, changes occurred in Trading Asset Ratio is primarily due to the announcement of VR rule.
- Additional **Hypothesis Testing** is also examined to understand if banks have fundamentally reduced their Risk-taking behavior after the announcement of VR.

## 2. Baseline Model

We construct a baseline model as below to analyze the change in trading assets ratio (TAR)

$$Y_{i,t} = \alpha + \beta * (after\_DFA_t * Affected_{BHC_i}) + \gamma_i + X_{i,t} + \epsilon_{i,t}$$

$Y_{i,t}$	Y <sub>i,t</sub> Trading asset ratio for the quarter t and bank i		Bank fixed effect
after_DFA <sub>t</sub>	after_DFA=0 if quarter in Q3 2004 to Q2 2009, else 1	$\in_{i,t}$	Time fixed effect
treat <sub>BHCi</sub>	Affected_BHC=1 if the bank was affected, else 0	$X_{i,t}$	Other Control Variables

We implemented our baseline model with four different variations. Table below shows the results of the regression. Once we control for the Fixed Effects in the model and run test for robustness by running it against several model's forms (such as including/excluding control variables). It is seen that the coefficient  $\beta$  for the interaction term (after\_DFA \* Affected\_BHC) is always **significant**.

Baseline Test Results									
1 2 3 4									
Dependent Variable	Trading Asset Ratio								
After_DFA SD	<b>0.000122</b> (0.000139)	<b>0.00005895</b> (0.0001631)	X	X					
Affected_BHC1 SD	<b>0.113 ***</b> (0.000707)	<b>0.1</b> *** (0.00073)	X	X					
After_DFA_11*Affected_BHC1 SD	<b>0.00386 ***</b> (0.001101)	<b>-0.00368 ***</b> (0.00107)	<b>-0.02286 ***</b> (0.0005272)	<b>-0.023338 ***</b> (0.000528)					
Controls FE R-squared	No No 0.527	Yes No 0.5557	No Yes 0.048563	Yes Yes 0.053					

## 3. Robustness Test: Propensity Score Match

We use Propensity Score Matching (**PSM**) to reduce selection bias problem by matching banks with **nearest propensity score** to form **treatment** and **control** group respectively. We have compared **three** different propensity matching approach against the baseline full model.

At first, we matched One treated bank with Three control bank (1:3) for Q3 2004, followed by matching One treated bank with Five control bank (1:5) for Q3 2004 & Q2 2009 respectively.

Robustness Test – Propensity Score Match								
	1	2	3	4				
Dependent Variable	Full Data	Q3 2004 with 1:3	Q3 2004 with 1:5	Q2 2009 with 1:5				
Affected_BHC * After_DFA	-0.02333*** -0.02767***		-0.02782***	-0.020893***				
Control variable & Fix Effects	YES	YES	YES	YES				
No. of Observations	40026	1668	2690	3295				
R-Squared	0.053135	0.18278	0.15674	0.086545				

Table 2: Robustness test using propensity score matching

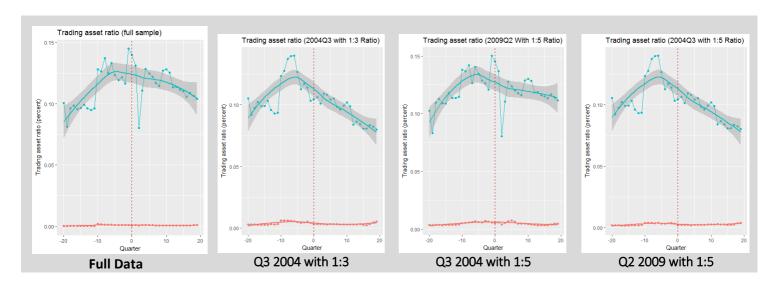


Fig1: Attributes of data for robustness comparisons

As shown in Fig1 and Table2, all our **PSM** models yields are **significant**, and the **coefficient** values are similar, giving a clear indication that the **effect in the outcome is due to treatment effect**. We did also try PSM using **Caliper matching** method. It gives an overall better matched and balanced data, but it resulted in having very few matching group (**6 treatment & 6 control with 1:1 ratio**) as against PSM with 'Nearest' method (**54 Treatment & 54 Control with 1:1 ratio**)

## 4. Placebo Test – Exogenous Shocks in the System

To prove that there is an exogenous shock, we have randomly assigned the treatment and control labels to the BHC's in the data set as in the model below. We observe the coefficient for interaction term to be **insignificant**. **Pr** (|t|) value of interaction term (**after\_DFA**<sub>t</sub> \* **Random**<sub>BHC<sub>i</sub></sub>) for each random assignment is shown in appendix.

Hence this indicates that there is an **exogenous shock** in the system driving the trading asset ratios.

$$Y_{i,t} = \alpha + \beta * (after\_DFA_t * Random_{BHC_i}) + \gamma_i + X_{i,t} + \epsilon_{i,t}$$

### 5. Top 10 and Bottom 10 group effects

We also divided the Matched dataset (Q3 2004 with 1:3) into 3 groups. Group 1 contained the top 10 banks with the maximum trading asset ratios before the Volcker rule, whereas the rest were in Treatment and Control groups.

$$Y_{i,t} = \alpha + \beta * \left( after_{DFA_t} * Affected_{BHC_i} \right) + \beta_2 * \left( top_{10_{players}} * Affected_{BHC_i} \right) \gamma_i + X_{i,t} + \in_{i,t}$$

Results showed that the **top 10 banks** responded more **significantly** to the Volcker rule by reducing their trading asset ratio by **6.54%** more than non-treated banks and **4.44%** more than the smaller treated bank. This would be because these banks would need to make a significant reduction in their trading asset ratio in compliance with the rule.

Similar analysis on the **Lowest 10 banks** shows that the banks with the lowest (but > 3%) trading asset ratio before the VR reduced their assets by **2.11%** compared to the average of **2.33%**.

## 6. Additional Hypothesis

The overall effectiveness of VR rule would largely depend on whether banks have fundamentally reduced risk taking behavior. To measure this a normalized **Z** score is calculated based on Returns and volatility of returns, whereby **Z-Score** = (ROA + Leverage Ratio)/ $\sigma ROA$ 

Where Return on Asset (**ROA**) and Leverage Ratio or Capital Asset Ratio signifies return on company's risk taking activities and  $\sigma ROA$  captures risk taking volatility. Since the term is highly skewed, a natural log transformation is performed and the following model is created:

$$log(Z\_Score)_{i,t} = \alpha + \beta * (after\_DFA_t * Random_{BHC_i}) + \gamma_i + X_{i,t} + \epsilon_{i,t}$$

#### **Key Finding**

- ➢ Risk taking appetite represented by log(Z\_Score)<sub>i,t</sub> increases across BHCs after the announcement of VR and the effect is statistically significant, concluding that VR rule has failed to decrease Bank's overall Risk Taking greed.
- Comparing affected BHCs with large trading books to those with less affected BHCs by VR, the risk taking appetite did not show a significant deviation

## 7. Reference

 $Keppo\ J$  and  $Korte\ J.$  Risk Targeting and Policy illusions – Evidence from the Announcement of the Volcker rule

SSRN: <a href="http://ssrn.com/abstract=2466477">http://ssrn.com/abstract=2466477</a> or <a href="http://dx.doi.org/10.2139/ssrn.2466477">http://dx.doi.org/10.2139/ssrn.2466477</a>

**Olmos A, Govindasamy P**, Propensity Scores: A Practical Introduction Using R. Journal of Multidisciplinary Evaluation. Vol 11, Issue 25, 2015. ISSN 1556-8180

## 8. Appendix

#### 8.1 Baseline Model

```
call:
plm(formula = TAR ~ Affected_BHC * After_DFA + ROA + Leverage_Ratio +
     Total_Asset + Credit_Risk_Ratio + Cost_Income_Ratio + Deposit_Ratio +
     Real_Estate_Ratio + Liquidity_Ratio + CPP, data = modified_data, index = c("id", "Time"))
Unbalanced Panel: n=2428, T=1-38, N=40026
Residuals :
                   1st Qu.
                                   Median
                                                3rd Qu.
        Min.
                                                                  мах.
-1.0927e-01 -2.2475e-04 -5.9395e-06 1.8227e-04 1.9179e-01
Coefficients:
                            Estimate Std. Error t-value Pr(>|t|)
-1.3017e-04 9.4527e-05 -1.3771 0.1685049
-2.0121e-04 8.0709e-03 -0.0249 0.9801108
After_DFA
ROA
                             3.2278e-03 1.8475e-03 1.7472 0.0806157 .
5.0860e-04 1.4875e-04 3.4191 0.0006289 ***
3.6595e-03 1.2871e-03 2.8431 0.0044705 **
2.0625e-04 1.2907e-04 1.5981 0.1100376
1.5023e-03 5.4999e-04 2.7315 0.0063071 **
Leverage_Ratio
Total_Asset
                                                           3.4191 0.0006289 ***
Credit_Risk_Ratio
Cost_Income_Ratio
Deposit_Ratio
Real_Estate_Ratio
                            -8.3544e-03
                                           6.7402e-04 -12.3948 < 2.2e-16 ***
Liquidity_Ratio
                            -6.0897e-04 1.0169e-03 -0.5988 0.5492936
CPP
                             -1.2342e-04
                                           1.4752e-04
                                                          -0.8366 0.4028371
Affected_BHC:After_DFA -2.3327e-02 5.2805e-04 -44.1755 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Total Sum of Squares:
                              1.2613
Residual Sum of Squares: 1.1943
R-Squared:
                   0.053135
Adj. R-Squared: -0.0082813
F-statistic: 191.751 on 11 and 37587 DF, p-value: < 2.22e-16
    8.2 Propensity Score Matching - Q3 2004 with 1:3
plm(formula = TAR ~ Affected_BHC * After_DFA + ROA + Leverage_Ratio +
     Total_Asset + Credit_Risk_Ratio + Cost_Income_Ratio + Deposit_Ratio +
     Real_Estate_Ratio + Liquidity_Ratio, data = matched_data_1,
     index = c("id", "Time"))
```

```
Unbalanced Panel: n=72, T=1-38, N=1668
Residuals :
                          Median
                                    3rd Ou.
      Min.
              1st Ou.
-0.11004955 -0.00387388 -0.00017831 0.00294318 0.18773522
Coefficients:
                       Estimate Std. Error t-value Pr(>|t|)
After_DFA
                     -0.00160454 0.00141700 -1.1324 0.2576568
                     ROA
Leverage_Ratio
                     0.06489552 0.03091499
                                           2.0992 0.0359605
Total_Asset
                     -0.01073257
                                0.00232409
                                           -4.6180 4.188e-06 ***
Credit Risk Ratio
                                            3.8783 0.0001095 ***
                     0.09322868 0.02403835
                     0.00095541 0.00087817
                                            1.0879 0.2767832
Cost_Income_Ratio
                                           3.0660 0.0022059 **
                                0.00740090
                     0.02269132
Deposit_Ratio
                    Real Estate Ratio
Liquidity Ratio
                                0.01413619
                                           -3 5932 0 0003366 ***
Affected_BHC:After_DFA -0.02767667 0.00218465 -12.6687 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Total Sum of Squares:
Residual Sum of Squares: 0.39694
R-Squared:
              0.18278
Adj. R-Squared: 0.14104
F-statistic: 35.4722 on 10 and 1586 DF, p-value: < 2.22e-16
```

#### 8.3 Propensity Score Matching - Q3 2004 with 1:5

```
plm(formula = TAR ~ Affected_BHC * After_DFA + ROA + Leverage_Ratio +
     Total_Asset + Credit_Risk_Ratio + Cost_Income_Ratio + Deposit_Ratio +
     Real_Estate_Ratio + Liquidity_Ratio, data = matched_data_3, index = c("id", "Time"))
Unbalanced Panel: n=108, T=1-38, N=2690
Residuals :
                   1st ou.
                                   Median
                                                 3rd Ou.
        Min.
-0.10986031 -0.00243204 -0.00010616 0.00202371 0.18927858
Coefficients:
                           Estimate Std. Error t-value Pr(>|t|)
-0.00031270 0.00085693 -0.3649 0.715214
-0.13467004 0.08986698 -1.4985 0.134113
0.05847152 0.01943044 3.0093 0.002644 **
-0.00815321 0.00143717 -5.6731 1.559e-08 ***
After_DFA
ROA
Leverage_Ratio
Total_Asset
                                            0.01516229 4.2317 2.401e-05 ***
0.00059464 1.0576 0.290349
0.00491342 2.2625 0.023750 *
Credit_Risk_Ratio
                             0.06416195
Cost Income Ratio
                            0.00062888 0.00059464
                             0.01111656 0.00491342
Deposit Ratio
Real_Estate_Ratio
                            -0.05469056 0.00557795 -9.8048 < 2.2e-16 ***
 iquidity Ratio
                            -0.03668125 0.00889303
                                                           -4.1247 3.830e-05 ***
Affected_BHC:After_DFA -0.02782090 0.00166286 -16.7307 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Total Sum of Squares:
Residual Sum of Squares: 0.41776
R-Squared:
                 0.15674
Adj. R-Squared: 0.11838
F-statistic: 47.807 on 10 and 2572 DF, p-value: < 2.22e-16
```

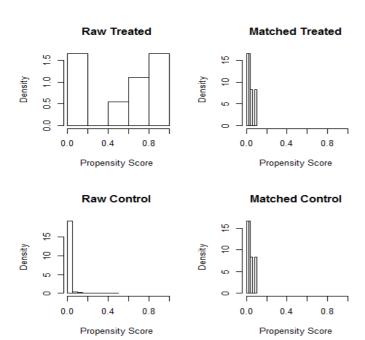
#### 8.4 Propensity Score Matching - Q2 2009 with 1:5

```
plm(formula = TAR ~ Affected_BHC * After_DFA + ROA + Leverage_Ratio +
    Total_Asset + Credit_Risk_Ratio + Cost_Income_Ratio + Deposit_Ratio +
    Real_Estate_Ratio + Liquidity_Ratio, data = matched_data_2,
    index = c("id", "Time"))
Unbalanced Panel: n=102, T=6-38, N=3295
Residuals :
Min. 1st Qu. Median 3rd Qu. Max. -0.07599745 -0.00223607 -0.00014941 0.00165545 0.17971603
Coefficients:
                         Estimate Std. Error t-value Pr(>|t|)
-0.00131174 0.00072307 -1.8141 0.0697541
-0.05038298 0.06752464 -0.7461 0.4556367
After_DFA
ROA
Leverage_Ratio
                         0.00505930 0.01343592
                                                    0.3766 0.7065329
                          0.00108895 0.00105045
                                                     1.0366 0.2999785
Total_Asset
Credit_Risk_Ratio
                          0.06029308
                                      0.01377620
                                                     4.3766 1.244e-05 ***
                          0.00071851 0.00065952
Cost_Income_Ratio
                                                     1.0894 0.2760453
Deposit_Ratio
                          0.01434226
                                       0.00381695
                                                     3.7575 0.0001747 ***
Real_Estate_Ratio
                         -0.00552953
                                       0.00459356 -1.2038 0.2287735
Affected_BHC:After_DFA -0.02089358  0.00139479 -14.9797 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Total Sum of Squares:
                           0.62733
Residual Sum of Squares: 0.57304
R-Squared:
                 0.086545
Adj. R-Squared: 0.05469
F-statistic: 30.157 on 10 and 3183 DF, p-value: < 2.22e-16
```

#### 8.5 Propensity Score Matching – Caliper Matching

Sample sizes:

	Control	Treated
All	783	18
Matched	6	6
unmatched	///	12
Discarded	0	0



### 8.6 Propensity Score Matching - Used Model

call:
matchit(formula = treat ~ X, data = data2, method = "nearest",
 ratio = 3)

Sample sizes:

Control Treated
All 783 18
Matched 54 18
Unmatched 729 0
Discarded 0 0

#### 8.7 Model for Placebo Test

```
plm(formula = TAR ~ random_BHC * After_DFA + ROA + Leverage_Ratio +
Total_Asset + Credit_Risk_Ratio + Cost_Income_Ratio + Deposit_Ratio +
    Real_Estate_Ratio + Liquidity_Ratio + CPP, data = modified_data,
model = "within", index = c("id", "Time"))
Unbalanced Panel: n=2428, T=1-38, N=40026
Residuals:
       Min.
                 1st Ou.
                               Median
                                           3rd Ou.
-0.10925732 -0.00026096 -0.00001302 0.00020608 0.19182712
Coefficients:
                         Estimate Std. Error t-value Pr(>|t|)
random_BHC
                      -3.2549e-05 7.6888e-05 -0.4233 0.6720562
After_DFA
                      -4.2909e-04 1.1451e-04 -3.7472 0.0001791 ***
ROA
                      -3.0634e-03 8.2776e-03 -0.3701 0.7113213
                     3.2098e-03 1.8949e-03 1.6940 0.0902810
4.6415e-04 1.5257e-04 3.0422 0.0023499
Leverage_Ratio
Total_Asset
                                                 3.0422 0.0023499
7.2058e-04 5.6381e-04 1.2781 0.2012390
-6.4014e-03 6.8982e-04 -9.2798 < 2.2e-16
Deposit Ratio
Real_Estate_Ratio
Liquidity_Ratio -2.3995e-03 1.0422e-03 -2.3023 0.0213258
random_BHC:After_DFA -3.2328e-05 1.2166e-04 -0.2657 0.7904525
signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Total Sum of Squares:
                          1.2613
Residual Sum of Squares: 1.2563
R-Squared:
                0.0039921
Adj. R-Squared: -0.06064
F-statistic: 12.554 on 12 and 37586 DF, p-value: < 2.22e-16
```

The **p-values** for the coefficient of the interaction term were found to be **insignificant** (at **95% confidence level**) for 10 random assignments, as shown in the table below:

Test Num	1	2	3	4	5	6	7	8	9	10
Pr (> t )	0.7427	0.1865	0.3449	0.7052	0.9436	0.9156	0.8002	0.8771	0.7034	0.8498

Table: Pr (>|t|) value for Interaction term for each Random Assignment

#### 8.8 Top Ten Grouping Effect

```
plm(formula = TAR ~ (After_DFA * top10) + (After_DFA * Affected_BHC) +
    ROA + Leverage_Ratio + Total_Asset + Credit_Risk_Ratio +
Cost_Income_Ratio + Deposit_Ratio + Real_Estate_Ratio + Liquidity_Ratio +
    CPP, data = top10AnalysisData, index = c("id",
Unbalanced Panel: n=72, T=1-38, N=1668
Residuals :
                             Median
                                        3rd Qu.
      Min.
                1st Ou.
                                                       Max.
-0.10990032 -0.00373428 -0.00027249 0.00271573 0.18809633
Coefficients:
                        Estimate Std. Error t-value Pr(>|t|)
                      -0.0020446 0.0013900 -1.4709 0.1415122
-0.0618440 0.1329178 -0.4653 0.6417946
After_DFA
ROA
Leverage_Ratio
                      0.0409597 0.0310584 1.3188 0.1874274
-0.0073540 0.0023199 -3.1700 0.0015534
Total_Asset
                      Credit_Risk_Ratio
Cost_Income_Ratio
Deposit_Ratio
Real_Estate_Ratio
Liquidity_Ratio
                     -0.0877978 0.0093267 -9.4136 < 2.2e-16 ***
                      -0.0474955 0.0138720 -3.4238 0.0006332 ***
                       -0.0014370 0.0016478 -0.8721 0.3832985
After_DFA:top10
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Total Sum of Squares:
                         0.48571
Residual Sum of Squares: 0.38055
R-Squared:
                0.21652
Adj. R-Squared: 0.17547
F-statistic: 36.4801 on 12 and 1584 DF, p-value: < 2.22e-16
```

#### 8.9 Additional Hypothesis

The regression model and summary results of for the additional hypothesis testing is shown below.

```
Where: Z_Score_Log = log((ROA + Leverage Ratio)/\sigma ROA)
\sigma ROA is computed from 10 quarters ROA with moving window approach
```

Coefficient of After\_DFA is positive and highly statistically significant, implying that BHCs in general increased risk appetite after VR announcement.

Coefficient of Affected BHC:After\_DFA is positive but not statistically significant, implying that risk attitude of BHCs with large trading book is not significantly different from those with small trading books.

```
Call:
plm(formula = Z_Score_log ~ Affected_BHC * After_DFA + TAR +
    Total_Asset + Credit_Risk_Ratio + Cost_Income_Ratio + Deposit_Ratio +
    Real_Estate_Ratio + Liquidity_Ratio + CPP, data = data1,
    index = c("id", "Time"))
Unbalanced Panel: n=2107, T=1-38, N=34353
Residuals :
    Min. 1st Qu.
                    Median 3rd Ou.
-7.720029 -0.378699 -0.010727 0.360137 5.043606
Coefficients :
                      Estimate Std. Error t-value Pr(>Itl)
                     0.8685200 0.0127977 67.8655 < 2.2e-16 ***
After_DFA
TAR
                    -3.0348504 0.6989585 -4.3420 1.416e-05 ***
                    Total_Asset
Credit_Risk_Ratio
                    -8.2800229 0.1947136 -42.5241 < 2.2e-16 ***
Cost_Income_Ratio
                     -0.0754841 0.0176421 -4.2786 1.886e-05 ***
Deposit_Ratio
                     -0.7329130 0.0758512 -9.6625 < 2.2e-16 ***
                     -1.8582113    0.0962177   -19.3126 < 2.2e-16 ***
Real_Estate_Ratio
                    -0.3861293 0.1450226 -2.6625 0.007759 **
Liquidity_Ratio
CPP
                      0.0069822 0.0200449 0.3483 0.727596
Affected_BHC:After_DFA 0.0279716 0.0726555 0.3850 0.700248
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Total Sum of Squares:
                     20197
Residual Sum of Squares: 16628
R-Squared:
           0.1767
Adj. R-Squared: 0.12266
F-statistic: 691.871 on 10 and 32236 DF, p-value: < 2.22e-16
```