# DSC5211C - Workshop 4

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# 1ai) Results suggest that the series is not stationary

| Sample: 1960M01 2018M12<br>Included observations: 708 |                     |    |       |        |        |       |  |
|---|---------------------|----|-------|--------|--------|-------|--|
| Autocorrelation                                       | Partial Correlation |    | AC    | PAC    | Q-Stat | Prob  |  |
|   |                     | 1  | 0.992 | 0.992  | 699.84 | 0.000 |  |
|   | l l                 | 2  | 0.980 | -0.257 | 1384.0 | 0.000 |  |
|   | ı ı                 | 3  | 0.968 | 0.008  | 2051.6 | 0.000 |  |
| 1   | ı <b>j</b> ı        | 4  | 0.955 | 0.030  | 2703.3 | 0.000 |  |
|   | 1 1                 | 5  | 0.944 | 0.004  | 3339.9 | 0.000 |  |
|   | 1 <b>0</b> 1        | 6  | 0.931 | -0.037 | 3961.0 | 0.000 |  |
| 1   | ı <b>İ</b> I        | 7  | 0.919 | 0.027  | 4567.3 | 0.000 |  |
| 1   | ı <b>İ</b> D        | 8  | 0.909 | 0.068  | 5160.5 | 0.000 |  |
| 1   | ı <b>İ</b>          | 9  | 0.901 | 0.111  | 5743.7 | 0.000 |  |
| 1   | ı ı                 | 10 | 0.893 | -0.004 | 6318.5 | 0.000 |  |
| 1   | <b>@</b>            | 11 | 0.886 | -0.055 | 6884.1 | 0.000 |  |
| 1   | <b></b>             | 12 |       | -0.113 | 7438.2 | 0.000 |  |
| 1   | 1 1                 | 13 | 0.866 | 0.016  | 7980.0 | 0.000 |  |
| 1   | ı <b>D</b>          | 14 | 0.856 | 0.069  | 8510.8 | 0.000 |  |
| 1   | ı <b>İ</b> ı        | 15 |       | -0.008 | 9031.3 | 0.000 |  |
| 1   | 111                 | 16 | 0.838 | 0.019  | 9542.0 | 0.000 |  |
| 1   | 111                 | 17 | 0.830 | 0.021  | 10043. | 0.000 |  |
| 1   | 1 1                 | 18 | 0.822 | 0.006  | 10535. | 0.000 |  |
| 1   | 1 1                 | 19 | 0.814 | 0.010  | 11018. | 0.000 |  |
| 1   | 1 1                 | 20 | 0.807 | 0.006  | 11494. | 0.000 |  |
| 1   | 1 <b>₫</b> 1        | 21 |       | -0.029 | 11963. | 0.000 |  |
| 1   | ı <b>l</b> ı        | 22 |       | -0.045 | 12423. | 0.000 |  |
| 1   | ı <b>l</b> ı        | 23 |       | -0.017 | 12873. | 0.000 |  |
| 1   | 1 1                 | 24 | 0.774 | 0.002  | 13314. | 0.000 |  |
| 1   | 1 <b>1</b> 11       | 25 | 0.766 | 0.034  | 13745. | 0.000 |  |
| 1   | 1 <b>. 1</b> 1      | 26 | 0.758 | 0.031  | 14168. | 0.000 |  |
| 1   | ' <b>II</b>         | 27 | 0.751 | 0.090  | 14585. | 0.000 |  |
| 1   | 1 1                 | 28 | 0.746 | 0.012  | 14997. | 0.000 |  |
| 1   | 1 1                 | 29 | 0.741 | 0.024  | 15404. | 0.000 |  |
| 1   | 1]1                 | 30 | 0.738 | 0.000  | 15807. | 0.000 |  |
| 1   | ų į                 | 31 | -     | -0.002 | 16207. | 0.000 |  |
| 1   | ' <b>D</b>          | 32 | 0.732 | 0.061  | 16605. | 0.000 |  |
| 1   | 1 1                 | 33 | 0.729 | 0.008  | 17001. | 0.000 |  |
|   | 111                 | 34 | 0.727 | 0.017  | 17395. | 0.000 |  |
|   | ' <b>]</b> li       | 35 | 0.724 | 0.048  | 17786. | 0.000 |  |
|   | <b>I</b> II 1       | 36 | 0.722 | -0.045 | 18176. | 0.000 |  |

1aii) Results show that t-stat is -0.733304 which has significance of 0.3988. This more than 0.05 hence there is no evidence to reject the null hypothesis that "COPPER" has unit root ( $\gamma$ =0). Hence it is also non-stationary.

| Null Hypothesis: COPPER has a unit root<br>Exogenous: None<br>Lag Length: 1 (Automatic - based on SIC, maxlag=19) |                       |                        |        |  |  |
|---|-----------------------|------------------------|--------|--|--|
|   |                       | t-Statistic            | Prob.* |  |  |
| Augmented Dickey-Fu<br>Test critical values:  | 1% level              | -0.733304<br>-2.568242 | 0.3988 |  |  |
|   | 5% level<br>10% level | -1.941272<br>-1.616398 |        |  |  |

1aiii) Similarly, Results show that t-stat is -3.29265 which has significance of 0.0683. This more than 0.05 hence there is no evidence to reject the null hypothesis that "COPPER" has unit root ( $\gamma$ =0). Hence it is also non-stationary.

| Null Hypothesis: COPPER has a unit root<br>Exogenous: Constant, Linear Trend<br>Lag Length: 1 (Automatic - based on SIC, maxlag=19) |  |  |        |  |  |
|---|--|--|--------|--|--|
|   |  | t-Statistic                                      | Prob.* |  |  |
| Augmented Dickey-Ful<br>Test critical values:   | ller test statistic<br>1% level<br>5% level<br>10% level | -3.292650<br>-3.971104<br>-3.416195<br>-3.130392 | 0.0683 |  |  |
|   |  |  |        |  |  |

# 1aiv) Only 1 lag term is significant.

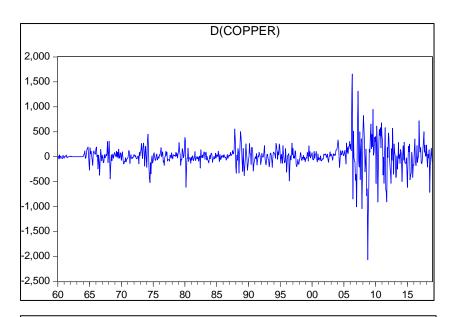
| Exogenous: None<br>Lag Length: 1 (Fixed)  |  |  |  |  |
|---|--|--|--|--|
|   |  |  | t-Statistic  | Prob.*   |
| Augmented Dickey-Ful  | ler test statistic   |  | -0.733304  | 0.3988   |
| Test critical values:   | 1% level   |  | -2.568242  |  |
|   | 5% level   |  | -1.941272  |  |
|   | 10% level  |  | -1.616398  |  |
| *MacKinnon (1996) on  | e-sided p-value  | S.   |  |  |
| Augmented Dickey-Ful<br>Dependent Variable: D<br>Method: Least Squares  | (COPPER)   | on   |  |  |
| Dependent Variable: D   | (COPPER)<br>19:58<br>60M03 2018M1  | 2  | t-Statistic  | Prob.  |
| Dependent Variable: D<br>Method: Least Squares<br>Date: 02/13/19 Time:<br>Sample (adjusted): 196<br>Included observations:<br>Variable  | (COPPER)<br>19:58<br>60M03 2018M1<br>706 after adjus   | 2<br>tments<br>Std. Error  |  |  |
| Dependent Variable: D<br>Method: Least Squares<br>Date: 02/13/19 Time:<br>Sample (adjusted): 196<br>Included observations:  | (COPPER)<br>19:58<br>60M03 2018M1<br>706 after adjus   | 2<br>tments  | t-Statistic<br>-0.733304<br>9.439353                     | Prob.<br>0.4636<br>0.0000                            |
| Dependent Variable: D Method: Least Squares Date: 02/13/19 Time: Sample (adjusted): 196 Included observations:  Variable  COPPER(-1)  | (COPPER)<br>5<br>19:58<br>50M03 2018M1<br>706 after adjus<br>Coefficient<br>-0.001762  | 2<br>tments<br>Std. Error<br>0.002403  | -0.733304<br>9.439353                                    | 0.4636   |
| Dependent Variable: D Method: Least Squares Date: 02/13/19 Time: Sample (adjusted): 196 Included observations:  Variable  COPPER(-1) D(COPPER(-1))  R-squared Adjusted R-squared                    | (COPPER)<br>19:58<br>60M03 2018M1<br>706 after adjus<br>Coefficient<br>-0.001762<br>0.335927<br>0.111507<br>0.110245             | 2<br>tments<br>Std. Error<br>0.002403<br>0.035588<br>Mean depend<br>S.D. dependo                 | -0.733304<br>9.439353<br>dent var<br>ent var             | 0.4636<br>0.0000<br>7.573839<br>243.9988             |
| Dependent Variable: D Method: Least Squares Date: 02/13/19 Time: Sample (adjusted): 196 Included observations:  Variable  COPPER(-1) D(COPPER(-1))  R-squared Adjusted R-squared S.E. of regression | (COPPER)<br>19:58<br>50M03 2018M1<br>706 after adjus<br>Coefficient<br>-0.001762<br>0.335927<br>0.111507<br>0.110245<br>230.1563 | 2<br>tments<br>Std. Error<br>0.002403<br>0.035588<br>Mean depend<br>S.D. depend<br>Akaike info c | -0.733304<br>9.439353<br>dent var<br>ent var<br>riterion | 0.4636<br>0.0000<br>7.573839<br>243.9988<br>13.71822 |
| Dependent Variable: D Method: Least Squares Date: 02/13/19 Time: Sample (adjusted): 196 Included observations:  Variable  COPPER(-1) D(COPPER(-1))  R-squared Adjusted R-squared                    | (COPPER)<br>19:58<br>60M03 2018M1<br>706 after adjus<br>Coefficient<br>-0.001762<br>0.335927<br>0.111507<br>0.110245             | 2<br>tments<br>Std. Error<br>0.002403<br>0.035588<br>Mean depend<br>S.D. dependo                 | -0.733304<br>9.439353<br>dent var<br>ent var<br>riterion | 0.4636<br>0.0000<br>7.573839<br>243.9988             |

Date: 02/13/19 Time: 20:04 Sample: 1960M01 2018M12 Included observations: 706

| Autocorrelation | Partial Correlation | AC        | PAC    | Q-Stat | Prob  |
|-----------------|---------------------|-----------|--------|--------|-------|
| 1 1             |                     | 1 0.016   | 0.016  | 0.1745 | 0.676 |
| ı <b>l</b> ı    | ı <b>l</b> ı        | 2 -0.040  | -0.040 | 1.3001 | 0.522 |
| ı <b>l</b> ı    | 101                 | 3 -0.034  | -0.033 | 2.1310 | 0.546 |
| ı <b>l</b> ı    | <b>II</b> 1         | 4 -0.042  | -0.042 | 3.3627 | 0.499 |
| ı <b>İ</b> D    |                     | 5 0.056   | 0.055  | 5.5948 | 0.348 |
| <b>[</b> ]      |                     | 6 -0.066  | -0.072 | 8.6803 | 0.192 |
|                 | <u> </u>            | 7 -0.014  | -0.010 | 8.8265 | 0.265 |
| <u> </u>        | l l                 | 8 -0.185  | -0.190 | 33.231 | 0.000 |
| ı <b>Q</b> ı    | 101                 | 9 -0.045  | -0.041 | 34.660 | 0.000 |
| 1 1             | 101                 | 10 0.003  | -0.025 | 34.667 | 0.000 |
| ı <b>İ</b>      |                     | 11 0.171  | 0.171  | 55.738 | 0.000 |
| 1 <b>þ</b> i    | 1 🖟                 | 12 0.061  | 0.035  | 58.440 | 0.000 |
| <b>Q</b> '      | <u> </u>            | 13 -0.115 | -0.091 | 67.902 | 0.000 |
| 11              | 111                 | 14 -0.015 | -0.032 | 68.058 | 0.000 |
| 1 1             | 1 1                 | 15 0.002  | 0.001  | 68.060 | 0.000 |
| ı <b>l</b> l    | <b>Q</b> +          | 16 -0.005 | -0.063 | 68.079 | 0.000 |
| ı <b>D</b> i    | I                   | 17 0.042  | 0.044  | 69.347 | 0.000 |
| ı <b>l</b> ı    | <b> </b>            | 18 -0.031 | -0.022 | 70.066 | 0.000 |
| <b>4</b> '      | 1 1                 | 19 -0.065 |        | 73.118 | 0.000 |
| 111             | 1 1                 | 20 -0.012 | 0.008  | 73.229 | 0.000 |
| ' <b>[</b> ]    |                     | 21 0.070  | 0.049  | 76.852 | 0.000 |
| I <b>I</b> II   |                     | 22 0.052  |        | 78.835 | 0.000 |
| ! <b>∄</b> !    | I                   | 23 0.046  | 0.040  | 80.400 | 0.000 |
| <b>q</b> ·      | <b> </b>            | 24 -0.058 |        | 82.905 | 0.000 |
| I <b>l</b> I    | 1 1                 | 25 -0.019 | 0.013  | 83.180 | 0.000 |
| <b>1</b>        | <u> </u>            | 26 -0.047 |        | 84.831 | 0.000 |
| <b>'∐</b> '     | 111                 |           | -0.031 | 85.667 | 0.000 |
| <u> </u>        | <b>9</b> 1          | 28 -0.039 |        | 86.797 | 0.000 |
| <b>"</b>   '    | '[['                | 29 -0.050 |        | 88.614 | 0.000 |
| <u> </u>        | <u> </u>            | 30 0.026  | 0.049  | 89.129 | 0.000 |
| <u> </u>        | <u> </u>            |           | -0.078 | 95.057 | 0.000 |
| 1 1             | <b> </b>            | i         | -0.047 | 95.104 | 0.000 |
| 1               | 11                  | i e       | -0.015 | 95.225 | 0.000 |
| t <b>∦</b> t    | <b>4</b>            | 34 -0.021 | -0.066 | 95.551 | 0.000 |
| ( <b>1</b> 1    |                     | 35 0.039  | 0.026  | 96.706 | 0.000 |
| ı <b>D</b> ı    |                     | 36 0.056  | 0.065  | 99.007 | 0.000 |

Test shows that the residuals in the above model are not correlated (see above). Hence the model with one lag satisfies the residual assumptions. The augmented dickey fuller test indicates that this series is not stationary.

1av)



Date: 02/13/19 Time: 20:17 Sample: 1960M01 2018M12 Included observations: 707

| Autocorrelation | Partial Correlation |    | AC     | PAC    | Q-Stat | Prob |
|-----------------|---------------------|----|--------|--------|--------|------|
| -               |                     | 1  | 0.333  | 0.333  | 78.954 | 0.00 |
| ı İ <u>l</u> ı  | <b>i</b>            | 2  |        | -0.055 | 81.743 | 0.00 |
| 1 <b>[</b> ]    | 111                 | 3  | -0.020 |        | 82.020 | 0.00 |
| ı <b>l</b> i    | 111                 | 4  | -0.037 | -0.021 | 82.987 | 0.00 |
| 1 1             | 1 1                 | 5  | 0.009  | 0.033  | 83.043 | 0.00 |
| <b>[</b>        |                     | 6  | -0.081 | -0.107 | 87.696 | 0.00 |
| □ ı             | <b>I</b>            | 7  | -0.098 | -0.045 | 94.588 | 0.00 |
| <u> </u>        |                     | 8  | -0.205 | -0.176 | 124.70 | 0.00 |
| <b>[</b>        | 1 <b>1</b> 1        | 9  | -0.090 | 0.037  | 130.57 | 0.00 |
| ı <b>İ</b> I    | 1 <b>0</b> 1        | 10 | 0.025  | 0.041  | 131.02 | 0.00 |
| ı <b>İ</b>      |                     | 11 | 0.166  | 0.160  | 150.89 | 0.00 |
| ı <b>İ</b> D    | <b>(</b>            | 12 | 0.074  | -0.058 | 154.87 | 0.00 |
| <b>□</b> i      | <b></b>             | 13 | -0.082 | -0.104 | 159.68 | 0.00 |
| ıııı            | 1 1                 | 14 | -0.040 | -0.004 | 160.86 | 0.00 |
| ı <b>l</b> ı    | 1 1                 | 15 | -0.012 | -0.004 | 160.96 | 0.00 |
| ı İı            | <b>1</b>            | 16 | -0.002 | -0.046 | 160.96 | 0.00 |
| 1 1             | 1 <b>0</b> 1        | 17 | 0.021  | 0.053  | 161.29 | 0.00 |
| ıııı            | ı                   | 18 | -0.039 | -0.037 | 162.37 | 0.00 |
| <b>(</b>        | T I                 | 19 | -0.066 | 0.001  | 165.51 | 0.00 |
| ı <b>l</b> ı    | ı <b>j</b> ı        | 20 | -0.007 | 0.026  | 165.54 | 0.00 |
| ı <b>İ</b> II   | <b> </b>            | 21 | 0.078  | 0.041  | 169.93 | 0.00 |
| ı <b>İ</b> II   | 111                 | 22 | 0.078  | -0.015 | 174.42 | 0.00 |
| ı <b>İ</b> li   | T I                 | 23 | 0.045  | 0.022  | 175.94 | 0.00 |
| ı <b>l</b> ı    | <b>(</b>            | 24 | -0.049 | -0.058 | 177.73 | 0.00 |
| ı <b>l</b> ı    | 1 1                 | 25 | -0.054 | -0.004 | 179.85 | 0.00 |
| <b>□</b> i      |                     | 26 | -0.076 | -0.092 | 184.05 | 0.00 |
| <b>(</b>        | 111                 | 27 | -0.073 | -0.024 | 187.94 | 0.00 |
|                 | <b>i</b>            | 28 | -0.075 | -0.057 | 192.07 | 0.00 |
| <b>4</b>        | 1 1                 | 29 | -0.071 | 0.007  | 195.75 | 0.00 |
| ı <b>l</b> ı    | ı <b>l</b> ı        | 30 | -0.026 | 0.021  | 196.25 | 0.00 |
| <b>.</b>        |                     | 31 | -0.085 | -0.104 | 201.62 | 0.00 |
| 1 <b>1</b> 1    | l l                 | 32 | -0.018 | -0.027 | 201.87 | 0.00 |
| 1 1             | TI I                | 33 | 0.004  | -0.014 | 201.88 | 0.00 |
| 1 1             | ı <b>d</b> ı        | 34 | 0.000  | -0.040 | 201.88 | 0.00 |
| ı <b>İ</b> D    |                     | 35 | 0.051  | 0.061  | 203.82 | 0.00 |
| , <b>j</b> ju   | I                   | 36 | 0.064  | 0.042  | 206.93 | 0.00 |

Null Hypothesis: D(COPPER) has a unit root

Exogenous: None

Lag Length: 0 (Automatic - based on SIC, maxlag=19)

|  |   | t-Statistic                                      | Prob.* |
|--|---|--|--------|
| Augmented Dickey-Fu<br>Test critical values: | ıller test statistic<br>1% level<br>5% level<br>10% level | -18.75198<br>-2.568242<br>-1.941272<br>-1.616398 | 0.0000 |

<sup>\*</sup>MacKinnon (1996) one-sided p-values.

Augmented Dickey-Fuller Test Equation Dependent Variable: D(COPPER,2)

Method: Least Squares Date: 02/13/19 Time: 20:17

Sample (adjusted): 1960M03 2018M12 Included observations: 706 after adjustments

| Variable   | Coefficient   | Std. Error  | t-Statistic                  | Prob.   |
|--|---|---|------------------------------|---|
| D(COPPER(-1))  | -0.665749   | 0.035503  | -18.75198                    | 0.0000  |
| R-squared<br>Adjusted R-squared<br>S.E. of regression<br>Sum squared resid<br>Log likelihood<br>Durbin-Watson stat | 0.332788<br>0.332788<br>230.0808<br>37320724<br>-4840.802<br>1.963378 | Mean depend<br>S.D. depende<br>Akaike info co<br>Schwarz crite<br>Hannan-Quir | ent var<br>riterion<br>erion | -0.188938<br>281.6753<br>13.71615<br>13.72261<br>13.71865 |

Results suggest that the D(copper) series is stationary.

- The graph of D(copper) shows no patterns.
- The correlogram shows that auto correlation of residuals tend to 0
- The augmented dickey-fuller test shows that the T-Stat is significant and that the null hypothesis can be rejected which suggest that the series is stationary.

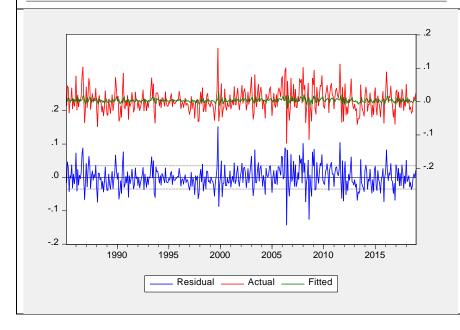
1b)

MA(1) – based on result below, model seems reasonable

Dependent Variable: DLOG(GOLD)
Method: ARMA Maximum Likelihood (OPG - BHHH)
Date: 02/13/19 Time: 19:56
Sample: 1985M02 2018M12
Included observations: 407
Convergence achieved after 16 iterations
Coefficient covariance computed using outer product of gradients

| Variable   | Coefficient  | Std. Error  | t-Statistic                      | Prob.   |
|--|--|---|----------------------------------|---|
| C<br>MA(1)<br>SIGMASQ  | 0.003484<br>0.167650<br>0.001196   | 0.002086<br>0.040449<br>6.34E-05  | 1.670293<br>4.144712<br>18.84932 | 0.0956<br>0.0000<br>0.0000  |
| R-squared<br>Adjusted R-squared<br>S.E. of regression<br>Sum squared resid<br>Log likelihood<br>F-statistic<br>Prob(F-statistic) | 0.022957<br>0.018120<br>0.034710<br>0.486726<br>791.8023<br>4.746237<br>0.009174 | Mean dependent var S.D. dependent var Akaike info criterion Schwarz criterion Hannan-Quinn criter. Durbin-Watson stat |                                  | 0.003484<br>0.035029<br>-3.876179<br>-3.846630<br>-3.864485<br>2.026107 |
| Inverted MA Roots  | 17   |   |                                  |   |

Both the coefficient is significant

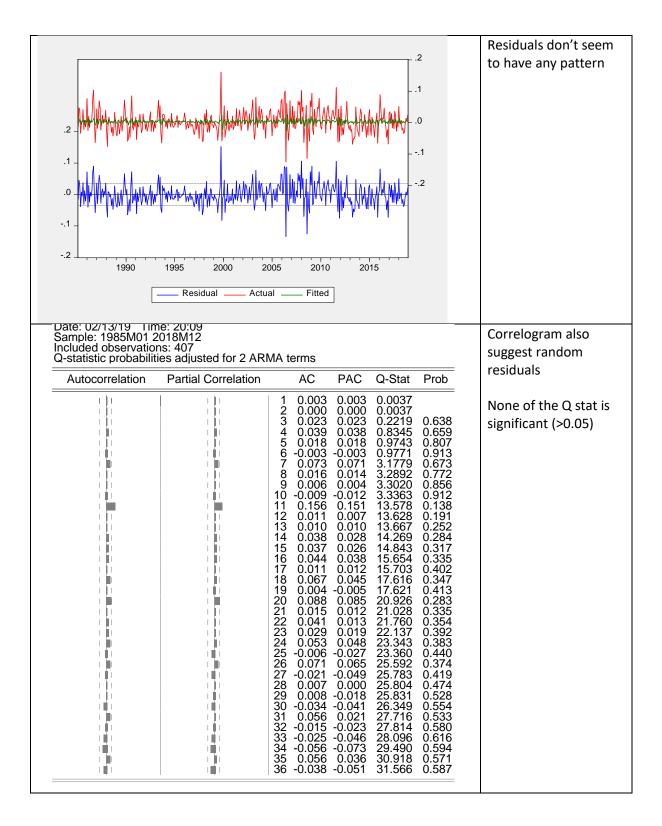


Residuals don't seem to have any pattern

Date: 02/13/19 Time: 19:58 Sample: 1985M01 2018M12 Included observations: 407 Q-statistic probabilities adjusted for 1 ARMA term Correlogram also suggest random residuals Autocorrelation Partial Correlation PAC Q-Stat Prob -0.014 -0.083 0.006 0.044 0.012 -0.009 -0.014 -0.084 0.004 0.037 0.015 -0.002 0.073 0.013 -0.002 0.0774 2.9417 2.9572 3.7588 3.8229 3.8558 5.9516 6.0305 6.0384 123456789 10 None of the Q stat is 0.086 0.228 0.289 0.431 0.570 0.429 0.536 significant (>0.05) -0.002 -0.013 0.150 0.005 0.020 0.028 0.025 6.0964 6.1854 16.262 16.277 16.296 16.689 17.181 -0.014 0.155 0.006 112341516178921223425678931333456 0.131 0.014 0.042 -0.006 17.723 19.070 19.071 21.741 21.778 22.175 22.446 23.295 23.332 25.267 25.478 25.483 25.483 25.491 25.989 27.526 0.004 0.056 -0.001 0.079 0.009 0.030 0.025 0.044 -0.009 -0.006 0.087 0.011 0.016 0.021 0.045 -0.021 0.434 0.444 0.500 0.007 -0.022 0.003 0.004 -0.034 0.059 -0.047 0.007 -0.022 -0.040 0.024 0.601 0.626 0.596 27.526 27.565 28.030 29.253 31.144 31.638 0.668 0.654 0.608 Ė 0.631

#### ARMA(2, 0): based on result below, model seems reasonable

| Dependent Variable: L<br>Method: ARMA Maxim<br>Date: 02/13/19 Time:<br>Sample: 1985M02 201<br>Included observations:<br>Convergence achieved<br>Coefficient covariance | All coefficients are significant   |  |   |   |  |
|--|--|--|---|---|--|
| Variable   | Coefficient  | Std. Error   | t-Statistic                                   | Prob.   |  |
| C<br>AR(1)<br>AR(2)<br>SIGMASQ   | 0.003473<br>0.150628<br>-0.105918<br>0.001188                                    | 0.001897<br>0.039910<br>0.043571<br>6.36E-05   | 1.830899<br>3.774163<br>-2.430929<br>18.67461 | 0.0679<br>0.0002<br>0.0155<br>0.0000                                    |  |
| R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood F-statistic Prob(F-statistic)   | 0.029621<br>0.022398<br>0.034634<br>0.483406<br>793.1888<br>4.100590<br>0.006942 | Mean depend<br>S.D. dependd<br>Akaike info c<br>Schwarz crite<br>Hannan-Quir<br>Durbin-Watsd | ent var<br>riterion<br>erion<br>nn criter.    | 0.003484<br>0.035029<br>-3.878078<br>-3.838679<br>-3.862486<br>1.992539 |  |
| Inverted AR Roots  | .08+.32i   | .0832i   |   |   |  |

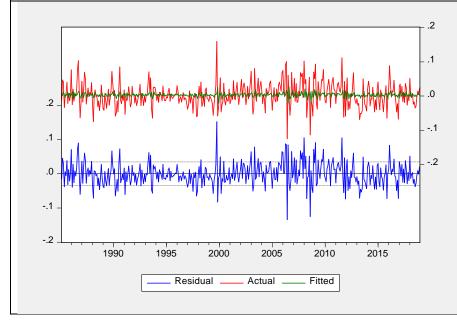


ARMA(0, 2): based on result below, model MA(2) is not significant which suggest that it can be dropped from the model, and hence this model should not be used

Dependent Variable: DLOG(GOLD)
Method: ARMA Maximum Likelihood (OPG - BHHH)
Date: 02/13/19 Time: 20:10
Sample: 1985M02 2018M12
Included observations: 407
Convergence achieved after 16 iterations
Coefficient covariance computed using outer product of gradients

| Variable   | Coefficient  | Std. Error   | t-Statistic                                   | Prob.   |
|--|--|--|---|---|
| C<br>MA(1)<br>MA(2)<br>SIGMASQ   | 0.003479<br>0.151899<br>-0.079066<br>0.001188                                    | 0.001948<br>0.040588<br>0.043340<br>6.36E-05   | 1.786143<br>3.742491<br>-1.824306<br>18.67115 | 0.0748<br>0.0002<br>0.0688<br>0.0000                                    |
| R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood F-statistic Prob(F-statistic) | 0.029432<br>0.022207<br>0.034637<br>0.483500<br>793.1497<br>4.073607<br>0.007200 | Mean dependent var<br>S.D. dependent var<br>Akaike info criterion<br>Schwarz criterion<br>Hannan-Quinn criter.<br>Durbin-Watson stat |   | 0.003484<br>0.035029<br>-3.877886<br>-3.838487<br>-3.862294<br>1.996835 |
| Inverted MA Roots  | .22  | 37   |   |   |

All coefficients are significant except MA(2) which has pvalue more than 0.05

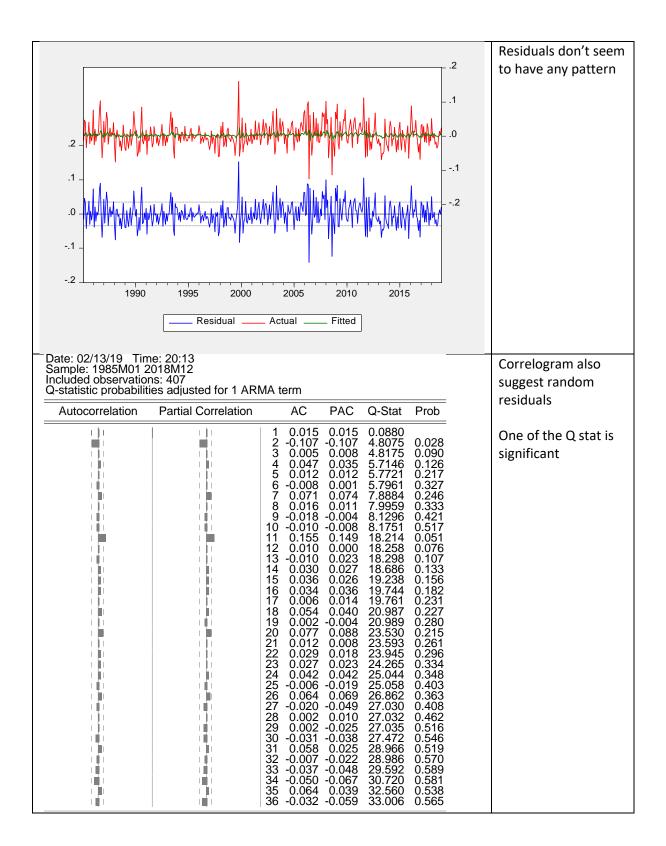


Residuals don't seem to have any pattern

Date: 02/13/19 Time: 20:12 Sample: 1985M01 2018M12 Included observations: 407 Q-statistic probabilities adjusted for 2 ARMA terms Correlogram also suggest random residuals Autocorrelation **Partial Correlation** PAC Q-Stat Prob 0.001 -0.004 -0.004 0.0003 0.001 123456789 None of the Q stat is -0.004 -0.004 0.0086 0.0164 0.898 significant (>0.05) ПÌП 10.1 0.654 0.806 0.912 0.670 0.777 0.045 0.045 ju 0.9810 0.9850 3.1919 3.2502 3.2594 0.018 0.018 -0.003 -0.003 0.073 0.074 0.012 0.010 0.073 0.012 0.005 þ п 0.004 0.860 -0.011 0.150 0.006 0.010 0.032 3.3135 13.484 13.525 13.552 14.023 -0.011 0.156 0.010 0.008 0.033 0.196 0.259 0.299 0.335 0.353 0.423 0.370 0.438 0.306 0.362 14.023 14.565 15.380 15.402 17.242 17.243 0.036 0.024 0.024 0.039 0.011 0.045 -0.005 0.085 0.044 0.044 0.007 0.066 0.001 0.087 0.012 0.042 0.025 0.053 20.496 20.557 21.311 21.578 22.838 22.834 25.001 25.193 25.207 25.222 25.698 27.155 27.276 27.531 28.937 30.460 b 0.011 0.042 0.014 0.025 0.019 0.053 0.048 -0.008 -0.026 0.070 0.066 0.424 0.413 ji i 0.471 ш b -0.021 -0.0460.452 0.006 -0.001 0.006 -0.016 -0.033 -0.042 0.057 0.023 0.507 0.562 0.590 ш 0.563 -0.016 -0.025 33 34 35 36 -0.024 -0.046 -0.056 -0.070 0.058 0.036 0.645 0.622 0.594 -0.038 -0.053 31.108 ſ 0.610

#### ARMA(1, 0): based on result below, residuals may not be stationary, hence not a good model

Dependent Variable: DLOG(GOLD)
Method: ARMA Maximum Likelihood (OPG - BHHH)
Date: 02/13/19 Time: 20:12
Sample: 1985M02 2018M12 All coefficients are significant Included observations: 407 Convergence achieved after 11 iterations Coefficient covariance computed using outer product of gradients Variable Coefficient Std. Error t-Statistic Prob. 0.003486 0.136010 0.001201 0.002101 0.039860 6.43E-05 1.659647 0.0978 AR(1) SIGMASQ 3.412218 18.67665 0.0007 0.0000 R-squared Adjusted R-squared 0.018565 0.013706 0.034788 0.003484 Mean dependent var S.D. dependent var 0.035029 Akaike info criterion Schwarz criterion Hannan-Quinn criter. Durbin-Watson stat -3.871717 -3.842168 -3.860024 S.É. of regression Sum squared resid 0.488914 Log likelihood F-statistic Prob(F-statistic) 790.8945 3.820989 1.969347 0.022702 Inverted AR Roots .14

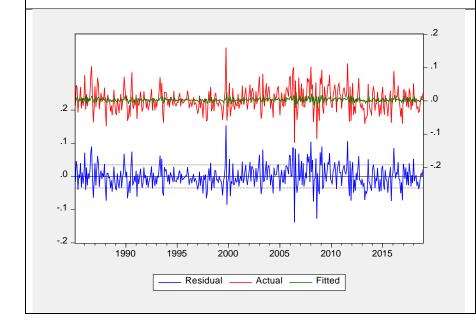


ARMA(1, 1): based on result below, AR(1) is not significant, which suggest that it can be dropped from the model, and hence this model should not be used

Dependent Variable: DLOG(GOLD)
Method: ARMA Maximum Likelihood (OPG - BHHH)
Date: 02/13/19 Time: 20:13
Sample: 1985M02 2018M12
Included observations: 407
Convergence achieved after 14 iterations
Coefficient covariance computed using outer product of gradients

| Variable   | Coefficient  | Std. Error   | t-Statistic                                   | Prob.   |
|--|--|--|---|---|
| C<br>AR(1)<br>MA(1)<br>SIGMASQ   | 0.003484<br>-0.330921<br>0.490279<br>0.001190                                    | 0.002013<br>0.215195<br>0.203645<br>6.33E-05   | 1.731338<br>-1.537772<br>2.407521<br>18.80114 | 0.0842<br>0.1249<br>0.0165<br>0.0000                                    |
| R-squared Adjusted R-squared S.E. of regression Sum squared resid Log likelihood F-statistic Prob(F-statistic) | 0.027818<br>0.020581<br>0.034666<br>0.484304<br>792.8132<br>3.843834<br>0.009822 | Mean dependent var<br>S.D. dependent var<br>Akaike info criterion<br>Schwarz criterion<br>Hannan-Quinn criter.<br>Durbin-Watson stat |   | 0.003484<br>0.035029<br>-3.876232<br>-3.836833<br>-3.860640<br>2.011501 |
| Inverted AR Roots<br>Inverted MA Roots   | 33<br>49   |  |   |   |

Not all coefficients are significant, AR(1) is not significant



Residuals don't seem to have any pattern

| luded observations: 407 statistic probabilities adjusted for 2 ARMA terms |                     |   |  |  |   |  | suggest random residuals          |  |
|---|---------------------|---|--|--|---|--|-----------------------------------|--|
| Autocorrelation   | Partial Correlation | AC  | PAC  | Q-Stat   | Prob  |  |                                   |  |
|   |                     | 1 -0.00<br>2 -0.03<br>3 -0.01<br>4 0.05<br>5 0.01<br>6 -0.00<br>7 0.07<br>8 0.01<br>10 -0.01<br>11 0.15<br>12 0.00<br>13 0.00<br>14 0.03<br>15 0.03<br>16 0.04<br>17 0.00<br>20 0.08<br>21 0.00<br>22 0.03<br>23 0.02<br>24 0.05<br>25 -0.00<br>26 0.06<br>27 -0.02<br>28 0.00<br>29 0.00<br>30 -0.03<br>31 -0.02<br>33 -0.02<br>34 -0.05<br>35 -0.03 | 3 -0.019<br>1 0.049<br>3 0.012<br>4 -0.001<br>2 0.075<br>0 0.009<br>1 -0.002<br>4 -0.010<br>5 0.149<br>6 0.012<br>2 0.034<br>6 0.022<br>1 0.040<br>1 -0.005<br>4 0.086<br>8 0.011<br>1 -0.048<br>9 0.041<br>1 -0.048<br>9 0.044<br>1 -0.016<br>2 0.044<br>1 -0.016<br>9 0.045<br>1 -0.045<br>1 -0.045<br>6 -0.046<br>9 0.037 | 0.0171<br>0.4172<br>0.5559<br>1.6855<br>1.6898<br>3.8780<br>3.8789<br>14.056<br>14.083<br>14.056<br>14.083<br>15.691<br>17.336<br>20.396<br>20.425<br>21.084<br>21.286<br>22.416<br>22.453<br>24.708<br>24.716<br>24.724<br>25.186<br>24.724<br>25.186<br>24.724<br>25.186<br>26.822<br>27.117<br>28.481<br>20.396 | 0.456<br>0.446<br>0.793<br>0.573<br>0.693<br>0.7861<br>0.120<br>0.169<br>0.228<br>0.333<br>0.432<br>0.333<br>0.432<br>0.3411<br>0.369<br>0.4435<br>0.4435<br>0.4435<br>0.4435<br>0.590<br>0.626 |  | None of the Q stat is significant |  |

Based on above, only the first 2 out of these 5 models are compared

- ARMA(0,1)
- ARMA(2,0)

The RSS, SBC, AIC and HQ of this 2 models are very close. Hence propse to use the model with less parameters, i.e. ARMA(0,1) because it is more parsimonous.

1bv) Forecasting

Dependent Variable: DLOG(GOLD)

Method: ARMA Generalized Least Squares (Gauss-Newton)

Date: 02/13/19 Time: 20:29 Sample: 1985M02 2018M12 Included observations: 407

Convergence achieved after 7 iterations

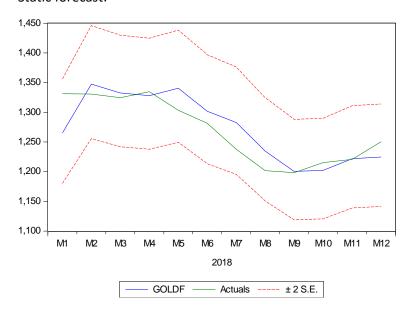
Coefficient covariance computed using outer product of gradients

d.f. adjustment for standard errors & covariance

| Variable                             | Coefficient          | Std. Error           | t-Statistic            | Prob.            |
|--------------------------------------|----------------------|----------------------|------------------------|------------------|
| C<br>MA(1)                           | 0.003484<br>0.168141 | 0.002007<br>0.049007 | 1.736294<br>3.430960   | 0.0833<br>0.0007 |
| R-squared                            | 0.022957             | Mean dependent var   |                        | 0.003484         |
| Adjusted R-squared                   | 0.020545             | S.D. depende         | 0.035029               |                  |
| S.E. of regression Sum squared resid | 0.034667<br>0.486726 | Akaike info c        | -3.881092<br>-3.861393 |                  |
| Log likelihood                       | 791.8023             | Hannan-Quinn criter. |                        | -3.873297        |
| F-statistic                          | 9.516057             | Durbin-Watson stat   |                        | 2.027007         |
| Prob(F-statistic)                    | 0.002176             |                      |                        |                  |
| Inverted MA Roots                    | 17                   |                      |                        |                  |

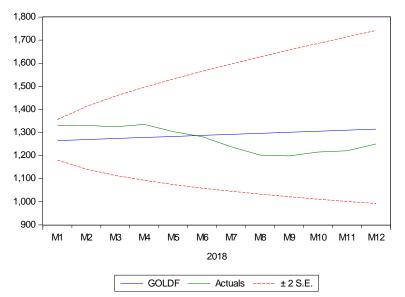
## Diagnostic looks reasonable

## Static forecast:



Forecast: GOLDF Actual: GOLD Forecast sample: 2018M01 2018M12 Included observations: 12 Root Mean Squared Error 29.58882 Mean Absolute Error 22.91981 Mean Abs. Percent Error 1.795537 Theil Inequality Coef. 0.011627 Bias Proportion 0.020820 Variance Proportion 0.002435 Covariance Proportion 0.976745 Theil U2 Coefficient 0.998494 Symmetric MAPE 1.794831

## Dynamic Forecast:

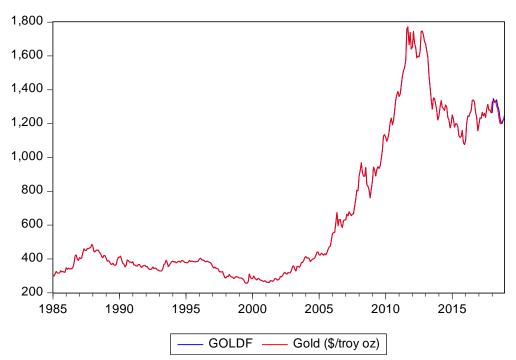


Forecast: GOLDF
Actual: GOLD
Forecast sample: 2018M01 2018M12
Included observations: 12
Root Mean Squared Error 68.85195
Mean Absolute Error 62.95120
Mean Abs. Percent Error 5.024407
Theil Inequality Coef. 0.026895
Bias Proportion 0.087829

Variance Proportion 0.281625 Covariance Proportion 0.630546 Theil U2 Coefficient 3.025021 Symmetric MAPE 4.942829

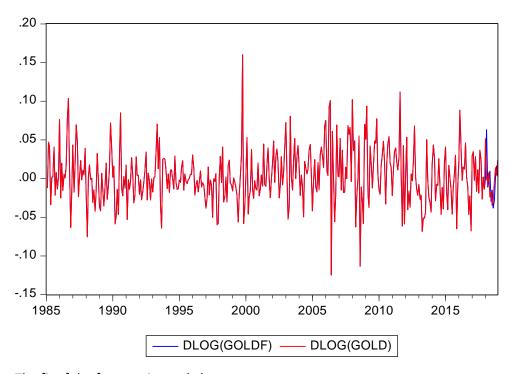
Static forecasts are better.

## Plot of goldf and gold



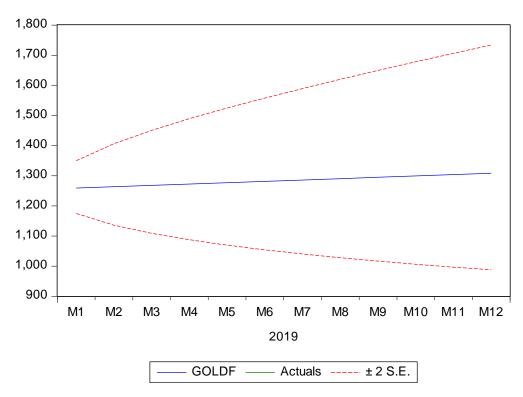
The fit of the forecast is good.

Plot of dlog(goldf) and dlog(gold)



The fit of the forecast is good also.

The gold price is expected to go up as the e(t-1) is positive and the coefficient is positive, the price is expected to be positive.



We cannot use static as there is no actual data. Dynamic forecast will take previously forecasted values while static forecast will take actual values to make next step forecast.