

Exercise 3.4.1 Let $R(A, B, C, D, E)$ be decomposed into relations with the following three sets of attributes: $\{A, B, C\}$, $\{B, C, D\}$, $\{A, C, E\}$. For each of the following sets of FD's, use the chase test to tell whether the decomposition of R is lossless. For those that are not lossless, give an example of an instance of R that returns more than R when projected onto the decomposed relations and rejoined.

- a) $B \rightarrow E, CE \rightarrow A$
- b) $AC \rightarrow E, BC \rightarrow D$
- c) $A \rightarrow D, D \rightarrow E, B \rightarrow D$
- d) $A \rightarrow D, CD \rightarrow E, E \rightarrow D$.

Exercise 3.4.2. For each of the sets of FD's in Exercise 3.4.1, are dependencies preserved by the decomposition?