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Roman numbers refer to chapters; Arabic numbers to sections within the chapter; *prob.* to problems appearing at the end of the chapter.

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