

Seminar Report

Semi-Supervised Locally Linear Embedding

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Abstract

- Why is dimensionality reduction desirable? Not only because it's easier to handle and visualize lower-dimensional data but because data-generating process is often truly of much lower dimension
- Our goal is to find the mapping from latent feature space embedded in the m -dimensional Euclidean space we observe to the d -dimensional space the embedding is locally homeomorphic to (unrolling the Swiss roll)
- This mapping can be constructed linearly or non-linearly (slapping the roll flat vs unrolling it), thereby defining the complexity of the manifolds we are able to learn
- Give brief intuition to manifold learning: what do we mean by topologies, manifolds, maps, charts?
- What methods are already out there?

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1 Introduction

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2 Theoretical Framework

2.1 Basic Concepts in Manifold Learning

AS BRIEF AS POSSIBLE, but concepts and corresponding notation should be introduced properly

2.1.1 “Mathematical Objects” (find proper title)

- Topologies
- Manifolds
- Tangent spaces

2.1.2 Spectral Decomposition

- Eigenvalues/eigenvectors
- Spectral decomposition

2.1.3 Evaluation of Manifold Learning

- How can we evaluate manifold learning?
- No details, but some foundation to base evaluation of experiments on

2.2 Neighborhoods and Basics of Spectral Graph Theory

- Neighborhoods and neighborhood graphs
- Linear reconstruction and reconstruction error
- Degree and adjacency matrices

2.3 Laplacian Eigenmaps

- Laplacian-Beltrami operator
- Laplacian eigenmaps

Can be interpreted as framework for both LLE and HLLE; only to the extent where it helps to frame LLE

3 Locally Linear Embedding (LLE)

3.1 Original LLE Algorithm

3.2 Strengths and Drawbacks

3.3 Extensions to LLE

- Brief explanation of Hessian LLE
- Brief motivation of SS-LLE

4 Semi-Supervised Locally Linear Embedding (SS-LLE)

4.1 Employment of Prior Information

- Why use labels in the first place?
- How will that help?

4.2 SS-LLE Algorithm

- What is different wrt standard LLE?

4.3 Choice of Prior Points

- How can we find prior points (if not by domain knowledge)?
- How many are considered necessary to yield tangible benefits?

5 Experiment Results

5.1 Data

5.2 Experimental Design

5.3 Results and Discussion

6 Conclusion

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A Appendix

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B Electronic Appendix

Data, code and figures are provided in electronic form.

Declaration of Authorship

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