

Semi-Supervised Locally Linear Embedding (SSLLE)

Application & Sensitivity Analysis of Critical Hyperparameters



0 AGENDA

- 1 Problem
- 2 Local graph-based manifold learning (LGML)
- 3 Techniques
 - 1 Unsupervised
 - 2 Semi-supervised
 - 3 Challenges
- 4 Sensitivity analysis
 - 1 Setup
 - 2 Results
- 5 Discussion

SSLLE

1 PROBLEM MANIFOLD LEARNING

Situation. Rapidly increasing amount of data thanks to novel applications and data sources

Problem. High data dimensionality detrimental to

- Model functionality
- Interpretability
- Generalization ability

Manifold assumption. Data in high-dimensional observation space truly sampled from low-dimensional manifold

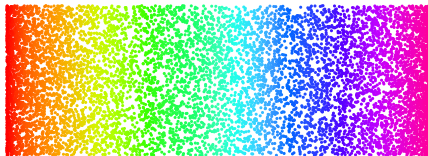


How to find a meaningful, structure-preserving embedding?

1 PROBLEM MANIFOLD LEARNING

Formal goal of manifold learning.

- **Given.** Data $\mathcal{X} = (\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_N)$, with $\mathbf{x}_i \in \mathbb{R}^D \forall i \in \{1, 2, \dots, N\}$ and $N, D \in \mathbb{N}$, supposedly lying on d -dimensional manifold \mathcal{M}
- ⇒ $\psi : \mathcal{M} \rightarrow \mathbb{R}^d$ with $d \ll D, d \in \mathbb{N}$
- ⇒ $\mathcal{X} \sim \mathcal{M} \subset \mathbb{R}^D$
- **Goal.** Find d -dimensional Euclidean representation
- ⇒ $\mathcal{Y} = (\mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_N)$, with $\mathbf{y}_i = \psi(\mathbf{x}_i) \in \mathbb{R}^d \forall i \in \{1, 2, \dots, N\}$.

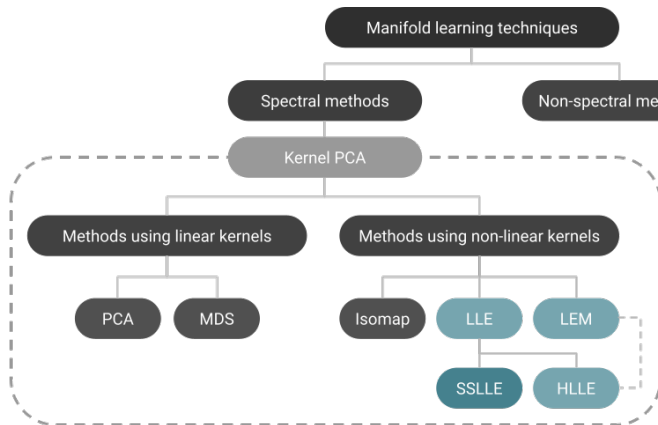


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2 LGML

2 LGML TAXONOMY

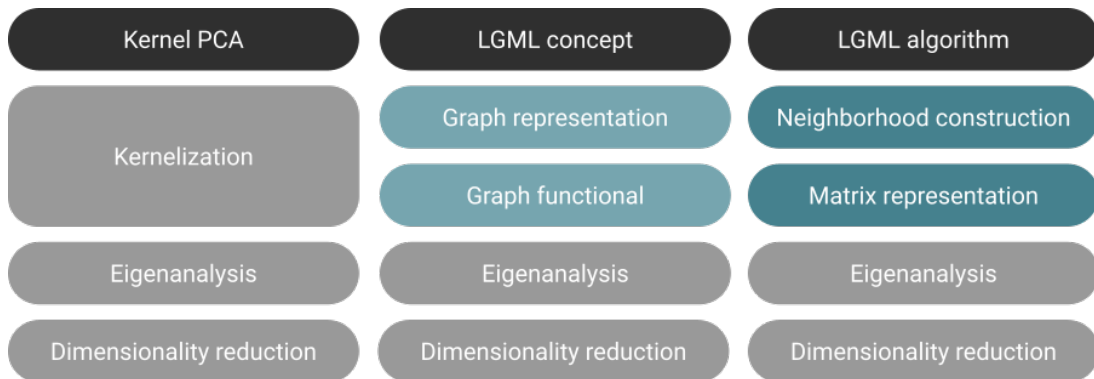
Landscape. Various approaches, many of which may be translated into one another



LEM Laplacian eigenmaps
LLE Locally linear embedding
HLLLE Hessian LLE
SSLLE Semi-supervised LLE

2 LGML CONCEPT

Idea. Capture intrinsic geometry, find principal axes of variability, retain most salient ones



2 LGML CONCEPT

Graph representation. Construct skeletal model of the manifold in \mathbb{R}^D

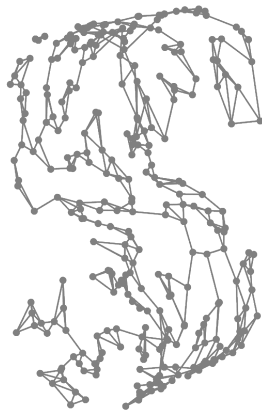
Vertices. Given by observations

Edges. Present between neighboring points

- Typically, k -neighborhoods
- Edge weights determined by nearness

Graph functional. Belief about intrinsic manifold properties at the heart of each method

- Local linearity **LLE** **SSLLE**
- Smoothness **LEM**
- Curvature **HLLE**
- ...



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3 TECHNIQUES

3.1 UNSUPERVISED LLE

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3.2 SEMI-SUPERVISED SSLLE

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3.3 CHALLENGES NEIGHBORHOOD RELATIONS

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4 SENSITIVITY ANALYSIS

4.1 SETUP SCENARIOS

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4.1 SETUP EVALUATION

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4.2 RESULTS **FOO**

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5 DISCUSSION

5 DISCUSSION **FOO**

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REFERENCES

G. Randauthor (2021): Most Relevant Shit, THE Journal, frontpage (what else)