

```

In[971]:= ClearAll["Global`*"]
SetDirectory["/Users/lisaleemcb/ADMX/ouroboros/code/"];
(*the files in Users/baker/My Documents/data/10_9_13/TUNING
are dB files and the Q script is made for re/im files. *)
fname = "../measurements/CAL_STRONG_S11.S1P";

file = Drop[Import[fname, "Table"], 12];
dataraw = file;
data = dataraw;
f = ToExpression[data[[All, 1]]];
S11dB = ToExpression[data[[All, 2]]];
S11ang = ToExpression[data[[All, 3]]];
(*S11Abs=Table[Abs[S11RE[[x]]+i S11IM[[x]]],{x,1,Length[S11RE]}];*)
Z0 = 50;
(*S11RE=(Z0*(1-(10^(S11dB/10))^2))/
(1+(10^(S11dB/10))^2-2*(10^(S11dB/10))*Cos[S11ang Degree]);
S11IM=2*Z0*(10^(S11dB/10))*Sin[S11ang Degree]/
(1+(10^(S11dB/10))^2-2*(10^(S11dB/10))*Cos[S11ang Degree]);*)
S11RE = (10^(S11dB/10))*Cos[S11ang Degree];
S11IM = (10^(S11dB/10))*Sin[S11ang Degree];
pos = Position[S11dB, Min[S11dB]][[1, 1]];
fresinitial = f[[pos]];

Sparam = Table[
  {
    (f[[x]] - fresinitial) / fresinitial, Abs[S11RE[[x]] + j * S11IM[[x]]]^2}, {x, 1, Length[f]};
(*Sparam=Table[{(f[[x]]-fresinitial)/fresinitial, 10^(S11dB[[x]]/10)}, {x, 1, Length[f]}];*)
t = 2 δ;
model = ρ^2 + (d^2 + 2 d ρ (Cos[φ] + QL (t - t0) Sin[φ])) / (1 + QL^2 (t - t0)^2);

vars = FindFit[Sparam, model, {{QL, 1400}, {ρ, 0.9}, {d, 0.5}, {φ, π}, {t0, 0}}, δ,
  MaxIterations → 10 000, Gradient → "FiniteDifference", AccuracyGoal → 10]
pmod = Plot[model /. vars, {δ, Min[Sparam[[All, 1]]], Max[Sparam[[All, 1]]]},
  PlotRange → All, Axes → False, Frame → True,
  PlotPoints → 10 000, PlotStyle → Green];
Splot = ListPlot[Sparam, PlotStyle → {Red, PointSize[Small]}];

Show[pmod, Splot, PlotRange → {{Min[Sparam[[All, 1]]], Max[Sparam[[All, 1]]]}, All},
  FrameLabel → {{ "|Γ|^2", ""}, {"δ", ""}},
  FrameStyle → Directive[Bold, 16, Medium], ImageSize → 600]
fres = fresinitial + fresinitial * vars[[5, 2]];
QL = vars[[1, 2]];
ρ = vars[[2, 2]];
d = vars[[3, 2]];
φ = vars[[4, 2]];
t0 = vars[[5, 2]];

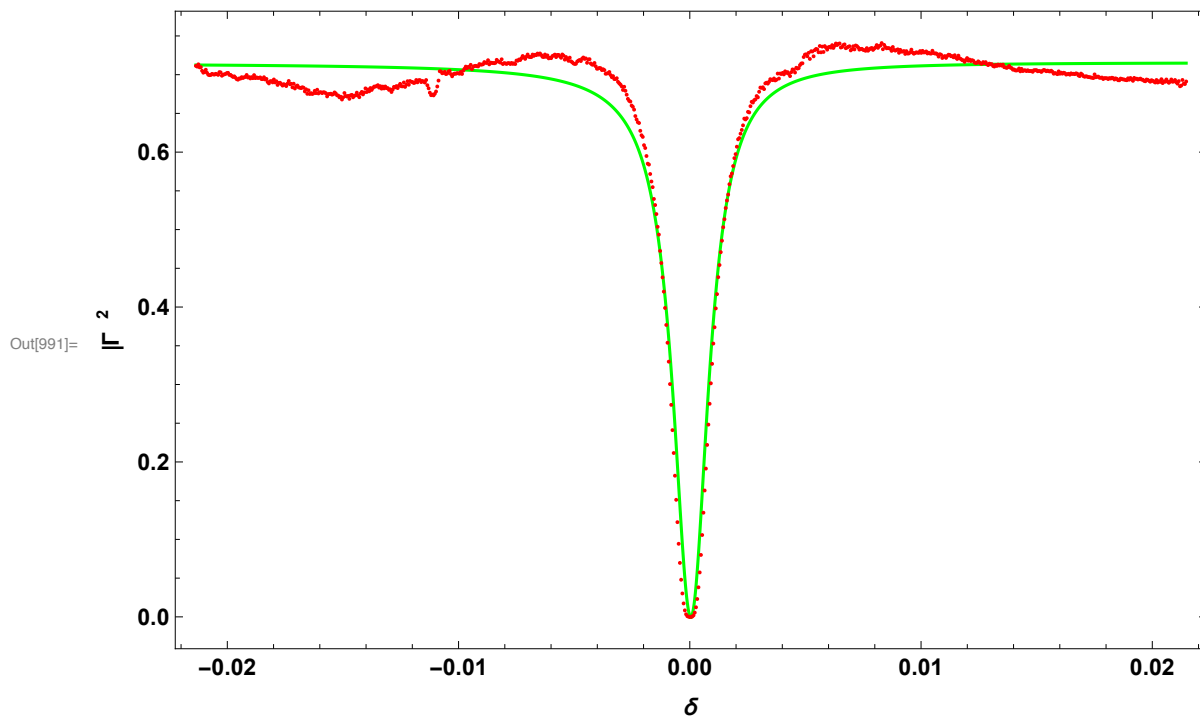
```

$$\kappa = \left(\frac{1}{\frac{1+\rho}{d} - 1} \right);$$

$$Q_0 = \left(\frac{1}{\frac{1+\rho}{d} - 1} + 1 \right) Q_L;$$

```
"Q0" -> ToString[Q0]
"fres[MHz]" -> ToString[fres]
"QL" -> ToString[QL]
"Coupling Coefficient" -> ToString[κ]
```

Out[988]= {QL → -537.237, ρ → 0.845591, d → 0.845748, ϕ → 3.16085, t0 → 0.000122118}



Out[1000]= $Q_0 \rightarrow -991.675$

Out[1001]= $f_{\text{res}}[\text{MHz}] \rightarrow 2.33541 \cdot 10^9$

Out[1002]= $Q_L \rightarrow -537.237$

Out[1003]= Coupling Coefficient $\rightarrow 0.845881$

```

In[958]:= pl = ListPlot[Table[{S11RE[[a]], S11IM[[a]]}, {a, 1, Length[f]}], PlotStyle →
  {Red, Thick}, PlotRange → All, AspectRatio → Automatic, AxesOrigin → {0, 0}];

R1 = {5, 10, 20, 30, 40, 60, 100, 300, 500};
X1 = {10, -10, 100, -100, -50, 50, -25, 25};
chart = Graphics[{Circle[{0, 0}], Gray, Table[
  Circle[{1 - 1 / (1 + R1[[a]] / Z0), 0}, 1 / (1 + R1[[a]] / Z0)], {a, 1, Length[R1]}],
  Table[Circle[{1, Z0 / X1[[a]]}, Abs[Z0 / X1[[a]]]], {a, 1, Length[X1]}],
  Line[{{-1, 0}, {1, 0}}, White, Thickness[0.45],
  Circle[{0, 0}, 1.5}], PlotRange → 1.1];
Show[chart, pl]
model

```

Part::pkspec1 : The expression x cannot be used as a part specification . >>

Part::pkspec1 : The expression x cannot be used as a part specification . >>

Part::pkspec1 : The expression x cannot be used as a part specification . >>

General::stop : Further output of Part::pkspec1 will be suppressed during this calculation . >>

Part::partw : Part 3 of

```

10 1/10 {-0.739543 , -0.74244 , -0.733496 , -0.745431 , -0.744487 , -0.759022 , -0.766563 , <<37 >> , -0.789687 , -0.78447 , -0.788544 , -0.776312 , -0.788312 , -0.78527 ,
Cos[° {-169.924 , -169.962 , -170.198 , -170.161 , -170.279 , -170.448 , -170.558 , -170.562 , <<35 >> , -
174.036 , -174.145 , -174.272 , -174.315 , -174.522 , -174.564 , -174.671 , <<751 >>}] [x]]
does not exist. >>

```

Part::partw : Part 3 of

```

10 1/10 {-0.739543 , -0.74244 , -0.733496 , -0.745431 , -0.744487 , -0.759022 , -0.766563 , <<37 >> , -0.789687 , -0.78447 , -0.788544 , -0.776312 , -0.788312 , -0.78527 ,
Sin[° {-169.924 , -169.962 , -170.198 , -170.161 , -170.279 , -170.448 , -170.558 , -170.562 , <<35 >> , -
174.036 , -174.145 , -174.272 , -174.315 , -174.522 , -174.564 , -174.671 , <<751 >>}] [x]]
does not exist. >>

```

Part::partw : Part 4 of

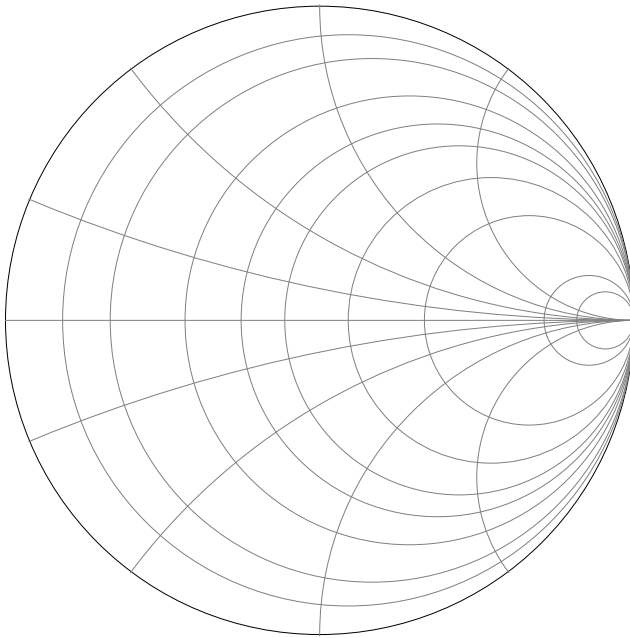
```

10 1/10 {-0.739543 , -0.74244 , -0.733496 , -0.745431 , -0.744487 , -0.759022 , -0.766563 , <<37 >> , -0.789687 , -0.78447 , -0.788544 , -0.776312 , -0.788312 , -0.78527 ,
Cos[° {-169.924 , -169.962 , -170.198 , -170.161 , -170.279 , -170.448 , -170.558 , -170.562 , <<35 >> , -
174.036 , -174.145 , -174.272 , -174.315 , -174.522 , -174.564 , -174.671 , <<751 >>}] [x]]
does not exist. >>

```

General::stop : Further output of Part::partw will be suppressed during this calculation . >>

Out[962]=



\$RecursionLimit ::reclim : Recursion depth of 1024 exceeded. >>

Out[963]= Hold[ρ^2]

```
In[964]:=  $\Gamma = \text{Abs} \left[ \text{Exp} \left[ i (\phi - \gamma) \right] \left( \rho + \frac{d \text{Exp} [i \gamma]}{1 + i Q L t} \right) \right]^2$ 
Smithparam = Table[{S11RE[[x]], S11IM[[x]]}, {x, 1, Length[S11RE]};
smithvar = FindFit[Smithparam,  $\Gamma$ , { $\gamma$ },  $\delta$ ]
ListPlot[Smithparam]
 $\Gamma /. \text{smithvar}$ 
Plot[( $\Gamma$ )1/2 /. smithvar, { $\delta$ , -0.8, 0.8}]
```

\$RecursionLimit ::reclim : Recursion depth of 1024 exceeded. >>

Out[964]= $e^{i(-\gamma + \phi)}$ Hold[ρ^2]

Part::partd : Part specification (-0.830414)[[1]] is longer than depth of object. >>

Part::partd : Part specification (-0.147564)[[1]] is longer than depth of object. >>

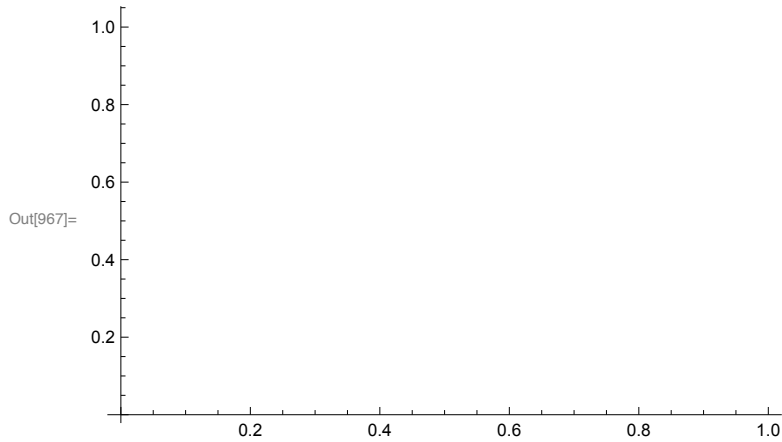
Part::partd : Part specification (-0.829958)[[2]] is longer than depth of object. >>

General::stop : Further output of Part::partd will be suppressed during this calculation. >>

FindFit::nrlnum : The function value { $\Gamma - 1.(-0.147564)[[1]], \Gamma - 1.(-0.146914)[[2]]$ } is not a list of real numbers with dimensions {2} at { γ } = {1.}. >>

FindFit::nrlnum : The function value { $\Gamma - 1.(-0.147564)[[1]], \Gamma - 1.(-0.146914)[[2]]$ } is not a list of real numbers with dimensions {2} at { γ } = {1.}. >>

```
Out[966]= FindFit[
{{(-0.830414)[[1]], (-0.147564)[[1]]}, {(-0.829958)[[2]], (-0.146914)[[2]]}},  $\Gamma$ , { $\gamma$ },  $\delta$ ]
```



FindFit::nrlnum : The function value $\{\Gamma - 1. (-0.147564) \llbracket 1 \rrbracket, \Gamma - 1. (-0.146914) \llbracket 2 \rrbracket\}$ is not a list of real numbers with dimensions $\{2\}$ at $\{\gamma\} = \{1.\}$. >>

ReplaceAll::reps :

{FindFit[{{(-0.830414) $\llbracket 1 \rrbracket$, (-0.147564) $\llbracket 1 \rrbracket$ }, {(-0.829958) $\llbracket 2 \rrbracket$, (-0.146914) $\llbracket 2 \rrbracket$ }}, Γ , $\{\gamma\}$, δ]} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing . >>

Out[968]= Γ /. FindFit[
 $\{\{(-0.830414) \llbracket 1 \rrbracket, (-0.147564) \llbracket 1 \rrbracket\}, \{(-0.829958) \llbracket 2 \rrbracket, (-0.146914) \llbracket 2 \rrbracket\}\}, \Gamma, \{\gamma\}, \delta]$

General::ivar : -0.8 is not a valid variable . >>

ReplaceAll::reps :

{FindFit[{{(-0.830414) $\llbracket 1 \rrbracket$, (-0.147564) $\llbracket 1 \rrbracket$ }, {(-0.829958) $\llbracket 2 \rrbracket$, (-0.146914) $\llbracket 2 \rrbracket$ }}, Γ , $\{\gamma\}$, -0.8]} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing . >>

General::ivar : -0.8 is not a valid variable . >>

ReplaceAll::reps :

{FindFit[{{(-0.830414) $\llbracket 1 \rrbracket$, (-0.147564) $\llbracket 1 \rrbracket$ }, {(-0.829958) $\llbracket 2 \rrbracket$, (-0.146914) $\llbracket 2 \rrbracket$ }}, Γ , $\{\gamma\}$, -0.8]} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing . >>

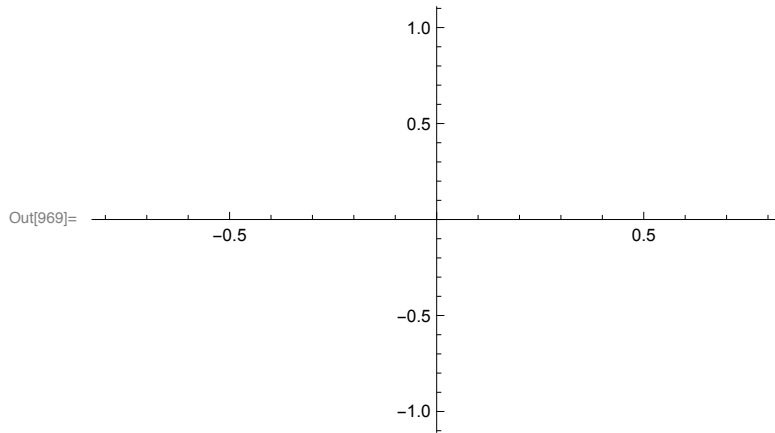
General::ivar : -0.799967 is not a valid variable . >>

General::stop : Further output of General::ivar will be suppressed during this calculation . >>

ReplaceAll::reps :

{FindFit[{{(-0.830414) $\llbracket 1 \rrbracket$, (-0.147564) $\llbracket 1 \rrbracket$ }, {(-0.829958) $\llbracket 2 \rrbracket$, (-0.146914) $\llbracket 2 \rrbracket$ }}, Γ , $\{\gamma\}$, -0.799967]} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing . >>

General::stop : Further output of ReplaceAll::reps will be suppressed during this calculation . >>



In[970]:= **S11RE**

Part::pkspec1 : The expression x cannot be used as a part specification . >>

Part::pkspec1 : The expression x cannot be used as a part specification . >>

Out[970]= $10^{\frac{1}{10}}$ {-0.739543, -0.74244, -0.733496, -0.745431, -0.744487, -0.759022, -0.766563, -0.763719, -0.754953, -0.7672, -0.774757, -0.7

Cos [

° {-169.924, -169.962, -170.198, -170.161, -170.279, -170.448, -170.558, -170.562, -170.795, -170.838, -170.941, -171.003, -171.051, -171.243, -171.314, -171.388, -171.421, -171.592, -171.662, -171.843, -171.933, -172.012, -172.05, -172.127, -172.253, -172.417, -172.476, -172.58, -172.739, -172.815, -172.903, -172.995, -173.076, -173.131, -173.321, -173.351, -173.452, -173.594, -173.588, -173.687, -173.846, -173.834, -173.927, -174.036, -174.145, -174.272, -174.315, -174.522, -174.564, -174.671, -174.832, -174.906, -175.054, -175.14, -175.272, -175.436, -175.501, -175.624, -175.774, -175.877, -175.986, -176.122, -176.235, -176.313, -176.455, -176.56, -176.627, -176.856, -176.884, -176.983, -177.114, -177.246, -177.385, -177.437, -177.531, -177.643, -177.811, -177.962, -178.009, -178.131, -178.222, -178.271, -178.431, -178.621, -178.676, -178.736, -178.767, -178.912, -179.062, -179.167, -179.287, -179.358, -179.458, -179.584, -179.711, -179.832, -179.95, 179.947, 179.865, 179.793, 179.566, 179.536, 179.428, 179.227, 179.123, 179.01, 178.939, 178.815, 178.66, 178.503, 178.418, 178.307, 178.275, 178.042, 178.023, 177.842, 177.701, 177.657, 177.493, 177.438, 177.291, 177.25, 177.113, 177.002, 176.917, 176.745, 176.67, 176.535, 176.451, 176.329, 176.266, 176.151, 175.993, 175.94, 175.85, 175.755, 175.611, 175.531, 175.407, 175.278, 175.289, 175.126, 175.074, 174.984, 174.905, 174.756, 174.709, 174.637, 174.563, 174.405, 174.296, 174.173, 174.114, 173.987, 173.945, 173.865, 173.67, 173.665, 173.528, 173.378, 173.373, 173.218, 173.192, 173.072, 172.991, 172.893, 172.751, 172.658, 172.576, 172.441, 172.371, 172.203, 172.149, 171.994, 171.899, 171.797, 171.793, 171.599, 171.506, 171.406, 171.256, 171.216, 171.094, 170.999, 170.877, 170.751, 170.674, 170.54, 170.403, 170.283, 170.087, 170.058, 169.979, 169.928, 169.857, 169.83, 169.692, 169.619, 169.575, 169.494, 169.347, 169.274, 169.173, 169.153, 168.992, 168.937, 168.812, 168.719, 168.598, 168.477, 168.419, 168.32, 168.244, 168.12, 168.003, 167.939, 167.835, 167.66, 167.555, 167.474, 167.36, 167.255, 167.094, 167.001, 166.873, 166.764, 166.666, 166.58, 166.454, 166.371, 166.247, 166.207, 166.101, 165.986, 165.859, 165.783, 165.674, 165.548, 165.496, 165.401, 165.27, 165.221, 165.053, 164.976, 164.813, 164.708, 164.608, 164.486, 164.415, 164.3, 164.189, 164.079, 163.947, 163.828, 163.742, 163.643, 163.573, 163.392,

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122.074, 121.989, 121.888, 121.749, 121.677, 121.625, 121.538, 121.399} [[x]] ]
```