

CODE

Print Function

#printPDF function receives two vectors and a filename. It prints three plots for each vector to the specified filename: ts plot, hist, acf.

```
printPDF <- function(m.s,s.s,filename) {  
  
  pdf(filename)  
  #PLOTS to PDF  
  par(mfrow=c(3,2)) #split plotting window into 3 rows and 2 columns  
  ts.plot(m.s,xlab="Iterations")  
  ts.plot(s.s,xlab="Iterations")  
  hist(m.s,probability=T, cex.lab=1.5, cex.axis=1.5)  
  hist(s.s,probability=T, cex.lab=1.5, cex.axis=1.5)  
  acf(m.s)  
  acf(s.s)  
  dev.off()  
  
}
```

Gibbs Function

#Gibbs function receives five parameters: "data" for the data values of interest, "m" for the population mean, "m0","s0","n0","k0" as prior parameters (μ , σ^2 , ν , κ), "N" for number of realizations, "lag" for determining how many realizations to skip between saves, and "burnin" for determining how many realizations to skip before starting to save. Gibbs generates N independent random normal values.

```
gibbs <- function(data,m,m0,s0,n0,k0,N,lag,burnin) {  
  
  #obtain mean (y.bar), variance (s.sqr), and length (n) of data  
  y.bar = mean(data)  
  s.sqr = var(data)  
  n = length(data)  
  
  #Set N to be N*lag+burnin  
  N <- N*lag + burnin  
  
  #Initialize vectors to hold mu and sigma sqr
```

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```
m.s <- NULL
s.s <- NULL
#Vector to hold y values from normal distribution with each mu, sigma sqr as parameters
y.s <- NULL

for(i in 1:N) {

  #generate a sigma sqr s using mean (y.bar), variance (s.sqr), length (n) of data, and prior
parameters
  s <- 1/rgamma(1,(n+1+n0)/2,((n-1)*s.sqr + n*(y.bar-m)^2 + ((m-m0)^2)*k0 + n0*s0)/2)
  #generate a mu m using mean (y.bar) and length (n) of data and sigma sqr (s) from last step
  m <- rnorm(1, (y.bar*n + m0*k0)/(n + k0), (sqrt((s/n)/(n + k0))))

  y.s <- c(y.s,rnorm(1,m,sqrt(s)))

  #if i is greater than burnin and if i is a multiple of the lag, store m and s
  if(i > burnin) {
    if(i %% lag == 0) {
      m.s <- c(m.s,m)
      s.s <- c(s.s,s)
    }
  }
}
#filename = sprintf("Documents/R-FILES/HW6-%s-%s-%s.pdf",k0,n0,s0)
#printPDF(m.s,s.s,filename)

#vectors <- list("mu" = m.s, "sigsqr" = s.s)
#return(vectors)

return(y.s)
}
```

Attach File, Run Gibbs, and Obtain Results

```
data = read.table(file.choose(), header=F)
attach(data)
data = data$V1

#Set burnin to 10 and leave lag=1 and run Gibbs with N=2500
N = 2500
lag = 1
burnin = 10
m = 80
#FIX m0 at 20
m0 = 20
```

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```
#CHOOSE s0,n0,k0  
k0 = 1  
s0 = 1  
n0 = 1  
  
vectors = gibbs(data,m,m0,s0,n0,k0,N,lag,burnin)  
  
mean(vectors$mu)  
quantile(vectors$mu, 0.025)  
quantile(vectors$mu, 0.975)  
mean(vectors$sigsqr)  
quantile(vectors$sigsqr, 0.025)  
quantile(vectors$sigsqr, 0.975)
```

Posterior Predictive Distribution and Probabilities

```
y.10 = vector > 10  
prob = length(y.10[y.10=="TRUE"])/N  
  
quantile(vector, 0.025)  
quantile(vector, 0.975)
```

RESULTS

Plots at $\kappa_0 = 1$, $\nu_0 = 1$, $\sigma_0^2 = 1$ with Lag=1 and Burnin=10

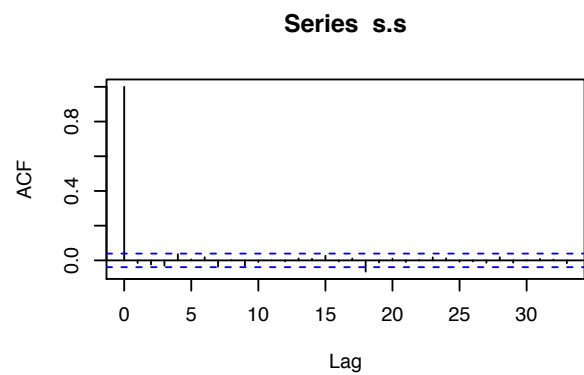
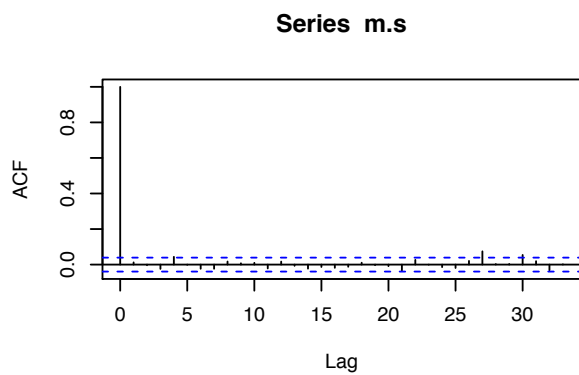
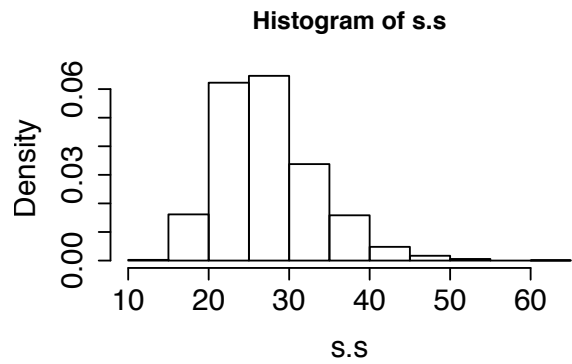
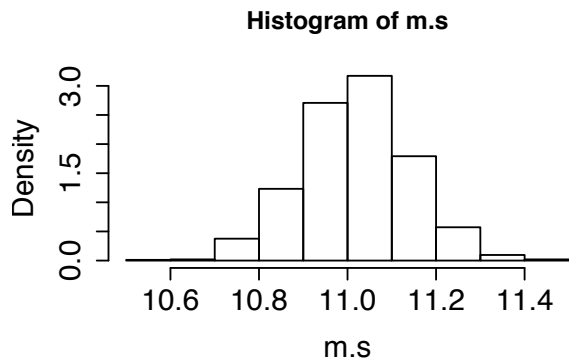
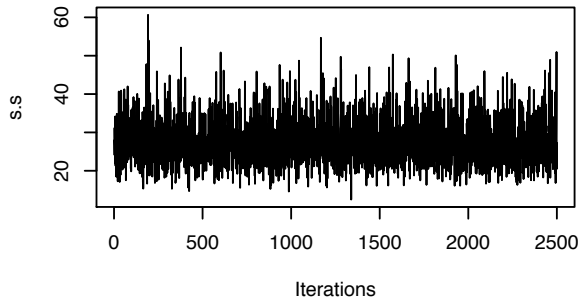
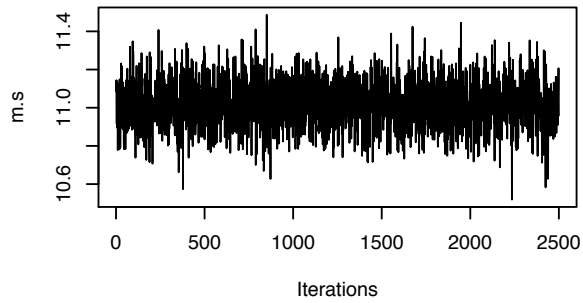
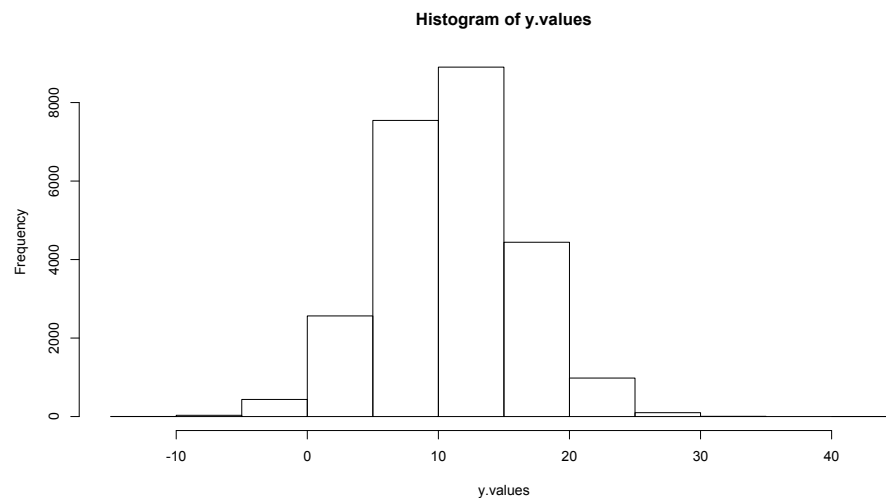


Table of μ and σ^2 Values for Different Combinations of κ_0 , ν_0 , and, σ_0^2

κ_0	ν_0	σ_0^2	μ	95% CI for μ	σ^2	95% CI for σ^2
1	1	1	11.02	10.78 – 11.26	27.33	17.72 – 40.96
99	1	1	17.22	16.99 – 17.44	84.58	55.21 – 129.50
99	1	777	17.23	16.96 – 17.48	101.45	68.50 – 152.31
99	500	1	17.21	17.15 – 17.29	7.61	6.75 – 8.57
1	1	777	11.02	10.72 – 11.32	45.52	29.93 – 68.34
1	500	1	11.02	10.94 – 11.09	3.09	2.75 – 3.47
1	500	777	11.02	9.84 – 12.23	718.28	638.99 – 807.00
99	500	777	17.23	16.58 – 17.89	721.34	639.50 – 814.46

The parameter μ increases from 11.02 to more than 17 only when κ_0 is large. The parameter σ^2 is affected most significantly when all hyper-parameters are large, i.e., σ^2 increases from 27.33 when all hyper-parameters are small to 721.34 when all hyper-parameters are large. When ν_0 is large and σ_0^2 is small, the value of σ^2 is significantly smaller, i.e., $\sigma^2 < 10$, than when all hyper-parameters are small, i.e., $\sigma^2 = 27.33$.

Posterior Predictive Distribution



Let x be the next observation.

$$P(x > 10) = 0.5758$$

The smallest interval that has 95% chance of containing x is (0.9, 21.34)